

# Module Interface Specification for Solar Water Heating Systems Incorporating Phase Change Material

Brooks MacLachlan and Spencer Smith

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# Contents

<b>1</b>	<b>Symbols, Abbreviations and Acronyms</b>	<b>1</b>
<b>2</b>	<b>Introduction</b>	<b>1</b>
<b>3</b>	<b>Notation</b>	<b>1</b>
<b>4</b>	<b>Module Decomposition</b>	<b>2</b>
<b>5</b>	<b>MIS of Control Module</b>	<b>4</b>
5.1	Module . . . . .	4
5.2	Uses . . . . .	4
5.3	Syntax . . . . .	4
5.3.1	Exported Access Programs . . . . .	4
5.4	Semantics . . . . .	4
5.4.1	State Variables . . . . .	4
5.4.2	Access Routine Semantics . . . . .	4
<b>6</b>	<b>MIS of Input Parameters Module</b>	<b>6</b>
6.1	Module . . . . .	6
6.2	Uses . . . . .	6
6.3	Syntax . . . . .	6
6.4	Semantics . . . . .	6
6.4.1	Environment Variables . . . . .	6
6.4.2	State Variables . . . . .	7
6.4.3	Assumptions . . . . .	8
6.4.4	Access Routine Semantics . . . . .	8
6.5	Considerations . . . . .	10
<b>7</b>	<b>MIS of Temperature ODEs Module</b>	<b>11</b>
7.1	Module . . . . .	11
7.2	Uses . . . . .	11
7.3	Syntax . . . . .	11
7.3.1	Exported Access Programs . . . . .	11
7.4	Semantics . . . . .	11
7.4.1	State Variables . . . . .	11
7.4.2	Assumptions . . . . .	11
7.4.3	Access Routine Semantics . . . . .	11
<b>8</b>	<b>MIS of ODE Solver Module</b>	<b>13</b>
8.1	Module . . . . .	13
8.2	Uses . . . . .	13
8.3	Syntax . . . . .	13

8.3.1	Exported Access Programs . . . . .	13
8.4	Semantics . . . . .	13
8.4.1	State Variables . . . . .	13
8.4.2	Access Routine Semantics . . . . .	13
<b>9</b>	<b>MIS of Energy Module</b>	<b>15</b>
9.1	Module . . . . .	15
9.2	Uses . . . . .	15
9.3	Syntax . . . . .	15
9.3.1	External Access Programs . . . . .	15
9.4	Semantics . . . . .	15
9.4.1	State Variables . . . . .	15
9.4.2	Assumptions . . . . .	15
9.4.3	Access Routine Semantics . . . . .	15
<b>10</b>	<b>MIS of Output Verification Module</b>	<b>17</b>
10.1	Module . . . . .	17
10.2	Uses . . . . .	17
10.3	Syntax . . . . .	17
10.3.1	Exported Constant . . . . .	17
10.3.2	Exported Access Programs . . . . .	17
10.4	Semantics . . . . .	17
10.4.1	State Variables . . . . .	17
10.4.2	Assumptions . . . . .	17
10.4.3	Access Routine Semantics . . . . .	17
10.4.4	Local Functions . . . . .	18
<b>11</b>	<b>MIS of Plotting Module</b>	<b>19</b>
11.1	Module . . . . .	19
11.2	Uses . . . . .	19
11.3	Syntax . . . . .	19
11.3.1	Exported Access Programs . . . . .	19
11.4	Semantics . . . . .	19
11.4.1	State Variables . . . . .	19
11.4.2	Environment Variables . . . . .	19
11.4.3	Assumptions . . . . .	19
11.4.4	Access Routine Semantics . . . . .	19
<b>12</b>	<b>MIS of Output Module</b>	<b>20</b>
12.1	Module . . . . .	20
12.2	Uses . . . . .	20
12.3	Syntax . . . . .	20
12.3.1	Exported Constants . . . . .	20

12.3.2	Exported Access Program . . . . .	20
12.4	Semantics . . . . .	20
12.4.1	State Variables . . . . .	20
12.4.2	Environment Variables . . . . .	20
12.4.3	Access Routine Semantics . . . . .	20
<b>13</b>	<b>MIS of Specification Parameters</b>	<b>21</b>
13.1	Module . . . . .	21
13.2	Uses . . . . .	21
13.3	Syntax . . . . .	21
13.3.1	Exported Constants . . . . .	21
13.4	Semantics . . . . .	22
<b>14</b>	<b>Appendix</b>	<b>23</b>

# 1 Symbols, Abbreviations and Acronyms

See SRS Documentation at <https://github.com/smiths/swhs>

## 2 Introduction

The following document details the Module Interface Specifications for the implemented modules in a program simulating a Solar Water Heating System with Phase Change Material. It is intended to ease navigation through the program for design and maintenance purposes.

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at <https://github.com/smiths/swhs>.

The specification is given in terms of functions, rather than sequences. For instance, the predicted temperature of the water is given as a function of time ( $\mathbb{R} \rightarrow \mathbb{R}$ ), not as a sequence ( $\mathbb{R}^n$ ). This approach is more straightforward for the specification, but in the implementation stage, it will likely be necessary to introduce a sequence, assuming that a numerical solver is used for the system of ODEs.

## 3 Notation

The structure of the MIS for modules comes from ?, with the addition that template modules have been adapted from ?. The mathematical notation comes from Chapter 3 of ?. For instance, the symbol  $:=$  is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by SWHS.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	$\mathbb{N}$	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$

The specification of SWHS uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, SWHS uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

## 4 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding	
Behaviour-Hiding	Input Parameters Output Format Output Verification Temperature ODEs Energy Equations Control Module Specification Parameters Module
Software Decision	Sequence Data Structure ODE Solver Plotting

Table 1: Module Hierarchy



## 5 MIS of Control Module

### 5.1 Module

main

### 5.2 Uses

Param (Section 6), Temperature (Section 7), Solver (Section 8), Energy (Section 9), verify\_output (Section 10), plot (Section 11), output (Section 12)

### 5.3 Syntax

#### 5.3.1 Exported Access Programs

Name	In	Out	Exceptions
main	-	-	-

### 5.4 Semantics

#### 5.4.1 State Variables

None

#### 5.4.2 Access Routine Semantics

main():

- transition: Modify the state of Param module and the environment variables for the Plot and Output modules by following these steps

Get (filenameIn: string) and (filenameOut: string) from user

load\_params(filenameIn)

*#Find temperature function ( $T_W^{\text{Solid}}, T_W^{\text{Melting}}, T_W^{\text{Liquid}}, T_P^{\text{Solid}}, T_P^{\text{Melting}}, T_P^{\text{Liquid}}$ ), and energy ( $Q_P$ ) and times of transition between solid, melting and liquid phases ( $t_{\text{melt}}^{\text{init}}, t_{\text{melt}}^{\text{final}}$ )*

$t_{\text{melt}}^{\text{init}}, [T_W^{\text{Solid}}, T_P^{\text{Solid}}]^T := \text{solve}(\text{ODE\_SolidPCM}, 0.0, [T_{\text{init}}, T_{\text{init}}]^T, \text{event\_StartMelt}, t_{\text{final}})$

$t_{\text{melt}}^{\text{final}}, [T_W^{\text{Melting}}, T_P^{\text{Melting}}, Q_P]^T := \text{solve}(\text{ODE\_MeltingPCM}, t_{\text{melt}}^{\text{init}}, [T_W^{\text{Solid}}(t_{\text{melt}}^{\text{init}}), T_P^{\text{Solid}}(t_{\text{melt}}^{\text{init}}), 0.0]^T, \text{event\_EndMelt}, t_{\text{final}})$

$[T_W^{\text{Liquid}}, T_P^{\text{Liquid}}]^T := \text{solveNoE}(\text{ODE\_LiquidPCM}, t_{\text{melt}}^{\text{final}}, [T_W^{\text{Melting}}(t_{\text{melt}}^{\text{final}}), T_P^{\text{Melting}}(t_{\text{melt}}^{\text{final}})]^T, t_{\text{final}})$



*#Combine temperatures for  $0 \leq t \leq t_{\text{final}}$*

$$T_W(t) = (0 \leq t < t_{\text{melt}}^{\text{init}} \Rightarrow T_W^{\text{Solid}}|t_{\text{melt}}^{\text{init}} \leq t < t_{\text{melt}}^{\text{final}} \Rightarrow T_W^{\text{Melting}}|t_{\text{melt}}^{\text{final}} \leq t \leq t_{\text{final}} \Rightarrow T_W^{\text{Liquid}})$$

$$T_P(t) = (0 \leq t < t_{\text{melt}}^{\text{init}} \Rightarrow T_P^{\text{Solid}}|t_{\text{melt}}^{\text{init}} \leq t < t_{\text{melt}}^{\text{final}} \Rightarrow T_P^{\text{Melting}}|t_{\text{melt}}^{\text{final}} \leq t \leq t_{\text{final}} \Rightarrow T_P^{\text{Liquid}})$$

*#Energy values ( $E_W(t), E_P(t)$ ) for  $0 \leq t \leq t_{\text{final}}$*

$$E_W(t) = (0 \leq t < t_{\text{melt}}^{\text{init}} \Rightarrow \text{energyWater}(T_W^{\text{Solid}})|t_{\text{melt}}^{\text{init}} \leq t < t_{\text{melt}}^{\text{final}} \Rightarrow \text{energyWater}(T_W^{\text{Melting}})|t_{\text{melt}}^{\text{final}} \leq t \leq t_{\text{final}} \Rightarrow \text{energyWater}(T_W^{\text{Liquid}}))$$

$$E_P(t) = (0 \leq t < t_{\text{melt}}^{\text{init}} \Rightarrow \text{energySolidPCM}(T_P^{\text{Solid}})|t_{\text{melt}}^{\text{init}} \leq t < t_{\text{melt}}^{\text{final}} \Rightarrow \text{energyMeltingPCM}(Q_P)|t_{\text{melt}}^{\text{final}} \leq t \leq t_{\text{final}} \Rightarrow \text{energyLiquidPCM}(T_P^{\text{Liquid}}))$$

*#Output calculated values to a file and to a plot. Verify calculated values obey conservation of energy.*

`verify_output( $T_w, T_p, E_w, E_p, t_{\text{final}}$ )`

`plot( $T_w, T_p, E_w, E_p, t_{\text{final}}$ )`

`output(filenameOut,  $T_w, T_p, E_w, E_p, t_{\text{final}}$ )`

## 6 MIS of Input Parameters Module

The secrets of this module are the data structure for input parameters, how the values are input and how the values are verified. The load and verify secrets are isolated to their own access programs.

### 6.1 Module

Param

### 6.2 Uses

SpecParam (Section 13)

### 6.3 Syntax

Name	In	Out	Exceptions
load_params	string	-	FileError
verify_params	-	-	badLength, badDiam, badPCMVolume, badPCMAndTankVol, badPCMArea, badPCMDensity, badMeltTemp, badCoilAndInitTemp, badCoilTemp, badPCMHeatCapSolid, badPCMHeatCapLiquid, badHeatFusion, badCoilArea, badWaterDensity, badWaterHeatCap, badCoilCoeff, badPCMCoeff, badInitTemp, badFinalTime, badInitAndMeltTemp
$L$	-	$\mathbb{R}$	
$D$	-	$\mathbb{R}$	
$V_P$	-	$\mathbb{R}$	
$A_P$	-	$\mathbb{R}$	
...	...	...	
$m_W^{\text{noPCM}}$	-	$\mathbb{R}$	
$\tau_W^{\text{noPCM}}$	-	$\mathbb{R}$	

### 6.4 Semantics

#### 6.4.1 Environment Variables

inputFile: sequence of string  $\#f[i]$  is the  $i$ th string in the text file  $f$

### 6.4.2 State Variables

# From R1

$L: \mathbb{R}$

$D: \mathbb{R}$

$V_P: \mathbb{R}$

$A_P: \mathbb{R}$

$\rho_P: \mathbb{R}$

$T_{\text{melt}}^P: \mathbb{R}$

$C_P^S: \mathbb{R}$

$C_P^L: \mathbb{R}$

$H_f: \mathbb{R}$

$A_C: \mathbb{R}$

$T_C: \mathbb{R}$

$\rho_W: \mathbb{R}$

$C_W: \mathbb{R}$

$h_C: \mathbb{R}$

$h_P: \mathbb{R}$

$T_{\text{init}}: \mathbb{R}$

$t_{\text{step}}: \mathbb{R}$

$t_{\text{final}}: \mathbb{R}$

$AbsTol: \mathbb{R}$

$RelTol: \mathbb{R}$

$ConsTol: \mathbb{R}$

# From R2

$V_{\text{tank}}: \mathbb{R}$

$m_W: \mathbb{R}$

$m_P: \mathbb{R}$

# From R3

$\tau_W: \mathbb{R}$

$\eta: \mathbb{R}$

$\tau_P^S: \mathbb{R}$

$\tau_P^L: \mathbb{R}$

# To Support IM4

$E_{P_{\text{melt}}}^{\text{init}}: \mathbb{R}$

$E_{P_{\text{melt}}}^{\text{all}}: \mathbb{R}$

# To Support Testing

$m_W^{\text{noPCM}}: \mathbb{R}$

$\tau_W^{\text{noPCM}}: \mathbb{R}$

### 6.4.3 Assumptions

- load\_params will be called before the values of any state variables will be accessed.
- The file contains the string equivalents of the numeric values for each input parameter in order, each on a new line. The order is the same as in the table in R1 of the SRS. Any comments in the input file should be denoted with a '#' symbol.

### 6.4.4 Access Routine Semantics

Param. $L$ :

- output:  $out := L$
- exception: none

Param. $D$ :

- output:  $out := D$
- exception: none

...

Param. $m_W^{\text{noPCM}}$ :

- output:  $out := m_W^{\text{noPCM}}$
- exception: none

Param. $\tau_W^{\text{noPCM}}$ :

- output:  $out := \tau_W^{\text{noPCM}}$
- exception: none

load\_params( $s$ ):

- transition: The filename  $s$  is first associated with the file  $f$ . `inputFile` is used to modify the state variables using the following procedural specification:

1. Read data sequentially from `inputFile` to populate the state variables from R1 ( $L$  to  $ConsTol$ ).

2. Calculate the derived quantities (all other state variables) as follows:

- $V_{\text{tank}} := \pi \times L \times \left(\frac{D}{2}\right)^2$
- $m_W := \rho_w(V_t - V_p)$
- $m_P := \rho_p V_p$
- $\tau_W := \frac{m_w C_w}{A_c h_c}$
- $\eta := \frac{h_p A_p}{h_c A_c}$
- $\tau_P^S := \frac{m_p C_{ps}}{h_p A_p}$
- $\tau_P^L := \frac{m_p C_{pl}}{h_p A_p}$
- $E_{P\text{melt}}^{\text{init}} := C_{ps} m_p (T_{\text{melt}} - T_{\text{init}})$
- $E_{P\text{melt}}^{\text{all}} := H_f m_p$
- $m_W^{\text{noPCM}} := \rho_w V_t$
- $\tau_W^{\text{noPCM}} := \frac{m_W^{\text{noPCM}} C_w}{h_c A_c}$

3. `verify_params()`

- exception: `exc :=` a file name  $s$  cannot be found OR the format of `inputFile` is incorrect  $\Rightarrow$  `FileError`

`verify_params()`:

- out: `out :=` none
- exception: `exc :=`

$\neg(L > 0)$	$\Rightarrow$ <code>badLength</code>
$\neg(L_{\min} \leq L \leq L_{\max})$	$\Rightarrow$ <code>warnLength</code>
$\neg(D > 0)$	$\Rightarrow$ <code>badDiam</code>
$\neg\left(\frac{D}{L_{\min}} \leq \frac{D}{L} \leq \frac{D}{L_{\max}}\right)$	$\Rightarrow$ <code>warnDiam</code>
$\neg(V_P > 0)$	$\Rightarrow$ <code>badPCMVVolume</code>
$\neg(V_P \geq \text{minfract} \cdot V_{\text{tank}}(D, L))$	$\Rightarrow$ <code>warnPCMVVol</code>
$\neg(V_P < V_{\text{tank}}(D, L))$	$\Rightarrow$ <code>badPCMAndTankVol</code>
$\neg(A_P > 0)$	$\Rightarrow$ <code>badPCMArea</code>
$\neg(V_P \leq A_P \leq \frac{2}{h_{\min}} V_P)$	$\Rightarrow$ <code>warnVolArea</code>
$\neg(\rho_P > 0)$	$\Rightarrow$ <code>badPCMDensity</code>
$\neg(\rho_P^{\min} < \rho_P < \rho_P^{\max})$	$\Rightarrow$ <code>warnPCMDensity</code>

etc. See Appendix (Section 14) for the complete list of exceptions and associated error messages.

## 6.5 Considerations

The value of each state variable can be accessed through its name (getter). An access program is available for each state variable. There are no setters for the state variables, since the values will be set and checked by load params and not changed for the life of the program.

## 7 MIS of Temperature ODEs Module

### 7.1 Module

Temperature

### 7.2 Uses

Param (Section 6)

### 7.3 Syntax

#### 7.3.1 Exported Access Programs

Name	In	Out	Exceptions
ODE_SolidPCM	–	$(\mathbb{R}^3 \rightarrow \mathbb{R})^2$	-
ODE_MeltingPCM	–	$(\mathbb{R}^4 \rightarrow \mathbb{R})^3$	-
ODE_LiquidPCM	–	$(\mathbb{R}^3 \rightarrow \mathbb{R})^2$	-
event_StartMelt	–	$\mathbb{R}^2 \rightarrow \mathbb{R}$	-
event_EndMelt	–	$\mathbb{R}^3 \rightarrow \mathbb{R}$	-

### 7.4 Semantics

#### 7.4.1 State Variables

none

#### 7.4.2 Assumptions

none

#### 7.4.3 Access Routine Semantics

ODE\_SolidPCM():

- output:  $out := \frac{d}{dt} \begin{bmatrix} T_W \\ T_P \end{bmatrix} = \begin{bmatrix} \frac{1}{\tau_W}[(T_C - T_W(t)) + \eta(T_P(t) - T_W(t))] \\ \frac{1}{\tau_P}(T_W(t) - T_P(t)) \end{bmatrix}$

- exception: none

ODE\_MeltingPCM():

- output:  $out := \frac{d}{dt} \begin{bmatrix} T_W \\ T_P \\ Q_P \end{bmatrix} = \begin{bmatrix} \frac{1}{\tau_W}[(T_C - T_W(t)) + \eta(T_P(t) - T_W(t))] \\ 0 \\ h_P A_P(T_W(t) - T_{\text{melt}}^P) \end{bmatrix}$

- exception: none

ODE\_LiquidPCM():

- output:  $out := \frac{d}{dt} \begin{bmatrix} T_W \\ T_P \end{bmatrix} = \begin{bmatrix} \frac{1}{\tau_W}[(T_C - T_W(t)) + \eta(T_P(t) - T_W(t))] \\ \frac{1}{\tau_P}(T_W(t) - T_P(t)) \end{bmatrix}$

- exception: none

event\_StartMelt():

- output:  $out := g([T_W, T_P]^T) = T_{\text{melt}}^P - T_P$

- exception: none

event\_EndMelt():

- output:  $out := g([T_W, T_P, Q_P]^T) = 1 - \phi$ , where  $\phi = \frac{Q_P}{E_{P\text{melt}}^{\text{all}}}$

- exception: none



## 8 MIS of ODE Solver Module

*#Bold font is used to indicate variables that are a sequence type*

### 8.1 Module

Solver( $n : \mathbb{N}$ ) *#n is the length of the sequences*

### 8.2 Uses

None

### 8.3 Syntax

#### 8.3.1 Exported Access Programs

Name	In	Out	Except.
solve	$\mathbf{f} : (\mathbb{R}^{n+1} \rightarrow \mathbb{R})^n, t_0 : \mathbb{R}, \mathbf{y}_0 : \mathbb{R}^n, g : \mathbb{R}^n \rightarrow \mathbb{R}, t_{\text{fin}} : \mathbb{R}$	$t_1 : \mathbb{R}, \mathbf{y} : (\mathbb{R} \rightarrow \mathbb{R})^n$	ODE_ERR, NO_EVENT
solveNoE	$\mathbf{f} : (\mathbb{R}^{n+1} \rightarrow \mathbb{R})^n, t_0 : \mathbb{R}, \mathbf{y}_0 : \mathbb{R}^n, t_{\text{fin}} : \mathbb{R}$	$\mathbf{y} : (\mathbb{R} \rightarrow \mathbb{R})^n$	ODE_ERR

### 8.4 Semantics

#### 8.4.1 State Variables

None

#### 8.4.2 Access Routine Semantics

*#Solving  $\frac{d}{dt}\mathbf{y} = \mathbf{f}(t, \mathbf{y}(t))$*

solve( $\mathbf{f}, t_0, \mathbf{y}_0, g, t_{\text{fin}}$ ):

- output:  $out := t_1, \mathbf{y}(t)$  where

$$\mathbf{y}(t) = \mathbf{y}_0 + \int_{t_0}^t \mathbf{f}(s, \mathbf{y}(s)) ds$$

with  $t_1$  determined by the first time where  $g(\mathbf{y}(t_1)) = 0$ .  $\mathbf{y}(t)$  is calculated from  $t = t_0$  to  $t = t_1$ .

- exception:  $exc := (\neg(\exists t : \mathbb{R} | t_0 \leq t \leq t_{\text{fin}} : g(\mathbf{y}(t)) = 0) \Rightarrow \text{NO\_EVENT} \mid \text{ODE Solver Fails} \Rightarrow \text{ODE\_ERR})$

solveNoE( $\mathbf{f}, t_0, \mathbf{y}_0, t_{\text{fin}}$ ):

- output:  $out := \mathbf{y}(t)$  where

$$\mathbf{y}(t) = \mathbf{y}_0 + \int_{t_0}^{t_{\text{fin}}} \mathbf{f}(s, \mathbf{y}(s)) ds$$

$y(t)$  is calculated from  $t = t_0$  to  $t = t_{\text{fin}}$ .

- exception:  $exc := (\text{ODE Solver Fails} \Rightarrow \text{ODE\_ERR})$

## 9 MIS of Energy Module

### 9.1 Module

Energy

### 9.2 Uses

Param (Section 6)

### 9.3 Syntax

#### 9.3.1 External Access Programs

Name	In	Out	Exceptions
energyWater	$\mathbb{R} \rightarrow \mathbb{R}$	$\mathbb{R} \rightarrow \mathbb{R}$	-
energySolidPCM	$\mathbb{R} \rightarrow \mathbb{R}$	$\mathbb{R} \rightarrow \mathbb{R}$	-
energyMeltingPCM	$\mathbb{R} \rightarrow \mathbb{R}$	$\mathbb{R} \rightarrow \mathbb{R}$	-
energyLiquidPCM	$\mathbb{R} \rightarrow \mathbb{R}$	$\mathbb{R} \rightarrow \mathbb{R}$	-

### 9.4 Semantics

#### 9.4.1 State Variables

None

#### 9.4.2 Assumptions

None

#### 9.4.3 Access Routine Semantics

energyWater( $T_W$ ):

- output:  $out := C_W m_W (T_W - T_{init})$
- exception: none

energySolidPCM( $T_P$ ):

- output:  $out := C_P^S m_P (T_P - T_{init})$
- exception: none

energyMeltingPCM( $Q_P$ ):

- output:  $out := E_{P_{\text{melt}}}^{\text{init}} + Q_P$
- exception: none

energyLiquidPCM( $T_P$ ):

- output:  $out := E_{P_{\text{melt}}}^{\text{init}} + H_f m_p + C_P^L m_P (T_P(t) - T_{\text{melt}}^P)$
- exception: none

## 10 MIS of Output Verification Module

### 10.1 Module

verify\_output

### 10.2 Uses

Param (Section 6)

### 10.3 Syntax

#### 10.3.1 Exported Constant

ADMIS\_ER =  $1 \times 10^{-6}$

#### 10.3.2 Exported Access Programs

Name	In	Out	Exceptions
verify_output	$T_W(t) : \mathbb{R} \rightarrow \mathbb{R}, T_P(t) : \mathbb{R} \rightarrow \mathbb{R}, E_W(t) : \mathbb{R} \rightarrow \mathbb{R}, E_P(t) : \mathbb{R} \rightarrow \mathbb{R}, t_{\text{final}} : \mathbb{R}$	-	EWAT_NOT_CONSERVE, EPCM_NOT_CONSERVE

### 10.4 Semantics

#### 10.4.1 State Variables

None

#### 10.4.2 Assumptions

All of the fields of the input parameters structure have been assigned a value.

#### 10.4.3 Access Routine Semantics

verify\_output( $T_W, T_P, E_W, E_P, t_{\text{final}}$ ):

- exception: exc := (

$(\forall t | 0 \leq t \leq t_{\text{final}} : \text{relErr}(E_W, \int_0^t h_C A_C (T_C - T_W(t)) dt - \int_0^t h_P A_P (T_W(t) - T_P(t)) dt) < \text{ADMIS\_ER}) \Rightarrow \text{EWAT\_NOT\_CONSERVE}$

|  
 $(\forall t | 0 \leq t \leq t_{\text{final}} : \text{relErr}(E_P, \int_0^t h_P A_P (T_W(t) - T_P(t)) dt) < \text{ADMIS\_ER}) \Rightarrow \text{EPCM\_NOT\_CONSERVE}$   
)

#### 10.4.4 Local Functions

relErr:  $\mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$

$\text{relErr}(t, e) \equiv \frac{|t-e|}{|t|}$

# 11 MIS of Plotting Module

## 11.1 Module

plot

## 11.2 Uses

N/A

## 11.3 Syntax

### 11.3.1 Exported Access Programs

Name	In	Out	Exceptions
plot	$T_W(t) : \mathbb{R} \rightarrow \mathbb{R}, T_P(t) : \mathbb{R} \rightarrow \mathbb{R}, E_W(t) : \mathbb{R} \rightarrow \mathbb{R}, E_P(t) : \mathbb{R} \rightarrow \mathbb{R}, t_{\text{final}} : \mathbb{R}$	-	-

## 11.4 Semantics

### 11.4.1 State Variables

None

### 11.4.2 Environment Variables

win: 2D sequence of pixels displayed on the screen

### 11.4.3 Assumptions

None

### 11.4.4 Access Routine Semantics

plot( $T_w, T_p, E_w, E_p, t_{\text{final}}$ ):

- transition: Modify win to display a plot where the vertical axis is time and one horizontal axis is temperature and the other horizontal axis is energy. The time should run from 0 to  $t_{\text{final}}$
- exception: none

## 12 MIS of Output Module

### 12.1 Module

output

### 12.2 Uses

Param (Section 6)

### 12.3 Syntax

#### 12.3.1 Exported Constants

*max\_width*: integer

#### 12.3.2 Exported Access Program

Name	In	Out	Exceptions
output	fname: string, $T_W(t) : \mathbb{R} \rightarrow \mathbb{R}$ , $T_P(t) : \mathbb{R} \rightarrow \mathbb{R}$ , $E_W(t) : \mathbb{R} \rightarrow \mathbb{R}$ , $E_P(t) : \mathbb{R} \rightarrow \mathbb{R}$ , $t_{\text{final}} : \mathbb{R}$	-	-

### 12.4 Semantics

#### 12.4.1 State Variables

None

#### 12.4.2 Environment Variables

file: A text file

#### 12.4.3 Access Routine Semantics

output(fname,  $T_w$ ,  $T_p$ ,  $E_w$ ,  $E_p$ ,  $t_{\text{final}}$ ):

- transition: Write to environment variable named fname the following: the input parameters from Param, and the calculated values  $T_w$ ,  $T_p$ ,  $E_w$ ,  $E_p$  from times 0 to  $t_{\text{final}}$ . The functions will be output as sequences in this file. The spacing between points in the sequence should be selected so that the heating behaviour is captured in the data.
- exception: none



## 13 MIS of Specification Parameters

The secrets of this module is the value of the specification parameters.

### 13.1 Module

SpecParam

### 13.2 Uses

N/A

### 13.3 Syntax

#### 13.3.1 Exported Constants

# From Table 2 in SRS

$L_{\min} := 0.1$

$L_{\max} := 50$

$\frac{D}{L}_{\min} := 0.002$

$\frac{D}{L}_{\max} := 200$

$\text{minfrac} := 10^{-6}$

$h_{\min} := 0.001$

$\rho_P^{\min} := 500$

$\rho_P^{\max} := 20000$

$C_{P_{\min}}^S := 100$

$C_{P_{\max}}^S := 4000$

$C_{P_{\min}}^L := 100$

$C_{P_{\max}}^L := 5000$

$A_C^{\max} := \pi(\frac{D}{2})^2$

$\rho_W^{\min} := 950$

$\rho_W^{\max} := 1000$

$C_W^{\min} := 4170$

$C_W^{\max} := 4210$

$h_C^{\min} := 10$

$h_C^{\max} := 10000$

$h_P^{\min} := 10$

$h_P^{\max} := 10000$

$t_{\text{final}}^{\max} := 86400$

$A_C^{\max}$  shouldn't be in this table of constants —SS]

## 13.4 Semantics

N/A

## 14 Appendix

Table 2: Possible Exceptions

Message ID	Error Message
badLength	Error: Tank length must be $> 0$
badDiam	Error: Tank diameter must be $> 0$
badPCMVolume	Error: PCM volume must be $> 0$
badPCMAndTankVol	Error: PCM volume must be $<$ tank volume
badPCMArea	Error: PCM area must be $> 0$
badPCMDensity	Error: $\rho_p$ must be $> 0$
badMeltTemp	Error: $T_{melt}$ must be $> 0$ and $< T_c$
badCoilAndInitTemp	Error: $T_c$ must be $> T_{init}$
badCoilTemp	Error: $T_c$ must be $> 0$ and $< 100$
badPCMHeatCapSolid	Error: $C_{ps}$ must be $> 0$
badPCMHeatCapLiquid	Error: $C_{pl}$ must be $> 0$
badHeatFusion	Error: $H_f$ must be $> 0$
badCoilArea	Error: $A_c$ must be $> 0$
badWaterDensity	Error: $\rho_w$ must be $> 0$
badWaterHeatCap	Error: $C_w$ must be $> 0$
badCoilCoeff	Error: $h_c$ must be $> 0$
badPCMCoeff	Error: $h_p$ must be $> 0$
badInitTemp	Error: $T_{init}$ must be $> 0$ and $< 100$
badFinalTime	Error: $t_{final}$ must be $> 0$
badInitAndMeltTemp	Error: $T_{init}$ must be $< T_{melt}$
ODE_ACCURACY	$reltol$ and $abstol$ were not satisfied by the ODE solver for a given solution step.
ODE_BAD_INPUT	Invalid input to ODE solver
ODE_MAXSTEP	ODE solver took $MaxStep$ steps and did not find solution
warnLength	Warning: It is recommended that $0.1 \leq L \leq 50$
warnDiam	Warning: It is recommended that $0.002 \leq D/L \leq 200$
warnPCMVol	Warning: It is recommended that $V_p$ be $\geq 0.0001\%$ of $V_t$
warnVolArea	Warning: It is recommended that $V_p \leq A_p \leq (2/0.001) * V_p$
warnPCMDensity	Warning: It is recommended that $500 < \rho_p < 20000$
warnPCMHeatCapSolid	Warning: It is recommended that $100 < C_{ps} < 4000$

warnPCMHeatCapLiquid	Warning: It is recommended that $100 < C_{pl} < 5000$
warnCoilArea	Warning: It is recommended that $Ac \leq \pi * (D/2)^2$
warnWaterDensity	Warning: It is recommended that $950 < \rho_w \leq 1000$
warnWaterHeatCap	Warning: It is recommended that $4170 < C_w < 4210$
warnCoilCoeff	Warning: It is recommended that $10 < hc < 10000$
warnPCMCoeff	Warning: It is recommended that $10 < hp < 10000$
warnFinalTime	Warning: It is recommended that $0 < t_{final} < 86400$
warnWaterError	Warning: There is greater than $x\%$ relative error between the energy in the water output and the expected output based on the law of conservation of energy. (Where $x$ is the value of <i>ConsTol</i> )
warnPCMError	Warning: There is greater than $x\%$ relative error between the energy in the PCM output and the expected output based on the law of conservation of energy. (Where $x$ is the value of <i>ConsTol</i> )

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