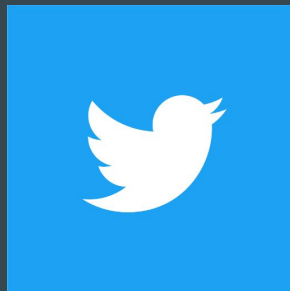
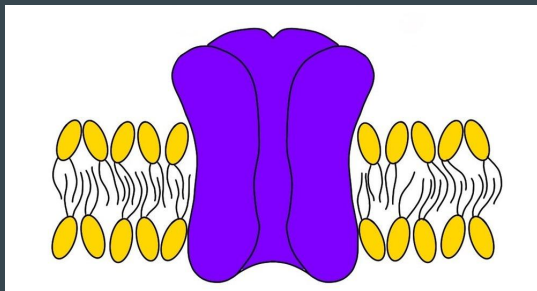


Baseball's Unprecedented Half-innings and Other Insights from Markov Chains

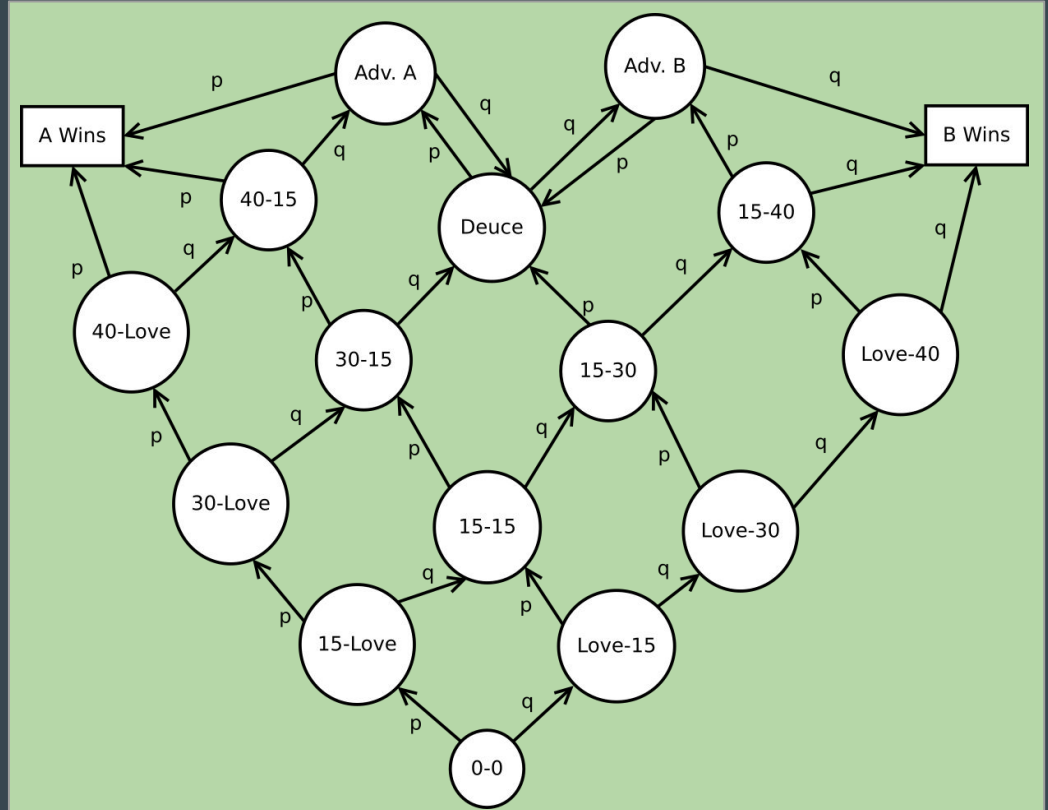
...

Sean G. Carver, Ph.D.

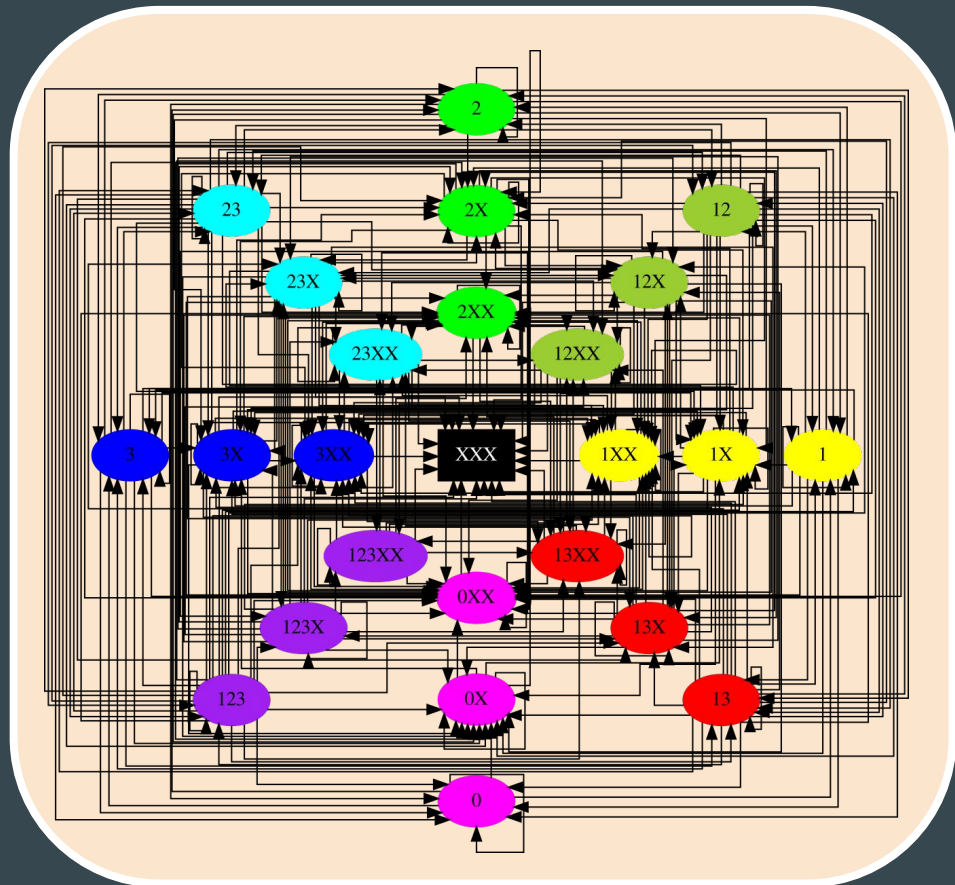
September 12, 2019



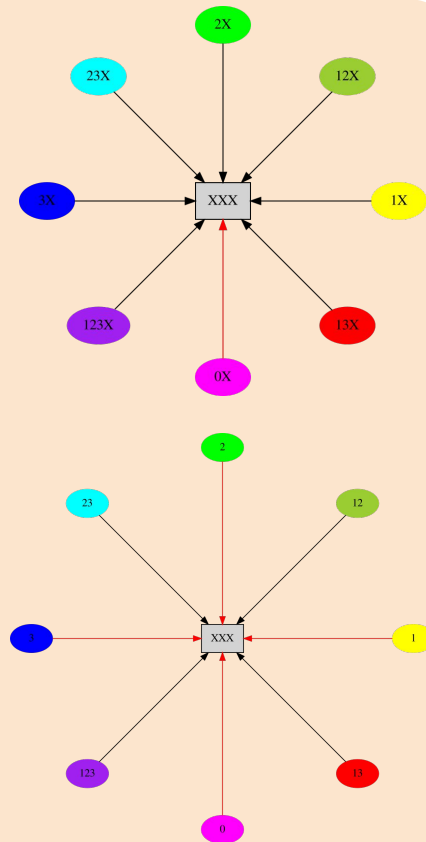
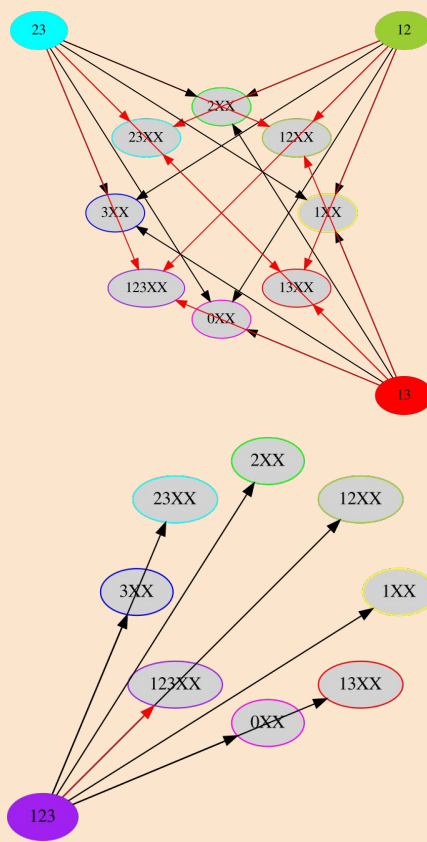
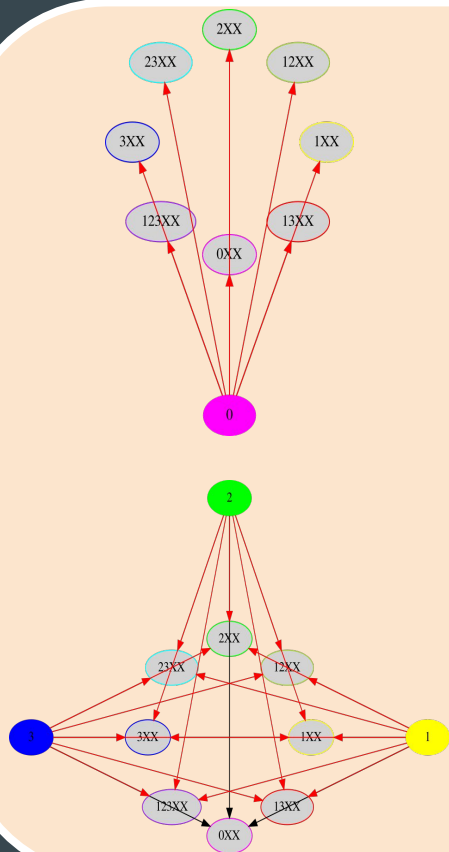
What is a Markov Chain?



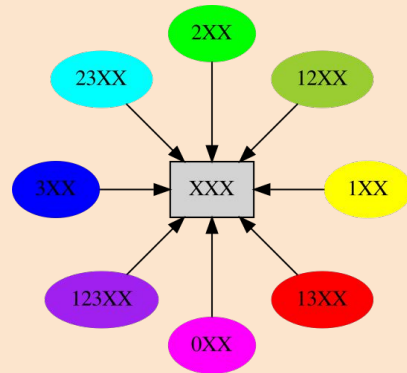
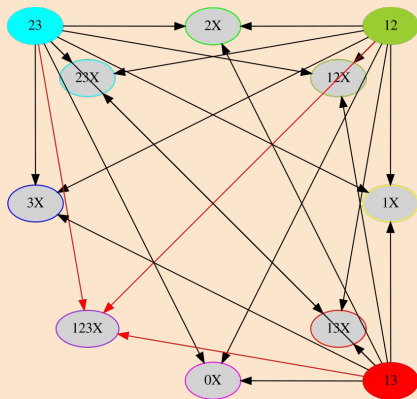
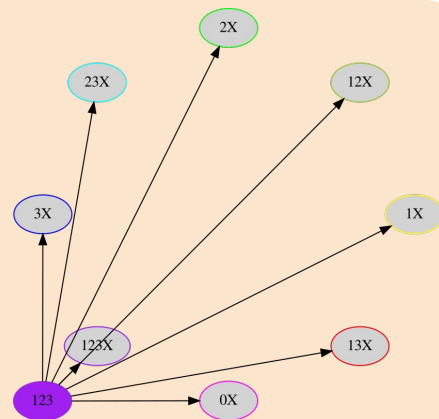
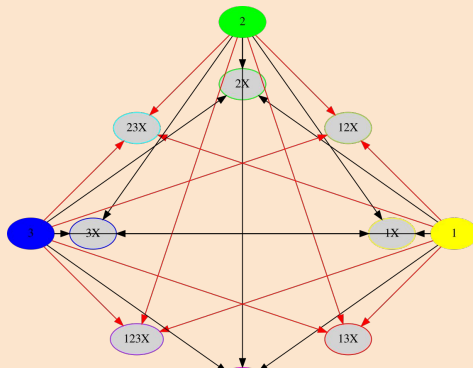
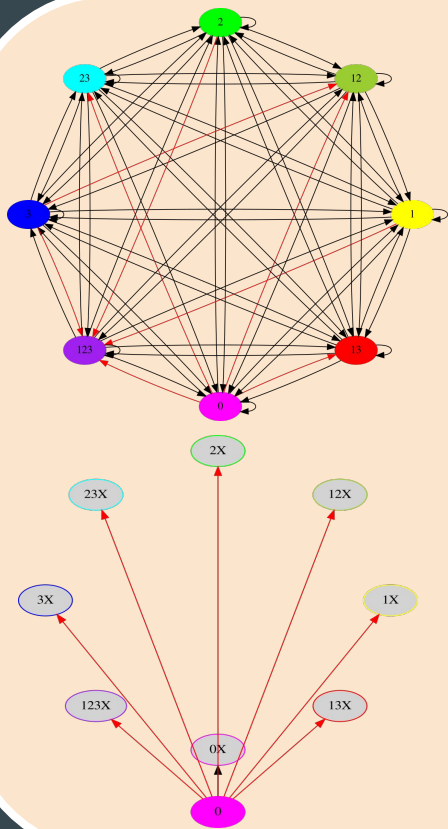
Baseball's Graph as a Markov Chain



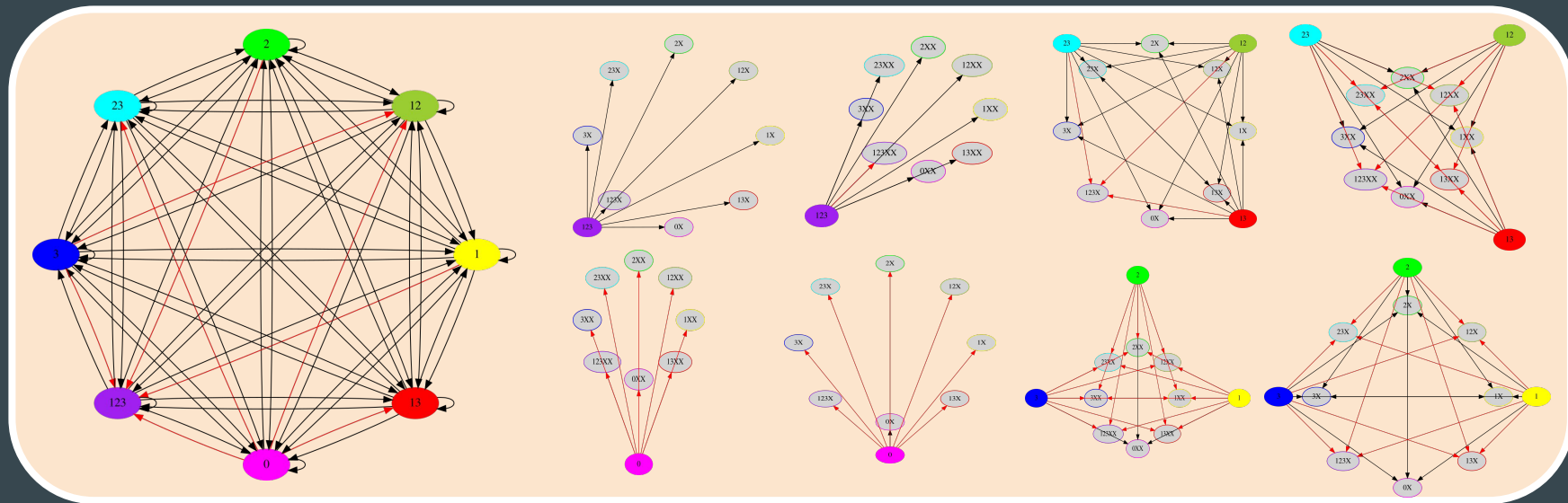
Visualizing Baseball's Graph (Double and Triple Plays)



Visualizing Baseball's Graph (Clean and Single Plays)



Symmetry and Asymmetry in Baseball's Graph



Rules of symmetric & real baseball: $\Delta \text{ Outs} \geq 0$ AND $0 \leq \text{Runners-on-base} \leq 3$
 $\Delta \text{ Runners-on-base} = 1 - \Delta \text{ Outs} - \Delta \text{ Score}$
 $\Delta \text{ Score} \geq 0$

Additional asymmetries in real baseball: Three outs and it's over!
 3:12 (3X:12X, ...) impossible---runners cannot retreat!

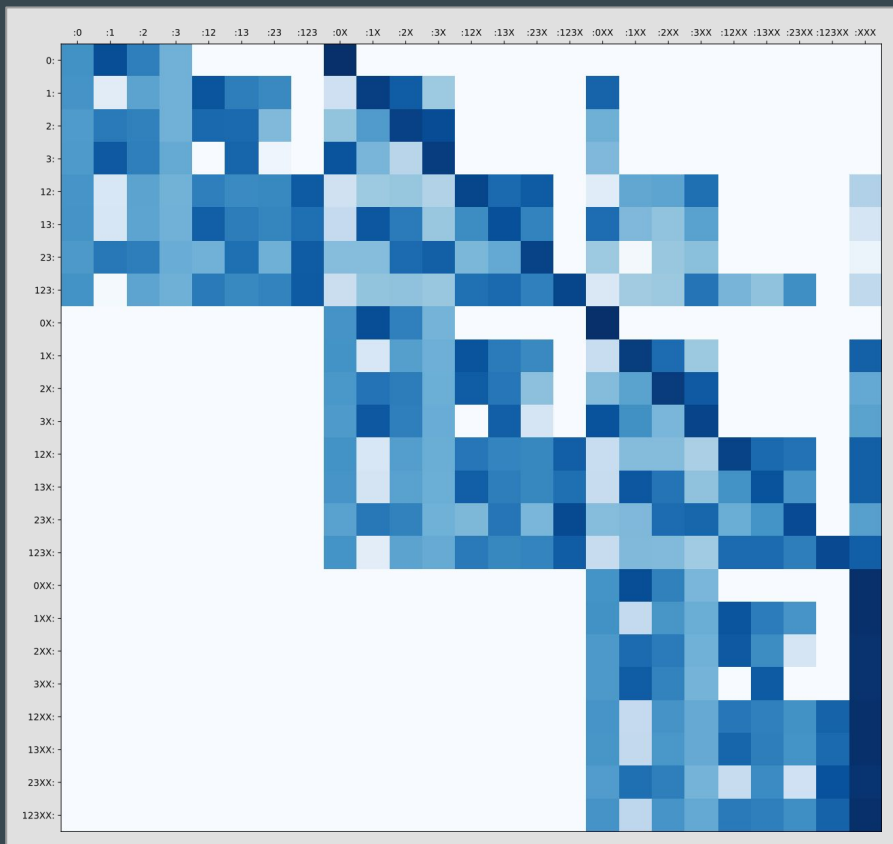
Transition Probability Matrix -- Clean Plays, No Outs

	:0	:1	:2	:3	:12	:13	:23	:123
0:	0.02461	0.25336	0.04649	0.00708	0	0	0	0
1:	0.022	0.00027	0.01252	0.00713	0.19619	0.04865	0.03269	0
2:	0.01757	0.05453	0.04364	0.00725	0.1006	0.09487	0.00528	0
3:	0.01819	0.16967	0.04674	0.00963	0	0.11433	0.00015	0
12:	0.02192	0.00039	0.01232	0.00702	0.04658	0.03199	0.03381	0.16033
13:	0.02273	0.00042	0.01208	0.00726	0.13831	0.04993	0.03784	0.07977
23:	0.01894	0.05878	0.04808	0.00878	0.00721	0.07985	0.00758	0.15326
123:	0.02439	0.00011	0.01215	0.0077	0.05556	0.03441	0.04034	0.16284

$$\text{Prob.} = \frac{\# (\text{From} \rightarrow \text{To})}{\# \text{ From}}$$

Computed with respect to a
population of transitions

Full Transition Probability Matrix

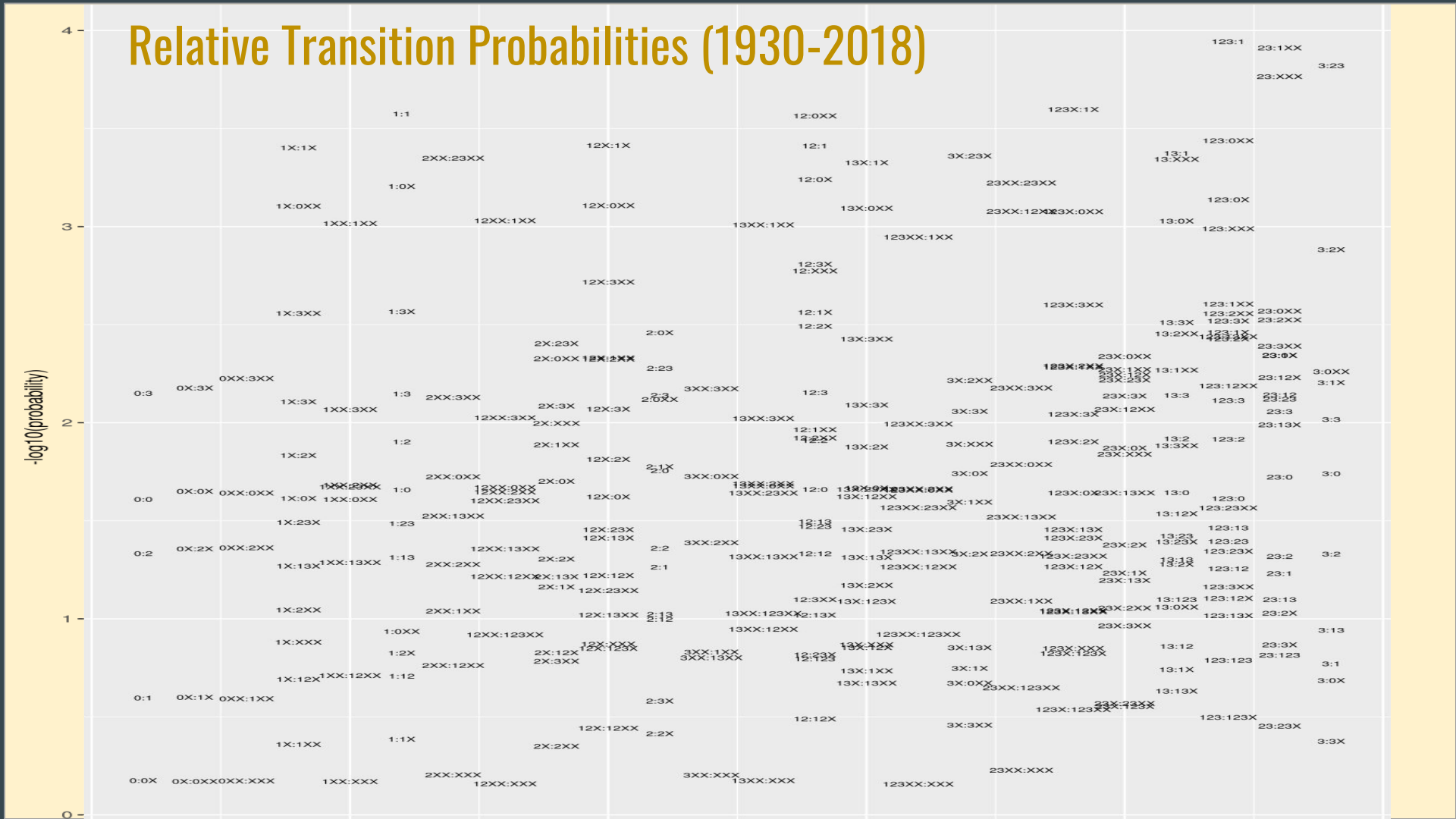


Population:
All MLB teams, 1930-2018,
Regular season

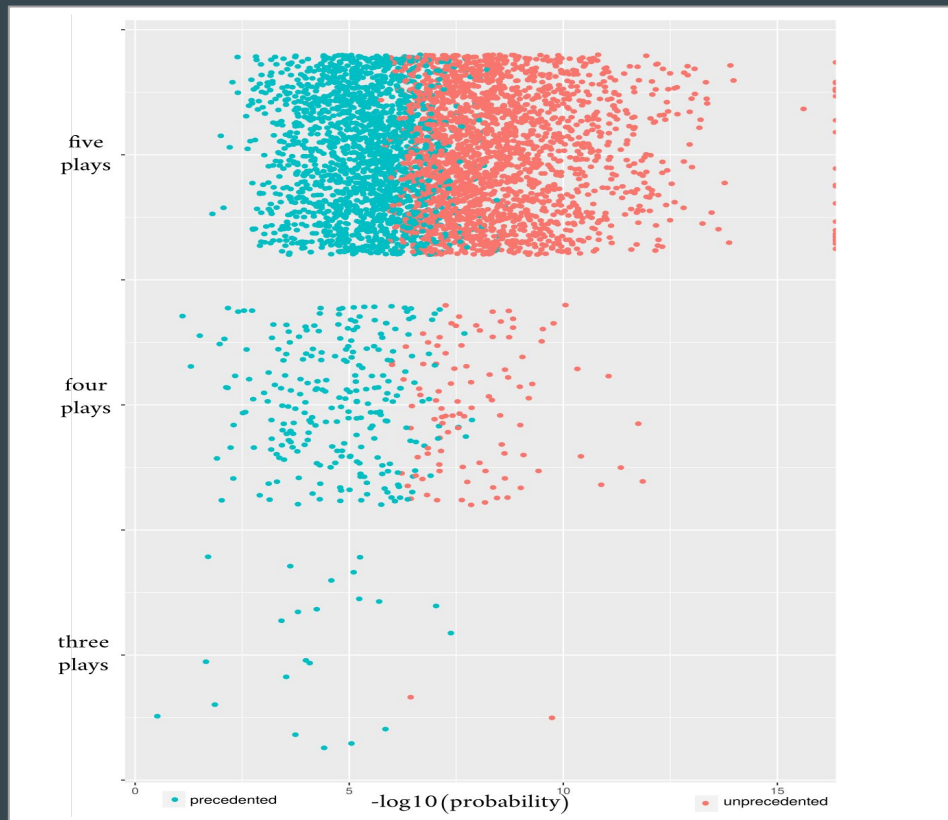
Many More Probabilities Are Zero for Subpopulations



Washington Nationals, batting at home, 2018

$-\log_{10}(\text{probability})$ 

Baseball's Unprecedented Half-innings

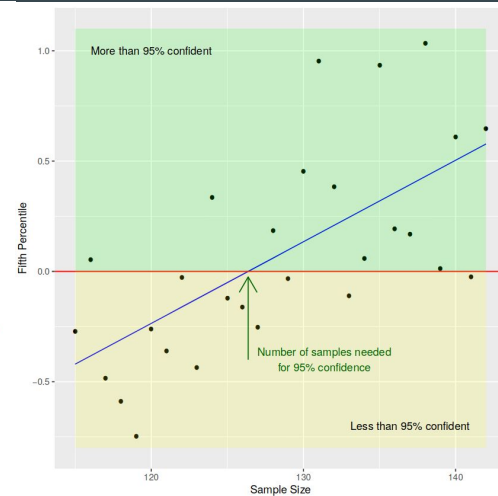
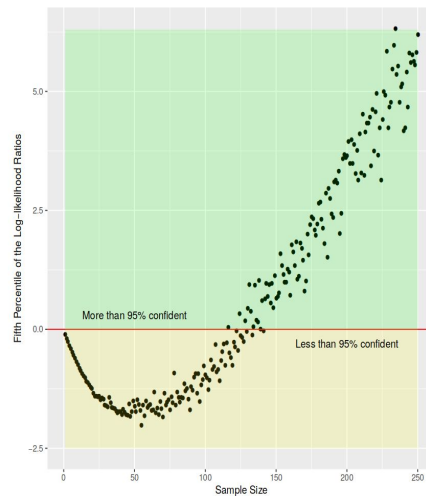
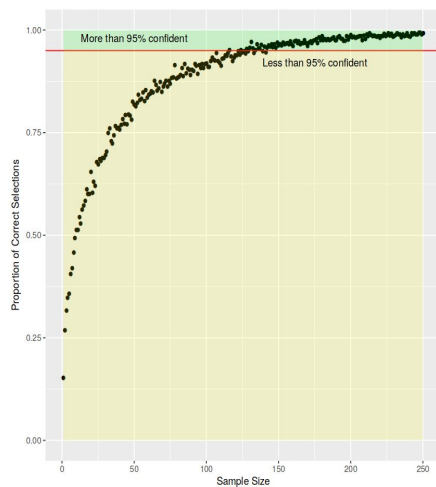
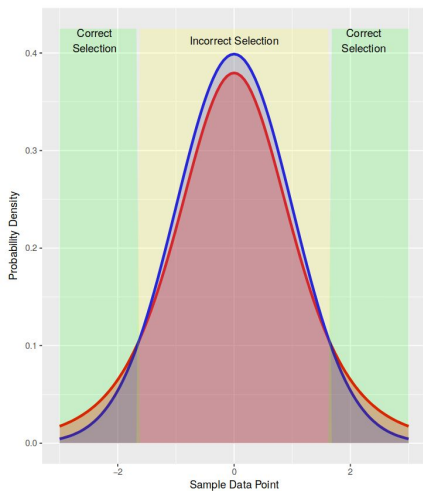


The most unlikely unprecedented half-innings:

sequence	$-\log_{10}(\text{probability})$
Three Plays	
0:3:13:XXX	6.43509767499117
0:3:23:XXX	9.73543779430501
Four Plays	
0:2:3:23:XXX	11.0579993507313
0:0:3:23:XXX	11.3442887847059
0:3:3:23:XXX	11.7519898723546
0:3:23:23:XXX	11.855734799529
Five Plays	
0:3:23:3:23:XXX	15.6122744428876
3XX:23XX	Infinity

$$\log_{10}(\text{number of half-innings played}) = 6.45$$

Quantifying the Similarity Between Model Baseball Teams

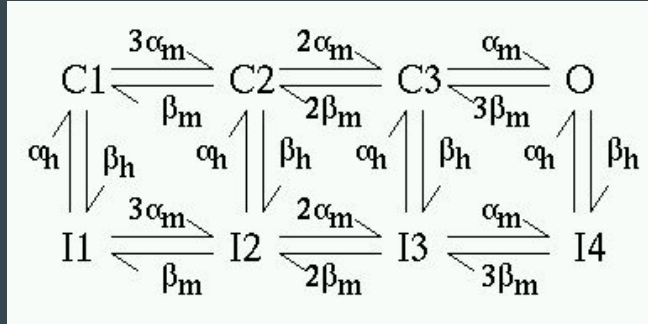


Result: it takes 30 ± 1 half-innings, simulated from the 2011 Baltimore Orioles model, to reject, with 95% confidence, the statement that these half-innings were sampled from the 2011 New York Yankees model.

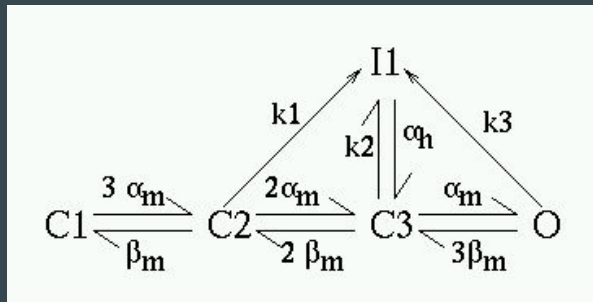
**Making Half-inning History and
Markov Transition Probabilities
Easily Accessible to All**



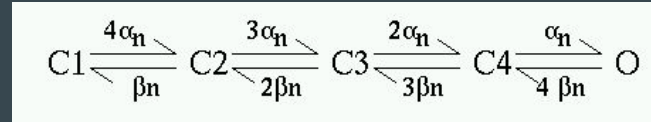
Beyond Sports



Hodgkin-Huxley Sodium Channel



Modern Model of Sodium Channel



Potassium Channel



Exposure
Incubation
Transmission
Immunity

Collaborators on Related Projects



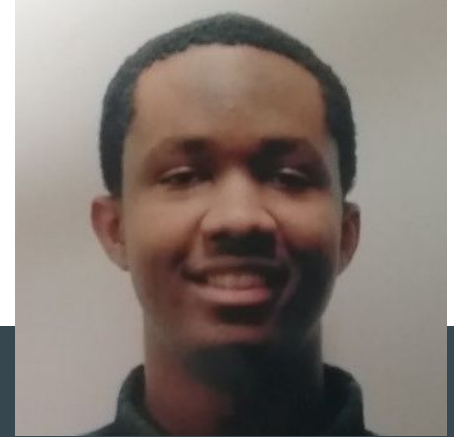
Jacob Ward

Formerly Professorial
Lecturer, American
University



Jake Berberian

Class of 2022, American
University



Kingsley Iyawe

Masters Student, American
University, expected
graduation: May 2020