The 'pst-3d' package Tilting and other pseudo-3D tricks with PSTricks

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 $Version \ 1.00 \ 2005/09/03$ Documentation revised September 10, 2005 (hv)

Abstract

 ${\tt pst-3d}$ provides basic macros for shadows, tilting and three dimensional representations of text or graphical objects.

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1 introduction

The base package pstricks already disposes of some macros with which three dimensional effects can be obtained. There are several packages though which support the creation of three dimensional objects or functions. A compilation is shown in table 1. Here already several of the packages overlap, for parallel developments are nothing unusual in the TeX world. Although pst-3d is one of the older packages, it shall be dealt with nevertheless, for it also contains the preliminary stage of the 3D representations, that is shadow creation and tilting.

Table 1: Summary of all 3D packages

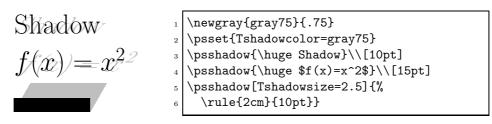
$_package$	content
pst-3d	basic 3D operations
pst-3dplot	Three dimensional plots
pst-fr3d	Three dimensional framed Boxes
pst-gr3d	3D grids
pst-map3dII	3D Geographical Projection
pst-ob3d	Three dimensional basic objects
pst-vue3d	Three dimensional views

2 Shadow

pst-3d defines the macro \psshadow with the following syntax:

\psshadow[<parameters>]{<material>]

As parameters the ones given in table 2 are available next to all previously defined, if they have a meaning for the material to be shadowed. This can be anything text-like, text, rules and mathematical expressions in inline mode.



2.1 Parameters

Table 2 shows a compilation of the used parameters.

Table 2: Summary of all shadow parameters

name	values	de fault
Tshadowangle	<angle></angle>	60
Tshadowcolor	<colour></colour>	lightgray
Tshadowsize	<value></value>	1

2.1.1 Tshadowangle

Tshadowangle denotes the angle of the shadow, referring to the perpendicular of the paper plane. The angle of 90r therewith corresponds to the text itself. Negative angles cause the shadow to arise from the paper plane.

```
Shadow | \newgray{gray75}\{.75\} \psset{Tshadowcolor=gray75\} \psshadow{\huge shadow}\\[5pt] \psshadow[Tshadowangle=30]\{\huge shadow}\\[5pt] \psshadow[Tshadowangle=70]\{\huge shadow}\\[5pt] \psshadow[Tshadowangle=-30]\{\huge shadow}\}
```

• Angular values of 0ř and 180ř are not allowed.

2.1.2 Tshadowcolor

Tshadowcolor deontes the shadow colour.

```
Shadow

shadow

psshadow{\huge shadow}\\[5pt]

psshadow[Tshadowcolor=red]{\huge shadow}\\[5pt]

psshadow[Tshadowcolor=green]{\huge shadow}\\[5pt]

psshadow[Tshadowcolor=blue]{\huge shadow}
```

2.1.3 Tshadowsize

Tshadowsize determines the size of the shadow as a scaling factor.

```
Shadow

Shadow

| \pshadow{\Huge shadow}\\[5pt] \pshadow{\Tshadowsize=0.5]{\Huge shadow}\\[10pt] \pshadow[Tshadowsize=1.5]{\Huge shadow}\\[20pt] \pshadow[Tshadowsize=2.5]{\Huge shadow}\\[20pt] \pshadow[Tshadowsize=2.5]{\Huge shadow}
```

3 Tilting

With the tilting of objects the perspective views of three dimensional objects can be simulated. pst-3d defines two macros for this.

```
\pstilt[<parameters>]{<angle>}{<material>}
\psTilt[<parameters>]{<angle>}{<material>}
```

Figure 1 shows the difference between these two macros. Principally everything can be given as argument to those macros and therewith tilted. With vertical material, as distinguished formulae, eventually the argument has to be put into a \parbox before (see example),

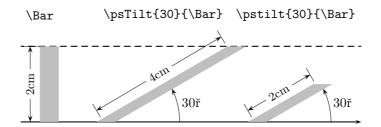
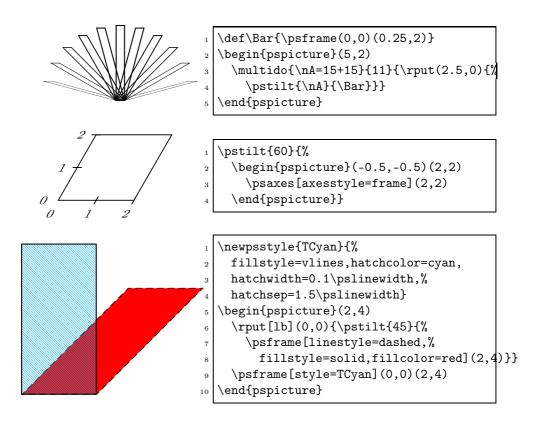


Figure 1: Demonstration of the difference between \pstilt and \psTilt

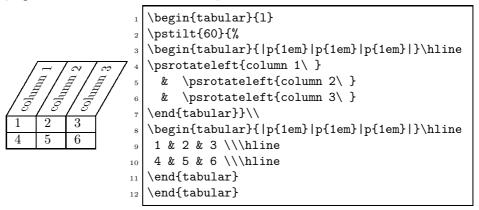
• Angular values of 0° and 180° are not allowed.

3.1 \pstilt

\pstilt tilts objects that their original height appears as new length of the tilted object, wherewith the object becomes smaller. The hynotenuse of the triangle from nadir, height and perpendicular now corresponds to the old height (see figure 1). At this the length is calculated from the middle of the base side.



With the package rotating macros to rotate text are provided, to achieve slant table headings for example. It is more difficult when they are provided with a frame. With \pstilt or \psTilt this is no problem. The program listing given below only shows the application of \pstilt for the macro only has to be replaced by \psTilt to obtain the other example.



3.2 \psTilt

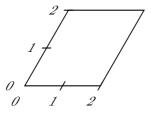
\psTilt tilts objects that their original height is preserved, so that the object could become infinitely long in theory (see figure 1).

```
begin{pspicture}(5,2)

def\Bar{\psframe(0,0)(0.25,2)}

multido{\nA=15+15}{11}{\rput(2.5,0){%}

psTilt{\nA}{\Bar}}}
bend{pspicture}
```



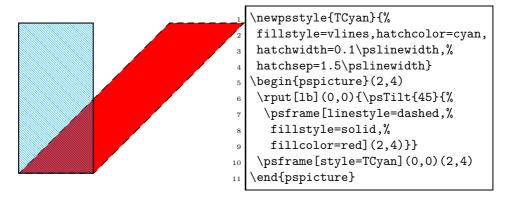
```
\psTilt{60}{%

begin{pspicture}(-0.5,-0.5)(2,2)

psaxes[axesstyle=frame](2,2)

end{pspicture}}

\[
\]
```



4 Three dimensional representations¹

pst-3d only supports parallel projections, so that geometrical objects such as spheres or cylinders can only be displayed restricted. Although pst-3d principally only defines one single macro for the 3D projection, the package is very efficient in its application and is also used as a base for other packages. [?][?]

4.1 \ThreeDput

pst-3d only defines this single macro, which can be used to arbitrarily display line or area shaped objects in the three dimensional space in the end though.

```
\ThreeDput[<parameters>] {<material>}
\ThreeDput[<parameters>] (<x,y,z>) {<material>}
```

Without a specification of coordinates, (0,0,0) is taken as origin of ordinates as a rule. As "material" anything is understood that can be put into a box. If it is vertical material in the T_EX sense, it has to be put in a \parbox or minipage before.

To simplify the specified source code, the macro \IIIDKOSystem is used in the following, which draws the coordinate axes with the grid and is not specified in the following anymore.

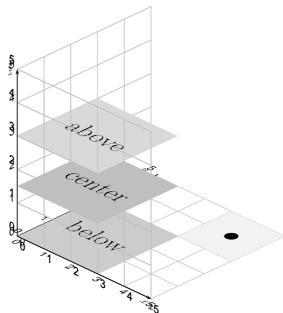
newgraygray850.85

```
makeatletter
def\xyPlain#1{%

ThreeDput[normal=0 0 1](0,0,0){% xy-plane
psgrid[subgriddiv=0,gridcolor=lightgray](0,0)(#1,#1)
```

¹Some of the examples were created by Manuel Luque.

```
psline{->}(0,0)(0,#1) psline{->}(0,0)(#1,0)
     \ifdim\psk@gridlabels pt>\z@
6
        \displaystyle \left[180] \{0.2\} (0,\#1) \{\$y\$\} \left[-90] \{0.2\} (\#1,0) \{\$x\$\} \right] 
7
   \def\xzPlain#1{%
   ThreeDput[normal=0 -1 0](0,0,0){\% xz-plane}
     \psgrid[subgriddiv=0,gridcolor=lightgray](0,0)(#1,#1)
10
     psline{->}(0,0)(0,5) psline{->}(0,0)(#1,0)
11
     \ifdim\psk@gridlabels pt>\z@
12
       \t [180] {0.2} (0,#1) {$z$} \t [-90] {0.2} (#1,0) {$x$}%
13
    \fi }}
14
  \def\yzPlain#1{%
15
   ThreeDput[normal=1 0 0](0,0,0){\% yz-plane}
16
     \psgrid[subgriddiv=0,gridcolor=lightgray](0,0)(#1,#1)
17
    psline{->}(0,0)(0,#1) psline{->}(0,0)(#1,0)
18
    \ifdim\psk@gridlabels pt>\z@
       \uput[180]{0.2}(0,#1){$z$}\uput[-90]{0.2}(#1,0){$y$}%
20
    \fi }}
21
  \def\IIIDKOSystem{\@ifnextchar[{\IIIDKOSystem@i}{\IIIDKOSystem@i[]}}
  \def\IIIDKOSystem@i[#1]#2{%
   \psset{#1}%
24
   \xyPlain{#2}\xzPlain{#2}\yzPlain{#2}}
25
26 \makeatother
27 \newgray{gray75}{0.75}
  \newgray{gray80}{0.8}
  \newgray{gray85}{0.85}
  \newgray{gray95}{0.95}
  \begin{pspicture}(0,-1.25)(5,6)
   \psset{viewpoint=1 -1 0.75}
32
   \IIIDKOSystem{5}
33
   \ThreeDput{\psframe*[linecolor=gray80](3,3)}
   \ThreeDput(1.5,1.5,0){\Huge below}
   \ThreeDput(0,0,1.5){\psframe*[linecolor=gray75](3,3)}
36
   \ThreeDput(1.5,1.5,1.5){\Huge center}
37
   \ThreeDput(0,0,3){\psframe*[linecolor=gray85](3,3)}
   \ThreeDput(1.5,1.5,3){\Huge above}
   \xzPlain{5}
40
   \label{linecolor} $$ \ThreeDput(4,4,0){\operatorname{\psframe}}(-1,-1)(1,1)$ }
   \ThreeDput(4,4,0){\psdot[dotscale=3]}
  \end{pspicture}
```



The coordinates of ThreeDput refer to the centre of the object, which does not necessarily need to be the geometrical centre.

```
\psframe(2,2)% centre bottom left (0,0)
\psframe(-1,-1(1,1)% centre in the middle (0,0)
arbitrary text% centre in the middle of the base line
```

In the above example the smaller square with its centre (0,0) has been set exactly to the coordinated (4,4,0). The macro ThreeDput can be manifoldly applied, which is performed especially by the package pst-vue3d[?]. By specifying the normal vector \vec{n} and a point P(x,y,z) of the stright line and/or the plane the posture in space can be determined definitely. Areas can be provided with different levels of brightness to increase the spatial impression.

```
\newgray{gray75}{0.75}\newgray{gray85}{0.85}\newgray{gray95}{0.95}

begin{pspicture}(-4.5,-3.5)(3,4.75)

\psset{viewpoint=1 1.5 1}

\IIIDKOSystem[gridlabels=0pt,gridcolor=lightgray,subgriddiv=0]{5}%

\ThreeDput[normal=0 0 1]{% xy-plane

\psline[linewidth=3pt,linecolor=blue]{->}(4,4)(4,5.5)%

\uput[90](4,5.5){\color{blue}$\vec{n}-{A}$$}}%

\ThreeDput[normal=0 -1 0]{% xz-plane

\psline[linewidth=3pt,linecolor=green]{->}(4,0)(5.5,0)%

\uput[90](5.5,0){\psscalebox{-1 1}{%}

\textcolor{green}{$\vec{n}-B$}}}}%

\end{array}

\[
\textcolor{green}{$\vec{n}-B$}}}\]

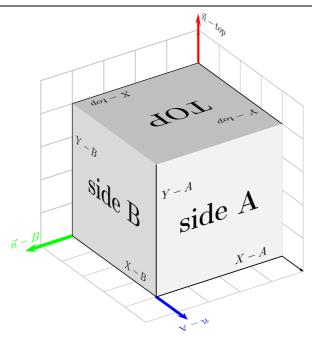
\[
\textcolor{green}{$\vec{n}-B$}}}\]

\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]

\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]

\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\]
\[
\textcolor{green}{$\vec{n}-B$}}}\]
\[
\textcolor{green}{\vec{n}-B$}}\]
\[
\textcolor{green}{\vec{n}-B$}
```

```
\ThreeDput[normal=1 0 0]{% yz-plane
                \psline[linewidth=3pt,linecolor=red]\{->\}(0,4)(0,5.5)\%
13
                \[0](0,5.5){\vec{n}-\{top}$\}}\ cube and axes
14
          \ThreeDput[normal=0 0 1](0,0,4){%
15
                 \psframe*[linecolor=gray75](4,4)\rput(2,2){\Huge\textbf{TOP}}}%
16
          \ThreeDput[normal=0 1 0](4,4,0){%
17
                 \psframe*[linecolor=gray95](4,4)\rput(2,2){\Huge\textbf{side A}}}\%
18
          ThreeDput[normal=1 0 0](4,0,0){\%}
19
                \psframe*[linecolor=gray85](4,4)\rput(2,2){\Huge\textbf{side B}}}\%
20
          \ThreeDput[normal=0 0 1](0,0,4){%
21
                \psline(4,0)\uput[90](3,0){$X-top$}\psline(0,4)\uput[0](0,3){$Y-top$}}%
22
          ThreeDput[normal=0 1 0](4,4,0){\%}
23
                \psline(4,0)\psline(0,4)\psline(0,3){$Y-A$}}
24
          ThreeDput[normal=1 0 0](4,0,0){\%}
25
                \prootember \pro
          \end{pspicture}
```



4.2 3D parameters

Table 3 shows a compilation of the parameters which can be used to influence 3D representations.

4.2.1 viewpoint

The viewing direction to the 3D object influences the representation essentially. With viewpoint the (x, y, z) coordinates which denote the vector of the viewing

Table 3: Summary of all 3D parameters

name	values	default
viewpoint	<pre><valuex valuey="" valuez=""></valuex></pre>	1 -1 1
viewangle	<angle></angle>	0
normal	<pre><valuex valuey="" valuez=""></valuex></pre>	0 0 1
embedangle	<angle></angle>	0

direction are specified. Because of the parallel projection the length of this vector is unimportant, so that (10.5 1.5) and (2 1 3) yield the same representations. Figure 2 shows who somebody would regard this representation, whereat the representation itself is of course regarded from another point in this case, otherwise one had to look directly onto the vector.

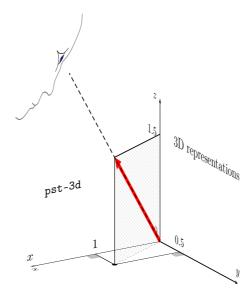


Figure 2: Definition of the viewpoints

For figure 2 a viewpoint of viewpoint=3 5 2 was defined. If one desires to regard it for instance from the y axis from a larger height, viewpoint=0 1 3 could be chosen. The viewer has moved one unit in y direction and four units in z direction from the centre (origin) and regards everything from there.

• The viewpoint principally has to be defined with values not equal to zero, for this would lead to a division by zero. Specifications of 0.001 for a coordinate are already sufficing to escape the division by zero and blind out the coordinate.

A good value for the viewpoint would be viewpoint=1 1 0.5 for instance, which corresponds to a horizontal rotation by 45° and a vertical by ca. 20°.

Another meaningful point is also viewpoint=1.5 1 0.5, which now corresponds to a horizontal rotation by 33ř and the same vertical rotation. Both can be seen in the examples below.

```
begin{pspicture}(-3,-2.5)(-3,4)

psset{unit=0.75}

psset{viewpoint=1 1 0.5}

IIIDKOSystem{5}

end{pspicture}\hfill

begin{pspicture}(-3,-2.5)(2.2,4)

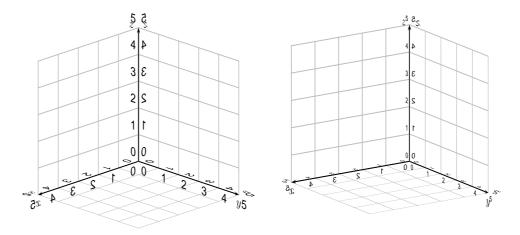
psset{unit=0.75}

psset{viewpoint=1 1.5 0.5}

psset{gridlabels=6pt}

IIIDKOSystem{5}

end{pspicture}
```



4.2.2 viewangle

Additional to the viewpoint option one can rotate the object by another option called viewangle. This could also be done by the macro \rotatebox, but viewangle has some advantages.

```
begin{pspicture}(-1,-2.5)(4,4)
psset{unit=0.7,viewpoint=1 1 0.5,viewangle=20}
illiDKOSystem{5}
```

```
ThreeDput(0,0,0){\psframe*[linecolor=gray80](4,4)}

ThreeDput(2,2,0){\Huge Unten}

end{pspicture}

begin{pspicture}(-3,-2.5)(1,4)

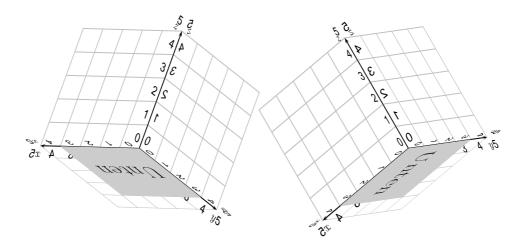
s \psset{unit=0.7,viewpoint=1 1.5 0.5,viewangle=-30}

IIIDKOSystem{5}

ThreeDput(0,0,0){\psframe*[linecolor=gray80](4,4)}

ThreeDput(2,2,0){\Huge Unten}

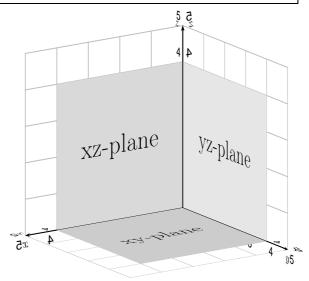
end{pspicture}
```



4.2.3 normal

normal denotes the direction of the normal vector which is perpendicular to a corresponding area. Therewith the posture of an object in three dimensional space is definitely determined by the normal vector.

```
\psline{->}(0,0)(0,5)\psline{->}(0,0)(5,0)\
\ThreeDput[normal=0 1 0](0,0,0){\psline{->}(0,0)(0,5)}
\end{pspicture}
```



Without a assignment through the normal vector the above example could not have been created that easily. Let us step through the code for a better understanding.

\psset{viewpoint=1 1.5 0.5}: the viewpoint is set to the point P(1, 1.5, 0.5).

\IIIDKOSystem{5}: first the coordinate system with the grid is drawn, so that axes and grid remain visible on the areas, which makes a better optical allocation possible.

\ThreeDput(0,0,0){\psframe*[linecolor=gray80] (4,4)}: puts a square with a side length of four into the origin of ordinates with the lower left edge. Since no normal vector is specified here, the default value $\vec{n} = (0,0,1)$ is taken, wherewith the area is positioned in the first quadrant of the xy plane.

\ThreeDput(2,2,0){\huge\psrotatedown{xy-plane}}: puts the text rotated by 180r centric to the point (2,2,0) in the xy-plane.

\ThreeDput[normal=0 -1 0](0,0,0){\psframe*[linecolor=gray85](4,4)}: puts a square with a side length of four in the origin of ordinates with the lower left edge. Since the normal vector is the "negative" y axis, the square is positioned in the first quadrant of the xz plane. With normal=0 1 0 it would have been the second quadrant.

- \ThreeDput [normal=0 1 0] (2,0,2) {\huge xz-plane}: puts the text in the xy-plane centric to the point (2,0,2). Because the xz plane is regarded from the back from the viewpoint, the normal vector of the area has to be reversed, otherwise the text would be read from the "back".
- \ThreeDput [normal=1 0 0] (0,0,0) {\psframe*[linecolor=gray90] (4,4)}: puts a square with a side length of four in the origin of ordinates with the lower left edge. The unit vector is the "positive" x axis, therefore the square is positioned in the first quadrant of the yz plane.
- \ThreeDput[normal=1 0 0](0,2,2){\huge yz-plane}: puts the text in the yz-plane centric to the point (0,2,2). Since the text is written at the "positive" side of the area, the normal vector stays the same.
- \ThreeDput[normal=0 0 1](0,0,0): the coordinate axes have been overwritten by the three areas and are redrawn now, first the xy axes.

\ThreeDput[normal=0 1 0](0,0,0): and now the z axis is drawn.

4.2.4 embedangle

With viewangle a rotation perpendicular to the plane of the viewer could be made. With embedangle a rotation perpendicular to the normal vector can be made. The counting of the angles is made in the mathematical sense, counterclockwise.

```
\def\tBlack#1#2{%
   \psframe[style=#2](2,2)
3
   \rput(1,1){\textcolor{#1}{\textbf{PSTricks}}}}
  \newpsstyle{SolidYellow}{fillstyle=solid,fillcolor=yellow}
  \newpsstyle{TransparencyRed}{fillstyle=vlines,hatchcolor=red,
    hatchwidth=0.1\pslinewidth,hatchsep=1\pslinewidth}
  \newpsstyle{TransparencyBlue}{fillstyle=vlines,hatchcolor=gray75,%
    hatchwidth=0.1\pslinewidth,hatchsep=1\pslinewidth}
  \begin{array}{l} \begin{array}{l} & \\ & \\ & \end{array} \end{array}
    \ThreeDput{\psgrid[subgriddiv=0](-2,0)(4,3)}
11
    \ThreeDput(-1,0,0){\tBlack{black}{SolidYellow}}
12
    \ThreeDput(2,0,0){\tBlack{black}{SolidYellow}}
13
    \ThreeDput[embedangle=50](-1,0,0){\tBlack{gray}{TransparencyRed}}
14
    \ThreeDput[embedangle=50](2,0,0){\tBlack{gray}{TransparencyBlue}}
15
    \ThreeDput[normal=0 1 0](-1,0,0){\psline[linewidth=0.1,linecolor=red](0,4)}
16
    \ThreeDput[normal=0 1 0](2,0,0){\psline[linewidth=0.1,linecolor=\psi lue](0,4)}
17
  \end{pspicture}
18
  \psset{viewpoint=1 1 100}
19
  \beta = \frac{1.7}{2.5}
ThreeDput{\psgrid[subgriddiv=0](-2,0)(4,3)}
```

```
ThreeDput(-1,0,0) {\tBlack{black}{SolidYellow}}

ThreeDput(2,0,0) {\tBlack{black}{SolidYellow}}

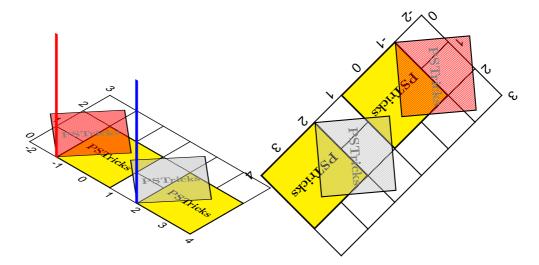
ThreeDput[embedangle=50](-1,0,0) {\tBlack{gray}{TransparencyRed}}

ThreeDput[embedangle=50](2,0,0) {\tBlack{gray}{TransparencyBlue}}

ThreeDput[normal=0 1 0](-1,0,0) {\psline[linewidth=0.1,linecolor=red](0,4)}

ThreeDput[normal=0 1 0](2,0,0) {\psline[linewidth=0.1,linecolor=blue](0,4)}

end{pspicture}
```



5 Driver file

The next bit of code contains the documentation driver file for TEX, i.e., the file that will produce the documentation you are currently reading. It will be extracted from this file by the docstrip program.

6 'pst-3d' ₽T_FX wrapper

```
1 \( *\lambda\tex - wrapper \)
2 \( *\lambda\tex - wrapper \)
3 \\RequirePackage{pstricks}
4 \\ProvidesPackage{pst-3d}[2005/09/02 package wrapper for
5  pst-3d.tex (hv)]
6 \\input{pst-3d.tex}
7 \\ProvidesFile{pst-3d.tex}
8  [\filedate\space v\fileversion\space 'PST-3d' (tvz)]
9 \( \lambda\tex - wrapper \)
```

7 'pst-3d' code

<*pst-3d>

pst-3d Require the basic pstricks package and for the key value operations the pst-xkey package.

- 10 \ifx\PSTricksLoaded\endinput\else\input pstricks.tex\fi
- 11 \ifx\PSTXKeyLoaded\endinput\else\input pst-xkey \fi % (hv 2005-09-03)

Catcodes changes.

- 12 \edef\PstAtCode{\the\catcode'\@}
- 13 \catcode'\@=11\relax

Add the key-family name to the xkeyval package

14 \pst@addfams{pst-3d}

Mark the package as loaded

- 15 \csname PSTthreeDLoaded\endcsname
- 16 \let\PSTthreeDLoaded\endinput

7.1 Basic 3D transformations

\tx@SetMatrixThreeD

Viewpoint for 3D coordinates is given by three angles: α , β and γ . α and β determine the direction from which one is looking. γ then determines the orientation of the observing. When α , β and γ are all zero, the observer is looking from the negative part of the y-axis, and sees the xz-plane the way in 2D one sees the xy plan. Hence, to convert the 3D coordinates to their 2D project, $\langle x,y,z\rangle$ map to $\langle x,z\rangle$. When the orientation is different, we rotate the coordinates, and then perform the same projection. We move up to latitude β , over to longitude α , and then rotate by γ . This means that we first rotate around y-axis by γ , then around x-axis by β , and the around z-axis by α .

Here are the matrices:

$$R_{z}(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R_{x}(\beta) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & \sin \beta \\ 0 & -\sin \beta & \cos \beta \end{bmatrix}$$

$$R_{y}(\gamma) = \begin{bmatrix} \cos \gamma & 0 & -\sin \gamma \\ 0 & 1 & 0 \\ \sin \gamma & 0 & \cos \gamma \end{bmatrix}$$

The rotation of a coordinate is then performed by the matrix $R_z(\alpha)R_x(\beta)R_y(\gamma)$. The first and third columns of the matrix are the basis vectors of the plan upon which the 3D coordinates are project (the old basis vectors were $\langle 1,0,0 \rangle$ and $\langle 0,0,1 \rangle$; rotating these gives the first and third columns of the matrix).

These new base vectors are:

$$\tilde{x} = \begin{bmatrix} \cos \alpha \cos \gamma - \sin \beta \sin \alpha \sin \gamma \\ \sin \alpha \cos \gamma + \sin \beta \cos \alpha \sin \gamma \\ \cos \beta \sin \gamma \end{bmatrix}$$

$$\tilde{z} = \begin{bmatrix} -\cos \alpha \sin \gamma - \sin \beta \sin \alpha \cos \gamma \\ -\sin \alpha \sin \gamma + \sin \beta \cos \alpha \cos \gamma \\ \cos \beta \cos \gamma \end{bmatrix}$$

Rather than specifying the angles α and β , the user gives a vector indicating where the viewpoint is. This new viewpoint is the rotation o the old viewpoint. The old viewpoint is (0, -1, 0), and so the new viewpoint is

$$R_z(\alpha)R_x(\beta) \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} \cos\beta\sin\alpha \\ -\cos\beta\cos\alpha \\ \sin\beta \end{bmatrix} = \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

Therefore,

$$lpha = \arctan(v_1/-v_2)$$

 $eta = \arctan(v_3 \sin lpha/v_1)$

Unless $p_1 = p_2 = 0$, in which case $\alpha = 0$ and $\beta = \text{sign}(p_3)90$, or $p_1 = p_3 = 0$, in which case $\beta = 0$.

The syntax of SetMatrixThreeD is

$$v_1 \ v_2 \ v_3 \ \gamma \ {\rm SetMatrixThreeD}$$

SetMatrixThreeD first computes

$$a = \sin \alpha$$
 $b = \cos \alpha$
 $c = \sin \beta$ $d = \cos \beta$
 $e = \sin \gamma$ $f = \cos \gamma$

and then sets Matrix3D to $[\tilde{x} \ \tilde{z}]$.

```
17 \pst@def{SetMatrixThreeD}<%
18 dup sin /e ED cos /f ED
   /p3 ED /p2 ED /p1 ED
   p1 0 eq
   { /a 0 def /b p2 0 le { 1 } { -1 } ifelse def
22
    p3 p2 abs
23 }
^{24}
   { p2 0 eq
      { /a p1 0 lt { -1 } { 1 } ifelse def /b 0 def
25
26
      p3 p1 abs
27
      { p1 dup mul p2 dup mul add sqrt dup
28
        p1 exch div /a ED
```

```
p2 exch div neg /b ED
30
        p3 p1 a div
31
32
33
      ifelse
34
    }
35
    ifelse
    atan dup sin /c ED cos /d ED
36
    /Matrix3D
37
38
39
      b f mul c a mul e mul sub
      a f mul c b mul e mul add
40
41
      b e mul neg c a mul f mul sub
      a e mul neg c b mul f mul add
44
      d f mul
    ] def>
45
```

\tx@ProjThreeD The syntax of the macro tx@ProjThreeD is

$$x y z$$
 ProjThreeD $x' y'$

```
where x' = \langle x, y, z \rangle \cdot \tilde{x} and y' = \langle x, y, z \rangle \cdot \tilde{z}.

46 \pst@def{ProjThreeD}<%

47  /z ED /y ED /x ED

48  Matrix3D aload pop

49  z mul exch y mul add exch x mul add

50  4 1 roll

51  z mul exch y mul add exch x mul add

52  exch>
```

To embed 2D $\langle x,y \rangle$ coordinates in 3D, the user specifies the normal vector and an angle. If we decompose this normal vector into an angle, as when converting 3D coordinates to 2D coordinates, and let $\hat{\alpha}$, $\hat{\beta}$ and $\hat{\gamma}$ be the three angles, then when these angles are all zero the coordinate $\langle x,y \rangle$ gets mapped to $\langle x,0,y \rangle$, and otherwise $\langle x,y \rangle$ gets mapped to

$$R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma}) \begin{bmatrix} x \\ 0 \\ y \end{bmatrix} = \begin{bmatrix} \hat{x}_1x + \hat{z}_1y \\ \hat{x}_2x + \hat{z}_2y \\ \hat{x}_3x + \hat{z}_3y \end{bmatrix}$$

where \hat{x} and \hat{z} are the first and third columns of $R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma})$. Now add on a 3D-origin:

$$\begin{bmatrix} \hat{x}_{1}x + \hat{z}_{1}y + x_{0} \\ \hat{x}_{2}x + \hat{z}_{2}y + y_{0} \\ \hat{x}_{3}x + \hat{z}_{3}y + z_{0} \end{bmatrix}$$

Now when we project back onto 2D coordinates, we get

$$x' = \tilde{x}_1(\hat{x}_1x + \hat{z}_1y + x_0) + \tilde{x}_2(\hat{x}_2x + \hat{z}_2y + y_0) + \tilde{x}_3(\hat{x}_3x + \hat{z}_3y + z_0)$$

$$= (\tilde{x}_1\hat{x}_1 + \tilde{x}_2\hat{x}_2 + \tilde{x}_3\hat{x}_3)x + (\tilde{x}_1\hat{z}_1 + \tilde{x}_2\hat{z}_2 + \tilde{x}_3\hat{z}_3)y + \tilde{x}_1x_0 + \tilde{x}_2y_0 + \tilde{z}_3z_0$$

$$y' = \tilde{z}_1(\hat{x}_1x + \hat{z}_1y + x_0) + \tilde{z}_2(\hat{x}_2x + \hat{z}_2y + y_0) + \tilde{z}_3(\hat{x}_3x + \hat{z}_3y + z_0)$$

$$= (\tilde{z}_1\hat{x}_1 + \tilde{z}_2\hat{x}_2 + \tilde{z}_3\hat{x}_3)x + (\tilde{z}_1\hat{z}_1 + \tilde{z}_2\hat{z}_2 + \tilde{z}_3\hat{z}_3)y + \tilde{z}_1x_0 + \tilde{z}_2y_0 + \tilde{z}_3z_0$$

Hence, the transformation matrix is:

$$\left[\begin{array}{c} \tilde{x}_1 \hat{x}_1 + \tilde{x}_2 \hat{x}_2 + \tilde{x}_3 \hat{x}_3) \\ \tilde{z}_1 \hat{x}_1 + \tilde{z}_2 \hat{x}_2 + \tilde{z}_3 \hat{x}_3) \\ \tilde{x}_1 \hat{z}_1 + \tilde{x}_2 \hat{z}_2 + \tilde{x}_3 \hat{z}_3) \\ \tilde{z}_1 \hat{z}_1 + \tilde{z}_2 \hat{z}_2 + \tilde{z}_3 \hat{z}_3) \\ \tilde{x}_1 x_0 + \tilde{x}_2 y_0 + \tilde{z}_3 z_0 \\ \tilde{z}_1 x_0 + \tilde{z}_2 y_0 + \tilde{z}_3 z_0 \end{array} \right]$$

\tx@SetMatrixEmbed The syntax of SetMatrixEmbed is

SetMatrixEmbed first sets <x1 x2 x3 y1 y2 y3> to the basis vectors for the view-point projection (the tilde stuff above). Then it sets Matrix3D to the basis vectors for the embedded plane. Finally, it sets the transformation matrix to the matrix given above.

```
53 \pst@def{SetMatrixEmbed}<%
54 \tx@SetMatrixThreeD
55 Matrix3D aload pop
   /z3 ED /z2 ED /z1 ED /x3 ED /x2 ED /x1 ED
    \tx@SetMatrixThreeD
57
   Γ
58
59
   Matrix3D aload pop
    z3 mul exch z2 mul add exch z1 mul add 4 1 roll
    z3 mul exch z2 mul add exch z1 mul add
   Matrix3D aload pop
    x3 mul exch x2 mul add exch x1 mul add 4 1 roll
    x3 mul exch x2 mul add exch x1 mul add
    3 -1 roll 3 -1 roll 4 -1 roll 8 -3 roll 3 copy
^{66} x3 mul exch x2 mul add exch x1 mul add 4 1 roll
67 z3 mul exch z2 mul add exch z1 mul add
68 ]
69
    concat>
```

7.2 Parameter

\psk@viewpoint

First we need a macro \pssetzlength for the third coordinate. It is adopted from the definition of the y-axes:

70 $\left| \text{let}\right|$

```
The viewpoint is set by its three coordinates (x \ y \ z). It is preset to x = 1, y = -1
                  and z = 1.
                  71 \define@key[psset]{pst-3d}{viewpoint}{%
                  72 \pst@expandafter\psset@@viewpoint#1 {} {} \@nil
                      \let\psk@viewpoint\pst@tempg}
                  74 \def\psset@@viewpoint#1 #2 #3 #4\@nil{%
                      \begingroup
                  76
                         \pssetxlength\pst@dima{#1}%
                  77
                         \pssetylength\pst@dimb{#2}%
                  78
                         \pssetzlength\pst@dimc{#3}%
                  79
                         \xdef\pst@tempg{%
                           \pst@number\pst@dima \pst@number\pst@dimb \pst@number\pst@dimc}%
                  80
                  81 \endgroup}
                  82 \pset[pst-3d]{viewpoint=1 -1 1}
   \psk@viewangle
                  83 \define@key[psset]{pst-3d}{viewangle}{%
                  84 \pst@getangle{#1}\psk@viewangle}
                  85 \psset[pst-3d]{viewangle=0}
      \psk@normal
                  86 \define@key[psset]{pst-3d}{normal}{%
                      \pst@expandafter\psset@@viewpoint#1 {} {} \@nil
                  88 \let\psk@normal\pst@tempg}
                  89 \psset[pst-3d]{normal=0 0 1}
  \psk@embedangle
                  90 \define@key[psset]{pst-3d}{embedangle}{%
                  91 \pst@getangle{#1}\psk@embedangle}
                  92 \psset[pst-3d]{embedangle=0}
   \psTshadowsize
                  93 \define@key[psset]{pst-3d}{Tshadowsize}{%
                  94 \pst@checknum{#1}\psTshadowsize}
                  95 \psset[pst-3d]{Tshadowsize=1}
\psk@Tshadowangle
                  97 \pst@getangle{#1}\psk@Tshadowangle}
                  98 \texttt{\psset[pst-3d]{Tshadowangle=60}}
  \psTshadowcolor
                  99 \define@key[psset]{pst-3d}{Tshadowcolor}{%
                  100 \pst@getcolor{#1}\psTshadowcolor}
                  101 \psset[pst-3d]{Tshadowcolor=lightgray}
```

7.3 PostScript code

```
\tx@TMSave
              102 \pst@def{TMSave}<%
              103 tx@Dict /TMatrix known not { /TMatrix { } def /RAngle { 0 } def } if
                   /TMatrix [ TMatrix CM ] cvx def>
\tx@TMRestore
              105 \pst@def{TMRestore}<%
              106 CP /TMatrix [ TMatrix setmatrix ] cvx def moveto>
              107 %
              The syntax:
\tx@TMChange
                  {<Proc for modifying tm>} TMChange
              108 \pst@def{TMChange}<%
                   \tx@TMSave
                   /cp [ currentpoint ] cvx def % ??? Check this later.
              110
              111
                  Set "standard" coordinate system, with pt units and origin at currentpoint.
               This let's us rotate, or whatever, around TEX's current point, without having to
               worry about strange coordinate systems that the dvi-to-ps driver might be using.
                  CP T \tx@STV
               Let M = old matrix (on stack), and M' equal current matrix. Then go from M'
               to M by applying M Inv(M').
                  CM matrix invertmatrix
                                              % Inv(M')
                  matrix concatmatrix
                                              % M Inv(M')
               Now modify transformation matrix:
                   exch exec
               Now apply M Inv(M')
                   concat cp moveto>
```

7.4 Three dimensional operations

There is only one macro which collects all the basic operations for three dimansional representation of a text or graphic object.

```
\verb|\ThreeDput|
```

```
117 \def\ThreeDput{\def\pst@par{}\pst@object{ThreeDput}}
118 \def\ThreeDput@ii{\@ifnextchar({\ThreeDput@ii}{\ThreeDput@ii(\z@,\z@,\z@)}}
119 \def\ThreeDput@ii(#1,#2,#3){%
120 \pst@killglue\pst@makebox{\ThreeDput@iii(#1,#2,#3)}}
121 \def\ThreeDput@iii(#1,#2,#3){%
122 \begingroup
123 \use@par
```

```
\if@star\pst@starbox\fi
124
       \pst@makesmall\pst@hbox
125
126
       \pssetxlength\pst@dima{#1}%
127
       \pssetylength\pst@dimb{#2}%
       \pssetzlength\pst@dimc{#3}%
128
       \leavevmode
129
       \hbox{%
130
          \pst@Verb{%
131
            { \pst@number\pst@dima
132
              \pst@number\pst@dimb
133
              \pst@number\pst@dimc
134
              \psk@normal
135
              \psk@embedangle
136
137
              \psk@viewpoint
138
              \psk@viewangle
              \tx@SetMatrixEmbed
139
            } \tx@TMChange}%
140
       \box\pst@hbox
141
       \pst@Verb{\tx@TMRestore}}%
142
     \endgroup
143
144
     \ignorespaces}
```

7.5 Arithmetic

\pst@sinandcos

Syntax:

% \pst@sinandcos{<dim>}{<int>}

<dim>, in "sp" units, should equal 100,000 times the angle, in degrees between 0 and 90. <int> should equal the angle's quadrant (0, 1, 2 or 3). \pst@dimg is set to $\sin(\theta)$ and \pst@dimh is set to $\cos(\theta)$ (in pt's).

The algorithms uses the usual McLaurin expansion.

```
145 \def\pst@sinandcos#1{%
     \begingroup
146
       \pst@dima=#1\relax
147
       \pst@dima=.366022\pst@dima
                                        %Now 1pt=1/32rad
148
149
       \pst@dimb=\pst@dima
                              % dimb->32sin(angle) in pts
150
       \pst@dimc=32\p@
                               % dimc->32cos(angle) in pts
151
       \pst@dimtonum\pst@dima\pst@tempa
152
       \pst@cntb=\tw@
       \pst@cntc=-\@ne
153
154
       \pst@cntg=32
155
       \loop
       \ifnum\pst@dima>\@cclvi % 256
156
          \pst@dima=\pst@tempa\pst@dima
157
          \divide\pst@dima\pst@cntg
158
          \divide\pst@dima\pst@cntb
159
          \ifodd\pst@cntb
160
161
            \advance\pst@dimb \pst@cntc\pst@dima
162
            \pst@cntc=-\pst@cntc
```

```
\else
163
            \advance\pst@dimc by \pst@cntc\pst@dima
164
165
          \fi
          \advance\pst@cntb\@ne
166
167
       \repeat
       \divide\pst@dimb\pst@cntg
168
       \divide\pst@dimc\pst@cntg
169
170
       \global\pst@dimg\pst@dimb
       \global\pst@dimh\pst@dimc
171
     \endgroup}
172
```

\pst@getsinandcos

\pst@getsinandcos normalizes the angle to be in the first quadrant, sets \pst@quadrant to 0 for the first quadrant, 1 for the second, 2 for the third, and 3 for the fourth, invokes \pst@sinandcos, and sets \pst@sin to the sine and \pst@cos to the cosine.

```
173 \def\pst@getsinandcos#1{%
     \pst@dimg=100000sp
174
     \pst@dimg=#1\pst@dimg
175
     \pst@dimh=36000000sp
176
     \pst@cntg=0
177
178
     \loop
179
     \ifnum\pst@dimg<\z@
180
       \advance\pst@dimg\pst@dimh
181
     \repeat
182
     \loop
     \ifnum\pst@dimg>\pst@dimh
183
       \advance\pst@dimg-\pst@dimh
184
     \repeat
185
     \pst@dimh=9000000sp
186
     \def\pst@tempg{%
187
       \ifnum\pst@dimg<\pst@dimh\else
188
189
          \advance\pst@dimg-\pst@dimh
190
          \advance\pst@cntg\@ne
          \ifnum\pst@cntg>\thr@@ \advance\pst@cntg-4 \fi
191
          \expandafter\pst@tempg
192
       fi}%
193
194
     \pst@tempg
     \chardef\pst@quadrant\pst@cntg
195
     \ifdim\pst@dimg=\z@
196
       \def\pst@sin{0}%
197
       \def\pst@cos{1}%
198
199
200
       \pst@sinandcos\pst@dimg
201
       \pst@dimtonum\pst@dimg\pst@sin
       \pst@dimtonum\pst@dimh\pst@cos
202
     \fi%
203
204 }
```

7.6 Tilting

```
\pstilt
        205 \ensuremath{$\ $$ \ensuremath{$\ $$}}
        206 \def\pstilt@#1{%
        207
             \begingroup
        208
                \leavevmode
                \pst@getsinandcos{#1}%
        209
        210
                \hbox{%
                  \ifcase\pst@quadrant
        211
        212
                    \kern\pst@cos\dp\pst@hbox
        213
                    \pst@dima=\pst@cos\ht\pst@hbox
        214
                    \ht\pst@hbox=\pst@sin\ht\pst@hbox
                    \dp\pst@hbox=\pst@sin\dp\pst@hbox
        215
                  \or
        216
                    \kern\pst@sin\ht\pst@hbox
        217
                    \pst@dima=\pst@sin\dp\pst@hbox
        218
        219
                    \ht\pst@hbox=\pst@cos\ht\pst@hbox
                    \dp\pst@hbox=\pst@cos\dp\pst@hbox
        220
        221
                  \or
        222
                    \kern\pst@cos\ht\pst@hbox
        223
                    \pst@dima=\pst@sin\dp\pst@hbox
        224
                    \pst@dimg=\pst@sin\ht\pst@hbox
                    \ht\pst@hbox=\pst@sin\dp\pst@hbox
        225
                    \dp\pst@hbox=\pst@dimg
        226
                  \or
        227
                    \kern\pst@sin\dp\pst@hbox
        228
                    \pst@dima=\pst@sin\ht\pst@hbox
        229
        230
                    \pst@dimg=\pst@cos\ht\pst@hbox
                    \ht\pst@hbox=\pst@cos\dp\pst@hbox
        231
        232
                    \dp\pst@hbox=\pst@dimg
        233
                  \fi
                  \pst@Verb{%
        234
                    { [ 1 0
        235
                        \pst@cos\space \ifnum\pst@quadrant>\@ne neg \fi
        236
                        \pst@sin\space
        237
                        \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
        238
                        \ifodd\pst@quadrant exch \fi
        239
                        0 0
        240
        241
                      ] concat
                    } \tx@TMChange}%
        242
        243
                  \box\pst@hbox
        244
                  \pst@Verb{\tx@TMRestore}%
        245
                  \kern\pst@dima}%
        246
             \endgroup}
\psTilt
```

247 \def\psTilt#1{\pst@makebox{\psTilt@{#1}}}

248 \def\psTilt@#1{%

\begingroup

 249

```
\leavevmode
250
       \pst@getsinandcos{#1}%
251
252
       \hbox{%
253
         \ifodd\pst@quadrant
           \pst@@divide{\dp\pst@hbox}{\pst@cos\p@}%
254
           \ifnum\pst@quadrant=\thr@@\kern\else\pst@dima=\fi\pst@sin\pst@dimg
255
           \pst@divide{\ht\pst@hbox}{\pst@cos\p@}%
256
           \ifnum\pst@quadrant=\@ne\kern\else\pst@dima=\fi\pst@sin\pst@dimg
257
258
         \else
           \ifdim\pst@sin\p@=\z@
259
             \@pstrickserr{\string\psTilt\space angle cannot be 0 or 180}\@ehpa
260
             \def\pst@sin{.7071}%
261
             \def\pst@cos{.7071}%
262
263
           \fi
           \pst@@divide{\dp\pst@hbox}{\pst@sin\p@}%
264
           \ifnum\pst@quadrant=\z@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
265
           \pst@divide{\ht\pst@hbox}{\pst@sin\p@}%
266
           \ifnum\pst@quadrant=\tw@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
267
         \fi
268
         \ifnum\pst@quadrant>\@ne
269
270
           \pst@dimg=\ht\pst@hbox
           \ht\pst@hbox=\dp\pst@hbox
271
           \dp\pst@hbox=\pst@dimg
272
273
         \fi
274
         \pst@Verb{%
           { [ 1 0
275
               \pst@cos\space \pst@sin\space
276
               \ifodd\pst@quadrant exch \fi
277
               \tx@Div
278
               \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
279
               \ifnum\pst@quadrant>\@ne -1 \else 1 \fi
280
281
282
             ] concat
           } \tx@TMChange}%
284
         \box\pst@hbox
         285
286
         \kern\pst@dima}%
     \endgroup}
287
```

7.7 Shadow

```
\psshadow
```

```
288 \def\psshadow{\pst@object{psshadow}}
289 \def\psshadow@ii{\pst@makebox{\psshadow@ii}}
290 \def\psshadow@ii{%}
291 \begingroup
292 \use@par
293 \leavevmode
294 \pst@getsinandcos{\psk@Tshadowangle}%
```

```
\hbox{%}
295
        \lower\dp\pst@hbox\hbox{%
296
297
          \pst@Verb{%
298
            { [ 1 0
                \pst@cos\space \psTshadowsize mul
299
                \ifnum\pst@quadrant>\@ne neg \fi
300
                \pst@sin\space \psTshadowsize mul
301
                \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
302
                \ifodd\pst@quadrant exch \fi
303
                0 0
304
              ] concat
305
            } \tx@TMChange}}%
306
307
        \hbox to\z0{%
                       patch 2 (hv), to get it run with xcolor _and_ TeX
308
         \pst@Verb{ gsave \pst@usecolor\psTshadowcolor}%
309
         \copy\pst@hbox
         \pst@Verb{ grestore}\hss}%
310
         311 %
        \pst@Verb{\tx@TMRestore}%
312
        \box\pst@hbox}%
313
314
    \endgroup}
```

7.8 Closing

Catcodes restoration.

315 \catcode'\@=\PstAtCode\relax

</pst-3d>

Change History

v0.90	xkey instead of the old pst-key
General: First public release. (tvz) 1	package; creating a dtx file; new
v1.00	L ^A T _E X wrapper file (hv) 1
General: using the extended pst-	

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