



AP[®] Physics C: Mechanics 2012 Free-Response Questions

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TABLE OF INFORMATION DEVELOPED FOR 2012

CONSTANTS AND CONVERSION FACTORS	
Proton mass, $m_p = 1.67 \times 10^{-27}$ kg	Electron charge magnitude, $e = 1.60 \times 10^{-19}$ C
Neutron mass, $m_n = 1.67 \times 10^{-27}$ kg	1 electron volt, $1 \text{ eV} = 1.60 \times 10^{-19}$ J
Electron mass, $m_e = 9.11 \times 10^{-31}$ kg	Speed of light, $c = 3.00 \times 10^8$ m/s
Avogadro's number, $N_0 = 6.02 \times 10^{23}$ mol ⁻¹	Universal gravitational constant, $G = 6.67 \times 10^{-11}$ m ³ /kg·s ²
Universal gas constant, $R = 8.31$ J/(mol·K)	Acceleration due to gravity at Earth's surface, $g = 9.8$ m/s ²
Boltzmann's constant, $k_B = 1.38 \times 10^{-23}$ J/K	
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27}$ kg = $931 \text{ MeV}/c^2$
Planck's constant,	$h = 6.63 \times 10^{-34}$ J·s = 4.14×10^{-15} eV·s
	$hc = 1.99 \times 10^{-25}$ J·m = 1.24×10^3 eV·nm
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12}$ C ² /N·m ²
Coulomb's law constant, $k = 1/4\pi\epsilon_0 = 9.0 \times 10^9$ N·m ² /C ²	
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7}$ (T·m)/A
Magnetic constant, $k' = \mu_0/4\pi = 1 \times 10^{-7}$ (T·m)/A	
1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5$ N/m ² = 1.0×10^5 Pa

UNIT SYMBOLS	meter,	m	mole,	mol	watt,	W	farad,	F
	kilogram,	kg	hertz,	Hz	coulomb,	C	tesla,	T
	second,	s	newton,	N	volt,	V	degree Celsius,	°C
	ampere,	A	pascal,	Pa	ohm,	Ω	electron-volt,	eV
	kelvin,	K	joule,	J	henry,	H		

PREFIXES		
Factor	Prefix	Symbol
10^9	giga	G
10^6	mega	M
10^3	kilo	k
10^{-2}	centi	c
10^{-3}	milli	m
10^{-6}	micro	μ
10^{-9}	nano	n
10^{-12}	pico	p

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES							
θ	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1
$\cos \theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0
$\tan \theta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	∞

The following conventions are used in this exam.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.

ADVANCED PLACEMENT PHYSICS C EQUATIONS DEVELOPED FOR 2012

MECHANICS		ELECTRICITY AND MAGNETISM	
$v = v_0 + at$	$a = \text{acceleration}$	$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$	$A = \text{area}$
$x = x_0 + v_0 t + \frac{1}{2} at^2$	$F = \text{force}$	$\mathbf{E} = \frac{\mathbf{F}}{q}$	$B = \text{magnetic field}$
$v^2 = v_0^2 + 2a(x - x_0)$	$f = \text{frequency}$	$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$	$C = \text{capacitance}$
$\Sigma \mathbf{F} = \mathbf{F}_{net} = m\mathbf{a}$	$h = \text{height}$	$E = -\frac{dV}{dr}$	$d = \text{distance}$
$\mathbf{F} = \frac{d\mathbf{p}}{dt}$	$I = \text{rotational inertia}$	$V = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i}$	$E = \text{electric field}$
$\mathbf{J} = \int \mathbf{F} dt = \Delta \mathbf{p}$	$J = \text{impulse}$	$U_E = qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$	$\mathcal{E} = \text{emf}$
$\mathbf{p} = m\mathbf{v}$	$K = \text{kinetic energy}$	$C = \frac{Q}{V}$	$F = \text{force}$
$F_{fric} \leq \mu N$	$k = \text{spring constant}$	$C = \frac{\kappa \epsilon_0 A}{d}$	$I = \text{current}$
$W = \int \mathbf{F} \cdot d\mathbf{r}$	$\ell = \text{length}$	$C_p = \sum_i C_i$	$J = \text{current density}$
$K = \frac{1}{2} mv^2$	$L = \text{angular momentum}$	$\frac{1}{C_s} = \sum_i \frac{1}{C_i}$	$L = \text{inductance}$
$P = \frac{dW}{dt}$	$m = \text{mass}$	$I = \frac{dQ}{dt}$	$\ell = \text{length}$
$P = \mathbf{F} \cdot \mathbf{v}$	$N = \text{normal force}$	$U_c = \frac{1}{2} QV = \frac{1}{2} CV^2$	$n = \text{number of loops of wire per unit length}$
$\Delta U_g = mgh$	$P = \text{power}$	$\oint \mathbf{B} \cdot d\boldsymbol{\ell} = \mu_0 I$	$N = \text{number of charge carriers per unit volume}$
$a_c = \frac{v^2}{r} = \omega^2 r$	$p = \text{momentum}$	$R = \frac{\rho \ell}{A}$	$P = \text{power}$
$\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F}$	$r = \text{radius or distance}$	$\mathbf{E} = \rho \mathbf{J}$	$Q = \text{charge}$
$\Sigma \boldsymbol{\tau} = \boldsymbol{\tau}_{net} = I\boldsymbol{\alpha}$	$\mathbf{r} = \text{position vector}$	$I = Nev_d A$	$q = \text{point charge}$
$I = \int r^2 dm = \Sigma mr^2$	$T = \text{period}$	$V = IR$	$R = \text{resistance}$
$\mathbf{r}_{cm} = \Sigma m\mathbf{r} / \Sigma m$	$U = \text{potential energy}$	$R_s = \sum_i R_i$	$r = \text{distance}$
$v = r\omega$	$\nu = \text{velocity or speed}$	$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$	$t = \text{time}$
$\mathbf{L} = \mathbf{r} \times \mathbf{p} = I\boldsymbol{\omega}$	$W = \text{work done on a system}$	$P = IV$	$U = \text{potential or stored energy}$
$K = \frac{1}{2} I\omega^2$	$x = \text{position}$	$\mathbf{F}_M = q\mathbf{v} \times \mathbf{B}$	$V = \text{electric potential}$
$\omega = \omega_0 + \alpha t$	$\mu = \text{coefficient of friction}$		$\nu = \text{velocity or speed}$
$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$	$\theta = \text{angle}$		$\rho = \text{resistivity}$
	$\tau = \text{torque}$		$\phi_m = \text{magnetic flux}$
	$\omega = \text{angular speed}$		$\kappa = \text{dielectric constant}$
	$\alpha = \text{angular acceleration}$		
	$\phi = \text{phase angle}$		
	$\mathbf{F}_s = -k\mathbf{x}$		
	$U_s = \frac{1}{2} kx^2$		
	$x = x_{\max} \cos(\omega t + \phi)$		
	$T = \frac{2\pi}{\omega} = \frac{1}{f}$		
	$T_s = 2\pi \sqrt{\frac{m}{k}}$		
	$T_p = 2\pi \sqrt{\frac{\ell}{g}}$		
	$\mathbf{F}_G = -\frac{Gm_1 m_2}{r^2} \hat{\mathbf{r}}$		
	$U_G = -\frac{Gm_1 m_2}{r}$		

ADVANCED PLACEMENT PHYSICS C EQUATIONS DEVELOPED FOR 2012

GEOMETRY AND TRIGONOMETRY

Rectangle

$$A = bh$$

Triangle

$$A = \frac{1}{2}bh$$

Circle

$$A = \pi r^2$$

$$C = 2\pi r$$

Rectangular Solid

$$V = \ell wh$$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r \ell + 2\pi r^2$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

$$S = 4\pi r^2$$

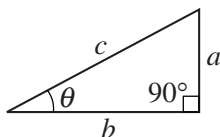
Right Triangle

$$a^2 + b^2 = c^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$



A = area

C = circumference

V = volume

S = surface area

b = base

h = height

ℓ = length

w = width

r = radius

CALCULUS

$$\frac{df}{dx} = \frac{df}{du} \frac{du}{dx}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, n \neq -1$$

$$\int e^x dx = e^x$$

$$\int \frac{dx}{x} = \ln|x|$$

$$\int \cos x dx = \sin x$$

$$\int \sin x dx = -\cos x$$

2012 AP[®] PHYSICS C: MECHANICS FREE-RESPONSE QUESTIONS

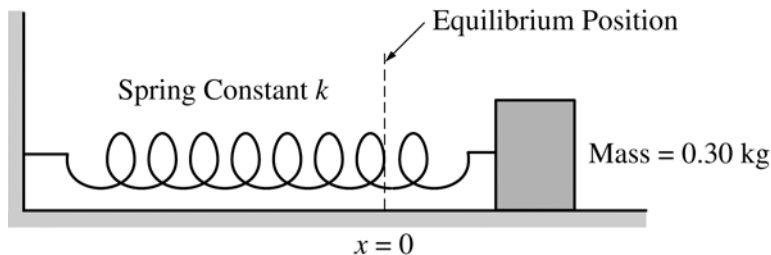
PHYSICS C: MECHANICS

SECTION II

Time—45 minutes

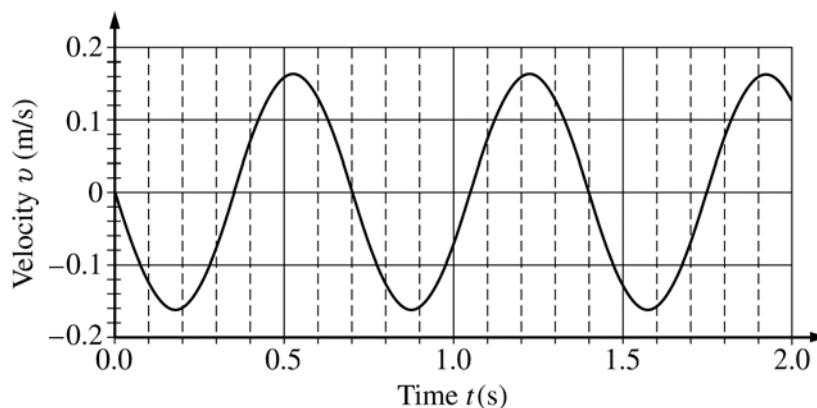
3 Questions

Directions: Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Mech. 1.

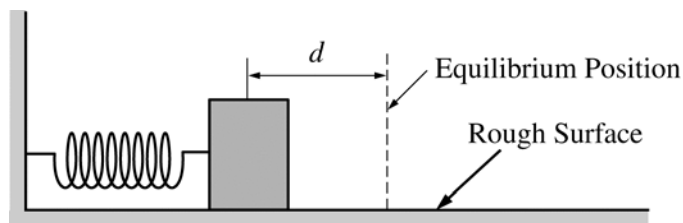
Experiment 1. A block of mass 0.30 kg is placed on a frictionless table and is attached to one end of a horizontal spring of spring constant k , as shown above. The other end of the spring is attached to a fixed wall. The block is set into oscillatory motion by stretching the spring and releasing the block from rest at time $t = 0$. A motion detector is used to record the position of the block as it oscillates. The resulting graph of velocity v versus time t is shown below. The positive direction for all quantities is to the right.



- Determine the equation for $v(t)$, including numerical values for all constants.
- Given that the equilibrium position is at $x = 0$, determine the equation for $x(t)$, including numerical values for all constants.
- Calculate the value of k .

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Experiment 2. The block and spring arrangement is now placed on a rough surface, as shown below. The block is displaced so that the spring is compressed a distance d and released from rest.



- (d) On the dots below that represent the block, draw and label the forces (not components) that act on the block when the spring is compressed a distance $x = d/2$ and the block is moving in the direction indicated below each dot.

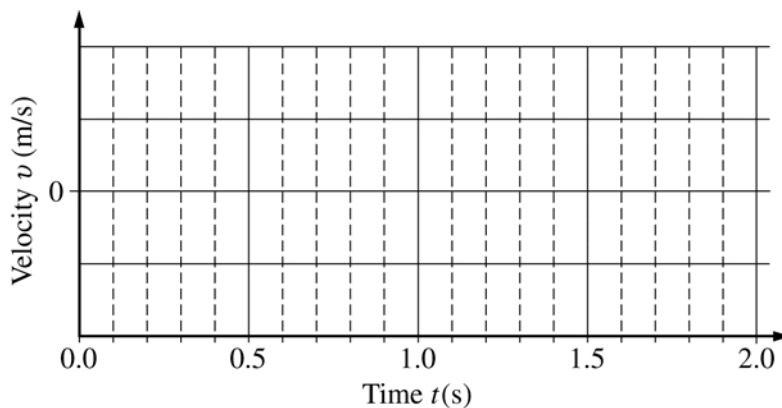


Toward
the equilibrium position



Away from
the equilibrium position

- (e) Draw a sketch of v versus t in this case. Assume that there is a negligible change in the period and that the positive direction is still to the right.



2012 AP[®] PHYSICS C: MECHANICS FREE-RESPONSE QUESTIONS

Mech. 2.

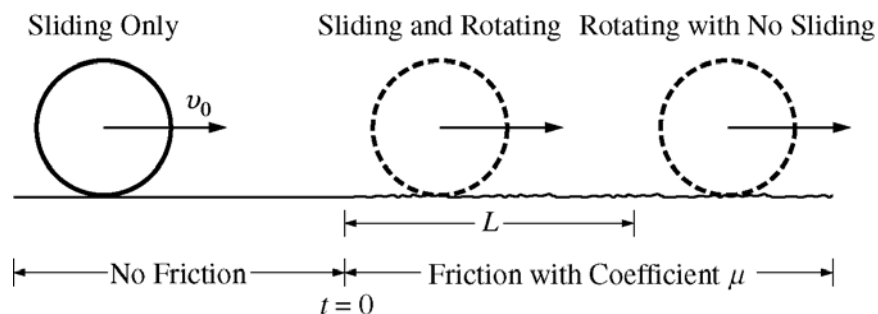
You are to perform an experiment investigating the conservation of mechanical energy involving a transformation from initial gravitational potential energy to translational kinetic energy.

- (a) You are given the equipment listed below, all the supports required to hold the equipment, and a lab table. On the list below, indicate each piece of equipment you would use by checking the line next to each item.

<input type="checkbox"/> Track	<input type="checkbox"/> Meterstick	<input type="checkbox"/> Set of objects of different masses
<input type="checkbox"/> Cart	<input type="checkbox"/> Electronic balance	<input type="checkbox"/> Lightweight low-friction pulley
<input type="checkbox"/> String	<input type="checkbox"/> Stopwatch	

- (b) Outline a procedure for performing the experiment. Include a diagram of your experimental setup. Label the equipment in your diagram. Also include a description of the measurements you would make and a symbol for each measurement.
- (c) Give a detailed account of the calculations of gravitational potential energy and translational kinetic energy both before and after the transformation, in terms of the quantities measured in part (b).
- (d) After your first trial, your calculations show that the energy increased during the experiment. Assuming you made no mathematical errors, give a reasonable explanation for this result.
- (e) On all other trials, your calculations show that the energy decreased during the experiment. Assuming you made no mathematical errors, give a reasonable physical explanation for the fact that the average energy you determined decreased. Include references to conservative and nonconservative forces, as appropriate.

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Mech. 3.

A ring of mass M , radius R , and rotational inertia MR^2 is initially sliding on a frictionless surface at constant velocity v_0 to the right, as shown above. At time $t = 0$ it encounters a surface with coefficient of friction μ and begins sliding and rotating. After traveling a distance L , the ring begins rolling without sliding. Express all answers to the following in terms of M , R , v_0 , μ , and fundamental constants, as appropriate.

- (a) Starting from Newton's second law in either translational or rotational form, as appropriate, derive a differential equation that can be used to solve for the magnitude of the following as the ring is sliding and rotating.
 - i. The linear velocity v of the ring as a function of time t
 - ii. The angular velocity ω of the ring as a function of time t
- (b) Derive an expression for the magnitude of the following as the ring is sliding and rotating.
 - i. The linear velocity v of the ring as a function of time t
 - ii. The angular velocity ω of the ring as a function of time t
- (c) Derive an expression for the time it takes the ring to travel the distance L .
- (d) Derive an expression for the magnitude of the velocity of the ring immediately after it has traveled the distance L .
- (e) Derive an expression for the distance L .

STOP

END OF EXAM