

version 0.1.0

## Title

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**persuasio4yz** — Conducts causal inference on persuasive effects for binary outcomes *y* and binary instruments *z*

## Syntax

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```
persuasio4yz depvar instrvar [covariates] [if] [in] [, level(#)  
model(string) method(string) nboot(#) title(string)]
```

## Options

<i>option</i>	<i>Description</i>
<b>level</b> (#)	Set confidence level; default is <b>level</b> (95)
<b>model</b> ( <i>string</i> )	Regression model when <i>covariates</i> are present; default > <i>t</i> is "no_interaction"
<b>method</b> ( <i>string</i> )	Inference method; default is <b>method</b> ("normal")
<b>nboot</b> (#)	Perform # bootstrap replications; default is <b>nboot</b> (5 > 0)
<b>title</b> ( <i>string</i> )	Title of estimation

## Description

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**persuasio4yz** conducts causal inference on persuasive effects for binary outcomes *y* and binary instruments *z*.

This command is for the case when persuasive treatment (*t*) is unobserved, using estimates of the lower bound on the average persuasion rate (APR) via this package's command **aprlb**.

*varlist* should include *depvar instrvar covariates* in order. Here, *depvar* is binary outcomes (*y*), *instrvar* is binary instruments (*z*), and *covariates* (*x*) are optional.

When treatment *t* is unobserved, the upper bound on the APR is just 1.

There are two cases: (i) *covariates* are absent and (ii) *covariates* are present.

- If *covariates* are absent, the lower bound (*theta\_L*) on the APR is defined by

$$\text{theta\_L} = \{\text{Pr}(y = 1 \mid z = 1) - \text{Pr}(y = 1 \mid z = 0)\} / \{1 - \text{Pr}(y = 1 \mid z = 0)\}.$$

The estimate and confidence interval are obtained by the following procedure:

1.  $\text{Pr}(y = 1 \mid z = 1)$  and  $\text{Pr}(y = 1 \mid z = 0)$  are estimated by regressing  $y$  on  $z$ .
2. The lower bound on the APR is computed using the estimates obtained above.
3. The standard error of the estimate is computed via STATA command **nlcom**.
4. Then, a confidence interval for the APR is set by  $[est - cv * se, est + cv * se]$ , where  $est$  is the estimate,  $se$  is the standard error, and  $cv$  is the one-sided standard normal critical value (e.g.,  $cv = 1.645$  for **level(95)**).

- If *covariates* are present, the lower bound ( $\text{theta\_L}$ ) on the APR is defined by

$$\text{theta\_L} = E[\text{theta\_L}(x)],$$

where

$$\text{theta\_L}(x) = \{\text{Pr}(y = 1 \mid z = 1, x) - \text{Pr}(y = 1 \mid z = 0, x)\} / \{1 - \text{Pr}(y = 1 \mid z = 0, x)\}.$$

The estimate and confidence interval are obtained by the following procedure.

If **model("no\_interaction")** is selected (default choice),

1.  $\text{Pr}(y = 1 \mid z, x)$  is estimated by regressing  $y$  on  $z$  and  $x$ .

Alternatively, if **model("interaction")** is selected,

- 1a.  $\text{Pr}(y = 1 \mid z = 1, x)$  is estimated by regressing  $y$  on  $x$  given  $z = 1$ .
- 1b.  $\text{Pr}(y = 1 \mid z = 0, x)$  is estimated by regressing  $y$  on  $x$  given  $z = 0$ .

After step 1, both options are followed by:

2. For each  $x$  in the estimation sample,  $\theta_L(x)$  is computed using the estimates obtained above.

3. The estimates of  $\theta_L(x)$  are averaged to obtain the estimate of  $\theta_L$ .

4. A bootstrap confidence interval for the APR is set by  $[\text{bs\_est}(\alpha), 1]$ , where  $\text{bs\_est}(\alpha)$  is the  $\alpha$  quantile of the bootstrap estimates of  $\theta_L$  and  $1 - \alpha$  is the confidence level.

The bootstrap procedure is implemented via STATA command **bootstrap**.

### Options

**model**(string) specifies a regression model of  $y$  on  $z$  and  $x$  when *covariates* are present.

The default option is "no\_interaction" between  $z$  and  $x$ . When "interaction" is selected, full interactions between  $z$  and  $x$  are allowed; this is accomplished by estimating  $\Pr(y = 1 \mid z = 1, x)$  and  $\Pr(y = 1 \mid z = 0, x)$ , separately.

**level**(#) sets confidence level; default is **level**(95).

**method**(string) refers the method for inference; default is **method**("normal")  
 > .  
 By the nature of identification, one-sided confidence intervals are produced  
 > .

1. When *covariates* are present, it needs to be set as **method**("bootstrap"); otherwise, the confidence interval will be missing.

2. When *covariates* are absent, both options "normal" and "bootstrap" yield non-missing confidence intervals.

**nboot**(#) chooses the number of bootstrap replications; default is **nboot**(50)  
 > .  
 It is only relevant when **method**("bootstrap") is selected.

**title**(string) specifies the title of estimation.

### Remarks

It is recommended to use `nboot(#)` with `#` at least 1000. A default choice of 50 is meant to check the code initially because it may take a long time to run the bootstrap part when there are a large number of covariates. The bootstrap confidence interval is based on percentile bootstrap. A use of normality-based bootstrap confidence interval is not recommended because bootstrap standard errors can be unreasonably large in applications.

## **Examples**

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We first call the dataset included in the package.

```
. use GKB, clear
```

The first example conducts inference on the APR without covariates, using normal approximation.

```
. persuasio4yz voteddem_all post, level(80) method("normal")
```

The second example conducts bootstrap inference on the APR.

```
. persuasio4yz voteddem_all post, level(80) method("bootstrap")  
nboot(1000)
```

The third example conducts bootstrap inference on the APR with a covariate, `MZwave2`, interacting with the instrument, `post`.

```
. persuasio4yz voteddem_all post MZwave2, level(80)  
model("interaction") method("bootstrap") nboot(1000)
```

The fourth example consider a large number of covariates. This example runs slower than the previous example.

```
. persuasio4yz voteddem_all post doperator*, level(80)  
method("bootstrap") nboot(1000)
```

## **Stored results**

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### **Matrices**

**e(lb\_est):** (1\*2 matrix) bounds on the average persuasion rate in the form of `[lb, 1]`

**e(lb\_ci):** (1\*2 matrix) confidence interval for the average persuasion rate in the form of `[lb_ci, 1]`

## **Macros**

**e(cilevel):** confidence level

**e(inference\_method):** inference method: "normal" or "bootstrap"

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## **License**

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GPL-3

## **References**

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Sung Jae Jun and Sokbae Lee (2019), Identifying the Effect of Persuasion, [arXiv:1812.02276](https://arxiv.org/abs/1812.02276) [[econ.EM](#)]