# The bitset package

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## Abstract

This package defines and implements the data type bit set, a vector of bits. The size of the vector may grow dynamically. Individual bits can be manipulated.

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### 1 Documentation

#### 1.1 Introduction

Annotations in the PDF format know entries whose values are integers. This numbers are interpreted as set of flags specifying properties. For example, annotation dictionaries can have a key /F. The bits of its integer value are interpreted the following way:

Bit position	Property name
1	Invisible
2	Hidden
3	Print
4	NoZoom
5	NoRotate
6	NoView
7	ReadOnly

Now, let's see how these values are set in package hyperref before it uses this package (before v6.77a):

```
\ifFld@hidden /F 6\else /F 4\fi
```

Where are the other flags? The following example for key /Ff in a widget annotation supports at least three properties:

```
\ifFld@multiline
  \ifFld@readonly /Ff 4097\else /Ff 4096\fi
\else
  \ifFld@password
   \ifFld@readonly /Ff 8193\else /Ff 8192\fi
  \else
   \ifFld@readonly /Ff 1\fi
  \fi
\fi
```

But you see the point. It would be a nightmare to continue this way in supporting the missing flag settings. This kind of integers may have up to 32 bits.

Therefore I wanted a data structure for setting and clearing individual bits. Also it should provide an export as decimal number. The snipsets above are executed in expansion contexts without TeX's stomach commands. It would be convenient to have an expandable conversion from the data structure to the integer that gets written to the PDF file.

This package bitset implements such a data structure. The interface is quite close to Java's class BitSet in order not to learn to many interfaces for the same kind of data structure.

## 1.2 Glossary

**Bit set:** A bit set is a vector of bits or flags. The vector size is unlimited and grows dynamically. An undefined bit set is treated as bit set where all bits are cleared.

Bit sets are addressed by name. A name should consists of letters or digits. Technically it must survive \csname, see LATEX's environment names for other names with such a constraint. Package babel's shorthands are not supported due to technical reasons. Shorthand support would break expandable operations.

Size: A size of a bit set is the number of bits in use. It's the number of the highest index, incremented by one. Sizes are in the range 0 up to 2147483647, the highest number supported by  $T_{\rm E}X$ .

Index: Bit positions in a bit set are addressed by an index number. The bit vector is zero based. The first and least significant bit is addressed by index 0 and the highest possible bit by 2147483646.

Bit: A bit is enoded as 0 for cleared/disabled or 1 for set/enabled.

## 1.3 Design principles

**Name conventions:** To avoid conflicts with existing macro names, the operations are prefixed by the package name.

**Zero based indexes:** The first bit is addressed by zero. (Convention of array indexing in C, Java, ...)

Unlimited size: There is no restriction on the size of a bit set other than usual memory limitations. \bitsetSetDec and \bitsetGetDec transparently switch to package bigintcalc if the numbers get too large for TeX's number limit.

**Expandibility:** Any operation that does not change the bit set is expandable. And all operations that extract or calculate some result do this in exact two expansion steps. For example, a macro \Macro wants a bit set as decimal number. But the argument must be a plain number without macros. Thus you could prefix \bitsetGetDec with \number. However this won't work for bit sets with 31 or more bits because of  $T_EX$ 's number limit of  $2^{31} - 1$ . then just hit the operator with two \expandafter:

\expandafter\expandafter\expandafter
\Macro\bitsetGetDec{foo}

\bitsetGetDec is hit first by the third \expandafter and then by the second one.

Format independence: This package is written as LATEX package, but it does not depend on LATEX. It will also work for other formats such as plain-TEX.

Independence from TeX engines: Vanilla TeX is all you need. Calculations are delegated to packages intcalc and bigintcalc. They don't need any special features, but they will switch to a little more efficient implementation if features such as \numexpr are available.

Numeric arguments: Anything that is accepted by \number. If  $\varepsilon$ -TeX is detected, also expressions for \numexpr are supported. The only exception so far is the number for \bitsetSetDec. The number might be too large for \number or \numexpr.

Error messages: In expandable contexts, only a limited set of TEX primitive commands work as expected. So called stomach commands behave like \relax and don't get expanded or executed. Unhappily also the error commands belong to this category. The expandable operations will throw an unknown control sequence instead to get TEX's and user's attention. The name of these control sequences starts with \BitSetError: with the type of error after the colon.

## 1.4 Operator overview

```
Miscellaneous (section 1.6.1)
                                                                                                          \langle BitSet \rangle
        \bitsetReset
        \bitsetLet
                                                                                      \langle BitSet \ A \rangle \ \langle BitSet \ B \rangle
Import (section 1.6.2)
        \bitsetSetBin, \bitsetSetOct, \bitsetSetHex
                                                                                               \langle BitSet \rangle \langle Value \rangle
        \bitsetSetDec
                                                                                              \langle BitSet \rangle \langle Value \rangle
Export<sup>a</sup> (section 1.6.3)
                                                                                           \langle BitSet \rangle \langle MinSize \rangle
        \bitsetGetBin, \bitsetGetOct, \bitsetGetHex
        \bitsetGetDec
                                                                                                          \langle BitSet \rangle
Logical operators (section 1.6.4)
        \bitsetAnd, \bitsetAndNot
                                                                                       \langle BitSet \ A \rangle \ \langle BitSet \ B \rangle
        \bitsetOr, \bitsetXor
                                                                                       \langle BitSet \ A \rangle \ \langle BitSet \ B \rangle
Shifting (section 1.6.5)
                                                                                    \langle BitSet \rangle \langle ShiftAmount \rangle
        \bitsetShiftLeft, \bitsetShiftRight
Bit manipulation (section 1.6.6)
        \bitsetClear, \bitsetSet, \bitsetFlip
                                                                                              \langle BitSet \rangle \langle Index \rangle
                                                                                   \langle BitSet \rangle \langle Index \rangle \langle Value \rangle
        \bitsetSetValue
        \bitsetClearRange, \bitsetSetRange, \bitsetFlipRange
                                                                       \langle BitSet \rangle \langle IndexFrom \rangle \langle IndexTo \rangle
                                                                       \langle BitSet \rangle \langle IndexFrom \rangle \langle IndexTo \rangle
        \bitsetSetValueRange
Bit retrieval<sup>a</sup> (section 1.6.7)
        \bitsetGet
                                                                                              \langle BitSet \rangle \langle Index \rangle
        \bitsetNextClearBit, \bitsetNextSetBit
                                                                                               \langle BitSet \rangle \langle Index \rangle
        \bitsetGetSetBitList
                                                                                                          \langle BitSet \rangle
Bit set properties (section 1.6.8)
        \bitsetSize, \bitsetCardinality
                                                                                                          \langle BitSet \rangle
Queries<sup>b</sup> (section 1.6.9)
        \bitsetIsDefined, \bitsetIsEmpty
                                                                                     \langle BitSet \rangle \langle Then \rangle \langle Else \rangle
        \bitsetEquals, \bitsetIntersects \langle BitSet A \rangle \langle BitSet B \rangle \langle Then \rangle \langle Else \rangle
                                                                         \langle BitSet \rangle \langle Index \rangle \langle Then \rangle \langle Else \rangle
        \bitsetQuery
```

## 1.5 Package loading

The package can be used as normal LATEX package:

\usepackage{bitset}

Also plain-T<sub>E</sub>X is supported:

\input bitset.sty\relax

## 1.6 Operators

The following macros work on and with bit sets. A bit set  $\langle BitSet \rangle$  is represented by a name. The should consist of letters and digits. Technically it must survive  $\backslash$ csname. It is the same constraint that must be satisfied by label or environment names in  $\LaTeX$ .

However active characters that are shorthands of package babel are not supported. Support for shorthands works by an assignment. But many operators such

 $<sup>^</sup>a$ Macros are expandable, full expansion by two steps.

<sup>&</sup>lt;sup>b</sup>Macros are expandable.

as \bitsetGetDec must be usable in expandable contexts. There assignments will not be executed in the best case or they will cause errors.

The bits in a bit set are addressed by non-negative integers starting from zero. Thus negative index numbers cause an error message. Because index numbers are TEX numbers. The largest index is 2147483647. But in practice memory limits and patience limits will be very likely reached much before.

#### 1.6.1 Miscellaneous

There isn't a separate operation for bit set creation. For simplicity an undefined bit set is treated as bit set with all bits cleared.

```
\bitsetReset \{\langle BitSet \rangle\}
```

Macro \bitsetReset clears all bits. The result is an empty bit set. It may also be used as replacement for an operation "new", because an undefined bit set is defined afterwards.

```
\bitsetLet \{\langle BitSet \ A \rangle\}\ \{\langle BitSet \ B \rangle\}
```

Macro \bitsetLet performs a simple assignment similar to TEX's \let. After the operation  $\langle BitSet\ A \rangle$  has the same value as  $\langle BitSet\ B \rangle$ . If  $\langle BitSet\ B \rangle$  is undefined, then  $\langle BitSet\ A \rangle$  will be the empty bit set.

Note: If  $\langle BitSet A \rangle$  exists, it will be overwritten.

#### 1.6.2 Import

```
\label{linear} $$ \begin{array}{l} \bitsetSetBin {\langle BitSet \rangle} {\langle BinaryNumber \rangle} \\ \bitsetSetOct {\langle BitSet \rangle} {\langle OctalNumber \rangle} \\ \bitsetSetHex {\langle BitSet \rangle} {\langle HexadecimalNumber \rangle} \\ \end{array}
```

The numbers are interpreted as bit vectors and the flags in the bit  $\langle BitSet \rangle$  set are set accordingly. These numeric arguments are the only arguments where spaces are allowed. Then the numbers are easier to read.

```
\bitsetSetDec \{\langle BitSet \rangle\}\ \{\langle DecimalNumber \rangle\}
```

Macro \bitsetSetDec uses  $\langle DecimalNumber \rangle$  to set the bit set  $\langle BitSet \rangle$ . The numeric argument must expand to a plain number consisting of decimal digits without command tokens or spaces. Internally this argument is expanded only. It cannot be passed to \number or \numexpr, because the number may be too large for them. However \number or \the\numexpr may be used explicitely. This also helps for unexpandable number command tokens or registers (\z0, \@ne, \count@, ...). Also IATEX' \value needs prefixing:

\bitsetSetDec{foo}{\number\value{bar}}

#### 1.6.3 Export

```
\bitsetGetBin \{\langle BitSet \rangle\}\ \{\langle MinSize \rangle\}\ \bitsetGetOct \{\langle BitSet \rangle\}\ \{\langle MinSize \rangle\}\ \bitsetGetHex \{\langle BitSet \rangle\}\ \{\langle MinSize \rangle\}\
```

These macros returns the bit set as binary, octal or hexadecimal number. If the bit size is smaller than  $\langle MinSize \rangle$  the gap is filled with leading zeros. Example:

Macro \bitsetGetHex uses the uppercase letters A to F. The catcode of the letters is one of 11 (letter) or 12 (other).

```
\bitsetGetDec \{\langle BitSet \rangle\}
```

Macro \bitsetGetDec returns the bit set  $\langle BitSet \rangle$  as decimal number. The returned number can be larger than TeX's number limit of  $2^{31} - 1$ .

## 1.6.4 Logical operators

```
\bitsetAnd \{\langle BitSet\ A\rangle\}\ \{\langle BitSet\ B\rangle\}
```

$$A_{\text{new}} := A_{\text{old}} \text{ and } B \qquad (\forall \text{ bits})$$

## $\verb|\bitsetAndNot {|} \{ BitSet A \} \} \{ \{ BitSet B \} \}$

$$A_{\text{new}} := A_{\text{old}} \text{ and } (\text{not } B)$$
 ( $\forall \text{ bits}$ )

## \bitsetOr $\{\langle BitSet\ A\rangle\}\ \{\langle BitSet\ B\rangle\}$

$$A_{\text{new}} := A_{\text{old}} \text{ or } B \qquad (\forall \text{ bits})$$

### \bitsetXor $\{\langle BitSet \ A \rangle\}\ \{\langle BitSet \ B \rangle\}$

$$A_{\text{new}} := A_{\text{old}} \text{ xor } B \qquad (\forall \text{ bits})$$

#### 1.6.5 Shifting

```
\bitsetShiftLeft \{\langle BitSet \rangle\}\ \{\langle ShiftAmount \rangle\}\\bitsetShiftRight \{\langle BitSet \rangle\}\ \{\langle ShiftAmount \rangle\}\
```

A left shift by one is a multiplication by two, thus left shifting moves the flags to higher positions. The new created low positions are filled by zeros.

A right shift is the opposite, dividing by two, movint the bits to lower positions. The number will become smaller, the lowest bits are lost.

If the  $\langle ShiftAmount \rangle$  is negative, it reverts the meaning of the shift operation. A left shift becomes a right shift. A  $\langle ShiftAmount \rangle$  of zero is ignored.

#### 1.6.6 Bit manipulation

```
\bitsetClear \{\langle BitSet \rangle\}\ \{\langle Index \rangle\}\\bitsetSet \{\langle BitSet \rangle\}\ \{\langle Index \rangle\}\\bitsetFlip \{\langle BitSet \rangle\}\ \{\langle Index \rangle\}\
```

This macros manipulate a single bit in  $\langle BitSet \rangle$  addressed by \Index. Macro \bitsetClear disables the bit, \bitsetSet enables it and \bitsetFlip reverts the current setting of the bit.

## \bitsetSetValue $\{\langle BitSet \rangle\}\ \{\langle Index \rangle\}\ \{\langle Bit \rangle\}$

Macro \bitsetSetValue puts bit  $\langle Bit \rangle$  at position  $\langle Index \rangle$  in bit set  $\langle BitSet \rangle$ .  $\langle Bit \rangle$  must be a valid TeX number equals to zero (disabled/cleared) or one (enabled/set).

#### 1.6.7 Bit retrieval

## \bitsetGet $\{\langle BitSet \rangle\}\ \{\langle Index \rangle\}$

Macro \bitsetGet extracts the status of the bit at position  $\langle Index \rangle$  in bit set  $\langle BitSet \rangle$ . Digit 1 is returned if the bit is set/enabled. If the bit is cleared/disabled and in cases of an undefined bitset or an index number out of range the return value is 0.

## \bitsetNextClearBit $\{\langle BitSet \rangle\}\ \{\langle Index \rangle\}$

Starting at position  $\langle Index \rangle$  (inclusive) the bits are inspected. The first position without a set bit is returned. Possible results are decimal numbers:  $\langle Index \rangle$ ,  $\langle Index \rangle + 1, \ldots, (\infty)$ 

## \bitsetNextSetBit $\{\langle BitSet \rangle\}\ \{\langle Index \rangle\}$

Starting at position  $\langle Index \rangle$  (inclusive) the bits are inspected and the index position of the first found set bit is returned. If there isn't such a bit, then the result is -1. In summary possible results are decimal numbers: -1,  $\langle Index \rangle$ ,  $\langle Index \rangle$  + 1, ...,  $(\infty)$ 

### \bitsetGetSetBitList $\{\langle BitSet \rangle\}$

Macro \bitsetGetSetBitList is an application for \bitsetNextSetBit. The set bits are iterated and returned as comma separated list of index positions in increasing order. The list is empty in case of an empty bit set.

## 1.6.8 Bit set properties

### \bitsetSize $\{\langle BitSet \rangle\}$

Macro \bitsetSize returns number of bits in use. It is the same as the index number of the highest set/enabled bit incremented by one.

### \bitsetCardinality $\{\langle BitSet \rangle\}$

Macro \bitsetCardinality counts the number of set/enabled bits.

### 1.6.9 Queries

Also the query procedures are expandable. They ask for a piece of information about a bit set and execute code depending on the answer.

### \bitsetIsDefined $\{\langle BitSet \rangle\}\ \{\langle Then \rangle\}\ \{\langle Else \rangle\}$

If the bit set with the name  $\langle BitSet \rangle$  exists the code given in  $\langle Then \rangle$  is executed, otherwise  $\langle Else \rangle$  is used.

```
\bitsetIsEmpty \{\langle BitSet \rangle\}\ \{\langle Then \rangle\}\ \{\langle Else \rangle\}
```

If the bit set  $\langle BitSet \rangle$  exists and at least one bit is set/enabled, the code in  $\langle Then \rangle$  is executed,  $\langle Else \rangle$  otherwise.

```
\bitsetEquals \{\langle BitSet\ A\rangle\}\ \{\langle BitSet\ B\rangle\}\ \{\langle Then\rangle\}\ \{\langle Else\rangle\}
```

Both bit sets are equal if and only if either both are undefined or both are defined and represents the same bit values at the same positions. Thus this definition is reflexive, symmetric, and transitive, enough for an equivalent relation.

```
\bitsetIntersects \{\langle BitSet\ A\rangle\}\ \{\langle BitSet\ B\rangle\}\ \{\langle Then\rangle\}\ \{\langle Else\rangle\}
```

If and only if  $\langle BitSet A \rangle$  and  $\langle BitSet B \rangle$  have at least one bit at the same position that is set, then code part  $\langle Then \rangle$  is executed.

```
\bitsetQuery \{\langle BitSet \rangle\}\ \{\langle Index \rangle\}\ \{\langle Then \rangle\}\ \{\langle Else \rangle\}
```

It's just a wrapper for **\bitsetGet**. If the bit at position  $\langle Index \rangle$  is enabled, code  $\langle Then \rangle$  is called.

## 2 Implementation

The internal format of a bit set is quite simple, a sequence of digits 0 and 1. The least significant bit is left. A bit set without any flag set is encoded by 0. Also undefined bit sets are treated that way. After the highest bit that is set there are no further zeroes. A regular expression of valid bit sets values:

```
0|[01]*1
1 (*package)
```

## 2.1 Reload check and package identification

Reload check, especially if the package is not used with LATEX.

```
2 \begingroup
    \catcode44 12 % ,
3
    \catcode45 12 % -
    \catcode46 12 % .
5
    \catcode58 12 % :
6
    \catcode64 11 % @
7
    \catcode123 1 % {
8
    \catcode125 2 % }
    \expandafter\let\expandafter\x\csname ver@bitset.sty\endcsname
10
    \ifx\x\relax % plain-TeX, first loading
11
12
    \else
13
      \def\empty{}%
14
      \ifx\x\empty % LaTeX, first loading,
        % variable is initialized, but \ProvidesPackage not yet seen
15
      \else
16
17
        \catcode35 6 % #
18
        \expandafter\ifx\csname PackageInfo\endcsname\relax
19
          \def\x#1#2{%}
             \immediate\write-1{Package #1 Info: #2.}%
20
21
          }%
22
           \def\x#1#2{\PackageInfo{#1}{#2, stopped}}%
23
24
        \fi
```

```
\x{bitset}{The package is already loaded}%
 25
          \aftergroup\endinput
 26
        \fi
 27
      \fi
 28
 29 \endgroup
Package identification:
 30 \begingroup
      \catcode35 6 % #
 31
 32
      \catcode40 12 % (
 33
      \catcode41 12 % )
      \colored{catcode44 12 \%} ,
 34
      \catcode45 12 % -
 35
      \colored{catcode46} 12 % .
 36
      \catcode47 12 % /
 37
      \catcode58 12 % :
 38
 39
      \catcode64 11 % @
 40
      \catcode91 12 % [
      \catcode93 12 % ]
 41
      \catcode123 1 % {
 42
 43
      \catcode125 2 % }
 44
      \expandafter\ifx\csname ProvidesPackage\endcsname\relax
 45
        \def\x#1#2#3[#4]{\endgroup
          \immediate\write-1{Package: #3 #4}%
 46
          \xdef#1{#4}%
 47
        }%
 48
      \else
 49
        \def \x#1#2[#3] {\endgroup}
 50
 51
          #2[{#3}]%
 52
          \ifx#1\@undefined
 53
            \xdef#1{#3}%
          \fi
 55
          \int x#1\relax
            \xdef#1{#3}%
 56
          \fi
 57
        }%
 58
      \fi
 59
 60 \expandafter\x\csname ver@bitset.sty\endcsname
 61 \ProvidesPackage{bitset}%
      [2007/09/28 v1.0 Data type bit set (HO)]
2.2
       Catcodes
 63 \begingroup
      \catcode123 1 % {
 64
      \catcode125 2 % }
 65
      \def\x{\endgroup
 66
 67
        \expandafter\edef\csname BitSet@AtEnd\endcsname{%
 68
          \catcode35 \the\catcode35\relax
 69
          \catcode64 \the\catcode64\relax
 70
          \catcode123 \the\catcode123\relax
          \catcode125 \the\catcode125\relax
 71
        }%
 72
     }%
 73
 74 \x
 75 \catcode35 6 % #
 76 \catcode64 11 % @
 77 \catcode123 1 % {
 78 \catcode125 2 % }
 79 \def\TMP@EnsureCode#1#2{%
```

\edef\BitSet@AtEnd{%

\catcode#1 \the\catcode#1\relax

\BitSet@AtEnd

80

81

82

```
\catcode#1 #2\relax
                                                     84
                                                     85 }
                                                     86 \TMP@EnsureCode{33}{12}%!
                                                     87 \TMP@EnsureCode{39}{12}% '
                                                     88 \TMP@EnsureCode{40}{12}% (
                                                     89 \TMP@EnsureCode{41}{12}% )
                                                     90 \TMP@EnsureCode{42}{12}% *
                                                     91 \TMP@EnsureCode{43}{12}% +
                                                     92 \TMP@EnsureCode{44}{12}% ,
                                                     93 \TMP@EnsureCode{45}{12}% -
                                                     94 \TMP@EnsureCode{46}{12}% .
                                                     95 \TMP@EnsureCode{47}{12}% /
                                                     96 \TMP@EnsureCode{58}{11}% : (letter!)
                                                     97 \TMP@EnsureCode{60}{12}% <
                                                     98 \TMP@EnsureCode{61}{12}% =
                                                     99 \TMP@EnsureCode{62}{12}% >
                                                    100 \TMP@EnsureCode{63}{14}% ? (comment!)
                                                    101 \TMP@EnsureCode{96}{12}%
                                                    102 \verb|\begingroup\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafte
                                                    103 \verb|\expandafter\ifx\csname| BitSet@TestMode\endcsname\relax|
                                                    104 \else
                                                    105
                                                               \catcode63=9 % ? (ignore)
                                                    106 \fi
                                                    107 ? \let\BitSet@@TestMode\BitSet@TestMode
                                                  2.3
                                                               Package loading
                                                    108 \begingroup\expandafter\expandafter\expandafter\endgroup
                                                    109 \expandafter\ifx\csname RequirePackage\endcsname\relax
                                                    110 \input infwarerr.sty\relax
                                                    111
                                                               \input intcalc.sty\relax
                                                    112 \input bigintcalc.sty\relax
                                                    113 \else
                                                               \RequirePackage{infwarerr}[2007/09/09]%
                                                    114
                                                                \RequirePackage{intcalc}[2007/09/27]%
                                                    115
                                                                \RequirePackage{bigintcalc}[2007/09/27]%
                                                    116
                                                    117 \fi
                                                  2.4
                                                              Help macros
                                                  2.4.1 Number constant
         \BitSet@MaxSize
                                                    118 \def\BitSet@MaxSize{2147483647}%
                                                  2.4.2 General basic macros
              \BitSet@Empty
                                                    119 \def\BitSet@Empty{}
  \BitSet@FirstOfOne
                                                    120 \def\BitSet@FirstOfOne#1{#1}
           \BitSet@Gobble
                                                    121 \def\BitSet@Gobble#1{}
  \BitSet@FirstOfTwo
                                                    122 \def\BitSet@FirstOfTwo#1#2{#1}
\BitSet@SecondOfTwo
                                                    123 \def\BitSet@SecondOfTwo#1#2{#2}
```

83 }%

```
\BitSet@Space
                      124 \def\BitSet@Space{ }
   \BitSet@ZapSpace
                      125 \def\BitSet@ZapSpace#1 #2{%
                      126
                           #1%
                      127
                           \ifx\BitSet@Empty#2%
                      128
                           \else
                             \expandafter\BitSet@ZapSpace
                      129
                      130
                      131
                           #2%
                      132 }
                     2.4.3 Tail recursion
         \BitSet@Fi
                      133 \let\BitSet@Fi\fi
    \BitSet@AfterFi
                      134 \def\BitSet@AfterFi#1#2\BitSet@Fi{\fi#1}
  \BitSet@AfterFiFi
                      135 \def\BitSet@AfterFiFi#1#2\BitSet@Fi{\fi\fi#1}%
\BitSet@AfterFiFiFi
                      136 \def\BitSet@AfterFiFiFi#1#2\BitSet@Fi{\fi\fi\fi#1}%
                     2.4.4 Check macros
\BitSet@IfUndefined
                      137 \def\BitSet@IfUndefined#1{%
                           \expandafter\ifx\csname BS@#1\endcsname\relax
                      138
                             \expandafter\BitSet@FirstOfTwo
                      139
                      140
                           \else
                             \expandafter\BitSet@SecondOfTwo
                      141
                      142
                      143 }
\BitSet@CheckIndex #1: continuation code
                     #2: BitSet
                     #3: Index
                      144 \def\BitSet@CheckIndex#1#2#3{%
                      145 \BitSet@IfUndefined{#2}{\bitsetReset{#2}}{}%
                           \expandafter\expandafter\BitSet@@CheckIndex
                      146
                           \intcalcNum{#3}!%
                      147
                           {#2}{#1}%
                      148
                      149 }
\BitSet@@CheckIndex #1: plain Index
                     #2: BitSet
                     #3: continuation code
                      150 \def\BitSet@@CheckIndex#1!#2#3{%
                           \ifnum#1<0 %
                      152
                             \BitSet@AfterFi{%
                      153
                               \@PackageError{bitset}{%
                      154
                                 Invalid negative index (#1)%
                      155
                               }\@ehc
                             }%
                      156
                      157
                           \else
                             \BitSet@AfterFi{%
                      158
```

```
#3{#2}{#1}%
                    159
                    160
                          \BitSet@Fi
                    161
                    162 }
                          Miscellaneous
                   2.5
     \bitsetReset
                    163 \def\bitsetReset#1{%
                         \expandafter\def\csname BS@#1\endcsname{0}%
                    165 }
       \bitsetLet
                    166 \def\bitsetLet#1#2{%
                         \BitSet@IfUndefined{#2}{%
                    167
                            \bitsetReset{#1}%
                    168
                    169
                         ንፈ%
                            \expandafter\let\csname BS@#1\expandafter\endcsname
                    170
                                            \csname BS@#2\endcsname
                    171
                    172
                         }%
                    173 }
                          Import
                   2.6
                   2.6.1 From binary number
    \bitsetSetBin
                    174 \def\bitsetSetBin#1#2{%
                         \edef\BitSet@Temp{#2}%
                    175
                          \edef\BitSet@Temp{%
                    176
                            \expandafter\expandafter\expandafter\BitSet@ZapSpace
                    177
                            \expandafter\BitSet@Temp\BitSet@Space\BitSet@Empty
                    178
                    179
                    180
                          \edef\BitSet@Temp{%
                            \expandafter\BitSet@KillZeros\BitSet@Temp\BitSet@Empty
                    181
                    182
                          \ifx\BitSet@Temp\BitSet@Empty
                    183
                            \expandafter\let\csname BS@#1\endcsname\BitSet@Zero
                    184
                    185
                          \else
                            \expandafter\edef\csname BS@#1\endcsname{%
                    186
                    187
                              \expandafter\BitSet@Reverse\BitSet@Temp!%
                            }%
                    188
                          \fi
                    189
                    190 }
\BitSet@KillZeros
                    191 \def\BitSet@KillZeros#1{%
                    192
                         \ifx#10%
                            \expandafter\BitSet@KillZeros
                    193
                          \else
                    194
                    195
                            #1%
                          \fi
                    196
                    197 }
  \BitSet@Reverse
                    198 \def\BitSet@Reverse#1#2!{%
                         \ifx\\#2\\%
                    199
                            #1%
                    200
                    201
                          \else
```

202

203

\BitSet@AfterFi{%

\BitSet@Reverse#2!#1%

```
204
                              }%
                            \BitSet@Fi
                       205
                       206 }
                      2.6.2 From octal/hex number
       \bitsetSetOct
                       207 \def\bitsetSetOct{%
                       208 \BitSet@SetOctHex\BitSet@FromFirstOct
                       209 }
       \bitsetSetHex
                       210 \def\bitsetSetHex{%
                       211 \BitSet@SetOctHex\BitSet@FromFirstHex
                       212 }
   \BitSet@SetOctHex
                       213 \def\BitSet@SetOctHex#1#2#3{%
                       214 \edef\BitSet@Temp{#3}%
                       215
                            \edef\BitSet@Temp{%
                       216
                              \verb|\expandafter\expandafter\expandafter\BitSet@ZapSpace|
                              \expandafter\BitSet@Temp\BitSet@Space\BitSet@Empty
                       217
                       218
                            }%
                       219
                            \edef\BitSet@Temp{%
                              \expandafter\BitSet@KillZeros\BitSet@Temp\BitSet@Empty
                       220
                       221
                       222
                            \ifx\BitSet@Temp\BitSet@Empty
                       223
                              \expandafter\let\csname BS@#2\endcsname\BitSet@Zero
                       224
                            \else
                       225
                              \edef\BitSet@Temp{%
                                \expandafter#1\BitSet@Temp!%
                       226
                       227
                       228
                              \ifx\BitSet@Temp\BitSet@Empty
                                \expandafter\let\csname BS@#2\endcsname\BitSet@Zero
                       229
                       230
                       231
                                 \expandafter\edef\csname BS@#2\endcsname{%
                       232
                                   \expandafter\BitSet@Reverse\BitSet@Temp!%
                       233
                                }%
                       234
                              \fi
                            \fi
                       235
                       236 }
\BitSet@FromFirstOct
                       237 \def\BitSet@FromFirstOct#1{%
                       238 \ifx#1!%
                       239 \else
                              \ifcase#1 \BitSet@AfterFiFi\BitSet@FromFirstOct
                       240
                       241
                       242
                              \or 10%
                       243
                              \or 11%
                       244
                              \or 100%
                       245
                              \or 101%
                              \or 110%
                       246
                              \or 111%
                       247
                              \else \BitSetError:WrongOctalDigit%
                       248
                       249
                              \expandafter\BitSet@FromOct
                       250
                           \BitSet@Fi
                       251
                       252 }
```

\BitSet@FromOct

```
253 \def\BitSet@FromOct#1{%
                             \ifx#1!%
                        254
                        255
                             \else
                               \ifcase#1 000%
                        256
                        257
                               \or 001%
                               \or 010%
                        258
                               \or 011%
                        259
                               \or 100%
                        260
                               \or 101%
                        261
                               \or 110%
                        262
                        263
                               \or 111%
                        264
                               \else \BitSetError:WrongOctalDigit%
                        265
                               \expandafter\BitSet@FromOct
                        266
                        267
                             \fi
                        268 }
\BitSet@FromFirstHex
                        269 \def\BitSet@FromFirstHex#1{%
                        270
                            \ifx#1!%
                             \else
                        271
                               \ifx#10%
                        272
                                 \BitSet@AfterFiFi\BitSet@FromFirstHex
                        273
                        274
                                \expandafter\ifx\csname BitSet@Hex#1\endcsname\relax
                        275
                                 \BitSetError:InvalidHexDigit%
                        276
                        277
                        278
                                  \expandafter\expandafter\expandafter\BitSet@KillZeros
                        279
                                  \csname BitSet@Hex#1\endcsname
                        280
                                \expandafter\BitSet@FromHex
                        281
                             \BitSet@Fi
                        282
                        283 }
     \BitSet@FromHex
                        284 \def\BitSet@FromHex#1{%
                        285
                             \ifx#1!%
                             \else
                        286
                        287
                                \expandafter\ifx\csname BitSet@Hex#1\endcsname\relax
                                  \BitSetError:InvalidHexDigit%
                        288
                        289
                        290
                                  \csname BitSet@Hex#1\endcsname
                        291
                                \fi
                               \expandafter\BitSet@FromHex
                        292
                             \fi
                        293
                        294 }
   \BitSet@Hex[0..F]
                        295 \def\BitSet@Temp#1{%
                             \expandafter\def\csname BitSet@Hex#1\endcsname
                        296
                        298 \BitSet@Temp 0{0000}%
                        299 \BitSet@Temp 1{0001}%
                        300 \BitSet@Temp 2{0010}%
                        301 \BitSet@Temp 3{0011}%
                        302 \BitSet@Temp 4{0100}%
                        303 \BitSet@Temp 5{0101}%
                        304 \BitSet@Temp 6{0110}%
                        305 \BitSet@Temp 7{0111}%
                        306 \BitSet@Temp 8{1000}%
                        307 \BitSet@Temp 9{1001}%
                        308 \BitSet@Temp A{1010}%
```

```
309 \BitSet@Temp B{1011}%
310 \BitSet@Temp C{1100}%
311 \BitSet@Temp D{1101}%
312 \BitSet@Temp E{1110}%
313 \BitSet@Temp F{1111}%
314 \BitSet@Temp a{1010}%
315 \BitSet@Temp b{1011}%
316 \BitSet@Temp c{1100}%
317 \BitSet@Temp d{1101}%
318 \BitSet@Temp e{1110}%
319 \BitSet@Temp f{1111}%
```

#### 2.6.3 From decimal number

\bitsetSetDec

```
320 \def\bitsetSetDec#1#2{%
               \edef\BitSet@Temp{#2}%
321
               \edef\BitSet@Temp{%
322
323
                      \expandafter\expandafter\expandafter\BitSet@ZapSpace
324
                      \expandafter\BitSet@Temp\BitSet@Space\BitSet@Empty
325
326
                \edef\BitSet@Temp{%
327
                      \expandafter\BitSet@KillZeros\BitSet@Temp\BitSet@Empty
328
                \ifx\BitSet@Temp\BitSet@Empty
329
                      \expandafter\let\csname BS@#1\endcsname\BitSet@Zero
330
                \else
331
                      \ifcase\bigintcalcSgn{\BitSet@Temp} %
332
                            \expandafter\let\csname BS@#1\endcsname\BitSet@Zero
333
334
                             \ifnum\bigintcalcCmp\BitSet@Temp\BitSet@MaxSize>0 %
335
                                   \expandafter\edef\csname BS@#1\endcsname{%
336
337
                                         \expandafter\BitSet@SetDecBig\BitSet@Temp!%
                                  }%
338
339
                            \else
                                  \expandafter\edef\csname BS@#1\endcsname{%
340
341
                                         \expandafter\BitSet@SetDec\BitSet@Temp!%
                                  ጉ%
342
                            \fi
343
                      \else
344
                             \@PackageError{bitset}{%
345
                                  Bit sets cannot be negative%
346
347
                            }\@ehc
348
                      \fi
349
               \fi
350 }
351 \ensuremath{\mbox{\mbox{$1$} \mbox{$4$}} \ensuremath{\mbox{\mbox{$4$}} \mbox{$4$}} \ensuremath{\mbox{$4$}} \ensuremath{\
                \ifx\\#9\\%
352
                      \BitSet@SetDec#1#2#3#4#5#6#7#8!%
353
354
                      \ifcase\BigIntCalcOdd#1#2#4#5#6#7#8#9! %
355
356
357
                      \or
```

\BitSet@SetDecBig

```
351 \def\BitSet@SetDecBig#1#2#3#4#5#6#7#8#9!{%
352 \ifx\\#9\\%
353 \BitSet@SetDec#1#2#3#4#5#6#7#8!%
354 \else
355 \ifcase\BigIntCalcOdd#1#2#4#5#6#7#8#9! %
356 O%
357 \or
358 1%
359 ? \else\BitSetError:ThisCannotHappen%
360 \fi
361 \BitSet@AfterFi{%
362 \expandafter\expandafter\BitSet@SetDecBig
363 \BigIntCalcShr#1#2#3#4#5#6#7#8#9!!%
364 }%
```

```
\BitSet@Fi
                   365
                   366 }
 \BitSet@SetDec
                   367 \def\BitSet@SetDec#1!{%
                   368
                       \ifcase#1 %
                        \or 1%
                   369
                  370
                       \else
                          \ifodd#1 %
                  371
                   372
                            1%
                   373
                          \else
                   374
                   375
                          \fi
                   376
                          \BitSet@AfterFi{%
                   377
                            \expandafter\expandafter\expandafter\BitSet@SetDec
                   378
                            \IntCalcShr#1!!%
                          }%
                   379
                        \BitSet@Fi
                   380
                  381 }
                  2.7
                         Export
                  2.7.1
                         To binary number
  \bitsetGetBin
                   382 \def\bitsetGetBin#1#2{%
                  383 \romannumeral0%
                        \expandafter\expandafter\expandafter\BitSet@@GetBin
                        \intcalcNum{#2}!{#1}%
                  385
                  386 }
\BitSet@@GetBin
                   387 \def\BitSet@@GetBin#1!#2{%
                   388
                       \BitSet@IfUndefined{#2}{%
                   389
                          \ifnum#1>1 %
                   390
                            \BitSet@AfterFi{%
                              \expandafter\expandafter\expandafter\BitSet@Fill
                   391
                   392
                              \IntCalcDec#1!!0%
                            }%
                   393
                          \else
                   394
                            \BitSet@AfterFi{ 0}%
                   395
                          \BitSet@Fi
                   396
                   397
                        }{%
                          \expandafter\expandafter\expandafter\BitSet@NumBinRev
                   398
                          \expandafter\expandafter\expandafter1%
                   399
                          \expandafter\expandafter\expandafter!%
                   400
                   401
                          \csname BS@#2\endcsname!!#1!%
                   402
                       }%
                   403 }
   \BitSet@Fill #1: number of leading digits 0
                  #2: result
                   404 \def\BitSet@Fill#1!{%
                        \ifnum#1>0 %
                   405
                   406
                          \BitSet@AfterFi{%
                   407
                            \expandafter\expandafter\expandafter\BitSet@Fill
                   408
                            \IntCalcDec#1!!0%
                   409
                          }%
                   410
                        \else
                          \BitSet@AfterFi{ }%
                   411
                       \BitSet@Fi
                  412
                  413 }
```

```
#1: bit counter (including #2)
 \BitSet@NumBinRev
                    #2#3: reverted number
                    #4: result
                    #5: min size
                     414 \def\BitSet@NumBinRev#1!#2#3!{%
                     415
                          \ifx\\#3\\%
                             \BitSet@AfterFi{%
                     416
                               \BitSet@NumBinFill#1!#2%
                     417
                     418
                            }%
                     419
                          \else
                     420
                             \BitSet@AfterFi{%
                               \expandafter\expandafter\expandafter\BitSet@NumBinRev
                     421
                     422
                               \IntCalcInc#1!!#3!#2%
                     423
                            }%
                     424
                          \BitSet@Fi
                     425 }
\BitSet@NumBinFill
                     426 \def\BitSet@NumBinFill#1!#2!#3!{%
                         \ifnum#3>#1 %
                     427
                            \BitSet@AfterFi{%
                     428
                               \expandafter\expandafter\expandafter\BitSet@Fill
                     429
                               \IntCalcSub#3!#1!!#2%
                     430
                     431
                            }%
                     432
                          \else
                     433
                            \BitSet@AfterFi{ #2}%
                     434
                          \BitSet@Fi
                     435 }
                    2.7.2
                            To octal/hexadecimal number
     \bitsetGetOct
                     436 \def\bitsetGetOct#1#2{%
                     437
                          \romannumeral0%
                          \bitsetIsEmpty{#1}{%
                     438
                             \verb|\expandafter| expandafter| BitSet@@GetOctHex|
                     439
                             \intcalcNum{#2}!3!230%
                     440
                          ጉና%
                     441
                     442
                             \expandafter\expandafter\expandafter\BitSet@@GetOct
                     443
                             \expandafter\expandafter\expandafter1%
                     444
                             \expandafter\expandafter\expandafter!%
                     445
                             \expandafter\expandafter\expandafter!%
                     446
                             \csname BS@#1\endcsname00%
                             \BitSet@Empty\BitSet@Empty\BitSet@Empty!{#2}%
                     447
                          }%
                     448
                     449 }
     \bitsetGetHex
                     450 \def\bitsetGetHex#1#2{%
                          \romannumeral0%
                     451
                          \verb|\bitsetIsEmpty{#1}{%}|
                     452
                     453
                             \expandafter\expandafter\expandafter\BitSet@@GetOctHex
                             \intcalcNum{#2}!4!340%
                     454
                     455
                          }{%
                     456
                             \expandafter\expandafter\expandafter\BitSet@@GetHex
                     457
                             \expandafter\expandafter\expandafter1%
                     458
                             \expandafter\expandafter\expandafter!%
                     459
                             \expandafter\expandafter\expandafter!%
                             \csname BS@#1\endcsname000%
                     460
                             \BitSet@Empty\BitSet@Empty\BitSet@Empty!{#2}%
                     461
                     462
                          }%
                     463 }
```

```
\BitSet@@GetOct #1: number of digits
                          #2: result
                          #3#4#5: bits
                           464 \def\BitSet@@GetOct#1!#2!#3#4#5{%
                                \ifx#5\BitSet@Empty
                           465
                                   \BitSet@AfterFi{%
                           466
                                     \expandafter\expandafter\expandafter\BitSet@GetOctHex
                           467
                           468
                                     \IntCalcDec#1!!#2!23%
                                  }%
                           469
                           470
                               \else
                                   \BitSet@AfterFi{%
                           471
                           472
                                     \expandafter\expandafter\expandafter\BitSet@@GetOct
                           473
                                     \number\IntCalcInc#1!\expandafter\expandafter\expandafter!%
                           474
                                     \csname BitSet@Oct#5#4#3\endcsname#2!%
                                   }%
                           475
                                \BitSet@Fi
                           476
                           477 }
  \BitSet@Oct[000..111]
                           478 \def\BitSet@Temp#1#2#3#4{%
                           479
                                 \expandafter\def\csname BitSet@Oct#1#2#3\endcsname{#4}%
                           480 }
                           481 \BitSet@Temp0000%
                           482 \BitSet@Temp0011%
                           483 \BitSet@Temp0102%
                           484 \BitSet@Temp0113%
                           485 \BitSet@Temp1004%
                           486 \BitSet@Temp1015%
                           487 \BitSet@Temp1106%
                           488 \BitSet@Temp1117%
        \BitSet@@GetHex #1: number of digits
                          #2: result
                          #3#4#5#6: bits
                           489 \def\BitSet@@GetHex#1!#2!#3#4#5#6{%
                                \ifx#6\BitSet@Empty
                           490
                                   \BitSet@AfterFi{%
                           491
                           492
                                     \expandafter\expandafter\expandafter\BitSet@GetOctHex
                                     \IntCalcDec#1!!#2!34%
                           493
                           494
                                  }%
                           495
                                \else
                           496
                                   \BitSet@AfterFi{%
                                     \verb|\expandafter| expandafter | \verb|\expandafter| BitSet@@GetHex| \\
                           497
                                     \number\IntCalcInc#1!\expandafter\expandafter\expandafter!%
                           498
                                     \csname BitSet@Hex#6#5#4#3\endcsname#2!%
                           499
                                  }%
                           500
                           501
                                 \BitSet@Fi
                           502 }
\BitSet@Hex[0000..1111]
                           503 \def\BitSet@Temp#1#2#3#4#5{%
                                \expandafter\def\csname BitSet@Hex#1#2#3#4\endcsname{#5}%
                           505 }
                           506 \BitSet@Temp00000%
                           507 \BitSet@Temp00011%
                           508 \BitSet@Temp00102%
                           509 \BitSet@Temp00113%
                           510 \BitSet@Temp01004%
                           511 \BitSet@Temp01015%
                           512 \BitSet@Temp01106%
                           513 \BitSet@Temp01117%
```

```
514 \BitSet@Temp10008%
                      515 \BitSet@Temp10019%
                     516 \BitSet@Temp1010A%
                     517 \BitSet@Temp1011B%
                      518 \BitSet@Temp1100C%
                      519 \BitSet@Temp1101D%
                      520 \BitSet@Temp1110E%
                     521 \BitSet@Temp1111F%
                    Leading zeros (\#4 - \#1 * 3 + 2)/3 if \#4 > \#1 * 3
 \BitSet@GetOctHex
                     #1: digit size
                     #2: result
                     #3: bits per digit - 1
                     #4: bits per digit #5: garbage
                     #6: min size
                      522 \def\BitSet@GetOctHex#1!#2!#3#4#5!#6{%
                           \expandafter\BitSet@@GetOctHex
                          \number\intcalcNum{#6}\expandafter\expandafter\expandafter!%
                      524
                           \IntCalcMul#1!#4!!#3#4#2%
                      526 }
\BitSet@@GetOctHex #1: plain min size
                     #2: digits * (bits per digit)
                     #3: bits per digit - 1
                     #4: bits per digit
                      527 \def\BitSet@@GetOctHex#1!#2!#3#4{%
                      528
                          \ifnum#1>#2 %
                      529
                             \BitSet@AfterFi{%
                      530
                               \expandafter\expandafter\expandafter
                      531
                               \expandafter\expandafter\expandafter\BitSet@Fill
                               \expandafter\IntCalcDiv\number
                      532
                               \expandafter\expandafter\IntCalcAdd
                      533
                      534
                               \IntCalcSub#1!#2!!#3!!#4!!%
                      535
                             }%
                           \else
                      536
                      537
                             \BitSet@AfterFi{ }%
                      538
                           \BitSet@Fi
                     539 }
                     2.7.3
                            To decimal number
     \bitsetGetDec
                      540 \def\bitsetGetDec#1{%
                           \romannumeral0%
                      541
                           \BitSet@IfUndefined{#1}{ 0}{%
                     542
                             \expandafter\expandafter\expandafter\BitSet@GetDec
                      543
                      544
                             \csname BS@#1\endcsname!%
                          }%
                      545
                      546 }
    \BitSet@GetDec
                      547 \def\BitSet@GetDec#1#2!{%}
                          \ifx\\#2\\%
                     548
                             \BitSet@AfterFi{ #1}%
                     549
                           \else
                      550
                             \BitSet@AfterFi{%
                      551
                               \BitSet@@GetDec2!#1!#2!%
                      552
                      553
                           \BitSet@Fi
                      554
                      555 }
```

```
\BitSet@@GetDec #1: power of two
                       #2: result
                       #3#4: number
                        556 \def\BitSet@@GetDec#1!#2!#3#4!{%
                             \ifx\\#4\\%
                        557
                               \ifx#31%
                        558
                                 \BitSet@AfterFiFi{%
                        559
                        560
                                   \expandafter\expandafter\expandafter\BitSet@Space
                        561
                                   \IntCalcAdd#1!#2!%
                                 }%
                        562
                        563
                               \else
                                 \BitSet@AfterFiFi{ #2}%
                        564
                        565
                               \fi
                        566
                            \else
                               \ifx#31%
                        567
                                 \BitSet@AfterFiFi{%
                        568
                                   \csname BitSet@N#1%
                        569
                                   \expandafter\expandafter\endcsname
                        570
                                   \IntCalcAdd#1!#2!!#4!%
                        571
                        572
                                 }%
                        573
                               \else
                        574
                                 \BitSet@AfterFiFi{%
                        575
                                   \csname BitSet@N#1\endcsname#2!#4!%
                        576
                               \fi
                        577
                             \BitSet@Fi
                        578
                        579 }
\BitSet@N[1,2,4,...]
                        580 \def\BitSet@Temp#1#2{%
                             \expandafter\def\csname BitSet@N#1\endcsname{%
                        581
                               \BitSet@@GetDec#2!%
                        582
                        583
                             }%
                        584 }
                        585 \BitSet@Temp{1}{2}
                        586 \BitSet@Temp{2}{4}
                        587 \BitSet@Temp{4}{8}
                        588 \BitSet@Temp{8}{16}
                        589 \BitSet@Temp{16}{32}
                        590 \BitSet@Temp{32}{64}
                        591 \BitSet@Temp{64}{128}
                        592 \BitSet@Temp{128}{256}
                        593 \BitSet@Temp{256}{512}
                        594 \BitSet@Temp{512}{1024}
                        595 \BitSet@Temp{1024}{2048}
                        596 \BitSet@Temp{2048}{4096}
                        597 \BitSet@Temp{4096}{8192}
                        598 \BitSet@Temp{8192}{16384}
                        599 \BitSet@Temp{16384}{32768}
                        600 \BitSet@Temp{32768}{65536}
                        601 \BitSet@Temp{65536}{131072}
                        602 \BitSet@Temp{131072}{262144}
                        603 \BitSet@Temp{262144}{524288}
                        604 \BitSet@Temp{524288}{1048576}
                        605 \BitSet@Temp{1048576}{2097152}
                        606 \BitSet@Temp{2097152}{4194304}
                        607 \BitSet@Temp{4194304}{8388608}
                        608 \BitSet@Temp{8388608}{16777216}
                        609 \BitSet@Temp{16777216}{33554432}
                        610 \BitSet@Temp{33554432}{67108864}
                        611 \BitSet@Temp{67108864}{134217728}
                        612 \BitSet@Temp{134217728}{268435456}
```

```
613 \BitSet@Temp{268435456}{536870912}
                      614 \text{BitSet@Temp} \{536870912\} \{1073741824\}
\BitSet@N1073741824
                      615 \expandafter\def\csname BitSet@N1073741824\endcsname{%
                      616 \BitSet@GetDecBig2147483648!%
                      617 }%
  \BitSet@GetDecBig
                     #1: current power of two
                      #2: result
                     #3#4: number
                      618 \def\BitSet@GetDecBig#1!#2!#3#4!{%
                           \ifx\\#4\\%
                      619
                              \ifx#31%
                      620
                      621
                                \BitSet@AfterFiFi{%
                      622
                                  \expandafter\expandafter\BitSet@Space
                                  \BigIntCalcAdd#1!#2!%
                      623
                                }%
                      624
                              \else
                      625
                                \BitSet@AfterFiFi{ #2}%
                      626
                              \fi
                      627
                      628
                           \else
                             \ifx#31%
                      629
                                \BitSet@AfterFiFi{%
                      630
                                  \expandafter\expandafter\expandafter\BitSet@@GetDecBig
                      631
                      632
                                  \BigIntCalcAdd#1!#2!!#1!#4!%
                      633
                                }%
                      634
                              \else
                      635
                                \BitSet@AfterFiFi{%
                      636
                                  \expandafter\expandafter\expandafter\BitSet@GetDecBig
                      637
                                  \BigIntCalcShl#1!!#2!#4!%
                                }%
                      638
                              \fi
                      639
                            \BitSet@Fi
                      640
                      641 }
\BitSet@@GetDecBig #1: result
                     #2: power of two
                     #3#4: number
                      642 \def\BitSet@@GetDecBig#1!#2!{%
                           \expandafter\expandafter\expandafter\BitSet@GetDecBig
                      644
                            \BigIntCalcShl#2!!#1!%
                      645 }
```

## 2.8 Logical operators

## 2.8.1 \bitsetAnd

\bitsetAnd Decision table for \bitsetAnd:

	undef(B)	empty(B)	cardinality(B)>0
undef(A)	A := empty	A := empty	A := empty
empty(A)			
$\overline{\text{cardinality}(A)} > 0$	A := empty	A := empty	A &= B

```
646 \def\bitsetAnd#1#2{%
647 \bitsetIsEmpty{#1}{%
648 \bitsetReset{#1}%
649 }{%
650 \bitsetIsEmpty{#2}{%
651 \bitsetReset{#1}%
652 }{%
```

```
\expandafter\edef\csname BS@#1\endcsname{%
               653
                           \expandafter\expandafter\expandafter\BitSet@And
               654
                           \csname BS@#1\expandafter\expandafter\expandafter\endcsname
               655
                           \expandafter\expandafter\expandafter!%
               656
               657
                           \csname BS@#2\endcsname!!%
                        }%
               658
               659
                        \expandafter\ifx\csname BS@#1\endcsname\BitSet@Empty
               660
                          \bitsetReset{#1}%
                        \fi
               661
                      }%
               662
                    }%
               663
               664 }
\BitSet@And
               665 \def\BitSet@And#1#2!#3#4!#5!{%
               666
                    \int x^{\#2}\
               667
                      \ifnum#1#3=11 #51\fi
               668
                    \else
               669
                      \ifx\\#4\\%
                        \ifnum#1#3=11 #51\fi
               670
                      \else
               671
                        \ifnum#1#3=11 %
               672
                          #51%
               673
                          \BitSet@AfterFiFiFi{%
               674
                             \BitSet@And#2!#4!!%
               675
                          }%
               676
               677
                        \else
               678
                          \BitSet@AfterFiFiFi{%
               679
                             \BitSet@And#2!#4!#50!%
               680
                          }%
                        \fi
               681
                      \fi
               682
                    \BitSet@Fi
               683
              684 }
```

#### 2.8.2 \bitsetAndNot

\bitsetAndNot Decision table for \bitsetAndNot:

	undef(B)	empty(B)	cardinality(B)>0
undef(A)	A := empty	A := empty	A := empty
empty(A)			
cardinality(A)>0			A &= !B

```
685 \def\bitsetAndNot#1#2{%
                             \bitsetIsEmpty{#1}{%
686
                                           \bitsetReset{#1}%
687
688
                                           \bitsetIsEmpty{#2}{%
689
                                         }{%
690
                                                      \expandafter\edef\csname BS@#1\endcsname{%
691
                                                                  \expandafter\expandafter\expandafter\BitSet@AndNot
692
                                                                  \verb|\csname| BS0#1\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter
693
694
                                                                  \expandafter\expandafter\expandafter!%
695
                                                                  \csname BS@#2\endcsname!!%
696
697
                                                       \expandafter\ifx\csname BS@#1\endcsname\BitSet@Empty
698
                                                                  \bitsetReset{#1}%
699
                                                      \fi
                                         }%
700
                           }%
701
702 }
```

#### \BitSet@AndNot

```
703 \def\BitSet@AndNot#1#2!#3#4!#5!{%
    \ifx\\#2\\%
704
       \ifnum#1#3=10 #51\fi
705
706
     \else
707
       \ifx\\#4\\%
708
         \ifnum#1#3=10 1\else 0\fi
709
         #2%
710
711
       \else
         \ifnum#1#3=10 %
712
           #51%
713
           \BitSet@AfterFiFiFi{%
714
             \BitSet@AndNot#2!#4!!%
715
           }%
716
         \else
717
           \BitSet@AfterFiFiFi{%
718
719
              \BitSet@AndNot#2!#4!#50!%
720
           }%
721
         \fi
722
       \fi
723
     \BitSet@Fi
724 }
```

#### 2.8.3 \bitsetOr

\bitsetOr Decision table for \bitsetOr:

	undef(B)	empty(B)	cardinality(B)>0
undef(A)	A := empty	A := empty	A := B
empty(A)			A := B
cardinality(A) > 0			A  = B

```
725 \def\bitsetOr#1#2{%
                                                                            \bitsetIsEmpty{#2}{%
                                                       726
                                                                                     \verb|\BitSet@IfUndefined{#1}{\bitsetReset{#1}}{}|
                                                       727
                                                       728
                                                                           }{%
                                                                                     \bitsetIsEmpty{#1}{%
                                                       729
                                                       730
                                                                                             \expandafter\let\csname BS@#1\expandafter\endcsname
                                                       731
                                                                                                                                                                \csname BS@#2\endcsname
                                                       732
                                                       733
                                                                                             \expandafter\edef\csname BS@#1\endcsname{%
                                                       734
                                                                                                      \verb|\expandafter| expandafter| BitSet@Or |
                                                                                                      \verb|\csname| BSQ#1\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter\expandafter
                                                       735
                                                                                                      \expandafter\expandafter\expandafter!%
                                                       736
                                                                                                      \csname BS@#2\endcsname!%
                                                       737
                                                       738
                                                                                            }%
                                                       739
                                                                                    }%
                                                       740
                                                                           }%
                                                       741 }
\BitSet@Or
                                                       742 \def\BitSet@Or#1#2!#3#4!{%
                                                                         \ifnum#1#3>0 1\else 0\fi
                                                       744
                                                                           \ifx\\#2\\%
                                                       745
                                                                                    #4%
                                                       746
                                                                            \else
                                                                                    \ifx\\#4\\%
                                                       747
                                                                                            #2%
                                                       748
                                                       749
                                                                                     \else
                                                                                             \BitSet@AfterFiFi{%
                                                       750
                                                                                                     \BitSet@0r#2!#4!%
                                                       751
```

```
752 }%
753 \fi
754 \BitSet@Fi
755}
```

#### 2.8.4 \bitsetXor

\bitsetXor Decision table for \bitsetXor:

	undef(B)	empty(B)	cardinality(B)>0
undef(A)	A := empty	A := empty	A := B
empty(A)			A := B
cardinality(A)>0			A = B

```
756 \def\bitsetXor#1#2{%
                                                                 \bitsetIsEmpty{#2}{%
                                                757
                                                                         \BitSet@IfUndefined{#1}{\bitsetReset{#1}}{}%
                                                758
                                                                 }{%
                                                759
                                                                         \bitsetIsEmpty{#1}{%
                                                760
                                                                                \expandafter\let\csname BS@#1\expandafter\endcsname
                                                761
                                                                                                                                       \csname BS@#2\endcsname
                                                762
                                                                        }{%
                                                763
                                                764
                                                                                \expandafter\edef\csname BS@#1\endcsname{%
                                                765
                                                                                       \expandafter\expandafter\BitSet@Xor
                                                766
                                                                                       \verb|\csname| BS0#1\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter\\expandafter
                                                767
                                                                                       \expandafter\expandafter!%
                                                768
                                                                                       \csname BS@#2\endcsname!!%
                                                                                }%
                                                769
                                                                                 \expandafter\ifx\csname BS@#1\endcsname\BitSet@Empty
                                                770
                                                                                       \bitsetReset{#1}%
                                                771
                                                772
                                                                                \fi
                                                                        }%
                                                773
                                                774
                                                                 }%
                                                775 }
\BitSet@Xor
                                                776 \def\BitSet@Xor#1#2!#3#4!#5!{%
                                                                 \ifx\\#2\\%
                                                778
                                                                         \ifx#1#3%
                                                                                \ifx\\#4\\%
                                                779
                                                780
                                                                                \else
                                                                                      #50#4%
                                                781
                                                                                \fi
                                                782
                                                                         \else
                                                783
                                                                                #51#4%
                                                784
                                                785
                                                                         \fi
                                                786
                                                                  \else
                                                                        \ifx\\#4\\%
                                                787
                                                788
                                                                                #5%
                                                                                \fint 1#30\else 1\fint 1
                                                789
                                                                                #2%
                                                790
                                                                         \else
                                                791
                                                                                \ifx#1#3%
                                                792
                                                                                       \BitSet@AfterFiFiFi{%
                                                793
                                                                                              \BitSet@Xor#2!#4!#50!%
                                                794
                                                                                      }%
                                                795
                                                796
                                                                                \else
                                                797
                                                                                      #51%
                                                                                       \BitSet@AfterFiFiFi{%
                                                798
                                                                                              \BitSet@Xor#2!#4!!%
                                                799
                                                                                      }%
                                                800
                                                                                \fi
                                                801
```

```
802
                              \fi
                           \BitSet@Fi
                      803
                      804 }
                     2.8.5
                             Shifting
                     2.8.6
                             \bitsetShiftLeft
  \bitsetShiftLeft
                      805 \def\bitsetShiftLeft#1#2{%
                           \BitSet@IfUndefined{#1}{%
                      806
                             \bitsetReset{#1}%
                      807
                      808
                           }{%
                             \bitsetIsEmpty{#1}{%
                      809
                      810
                             }{%
                                \expandafter\expandafter\expandafter\BitSet@ShiftLeft
                      811
                      812
                                \intcalcNum{#2}!{#1}%
                      813
                             }%
                      814
                           }%
                      815 }
 \BitSet@ShiftLeft
                      816 \def\BitSet@ShiftLeft#1!#2{%
                           \ifcase\intcalcSgn{#1} %
                      817
                      818
                           \or
                              \begingroup
                      819
                               \uccode'm='0 %
                      820
                      821
                              \uppercase\expandafter{\expandafter\endgroup
                      822
                                \expandafter\edef\csname BS@#2\expandafter\endcsname
                      823
                                \expandafter{%
                      824
                                  \romannumeral#1000\expandafter\BitSet@Space
                                  \csname BS@#2\endcsname
                      825
                      826
                               }%
                             }%
                      827
                           \else
                      828
                              \expandafter\BitSet@ShiftRight\BitSet@Gobble#1!{#2}%
                      829
                      830
                      831 }
                     2.8.7
                             \bitsetShiftRight
 \bitsetShiftRight
                      832 \def\bitsetShiftRight#1#2{%
                           \BitSet@IfUndefined{#1}{%
                      834
                              \bitsetReset{#1}%
                      835
                           }{%
                      836
                              \bitsetIsEmpty{#1}{%
                      837
                             }{%
                                \expandafter\expandafter\expandafter\BitSet@ShiftRight
                      838
                                \int \int d^2 x dx dx
                      839
                             }%
                      840
                      841
                           }%
                      842 }
\BitSet@ShiftRight
                      843 \def\BitSet@ShiftRight#1!#2{%
                      844
                           \ifcase\intcalcSgn{#1} %
                      845
                           \or
                              \expandafter\edef\csname BS@#2\endcsname{%
                      846
                                \expandafter\expandafter\expandafter\BitSet@Kill
                      847
                                \csname BS@#2\expandafter\endcsname\expandafter\BitSet@Empty
                      848
```

\expandafter=%

849

```
\expandafter{\expandafter}\expandafter{\expandafter}%
                    850
                             \romannumeral#1000!%
                    851
                           }%
                    852
                    853
                         \else
                    854
                           \expandafter\BitSet@ShiftLeft\BitSet@Gobble#1!{#2}%
                    855
                         \fi
                   856 }
    \BitSet@Kill
                   857 \def\BitSet@Kill#1#2=#3#4#5{%
                   858 #3#4%
                   859
                        \ifx#5!%
                    860
                          \ifx#1\BitSet@Empty
                    861
                    862
                           \else
                    863
                             #1#2%
                           \fi
                    864
                        \else
                    865
                           \ifx#1\BitSet@Empty
                    866
                             0%
                    867
                             \BitSet@AfterFiFi\BitSet@Cleanup
                    868
                    869
                           \else
                             \BitSet@Kill#2=%
                    870
                    871
                           \fi
                   872
                        \BitSet@Fi
                   873 }
                   2.9
                         Bit manipulation
    \bitsetClear
                   874 \def\bitsetClear{%
                   875 \BitSet@CheckIndex\BitSet@Clear
                   876 }
      \bitsetSet
                    877 \def\bitsetSet{%
                   878 \BitSet@CheckIndex\BitSet@Set
                    879 }
     \bitsetFlip
                    880 \def\bitsetFlip{%
                   881 \BitSet@CheckIndex\BitSet@Flip
                   882 }
 \bitsetSetValue
                    883 \def\bitsetSetValue#1#2#3{%
                        \expandafter\expandafter\expandafter\BitSet@SetValue
                         \intcalcNum{#3}!{#1}{#2}%
                    885
                   886 }
\BitSet@SetValue #1: plain value
                   #2: BitSet
                   #3: Index
                   887 \def\BitSet@SetValue#1!{%
                        \BitSet@CheckIndex{%
                    889
                           \ifcase#1 %
                    890
                             \expandafter\BitSet@Clear
                    891
                           \or
                             \verb|\expandafter\BitSet@Set| \\
                    892
                    893
                           \else
                             \BitSet@ErrorInvalidBitValue{#1}%
                    894
```

```
\expandafter\expandafter\expandafter\BitSet@Gobble
                                 895
                                          \expandafter\BitSet@Gobble
                                 896
                                 897
                                        \fi
                                 898
                                      }%
                                 899 }
                               #1: Wrong bit value
\BitSet@ErrorInvalidBitValue
                                 900 \def\BitSet@ErrorInvalidBitValue#1{%
                                     \@PackageError{bitset}{%
                                        Invalid bit value (#1) not in range 0..1%
                                902
                                903
                                     \ \ \@ehc
                                904 }
                               2.9.1
                                       Clear operation
               \BitSet@Clear
                               #1: BitSet
                               #2: plain and checked index
                                905 \def\BitSet@Clear#1#2{%
                                906
                                      \edef\BitSet@Temp{%
                                 907
                                        \expandafter\expandafter\expandafter\BitSet@Clear
                                        \csname BS@#1\expandafter\endcsname
                                 908
                                        \expandafter\BitSet@Empty\expandafter=\expandafter!%
                                 909
                                 910
                                        \romannumeral#2000!%
                                 911
                                      \expandafter\let\csname BS@#1\expandafter\endcsname
                                 912
                                      \ifx\BitSet@Temp\BitSet@Empty
                                 913
                                        \BitSet@Zero
                                 914
                                     \else
                                 915
                                        \BitSet@Temp
                                 916
                                917
                                      \fi
                                918 }
              \BitSet@@Clear
                                919 \def\BitSet@@Clear#1#2=#3!#4{%
                                     \ifx#4!%
                                 921
                                        \ifx#1\BitSet@Empty
                                 922
                                        \else
                                 923
                                          \ifx\BitSet@Empty#2%
                                 924
                                          \else
                                            #30#2%
                                 925
                                          \fi
                                 926
                                        \fi
                                 927
                                 928
                                      \else
                                 929
                                        \ifx#1\BitSet@Empty
                                 930
                                          \BitSet@AfterFiFi\BitSet@Cleanup
                                 931
                                        \else
                                 932
                                          \ifx#10%
                                 933
                                            \BitSet@AfterFiFiFi{%
                                 934
                                              \BitSet@@Clear#2=#30!%
                                            }%
                                 935
                                          \else
                                 936
                                            #31%
                                 937
                                 938
                                            \BitSet@AfterFiFiFi{%
                                              \BitSet@@Clear#2=!%
                                 939
                                 940
                                            }%
                                 941
                                          \fi
                                 942
                                        \fi
                                 943
                                      \BitSet@Fi
                                944 }
```

#### 2.9.2 Set operation

```
\BitSet@Set #1: BitSet
               #2: plain and checked Index
                945 \def\BitSet@Set#1#2{%
                     \expandafter\edef\csname BS@#1\endcsname{%
                947
                        \expandafter\expandafter\expandafter\BitSet@@Set
                948
                        \csname BS@#1\expandafter\endcsname
                        \expandafter\BitSet@Empty\expandafter=%
                949
                        \expandafter{\expandafter}\expandafter{\expandafter}%
                950
                        \romannumeral#2000!%
                951
                     }%
                952
                953 }
 \BitSet@@Set
                954 \def\BitSet@@Set#1#2=#3#4#5{%
                955
                      #3#4%
                956
                      \ifx#5!%
                957
                        1#2%
                958
                     \else
                        \ifx#1\BitSet@Empty
                959
                960
                          \BitSet@AfterFiFi\BitSet@@@Set
                961
                962
                        \else
                963
                          #1%
                          \BitSet@@Set#2=%
                964
                        \fi
                965
                     \BitSet@Fi
                966
                967 }
\BitSet@@@Set
                968 \def\BitSet@@Set#1{%
                969 \ifx#1!%
                970
                        1%
                      \else
                971
                972
                        0%
                        \expandafter\BitSet@@@Set
                973
                974
                      \fi
                975 }
               2.9.3
                      Flip operation
 \BitSet@Flip #1: BitSet
               #2: plain and checked Index
                976 \def\BitSet@Flip#1#2{%
                977
                      \edef\BitSet@Temp{%
                        \expandafter\expandafter\expandafter\BitSet@@Flip
                978
                979
                        \csname BS@#1\expandafter\endcsname
                980
                        \expandafter\BitSet@Empty\expandafter=\expandafter!%
                981
                        \romannumeral#2000!%
                982
                      \expandafter\let\csname BS0#1\expandafter\endcsname
                983
                      \ifx\BitSet@Temp\BitSet@Empty
                984
                        \BitSet@Zero
                985
                      \else
                986
                987
                        \BitSet@Temp
                988
                      \fi
                989 }
\BitSet@@Flip
                990 \def\BitSet@@Flip#1#2=#3!#4{%
```

```
\ifx#11%
                        992
                                  \ifx\BitSet@Empty#2%
                        993
                        994
                                  \else
                        995
                                   #30#2%
                        996
                                 \fi
                        997
                               \else
                        998
                                 #31#2%
                               \fi
                        999
                             \else
                       1000
                               \ifx#1\BitSet@Empty
                       1001
                       1002
                                 \BitSet@AfterFiFi\BitSet@@@Set
                       1003
                       1004
                                \else
                       1005
                                  \ifx#10%
                                   \BitSet@AfterFiFiFi{%
                       1006
                                      \BitSet@@Flip#2=#30!%
                       1007
                                   }%
                       1008
                                  \else
                       1009
                                   #31%
                       1010
                                    \BitSet@AfterFiFiFi{%
                       1011
                                      \BitSet@@Flip#2=!%
                       1012
                                   }%
                       1013
                       1014
                                 \fi
                       1015
                                \fi
                       1016
                             \BitSet@Fi
                       1017 }
                       2.9.4 Range operators
    \bitsetClearRange
                       1018 \def\bitsetClearRange{%
                             \BitSet@Range\BitSet@Clear
                       1020 }
      \bitsetSetRange
                       1021 \def\bitsetSetRange{%
                       1022 \BitSet@Range\BitSet@Set
                       1023 }
     \bitsetFlipRange
                       1024 \def\bitsetFlipRange{%
                       1025
                             \BitSet@Range\BitSet@Flip
                       1026 }
\bitsetSetValueRange
                       1027 \def\bitsetSetValueRange#1#2#3#4{%
                             \expandafter\expandafter\expandafter\BitSet@SetValueRange
                             \intcalcNum{#4}!{#1}{#2}{#3}%
                       1029
                       1030 }
\BitSet@SetValueRange
                       1031 \def\BitSet@SetValueRange#1!#2#3#4{%
                       1032
                             \ifcase#1 %
                               \BitSet@Range\BitSet@Clear{#2}{#3}{#4}%
                       1033
                             \or
                       1034
                               1035
                       1036
                             \else
                               \BitSet@ErrorInvalidBitValue{#1}%
                       1037
                       1038
                             \fi
                       1039 }
```

\ifx#4!%

991

```
\BitSet@Range #1: clear/set/flip macro
                        #2: BitSet
                        #3: Index from
                        #4: Index to
                        1040 \def\BitSet@Range#1#2#3#4{%
                              \edef\BitSet@Temp{%
                                 \noexpand\BitSet@@Range\noexpand#1{#2}%
                        1042
                                 \intcalcNum{#3}!\intcalcNum{#4}!%
                        1043
                              }%
                        1044
                              \BitSet@Temp
                        1045
                        1046 }
       \BitSet@@Range
                       #1: clear/set/flip macro
                        #2: BitSet
                        #3: Index from
                        #4: Index to
                        1047 \def\BitSet@@Range#1#2#3!#4!{%
                        1048
                              \ifnum#3<0 %
                        1049
                                \BitSet@NegativeIndex#1{#2}#3!#4!0!#4!%
                        1050
                              \else
                                \ifnum#4<0 %
                        1051
                                   \BitSet@NegativeIndex#1{#2}#3!#4!#3!0!%
                        1052
                        1053
                                 \else
                                   \ifcase\intcalcCmp{#3}{#4} %
                        1054
                        1055
                                     \@PackageError{bitset}{%
                        1056
                                       Wrong index numbers in range [#3..#4]\MessageBreak% hash-ok
                        1057
                                       for clear/set/flip on bit set '#2'.\MessageBreak
                        1058
                                      The lower index exceeds the upper index.\MessageBreak
                        1059
                                       Canceling the operation as error recovery%
                        1060
                        1061
                                    }\@ehc
                        1062
                                   \else
                                     \BitSet@@@Range#3!#4!#1{#2}%
                        1063
                        1064
                                   \fi
                        1065
                                \fi
                        1066
                              \fi
                        1067 }
\BitSet@NegativeIndex
                        1068 \def\BitSet@NegativeIndex#1#2#3!#4!#5!#6!{%
                              \@PackageError{bitset}{%
                        1069
                                Negative index in range [#3..#4]\MessageBreak % hash-ok
                        1070
                        1071
                                for \string\bitset
                        1072
                                \ifx#1\BitSet@Clear
                        1073
                                  Clear%
                        1074
                                \else
                        1075
                                  \ifx#1\BitSet@Set
                        1076
                                    Set%
                        1077
                                  \else
                        1078
                                    Flip%
                                  \fi
                        1079
                        1080
                                Range on bit set '#2'.\MessageBreak
                        1081
                        1082
                                Using [#5..#6] as error recovery% hash-ok
                        1083
                              }\@ehc
                              \BitSet@@Range#1{#2}#5!#6!%
                        1084
                        1085 }
       \BitSet@@Range
                        1086 \def\BitSet@@@Range#1!#2!#3#4{%
                        1087 \ifnum#1<#2 %
```

```
#3{#4}{#1}%
              1088
                      \BitSet@AfterFi{%
              1089
                        \expandafter\expandafter\expandafter\BitSet@@@Range
              1090
              1091
                        \IntCalcInc#1!!#2!#3{#4}%
              1092
                      }%
              1093
                    \BitSet@Fi
              1094 }
              2.10
                      Bit retrieval
              2.10.1 \bitsetGet
 \bitsetGet
              1095 \def\bitsetGet#1#2{%}
                    \number
                    \expandafter\expandafter\BitSet@Get
              1098
                    \intcalcNum{#2}!{#1}%
              1099 }
 \BitSet@Get #1: plain index
              #2: BitSet
              1100 \def\BitSet@Get#1!#2{%
                   \ifnum#1<0 %
              1101
              1102
                      \BitSet@AfterFi{%
              1103
                        0 \BitSetError:NegativeIndex%
              1104
                      }%
              1105
                    \else
              1106
                      \BitSet@IfUndefined{#2}{0}{%
              1107
                        \expandafter\expandafter\expandafter\BitSet@@Get
              1108
                        \csname BS@#2\expandafter\endcsname
                        \expandafter!\expandafter=%
              1109
                        \expandafter{\expandafter}\expandafter{\expandafter}%
              1110
                        \romannumeral\intcalcNum{#1}000!%
              1111
                      }%
              1112
                      \expandafter\BitSet@Space
              1113
                    \BitSet@Fi
              1114
              1115 }
\BitSet@@Get
              1116 \def\BitSet@@Get#1#2=#3#4#5{%
              1117
                   #3#4%
              1118
                    \ifx#5!%
                      \ifx#1!%
              1119
                        0%
              1120
                      \else
              1121
                        #1%
              1122
                      \fi
              1123
              1124
                   \else
                      \ifx#1!%
              1125
              1126
              1127
                        \BitSet@AfterFiFi\BitSet@Cleanup
              1128
                      \else
              1129
                        \BitSet@@Get#2=%
              1130
                      \fi
              1131
                    \BitSet@Fi
              1132 }
                       \bitsetNextClearBit, \bitsetNextSetBit
              2.10.2
```

\bitsetNextClearBit

1133 \def\bitsetNextClearBit#1#2{%

```
\number
                       1134
                              \expandafter\expandafter\expandafter\BitSet@NextClearBit
                       1135
                              \intcalcNum{#2}!{#1} %
                       1136
                        1137 }
\BitSet@NextClearBit #1: Index
                       #2: BitSet
                       1138 \def\BitSet@NextClearBit#1!#2{%
                             \ifnum#1<0 %
                       1139
                                \BitSet@NextClearBit0!{#2}%
                       1140
                                \BitSet@AfterFi{%
                       1141
                       1142
                                  \expandafter\BitSet@Space
                       1143
                                  \expandafter\BitSetError:NegativeIndex\romannumeral0%
                       1144
                                }%
                       1145
                              \else
                                \verb|\bitsetIsEmpty{#2}{#1}{%}|
                       1146
                       1147
                                  \expandafter\BitSet@Skip
                                  \number#1\expandafter\expandafter!%
                       1148
                                  \csname BS@#2\endcsname!!!!!!!!=%
                       1149
                                  {\BitSet@@NextClearBit#1!}%
                       1150
                                }%
                       1151
                       1152
                              \BitSet@Fi
                       1153 }
\BitSet@@NextClearBit #1: index for next bit in #2
                       #2: next bit
                       1154 \def\BitSet@@NextClearBit#1!#2{%
                             \ifx#2!%
                       1155
                                #1%
                       1156
                              \else
                       1157
                                \ifx#20%
                       1158
                                  #1%
                       1159
                                  \BitSet@AfterFiFi\BitSet@Cleanup
                       1160
                       1161
                                \else
                       1162
                                  \BitSet@AfterFiFi{%
                       1163
                                    \expandafter\expandafter\expandafter\BitSet@@NextClearBit
                       1164
                                    \IntCalcInc#1!!%
                                  }%
                       1165
                                \fi
                       1166
                              \BitSet@Fi
                       1167
                       1168 }
    \bitsetNextSetBit
                       1169 \def\bitsetNextSetBit#1#2{%
                              \expandafter\expandafter\expandafter\BitSet@NextSetBit
                       1172
                              \intcalcNum{#2}!{#1} %
                       1173 }
   \BitSet@NextSetBit #1: Index
                        #2: BitSet
                       1174 \def\BitSet@NextSetBit#1!#2{%
                             \ifnum#1<0 %
                       1175
                                \BitSet@NextSetBit0!{#2}%
                       1176
                       1177
                                \BitSet@AfterFi{%
                       1178
                                  \expandafter\BitSet@Space
                       1179
                                  \expandafter\BitSetError:NegativeIndex\romannumeral0%
                       1180
                                }%
                       1181
                              \else
                                1182
                                  \expandafter\BitSet@Skip
                       1183
                                  \number#1\expandafter\expandafter\expandafter!%
                       1184
```

```
\csname BS@#2\endcsname!!!!!!!!=%
                      1185
                                 {\BitSet@@NextSetBit#1!}%
                      1186
                              }%
                      1187
                            \BitSet@Fi
                      1188
                      1189 }
                     #1: index for next bit in #2
\BitSet@@NextSetBit
                      #2: next bit
                      1190 \def\BitSet@@NextSetBit#1!#2{%
                           \ifx#2!%
                      1191
                      1192
                              -1%
                      1193
                            \else
                      1194
                              \ifx#21%
                      1195
                                 #1%
                      1196
                                 \BitSet@AfterFiFi\BitSet@Cleanup
                      1197
                               \else
                      1198
                                 \BitSet@AfterFiFi{%
                                   \verb|\expandafter| expandafter| BitSet@@NextSetBit|
                      1199
                                   \IntCalcInc#1!!%
                      1200
                                }%
                      1201
                              \fi
                      1202
                            \BitSet@Fi
                      1203
                      1204 }
    \BitSet@Cleanup
                      1205 \def\BitSet@Cleanup#1!{}
                      #1: number of bits to skip
       \BitSet@Skip
                      #2: bits
                      #3: continuation code
                      1206 \def\BitSet@Skip#1!#2{%
                            \ifx#2!%
                      1208
                              \BitSet@AfterFi{%
                      1209
                                 \BitSet@SkipContinue%
                              }%
                      1210
                      1211
                            \else
                              \ifcase#1 %
                      1212
                                 \BitSet@AfterFiFi{%
                      1213
                      1214
                                   \BitSet@SkipContinue#2%
                      1215
                                }%
                      1216
                              \or
                      1217
                                 \BitSet@AfterFiFi\BitSet@SkipContinue
                      1218
                                 \BitSet@AfterFiFi{%
                      1219
                                   \expandafter\BitSet@SkipContinue\BitSet@Gobble
                      1220
                                }%
                      1221
                               \else
                      1222
                                 \ifnum#1>8 %
                      1223
                                   \BitSet@AfterFiFiFi{%
                      1224
                                     \expandafter\BitSet@Skip
                      1225
                                     \number\IntCalcSub#1!8!\expandafter!%
                      1226
                      1227
                                     \BitSet@GobbleSeven
                      1228
                                   }%
                      1229
                                 \else
                      1230
                                   \BitSet@AfterFiFiFi{%
                      1231
                                     \expandafter\expandafter\expandafter\BitSet@Skip
                                     \IntCalcDec#1!!%
                      1232
                                   }%
                      1233
                      1234
                                 \fi
                              \fi
                      1235
                            \BitSet@Fi
                      1236
                      1237 }
```

```
#1: remaining bits
  \BitSet@SkipContinue
                                                          #2: continuation code
                                                          1238 \def\BitSet@SkipContinue#1!#2=#3{%
                                                          1239 #3#1!%
                                                          1240 }
     \BitSet@GobbleSeven
                                                          1241 \def\BitSet@GobbleSeven#1#2#3#4#5#6#7{}
                                                          2.10.3 \bitsetGetSetBitList
  \bitsetGetSetBitList It's just a wrapper for \bitsetNextSetBit.
                                                          1242 \ensuremath{\mbox{\sc loss}}\xspace 1242 \ensuremath{\mbox{\sc loss}}\x
                                                                       \romannumeral0%
                                                          1243
                                                          1244
                                                                        \bitsetIsEmpty{#1}{ }{%
                                                          1245
                                                                              \expandafter\BitSet@GetSetBitList
                                                          1246
                                                                              \number\BitSet@NextSetBit0!{#1}!{#1}{}!%
                                                          1247
                                                                        }%
                                                          1248 }
\BitSet@GetSetBitList #1: found index
                                                          #2: BitSet
                                                          #3: comma #4: result
                                                          1249 \def\BitSet@GetSetBitList#1!#2#3#4!\{\%
                                                                      \ifnum#1<0 %
                                                          1250
                                                                             \BitSet@AfterFi{ #4}%
                                                          1251
                                                          1252
                                                                        \else
                                                                              \BitSet@AfterFi{%
                                                          1253
                                                                                   \expandafter\BitSet@GetSetBitList\number
                                                          1254
                                                          1255
                                                                                   \expandafter\expandafter\expandafter\BitSet@NextSetBit
                                                          1256
                                                                                   \IntCalcInc#1!!{#2}!{#2},#4#3#1!%
                                                                             }%
                                                          1257
                                                                         \BitSet@Fi
                                                          1258
                                                          1259 }
                                                                             Bit set properties
                                                          2.11
                         \bitsetSize
                                                          1260 \def\bitsetSize#1{%
                                                          1261
                                                                      \number
                                                                        \BitSet@IfUndefined{#1}{0 }{%
                                                          1262
                                                                             \expandafter\expandafter\BitSet@Size
                                                          1263
                                                                              \expandafter\expandafter\expandafter1%
                                                          1264
                                                          1265
                                                                             \expandafter\expandafter\expandafter!%
                                                          1266
                                                                              \csname BS@#1\endcsname!0!%
                                                          1267
                                                                        }%
                                                          1268 }
                      \BitSet@Size #1: counter
                                                          #2#3: bits
                                                          #4: result
                                                          1269 \def\BitSet@Size#1!#2#3!#4!{%
                                                          1270 \ifx#21%
                                                          1271
                                                                             \ifx\\#3\\%
                                                                                  \BitSet@AfterFiFi{#1 }%
                                                          1272
                                                          1273
                                                                             \else
                                                                                   \BitSet@AfterFiFi{%
                                                          1274
                                                                                       \expandafter\expandafter\expandafter\BitSet@Size
                                                          1275
                                                          1276
                                                                                        \IntCalcInc#1!!#3!#1!%
                                                          1277
                                                                                  }%
```

```
\fi
                      1278
                            \else
                      1279
                              \ifx\\#3\\%
                      1280
                      1281
                                \BitSet@AfterFiFi{#4 }%
                      1282
                               \else
                      1283
                                 \BitSet@AfterFiFi{%
                      1284
                                   \expandafter\expandafter\expandafter\BitSet@Size
                                   \IntCalcInc#1!!#3!#4!%
                      1285
                                }%
                      1286
                              \fi
                      1287
                            \fi
                      1288
                            \BitSet@Fi
                      1289
                      1290 }
 \bitsetCardinality
                      1291 \def\bitsetCardinality#1{%
                      1292
                            \number
                            \BitSet@IfUndefined{#1}{0 }{%
                      1293
                               \expandafter\expandafter\expandafter\BitSet@Cardinality
                      1294
                               \expandafter\expandafter\expandafter0%
                      1295
                               \expandafter\expandafter\expandafter!%
                      1296
                               \csname BS@#1\endcsname!%
                      1297
                      1298
                            }%
                      1299 }
\BitSet@Cardinality #1: result
                      #2#3: bits
                      1300 \def\BitSet@Cardinality#1!#2#3!{%
                      1301
                            \ifx#21%
                              \ifx\\#3\\%
                      1302
                                \BitSet@AfterFiFi{\IntCalcInc#1! }%
                      1303
                      1304
                               \else
                                 \BitSet@AfterFiFi{%
                      1305
                                   \expandafter\expandafter\expandafter\BitSet@Cardinality
                      1306
                                   \IntCalcInc#1!!#3!%
                      1307
                                }%
                      1308
                              \fi
                      1309
                      1310
                            \else
                              \int x^{\#3}\
                      1311
                      1312
                                \BitSet@AfterFiFi{#1 }%
                      1313
                               \else
                      1314
                                 \BitSet@AfterFiFi{%
                                   \BitSet@Cardinality#1!#3!%
                      1315
                                }%
                      1316
                              \fi
                      1317
                            \fi
                      1318
                            \BitSet@Fi
                      1319
                      1320 }
                      2.12
                              Queries
   \bitsetIsDefined
                      1321 \def\bitsetIsDefined#1{%
                           \BitSet@IfUndefined{#1}%
                            \BitSet@SecondOfTwo
                      1323
                            \BitSet@FirstOfTwo
                      1324
                      1325 }
     \bitsetIsEmpty
                      1326 \def\bitsetIsEmpty#1{%
                      1327 \BitSet@IfUndefined{#1}\BitSet@FirstOfTwo{%
```

```
\expandafter\ifx\csname BS@#1\endcsname\BitSet@Zero
                     1328
                                \expandafter\BitSet@FirstOfTwo
                     1329
                     1330
                     1331
                                \expandafter\BitSet@SecondOfTwo
                     1332
                              \fi
                     1333
                           }%
                     1334 }
      \BitSet@Zero
                     1335 \def\BitSet@Zero{0}
      \bitsetQuery
                     1336 \def\bitsetQuery#1#2{%
                     1337
                            \left( \frac{\#1}{\#2} = 1 \% \right)
                     1338
                              \expandafter\BitSet@FirstOfTwo
                     1339
                            \else
                              \expandafter\BitSet@SecondOfTwo
                     1340
                     1341
                            \fi
                     1342 }
     \bitsetEquals
                     1343 \def\bitsetEquals#1#2{%
                     1344
                            \BitSet@IfUndefined{#1}{%
                              \BitSet@IfUndefined{#2}\BitSet@FirstOfTwo\BitSet@SecondOfTwo
                     1345
                            }{%
                     1346
                              \BitSet@IfUndefined{#2}\BitSet@SecondOfTwo{%
                     1347
                     1348
                                \expandafter\ifx\csname BS@#1\expandafter\endcsname
                     1349
                                                 \csname BS@#2\endcsname
                                  \expandafter\BitSet@FirstOfTwo
                     1350
                     1351
                     1352
                                  \expandafter\BitSet@SecondOfTwo
                     1353
                                \fi
                     1354
                              }%
                     1355
                           }%
                     1356 }
 \bitsetIntersects
                     1357 \def\bitsetIntersects#1#2{%
                            \verb|\bitsetIsEmpty{#1}\BitSet@SecondOfTwo{%|}|
                     1358
                              \bitsetIsEmpty{#2}\BitSet@SecondOfTwo{%
                     1359
                     1360
                                \expandafter\expandafter\expandafter\BitSet@Intersects
                                \csname BS@#1\expandafter\expandafter\expandafter\endcsname
                     1361
                     1362
                                \expandafter\expandafter\expandafter!%
                     1363
                                \csname BS@#2\endcsname!%
                     1364
                              }%
                     1365
                           }%
                     1366 }
\BitSet@Intersects
                     1367 \def\BitSet@Intersects#1#2!#3#4!{%
                           \ifnum#1#3=11 %
                     1368
                              \BitSet@AfterFi\BitSet@FirstOfTwo
                     1369
                     1370
                            \else
                     1371
                              \ifx\\#2\\%
                                \BitSet@AfterFiFi\BitSet@SecondOfTwo
                     1372
                     1373
                     1374
                                \int \frac{\pi}{\pi} \frac{4}{\pi}
                     1375
                                  \BitSet@AfterFiFiFi\BitSet@SecondOfTwo
                     1376
                                \else
                                  \BitSet@AfterFiFiFi{%
                     1377
                                    \BitSet@Intersects#2!#4!%
                     1378
```

```
1379 }%
1380 \fi
1381 \fi
1382 \BitSet@Fi
1383 }
1384 \BitSet@AtEnd
1385 \( / package \)
```

# 3 Test

## 3.1 Catcode checks for loading

```
1386 (*test1)
1387 \catcode'\{=1 %
1388 \catcode'\}=2 %
1389 \catcode'\#=6 %
1390 \catcode'\@=11 %
1391 \expandafter\ifx\csname count@\endcsname\relax
                  \countdef\count@=255 %
1392
1393 \fi
1394 \expandafter\ifx\csname @gobble\endcsname\relax
                   \long\def\@gobble#1{}%
1395
1396 \fi
1397 \expandafter\ifx\csname @firstofone\endcsname\relax
                 \long\def\@firstofone#1{#1}%
1399 \fi
1400 \verb|\expandafter\ifx\csname loop\endcsname\relax|
1401 \expandafter\@firstofone
1402 \ensuremath{\setminus} else
1403
                   \expandafter\@gobble
1404 \fi
1405 {%
1406
                  \def\loop#1\repeat{%
1407
                         \def\body{#1}%
1408
                         \iterate
1409
              }%
1410
                 \def\iterate{%
1411
                        \body
1412
                               \let\next\iterate
1413
                         \else
                              \let\next\relax
1414
1415
                         \fi
1416
                         \next
1417
1418
                   \let\repeat=\fi
1419 }%
1420 \ensuremath{ \mbox{\mbox{\mbox{$1420$} \mbox{$\mbox{$\mbox{$def}$\mbox{$\mbox{$\mbox{$\mbox{$$}$}}$}}} 
1421 \count@=0 %
1422 \loop
                   \edef\RestoreCatcodes{%
1423
1424
                          \RestoreCatcodes
                          \catcode\the\count@=\the\catcode\count@\relax
1425
1426
1427 \ifnum\count@<255 %
                  \advance\count@ 1 %
1429 \repeat
1430
1431 \ensuremath{\mbox{\sc loss}} 1431
                  \count@=#1\relax
1432
                   \loop
1433
                         \catcode\count@=15 %
1434
```

```
\ifnum\count@<#2\relax
1435
1436
        \advance\count@ 1 %
1437
      \repeat
1438 }
1439 \verb|\expandafter\ifx\csname\ LoadCommand\endcsname\relax|
1440 \def\LoadCommand{\input bitset.sty\relax}%
1441 \fi
1442 \left\lceil \text{Test} \right\rceil
      \verb|\RangeCatcodeInvalid{0}{47}||
1443
      1444
      \RangeCatcodeInvalid{91}{96}%
1445
      \RangeCatcodeInvalid{123}{255}%
1446
      \catcode'\@=12 %
1447
     \catcode'\\=0 %
1448
1449 \catcode'\{=1 %
1450 \catcode'\}=2 %
1451 \catcode'\#=6 %
1452 \catcode'\[=12 \%
1453 \catcode'\]=12 %
1454 \catcode'\%=14 %
      \catcode'\ =10 %
1455
      \catcode13=5 %
1456
1457
      \LoadCommand
      \RestoreCatcodes
1458
1459 }
1460 \Test
1461 \csname @@end\endcsname
1462 \end
1463 (/test1)
```

#### 3.2 Macro tests

#### 3.2.1 Preamble

```
1464 (*test2)
1465 \NeedsTeXFormat{LaTeX2e}
1466 \setminus nofiles
1467 \documentclass{article}
1468 \makeatletter
1469 (*noetex)
1470 \let\SavedNumexpr\numexpr
1471 \let\SavedIfcsname\ifcsname
1472 \let\SavedCurrentgrouplevel\currentgrouplevel
1473 \def\ETeXDisable{%
1474
     \let\ifcsname\@undefined
1475
      \let\numexpr\@undefined
1476
      \let\currentgrouplevel\@undefined
1477 }
1478 \ETeXDisable
1479 (/noetex)
1480 \makeatletter
1481 \chardef\BitSet@TestMode=1 %
1482 \makeatother
1483 \usepackage{bitset}[2007/09/28]
1484 (*noetex)
1485 \def\ETeXEnable{%
\let\ifcsname\SavedIfcsname
1487
1488
     \let\currentgrouplevel\SavedCurrentgrouplevel
1489 }
1490 \ETeXEnable
1491 (/noetex)
1492 \usepackage{qstest}
```

```
1493 \IncludeTests{*}
1494 \setminus LogTests\{log\}\{*\}\{*\}
1495 \makeatletter
3.2.2 Time
1496 \begingroup\expandafter\expandafter\expandafter\endgroup
1497 \expandafter\ifx\csname pdfresettimer\endcsname\relax
1498 \else
1499
      \newcount\SummaryTime
1500
      \newcount\TestTime
1501
      \SummaryTime=\z@
1502
      \newcommand*{\PrintTime}[2]{%
1503
        \typeout{%
          [Time #1: \strip@pt\dimexpr\number#2sp\relax\space s]%
1504
        }%
1505
     }%
1506
      \newcommand*{\StartTime}[1]{%
1507
        \renewcommand*{\TimeDescription}{#1}%
1508
1509
        \pdfresettimer
1510
      \newcommand*{\TimeDescription}{}%
1511
1512
      \newcommand*{\StopTime}{%
1513
        \TestTime=\pdfelapsedtime
1514
        \global\advance\SummaryTime\TestTime
        \PrintTime\TimeDescription\TestTime
1515
      }%
1516
      \let\saved@qstest\qstest
1517
      \let\saved@endqstest\endqstest
1518
      \def\qstest#1#2{%}
1519
        \saved@qstest{#1}{#2}%
1520
1521
        \StartTime{#1}%
1522
      }%
1523
      \def\endqstest{%
1524
        \StopTime
        \saved@endqstest
1525
      }%
1526
      \AtEndDocument{%
1527
        \PrintTime{summary}\SummaryTime
1528
     }%
1529
1530 \fi
3.2.3 Detection of unwanted space
1531 \let\orig@qstest\qstest
1532 \let\orig@endqstest\endqstest
1533 \def\qstest#1#2{%}
      \orig@qstest{#1}{#2}%
      \setbox0\hbox\bgroup\begingroup\ignorespaces
1536 }
1537 \def\endqstest{%
1538
     \endgroup\egroup
      \Expect*{\the\wd0}{0.0pt}%
1539
      \orig@endqstest
1540
1541 }
       Test macros
3.2.4
1542 \newcounter{Test}
1543
1544 \def\TestError#1#2{%
1545
     \begingroup
1546
        \setcounter{Test}{0}%
1547
        \sbox0{%
          \def\@PackageError##1##2##3{%
```

```
1549
            \stepcounter{Test}%
1550
            \begingroup
               \let\MessageBreak\relax
1551
1552 (*noetex)
1553
               \ETeXEnable
1554 (/noetex)
1555
              \Expect{##1}{bitset}%
1556
              \Expect*{##2}*{#1}%
1557
            \endgroup
          }%
1558
1559 (*noetex)
          \ETeXDisable
1560
1561 (/noetex)
1562
          #2%
1563
        \Expect*{\theTest}{1}%
1564
1565
        \text{Expect}*{\the\wd0}{0.0pt}%
1566
      \endgroup
1567 }
1568
1569 \def\TestErrorNegativeIndex#1#2{%
     \TestError{Invalid negative index (#1)}{#2}%
1570
1571 }
1572
1573 \def\TestGetterUndefined#1{%
1574
      \CheckUndef{dummy}%
      \expandafter\expandafter\Expect
1575
      \expandafter\expandafter\expandafter{#1{dummy}}{0}%
1576
1577 }
1578
1579 \def\ExpectBitSet#1#2{%
1580
      \expandafter\expandafter\Expect
1581
      \expandafter\expandafter\expandafter
      {\csname BS@#1\endcsname}*{#2}%
1582
1583 }
1584 \def\Check#1#2{%
      \ExpectBitSet{#1}{#2}%
1586 }
1587 \def\CheckUndef#1{%
1588
      \begingroup
        \Expect*{%
1589
          \expandafter
1590
          \ifx\csname BS@#1\endcsname\relax true\else false\fi
1591
1592
        }{true}%
1593
      \endgroup
1594 }
1595 \def\RevCheck#1#2{%
1596
      \ExpectBitSet{#1}{\Reverse#2!!}%
1597 }
1598 \def\Set#1#2{%
      \expandafter\def\csname BS@#1\endcsname{#2}%
1599
1600 }
1601 \def\RevSet#1#2{%
      \expandafter\edef\csname BS@#1\endcsname{%
1602
1603
        \Reverse#2!!%
1604
      }%
1605 }
1606 \def\Reverse#1#2!#3!{%
1607
      \ifx\\#2\\%
        #1#3%
1608
        \expandafter\@gobble
1609
1610
      \else
```

```
1611
        \expandafter\@firstofone
1612
      {\Reverse#2!#1#3!}%
1613
1614 }
3.2.5
       Test sets
1615 \begin{qstest}{Let}{Let}
      \CheckUndef{abc}%
1616
      \CheckUndef{xyz}%
1617
      \bitsetLet{xyz}{abc}%
1618
1619
      \CheckUndef{abc}%
      \c \xyz}{0}%
1620
      \Set{abc}{1}%
1621
      \Check{abc}{1}%
1622
1623
      \Check{xyz}{0}%
1624
      \bitsetLet{xyz}{abc}%
1625
      \Check{abc}{1}%
      \Check{xyz}{1}%
1626
      \footnote{Set{xyz}{11}}%
1627
1628
      \Check{abc}{1}%
1629
      \Check{xyz}{11}%
1630 \end{qstest}
1631
1632 \begin{qstest}{Reset}{Reset}
      \bitsetReset{xyz}%
1633
1634
      \Check{xyz}{0}%
1635
      \bitsetReset{abc}%
      \Check{abc}{0}%
1636
1637
      \Set{abc}{10101}%
      \bitsetReset{abc}%
1638
      \check{abc}{0}%
1639
1640 \end{qstest}
1641
1642 \begin{qstest}{Get/Query}{Get/Query}
      \expandafter\expandafter\Expect
1643
1644
      \expandafter\expandafter\expandafter{%
1645
        \bitsetGet{dummy}{0}%
1646
      }{0}%
1647
      \begingroup
        \expandafter\def\csname BitSetError:NegativeIndex\endcsname{}%
1648
1649
        \Set{abc}{1}%
        \Expect*{\bitsetQuery{abc}{-1}{true}{false}}{false}%
1650
      \endgroup
1651
1652
      \def\Test#1#2#3{%
1653
        \Set{abc}{#1}%
1654
        \expandafter\expandafter\Expect
1655
        \expandafter\expandafter\expandafter{\bitsetGet{abc}{#2}}{#3}%
1656
        \Expect*{\bitsetQuery{abc}{#2}{true}{false}}%
1657
               *{\ifcase#3 false\or true\else error\fi}%
1658
      }%
      \Test{1}{100}{0}%
1659
1660
      Test{0}{0}{0}%
1661
      \Test{1}{0}{1}%
1662
      \Test{11}{1}{1}}%
      \Test{111}{1}{1}}%
1663
1664
      \Test{101}{1}{0}%
1665
      \Test{101}{2}{1}%
1666
      \Test{10100110011}{10}{1}%
1667 \end{qstest}
1668
1669 \begin{qstest}{Size}{Size}
      \TestGetterUndefined\bitsetSize
1670
      \def\Test#1#2{%}
1671
```

```
1672
       \Set{abc}{#1}%
       \expandafter\expandafter\Expect
1673
       \expandafter\expandafter\expandafter{\bitsetSize{abc}}{#2}%
1674
1675
1676
     Test{0}{0}
1677
     Test{1}{1}%
1678
     Test{00}{0}%
1679
     \Test{0000000}{0}%
1680
     Test{10}{1}%
     \Test{01}{2}%
1681
     \texttt{Test}\{11\}\{2\}\%
1682
     \Test{010}{2}%
1683
1684
     \Test{011}{3}%
     \Test{100110011}{9}%
1685
     \Test{0000011111000001111100000}{20}%
1686
     1688 \end{qstest}
1689
1690 \begin{qstest}{Cardinality}{Cardinality}
     \TestGetterUndefined\bitsetCardinality
1691
     \def\Test#1#2{%
1692
       \Set{abc}{#1}%
1693
       \expandafter\expandafter\Expect
1694
       \expandafter\expandafter\expandafter{%
1695
         \bitsetCardinality{abc}%
1696
1697
       }{#2}%
     }%
1698
     Test{0}{0}%
1699
1700
     \Test{1}{1}%
     \Test{00}{0}%
1701
     \Test{0000000}{0}%
1702
1703
     \Test{10}{1}%
1704
     \Test{01}{1}%
     \Test{11}{2}%
1705
     \Test{010}{1}%
1706
1707
     \Test{011}{2}%
1708
     \Test{100110011}{5}%
1709
     \Test{00000111110000011111100000}{10}%
     1710
1711 \end{qstest}
1712
1713 \begin{qstest}{NextClearBit/NextSetBit}{NextClearBit/NextSetBit}
     \def\Test#1#2{%
1714
       \expandafter\expandafter\Expect
1715
       \expandafter\expandafter\expandafter{%
1716
1717
         \TestOp{abc}{\#1}%
1718
       }{#2}%
1719
1720
     \def\Clear{\let\TestOp\bitsetNextClearBit}%
1721
      \def\Set{\let\TestOp\bitsetNextSetBit}%
     \begingroup
1722
       \catcode'\:=11 %
1723
       \bitsetSetBin{abc}{1}%
1724
1725
       \Clear
       \Test{-1}{1\BitSetError:NegativeIndex}%
1726
1727
1728
       \Test{-1}{0\BitSetError:NegativeIndex}%
1729
     \endgroup
1730
     \let\BS@abc\@undefined
1731
     \Clear
     \Test{0}{0}%
1732
     Test{1}{1}%
1733
```

- 1734 \Test{2}{2}%
- 1735 \Test{100}{100}%
- 1736 \Set
- 1737 \Test{0}{-1}%
- 1738 \Test{1}{-1}%
- 1739 \Test{100}{-1}%
- 1740 \bitsetReset{abc}%
- 1741 \Clear
- 1742 \Test{0}{0}%
- 1743 \Test{1}{1}%
- 1744 \Test{2}{2}%
- 1745 \Test{100}{100}%
- 1746 \Set
- 1747 \Test{0}{-1}%
- 1748 \Test{1}{-1}%
- 1749 \Test{100}{-1}%
- 1750 \bitsetSetBin{abc}{1}%
- 1751 \Clear
- 1752 \Test{0}{1}%
- 1753 \Test{1}{1}%
- 1754 \Test{2}{2}%
- 1755 \Test{100}{100}%
- 1756 \Set
- 1757 \Test{0}{0}%
- 1758 \Test{1}{-1}%
- 1759 \Test{100}{-1}%
- 1760 \bitsetSetBin{abc}{111000111000111000111}%
- 1761 \Clear
- $1762 \quad \texttt{Test{0}{3}}\%$
- 1763 \Test{1}{3}%
- 1764 \Test{2}{3}%
- 1765 \Test{3}{3}%
- 1766 \Test{4}{4}%
- 1767 \Test{5}{5}%
- 1768 \Test{6}{9}%
- 1769 \Test{7}{9}%
- 1770 \Test{8}{9}% 1771 \Test{9}{9}%
- 1772 \Test{10}{10}%
- 1773 \Test{11}{11}%
- 1774 \Test{12}{15}%
- 1775 \Test{13}{15}%
- 1776 \Test{14}{15}%
- 1777 \Test{15}{15}%
- 1778 \Test{16}{16}%
- 1779 \Test{17}{17}% 1780 \Test{18}{21}%
- 1781 \Test{19}{21}%
- 1782 \Test{20}{21}%
- 1783 \Test{21}{21}%
- 1784 \Test{22}{22}%
- 1785 \Test{100}{100}%
  1786 \Set
- 1787 \Test{0}{0}%
- 1788 \Test{1}{1}%
- 1789 \Test{2}{2}%
- 1790 \Test{3}{6}%
- 1791 \Test{4}{6}%
- 1792 \Test{5}{6}%
- 1793 \Test{6}{6}% 1794 \Test{7}{7}%
- 1795 \Test{8}{8}%

```
\Test{9}{12}%
1796
1797
      \Test{10}{12}%
      \Test{11}{12}%
1798
      \Test{12}{12}%
1800
      \Test{13}{13}%
1801
      \Test{14}{14}%
1802
      \Test{15}{18}%
1803
      \Test{16}{18}%
      \Test{17}{18}%
1804
      Test{18}{18}%
1805
      \Test{19}{19}%
1806
1807
      \Test{20}{20}%
     Test{21}{-1}%
1808
     Test{22}{-1}%
1809
     Test{100}{-1}%
1811
      \bitsetSetBin{abc}{1111111}%
1812
      \Clear
      Test{6}{7}%
1813
1814
      Test{7}{7}%
1815
      \Test{8}{8}%
      \Test{100}{100}%
1816
1817
      \Set
      Test{6}{6}%
1818
      Test{7}{-1}%
1819
1820
      Test{8}{-1}%
1821
      Test{100}{-1}%
      \bitsetSetBin{abc}{11111111}%
1822
      \Clear
1823
1824
      Test{7}{8}%
      Test{8}{8}%
1825
      Test{9}{9}%
1826
1827
      Test{100}{100}%
1828
      \Set
      Test{7}{7}%
1829
1830
      Test{8}{-1}%
1831
      Test{9}{-1}%
1832
      Test{100}{-1}%
      \bitsetSetBin{abc}{111111111}%
1833
1834
      \Clear
      Test{8}{9}%
1835
      Test{9}{9}%
1836
      \Test{10}{10}%
1837
1838
      Test{100}{100}%
1839
      \Set
1840
      Test{8}{8}%
1841
      \Test{9}{-1}%
1842
      Test{10}{-1}%
1843
      Test{100}{-1}%
1844
      \verb|\bitsetSetBin{abc}{1111111111}| %
1845
      \Clear
      Test{9}{10}%
1846
      Test{10}{10}%
1847
      \Test{11}{11}%
1848
      Test{100}{100}%
1849
1850
      \Set
1851
      Test{9}{9}%
1852
      Test{10}{-1}%
1853
     Test{11}{-1}%
1854
      Test{100}{-1}%
1855 \end{qstest}
1856
```

1857 \begin{qstest}{GetSetBitList}{GetSetBitList}

```
\let\BS@abc\@undefined
1858
      \expandafter\expandafter\Expect
1859
      \expandafter\expandafter\expandafter{%
1860
        \bitsetGetSetBitList{abc}%
1861
1862
1863
      \def\Test#1#2{%}
1864
        \bitsetSetBin{abc}{#1}%
1865
        \expandafter\expandafter\Expect
        \expandafter\expandafter\expandafter{%
1866
          \bitsetGetSetBitList{abc}%
1867
        }{#2}%
1868
     }%
1869
      Test{0}{}%
1870
      Test{1}{0}%
1871
      Test{10}{1}%
1872
      Test{11}{0,1}%
1873
1874
      \Test{10110100}{2,4,5,7}%
      \Test{101101001010011}{0,1,4,6,9,11,12,14}%
1875
1876 \end{qstest}
1877
1878 \begin{qstest}{GetDec}{GetDec}
      \TestGetterUndefined\bitsetGetDec
1879
      \def\Test#1#2{%}
1880
        \RevSet{abc}{#1}%
1881
1882 (*noetex)
        \begingroup\expandafter\expandafter\expandafter\endgroup
1883
1884 (/noetex)
1885
        \expandafter\expandafter\Expect
1886
        \expandafter\expandafter\expandafter{%
          \bitsetGetDec{abc}%
1887
        }{#2}%
1888
1889
     }%
1890
      \Test{0}{0}%
      Test{1}{1}%
1891
      \Test{10}{2}%
1892
1893
      \Test{11}{3}%
1894
      \Test{100}{4}%
1895
      Test{101}{5}%
      \texttt{Test}\{110\}\{6\}\%
1896
1897
      \Test{111}{7}%
      \Test{1000}{8}%
1898
      \Test{000111}{7}%
1899
      1900
1901
            111111111111111}{2147483647}%
1902
      1903
            1111111111111111}{2147483647}%
1904
      \Test{10000000000000000%
1905
            00000000000000000}{2147483648}%
1906
      \Test{10000000000000000%
            000000000000000000000}{4294967296}%
1907
      \Test{0001000000000000000000%
1908
1909
            00000000000000000}{4294967296}%
      \Test{11000000000000000%
1910
1911
            000000000000011}{6442450947}%
1912 \end{qstest}
1913
1914 \begin{qstest}{Clear}{Clear}
1915
      \def\Test#1#2#3{%}
1916
        \RevSet{abc}{#1}%
        \bitsetClear{abc}{#2}%
1917
        \Expect*{\BS@abc}*{\Reverse#3!!}%
1918
1919
     }%
```

```
\bitsetClear{abc}{2}%
1920
      \RevCheck{abc}{0}%
1921
      \TestErrorNegativeIndex{-1}{\bitsetClear{abc}{-1}}%
1922
      \RevCheck{abc}{0}%
1923
1924
      \Test{0}{0}{0}%
1925
      \Test{1}{0}{0}%
1926
      \Test{111}{1}{101}%
1927
      \Test{111}{30}{111}%
      Test{0000111}{5}{0000111}% 111 would also be ok
1928
      \Test{10000111}{5}{10000111}%
1929
      \texttt{\Test{1001001}{3}{1000001}{\%}}
1930
1931 \end{qstest}
1932
1933 \begin{qstest}{Set}{Set}
      \def\Test#1#2#3{%
1934
1935
        \RevSet{abc}{#1}%
1936
        \bitsetSet{abc}{#2}%
        \Expect*{\BS@abc}*{\Reverse#3!!}%
1937
      }%
1938
1939
      \bitsetSet{abc}{2}%
1940
      \RevCheck{abc}{100}%
      \TestErrorNegativeIndex{-1}{\bitsetSet{abc}{-1}}%
1941
      \RevCheck{abc}{100}%
1942
      \Test{0}{0}{1}%
1943
      Test{1}{0}{1}%
1944
      \Test{100}{1}{110}%
1945
1946
      \Test{111}{1}{111}%
1947
      \Test{11}{1}{11}%
1948
      \Test{11}{2}{111}%
1949
      \Test{11}{3}{1011}%
      \Test{111}{10}{10000000111}%
1950
1951
      Test{0000111}{5}{0100111}% 100111 would also be ok
1952
      \Test{10000111}{5}{10100111}%
1953
      \Test{1000001}{3}{1001001}%
      \Test{1001001}{3}{1001001}%
1954
1955 \end{qstest}
1956
1957 \begin{qstest}{Flip}{Flip}
1958
      \def\Test#1#2#3{%
1959
        \RevSet{abc}{#1}%
        \bitsetFlip{abc}{#2}%
1960
        \Expect*{\BS@abc}*{\Reverse#3!!}%
1961
1962
     }%
1963
      \bitsetFlip{abc}{2}%
1964
      \RevCheck{abc}{100}%
1965
      \TestErrorNegativeIndex{-1}{\bitsetFlip{abc}{-1}}%
1966
      \RevCheck{abc}{100}%
1967
      \Test{0}{0}{1}%
1968
      Test{1}{0}{0}%
1969
      \Test{0}{2}{100}%
      \Test{100}{1}{110}%
1970
1971
      \Test{111}{1}{101}%
      \Test{11}{1}{1}}%
1972
1973
      \Test{11}{2}{111}%
1974
      \Test{11}{3}{1011}%
1975
      \Test{111}{10}{10000000111}%
1976
      Test{0000111}{5}{0100111}% 100111 would also be ok
1977
      \Test{10000111}{5}{10100111}%
1978
      \Test{1000001}{3}{1001001}%
1979
      \Test{1001001}{3}{1000001}%
      Test{11111}{2}{11011}%
1980
1981 \end{qstest}
```

```
1982
1983 \begin{qstest}{SetValue}{SetValue}
1984
      \def\Test#1#2{%}
        \TestError{Invalid bit value (#2) not in range 0..1}{%
1985
          \bitsetSetValue{abc}{#1}{#2}%
1986
1987
        }%
1988
      }%
1989
      Test{0}{-1}%
      Test{0}{2}%
1990
      \Test{0}{10}%
1991
      \def\Test#1#2#3{%
1992
        \let\BS@abc\@undefined
1993
1994
        \bitsetSetValue{abc}{#1}{#2}%
1995
        \bitsetSetBin{result}{#3}%
        \Expect*{\BS@abc}*{\BS@result}%
1996
1997
      }%
1998
      Test{0}{0}{0}
      Test{0}{1}{1}%
1999
      \Test{1}{0}{0}%
2000
2001
      \Test{1}{1}{10}%
2002
      \def\Test#1#2#3#4{%
        \bitsetSetBin{abc}{#1}%
2003
2004
        \bitsetSetBin{result}{#4}%
2005
        \bitsetSetValue{abc}{#2}{#3}%
        \Expect*{\BS@abc}*{\BS@result}%
2006
2007
      }%
2008
      \Test{0}{0}{0}{0}}%
2009
      \Test{0}{0}{0}{0}}%
2010
      \Test{0}{0}{1}{1}%
2011
      \Test{0}{1}{0}{0}%
      \Test{0}{1}{1}{10}%
2012
2013
      \Test{1010}{2}{1}{1110}%
2014
      \Test{1010}{4}{1}{11010}%
2015
      \Test{1010}{6}{1}{1001010}%
2016
      \Test{1010}{1}{0}{1000}%
2017
      \Test{1010}{2}{0}{1010}%
2018
      \Test{1010}{3}{0}{10}%
2019
      \Test{1010}{4}{0}{1010}%
2020
      \Test{1010}{6}{0}{1010}%
      2021
      \label{locality} $$\operatorname{1010}_{1}{\csname iffalse\endsname 1\leq 0\fi}_{1000}\%$
2022
2023 \end{qstest}
2024
2025 \begin{qstest}{IsDefined}{IsDefined}
2026
      \let\BS@abc\@undefined
2027
      \Expect*{\bitsetIsDefined{abc}{true}{false}}{false}%
2028
      \bitsetReset{abc}%
2029
      \Expect*{\bitsetIsDefined{abc}{true}{false}}{true}%
2030 \end{qstest}
2031
2032 \begin{qstest}{IsEmpty}{IsEmpty}
2033
      \let\BS@abc\@undefined
      \Expect*{\bitsetIsEmpty{abc}{true}{false}}{true}%
2034
2035
      \bitsetReset{abc}%
2036
      \Expect*{\bitsetIsEmpty{abc}{true}{false}}{true}%
2037
      \bitsetSet{abc}{1}%
2038
      \Expect*{\bitsetIsEmpty{abc}{true}{false}}{false}%
2039 \end{qstest}
2040
2041 \begin{qstest}{Equals}{Equals}
      \def\Test#1#2#3{%
2042
        \Expect*{\bitsetEquals{#1}{#2}{true}{false}}{#3}%
2043
```

```
}%
2044
               \let\BS@abc\@undefined
2045
               \Test{abc}{abc}{true}%
2046
               \Test{abc}{foo}{true}%
2047
2048
               \Test{foo}{abc}{true}%
2049
               \bitsetReset{abc}%
2050
               \Test{abc}{abc}{true}%
2051
               \Test{abc}{foo}{false}%
2052
              \Test{foo}{abc}{false}%
              \bitsetReset{foo}%
2053
              \Test{abc}{foo}{true}%
2054
              \Test{foo}{abc}{true}%
2055
2056
              \bitsetSet{abc}{4}%
              \Test{abc}{foo}{false}%
2057
              \Test{foo}{abc}{false}%
2058
2059
              \bitsetFlip{foo}{4}%
2060
              \Test{abc}{foo}{true}%
2061
               \Test{foo}{abc}{true}%
2062 \end{qstest}
2063
2064 \begin{qstest}{Intersects}{Intersects}
2065
               \def\Test#1{%
                    \Expect*{\bitsetIntersects{abc}{foo}{true}{false}}{#1}%
2066
2067
               }%
               \let\BS@abc\@undefined
2068
2069
               \let\BS@foo\@undefined
2070
               \Test{false}%
2071
               \Set{abc}{0}%
2072
              \Test{false}%
2073
               \Set{foo}{0}%
              \Test{false}%
2074
               \let\BS@abc\@undefined
2075
2076
              \Test{false}%
2077
              \Set{foo}{1}%
              \Test{false}%
2078
2079
              \Set{abc}{0}%
2080
              \Test{false}%
2081
               \Set{abc}{1}%
2082
              \Test{true}%
               \let\BS@foo\@undefined
2083
              \Test{false}%
2084
               \footnote{1}% \cite{1}% 
2085
2086
               \Test{false}%
2087
               \def\Test#1#2#3{%
2088
                    \bitsetSetBin{abc}{#1}%
2089
                    \bitsetSetBin{foo}{#2}%
2090
                    \Expect*{\bitsetIntersects{abc}{foo}{true}{false}}{#3}%
2091
              }%
2092
               Test{1010}{0101}{false}%
2093
               Test{0}{10}{false}%
               \Test{1}{11}{true}%
2094
               \Test{11}{1}{true}%
2095
              Test{10}{1}{false}%
2096
2097 \end{qstest}
2098
2099 \begin{qstest}{And/AndNot/Or/Xor}{And/AndNot/Or/Xor}
2100
              \def\@Test#1#2#3#4#5{%
2101
                    \begingroup
2102
                         #5%
2103
                         \begingroup
                              \verb|\label{lem:condefined||} \label{lem:condefined||} $$ \operatorname{Let}BS@foo\\@undefined||
2104
2105
                              \csname bitset#1\endcsname{abc}{foo}%
```

```
\CheckUndef{foo}%
2106
             \Check{abc}{#2}%
2107
           \endgroup
2108
           \begingroup
2109
2110
             \bitsetReset{foo}%
             \csname bitset#1\endcsname{abc}{foo}%
2111
2112
             \Check{foo}{0}%
2113
             \Check{abc}{#3}%
2114
           \endgroup
           \begingroup
2115
             \def\BS@foo{0101}%
2116
             \c \c bitset #1\end csname {abc}{foo}{\%}
2117
             \Check{foo}{0101}%
2118
2119
             \Check{abc}{#4}%
2120
           \endgroup
2121
        \endgroup
2122
      }%
      \def\Test#1{%}
2123
        \def\0p{\#1}%
2124
2125
        \Test@
2126
      \def\Test@#1#2#3#4#5#6#7#8#9{%
2127
        \@Test\Op{#1}{#2}{#3}{%
2128
           \let\BS@abc\@undefined
2129
2130
2131
        \@Test\Op{#4}{#5}{#6}{%
2132
           \bitsetReset{abc}%
        }%
2133
        \@Test\Op{#7}{#8}{#9}{%
2134
           \def\BS@abc{1001}%
2135
        }%
2136
2137
      }%
      \Test{And}%
2138
            {0}{0}{0}%
2139
2140
            {0}{0}{0}%
2141
            {0}{0}{0001}%
2142
      \Test{AndNot}%
2143
            {0}{0}{0}}%
2144
            {0}{0}{0}%
            {1001}{1001}{1}%
2145
      \texttt{\Test{Or}}\%
2146
            {0}{0}{0101}%
2147
            {0}{0}{0101}%
2148
2149
            {1001}{1001}{1101}%
2150
      \Test{Xor}%
2151
            {0}{0}{0101}%
2152
            {0}{0}{0101}%
2153
            {1001}{1001}{11}%
2154
      \def\Test#1#2#3{%
2155
        \bitsetSetBin{abc}{#1}%
        \bitsetSetBin{foo}{#2}%
2156
        \csname bitset\Op\endcsname{abc}{foo}%
2157
        \RevCheck{foo}{#2}%
2158
2159
        \RevCheck{abc}{#3}%
      }%
2160
2161
      \def\Dp{And}%
2162
      \Test{1}{111}{1}%
2163
      Test{111}{1}{1}
2164
      \Test{10}{111}{10}%
2165
      \Test{111}{10}{10}%
      \Test{111}{1000}{0}%
2166
2167
      \Test{1000}{111}{0}%
```

```
\def\Op{AndNot}%
2168
      \Test{1010}{11}{1000}%
2169
      \Test{100}{100}{0}%
2170
      \Test{111}{1111}{0}%
2171
2172
      \Test{100}{111}{0}%
2173
      \def\0p{0r}%
2174
      \Test{0}{0}{0}}%
2175
      \Test{1}{0}{1}%
2176
      \Test{0}{1}{1}%
      \Test{1}{1}{1}%
2177
      Test{1000}{10}{1010}%
2178
      \Test{10}{1000}{1010}%
2179
2180
      \def\Op{Xor}%
      \Test{0}{0}{0}%
2181
      Test{1}{0}{1}%
2182
2183
      \Test{0}{1}{1}%
2184
      Test{1}{1}{0}%
      \Test{1000}{10}{1010}%
2185
      \Test{10}{1000}{1010}%
2186
2187
      \Test {110011001100}%
           {111000111000111}%
2188
           {111110100001011}%
2189
2190
      \Test{111000111000111}%
              {110011001100}%
2191
           {111110100001011}%
2192
2193 \end{qstest}
2194
2195 \begin{qstest}{GetUndef}{GetUndef, GetBin, GetOct, GetHex}
2196
      \def\TestUndef#1#2{%
2197
        \let\BS@abc\@undefined
        \expandafter\expandafter\Expect
2198
2199
        \expandafter\expandafter\expandafter{%
2200
          x{abc}{#1}%
2201
        }{#2}%
2202
2203
      \let\x\bitsetGetBin
2204
      TestUndef{-1}{0}%
2205
      \TestUndef{0}{0}%
      \texttt{\TestUndef\{1\}\{0\}\%}
2206
2207
      TestUndef{2}{00}%
      \TestUndef{8}{00000000}%
2208
2209
      \let\x\bitsetGetOct
      TestUndef{-1}{0}%
2210
2211
      \TestUndef{0}{0}%
2212
      \TestUndef{1}{0}%
2213
      \TestUndef{2}{0}%
2214
      \TestUndef{3}{0}%
2215
      \TestUndef{4}{00}%
2216
      \TestUndef{5}{00}%
2217
      \TestUndef{6}{00}%
      \TestUndef{7}{000}%
2218
      \TestUndef{8}{000}%
2219
      \TestUndef{9}{000}%
2220
2221
      \TestUndef{10}{0000}%
2222
      \let\x\bitsetGetHex
2223
      \TestUndef{-1}{0}%
2224
      \TestUndef{0}{0}%
2225
      TestUndef{1}{0}%
2226
      \TestUndef{2}{0}%
2227
      \TestUndef{3}{0}%
      \TestUndef{4}{0}%
2228
2229
      \TestUndef{5}{00}%
```

```
\TestUndef{6}{00}%
2230
      \TestUndef{7}{00}%
2231
      \TestUndef{8}{00}%
2232
      \TestUndef{9}{000}%
2233
2234
      \TestUndef{10}{000}%
2235
      \TestUndef{12}{000}%
2236
      \TestUndef{13}{0000}%
2237
      \TestUndef{16}{0000}%
      TestUndef{17}{00000}%
2238
2239 \end{qstest}
2240
2241 \begin{qstest}{SetBin}{SetBin}
      \def\Test#1#2{%}
2242
2243
        \let\BS@abc\@undefined
2244
        \bitsetSetBin{abc}{#1}%
2245
        \expandafter\Expect\expandafter{\BS@abc}{#2}%
2246
     }%
      \Test{}{0}%
2247
      Test{0}{0}%
2248
2249
      \Test{1}{1}%
      \Test{10}{01}%
2250
      \Test{11}{11}%
2251
2252
      \Test{010}{01}%
      \Test{011}{11}%
2253
      \Test{0010}{01}%
2254
2255
      \Test{1010}{0101}%
2256 \end{qstest}
2257
2258 \begin{qstest}{SetOct}{SetOct}
      \def\Test#1#2{%}
2259
        \bitsetSetOct{abc}{#1}%
2260
2261
        \expandafter\Expect\expandafter{\BS@abc}{#2}%
2262
     }%
      Test{}{0}%
2263
2264
     \Test{0}{0}%
2265
     \Test{000}{0}%
2266
     Test{1}{1}%
2267
      \Test{001}{1}%
      Test{010}{0001}%
2268
2269
      \Test{020}{00001}%
2270
      \Test{42}{010001}%
2271
      \Test{377}{11111111}%
2272
      \Test{0377}{11111111}%
2273
      \Test{76543210}{000100010110001101011111}%
2274
      \Test{ 0 7 0 7 1 }{100111000111}%
2275 \end{qstest}
2276
2277 \begin{qstest}{SetHex}{SetHex}
2278
      \def\Test#1#2{%}
        \verb|\bitsetSetHex{abc}{#1}||
2279
        \expandafter\Expect\expandafter{\BS@abc}{#2}%
2280
      }%
2281
      Test{}{0}%
2282
2283
      \Test{0}{0}%
2284
      \Test{000}{0}%
2285
      Test{1}{1}%
2286
      \Test{001}{1}%
2287
      \Test{010}{00001}%
2288
      \Test{020}{000001}%
2289
      \Test{42}{0100001}%
      \Test{3F}{111111}%
2290
2291
     \Test{03F}{111111}%
```

```
\Test{43210}{0000100001001100001}%
2292
      \Test{98765}{10100110111000011001}%
2293
      \Test{FEDCBA}{010111010011101101111111}%
2294
      \Test{ 0 F 0 F 1 }{1000111100001111}%
2296 \end{qstest}
2297
2298
   \begin{qstest}{SetDec}{SetDec}
2299
     \def\Test#1#2{%
       \bitsetSetDec{abc}{#1}%
2300
       \expandafter\Expect\expandafter{\BS@abc}{#2}%
2301
     }%
2302
2303
     \Test{}{0}%
     Test{0}{0}%
2304
     \Test{000}{0}%
2305
     Test{1}{1}%
2306
2307
     \Test{7}{111}%
2308
     \Test{8}{0001}%
     \Test{001}{1}%
2309
     \Test{010}{0101}%
2310
2311
     \Test{020}{00101}%
2312
     \Test{53}{101011}%
     \Test{255}{11111111}%
2313
2314
      \Test{256}{000000001}%
      \Test{99999999}{111111111001001101011001110111}%
2315
      2317
      \Test{4210987654}{0110000101001001011111111010111111}%
2318
     \Test{2147483647}{11111111111111111111111111111}%
2319
     2320 \end{qstest}
2321
2322 \begin{qstest}{GetBin}{GetBin}
2323
     \def\TestUndef#1#2{%
2324
       \let\BS@abc\@undefined
2325
       \expandafter\expandafter\Expect
       \expandafter\expandafter\expandafter{%
2326
2327
         \bitsetGetBin{abc}{#1}%
2328
       }{#2}%
2329
     }%
2330
     \TestUndef{-1}{0}%
     \TestUndef{0}{0}%
2331
2332
     \TestUndef{1}{0}%
     \TestUndef{2}{00}%
2333
2334
     \TestUndef{8}{00000000}%
2335
      \def\Test#1#2{%}
2336
       \bitsetSetBin{abc}{#2}%
2337
       \expandafter\expandafter\Expect
2338
       \expandafter\expandafter\expandafter{%
2339
         \bitsetGetBin{abc}{#1}%
2340
       }{#2}%
2341
     ጉ%
     Test{-1}{0}%
2342
2343
     \Test{0}{0}%
     \Test{1}{0}%
2344
2345
     \Test{1}{1}%
2346
     \Test{2}{01}%
2347
     Test{2}{10}%
2348
     \Test{3}{010}%
2349
     Test{2}{00}%
2350
     Test{2}{01}%
     \Test{8}{00101100}%
2351
     \Test{2}{10101}%
2352
     \Test{-100}{11011}%
2353
```

```
2354 \end{qstest}
2355
2356 \begin{qstest}{GetOct}{GetOct}
      \def\Test#1#2#3{%
2357
2358
        \edef\x{\zap@space#1 \@empty}%
2359
        \edef\x{\noexpand\bitsetSetBin{abc}{\x}}%
2360
2361
        \expandafter\expandafter\Expect
2362
        \expandafter\expandafter\expandafter{%
          \bitsetGetOct{abc}{#2}%
2363
2364
        }{#3}%
2365
     }%
      \Test{111 110 101 100 011 010 001 000}{0}{76543210}%
2366
      \Test{000 111}{0}{7}%
      \Test{101 000}{-1}{50}%
2368
2369
      \Test{111}{-1}{7}%
2370
      \Test{111}{0}{7}%
2371
      \Test{111}{1}{7}%
      \Test{111}{3}{7}%
2372
2373
      \Test{111}{4}{07}%
2374
      \Test{111}{6}{07}%
      \Test{111}{7}{007}%
2375
2376
      \Test{111 010}{6}{72}%
      \Test{111 010}{7}{072}%
2377
      \Test{011 111}{0}{37}%
2378
      \Test{011 111}{6}{37}%
2379
2380
      \Test{011 111}{7}{037}%
      \Test{001 111}{0}{17}%
2381
2382
      \Test{001 111}{6}{17}%
      \Test{001 111}{7}{017}%
2383
2384 \end{qstest}
2385
2386 \begin{qstest}{GetHex}{GetHex}
      \def\Test#1#2#3{%
2387
        \bitsetSetBin{abc}{#1}%
2388
2389
        \expandafter\expandafter\Expect
2390
        \expandafter\expandafter\expandafter{%
2391
          \bitsetGetHex{abc}{#2}%
2392
        }{#3}%
     ጉ%
2393
      \Test{1111 1110 1101 1100 1011 1010 1001 1000}{0}{FEDCBA98}%
2394
      \Test{0111 0110 0101 0100 0011 0010 0001 0000}{0}{76543210}%
2395
      \Test{0000 1111}{0}{F}%
2396
2397
      \Test{0101 0000}{-1}{50}%
2398
      Test{1111}{-1}{F}%
      \Test{1111}{0}{F}%
2400
      \Test{1111}{1}{F}%
2401
      \Test{1111}{4}{F}%
2402
      \Test{1111}{5}{0F}%
2403
      \Test{1111}{8}{0F}%
      \Test{1111}{9}{00F}%
2404
2405
      \Test{1111 0010}{8}{F2}%
      \Test{1111 0010}{9}{0F2}%
2406
2407
      \Test{0111 1111}{0}{7F}%
2408
      \Test{0111 1111}{8}{7F}%
      \Test{0111 1111}{9}{07F}%
2410
      \Test{0011 1111}{0}{3F}%
2411
      \Test{0011 1111}{8}{3F}%
2412
      \Test{0011 1111}{9}{03F}%
2413
     \Test{0001 1111}{0}{1F}%
     \Test{0001 1111}{8}{1F}%
2414
     Test{0001 1111}{9}{01F}%
```

```
2416 \end{qstest}
2417
2418 \begin{qstest}{Range}{Range}
      \TestError{%
        Wrong index numbers in range [9..8] \MessageBreak% hash-ok
2420
2421
        for clear/set/flip on bit set 'abc'.\MessageBreak
2422
        The lower index exceeds the upper index.\MessageBreak
2423
        Canceling the operation as error recovery%
2424
      ጉ{%
        \bitsetSetRange{abc}{9}{8}%
2425
      }%
2426
      \def\TestErrorNegInd#1#2#3#4#5#6{%
2427
        \TestError{%
2428
          Negative index in range [#2..#3]\MessageBreak % hash-ok
2429
          for \string\bitset #1Range on bit set 'abc'.\MessageBreak
2430
          Using [#4..#5] as error recovery% hash-ok
2431
2432
        }{%
          \csname bitset#1Range\endcsname{abc}{#2}{#3}%
2433
          \global\let\BS@global\BS@abc
2434
2435
        }%
2436
        \Check{global}{#6}%
2437
      }%
2438
      \Set{abc}{111}%
      \TestErrorNegInd{Clear}{-1}{0}{0}{0}{111}%
2439
      \TestErrorNegInd{Clear}{0}{-1}{0}{0}{111}%
2440
      \TestErrorNegInd{Clear}{-2}{2}{0}{2}{001}%
2441
2442
      \bitsetReset{abc}%
2443
      \TestErrorNegInd{Set}{-1}{0}{0}{0}{0}%
2444
      2445
      \label{testErrorNegInd} $$\operatorname{TestErrorNegInd}_{-2}_{2}_{0}_{2}_{11}_{x}$
      \footnote{Months} \Set{abc}{101}%
2446
      \label{temp} $$\operatorname{TestErrorNegInd}_{-1}_{0}_{0}_{0}_{101}%$
2447
2448
      \TestErrorNegInd{Flip}{0}{-1}{0}{0}{101}%
2449
      \TestErrorNegInd{Flip}{-2}{2}{0}{2}{011}%
      \def\Test#1#2#3#4{%
2450
2451
        \bitsetSetBin{abc}{#1}%
2452
        \csname bitset\TestOp Range\endcsname{abc}{#2}{#3}%
2453
        \Expect*{\bitsetGetBin{abc}{0}}{#4}%
2454
     ጉ%
      \def\TestOp{Clear}%
2455
      Test{0}{0}{1}{0}
2456
      \Test{1111}{1}{2}{1101}%
2457
      Test{1111}{1}{3}{1001}%
2458
2459
      \texttt{\Test\{1111111100000000\}\{12\}\{14\}\{1100111100000000\}\%}
2460
      \def\TestOp{Set}%
2461
      \Test{0}{0}{1}{1}%
2462
      \Test{1000}{1}{2}{1010}%
2463
      \Test{0}{1}{2}{10}%
      \Test{1}{12}{15}{111000000000001}%
2464
2465
      \Test{1111}{1}{3}{1111}%
      2466
2467
      \def\TestOp{Flip}%
      \Test{0}{0}{1}{1}%
2468
      \Test{1}{0}{1}{0}%
2469
2470
      \Test{10101010}{1}{5}{10110100}%
2471
      \def\Test#1#2#3#4#5{%
2472
        \bitsetSetBin{abc}{#1}%
2473
        \bitsetSetValueRange{abc}{#2}{#3}{#4}%
2474
        \Expect*{\bitsetGetBin{abc}{0}}{#5}%
2475
     ጉ%
      \Test{0}{0}{1}{0}{0}%
2476
     \Test{0}{0}{1}{1}{1}}%
2477
```

```
\Test{1010}{1}{3}{0}{1000}%
2478
2479
     \Test{1010}{1}{3}{1}{1110}%
2480 \end{qstest}
2481
2482 \begin{qstest}{ShiftLeft/ShiftRight}{ShiftLeft/ShiftRight}
2483
     \def\@Test#1#2{%
2484
        \let\BS@abc\@undefined
2485
        \csname bitsetShift#1\endcsname{abc}{#2}%
        \Expect*{\BS@abc}{0}%
2486
     }%
2487
     \def\Test#1{%
2488
       \@Test{Left}{#1}%
2489
        \verb|\CTest{Right}{#1}||
2490
2491
     \Test{-16}%
2492
2493
     \Test{-1}%
2494
     \text{Test}\{0\}\%
     \Test{1}%
2495
     \Test{16}%
2496
2497
     \def\Test#1#2#3{%
2498
        \bitsetSetBin{abc}{#1}%
        \bitsetSetBin{result}{#3}%
2499
        \csname bitsetShift\Op\endcsname{abc}{#2}%
2500
        \Expect*{\bitsetGetBin{abc}{0}}*{\bitsetGetBin{result}{0}}%
2501
2502
2503
      \def\Op{Left}%
2504
     \Test{0}{0}{0}}%
2505
     \Test{0}{1}{0}%
2506
     Test{0}{-1}{0}%
     Test{1}{0}{1}%
2507
     \Test{1}{1}{10}%
2508
2509
     Test{1}{-1}{0}%
2510
     \Test{10}{1}{100}%
2511
     Test{10}{-1}{1}%
     2512
2513
     \Test{1}{-100}{0}%
2514
     \def\Op{Right}%
2515
     \Test{0}{0}{0}}%
2516
     \Test{0}{1}{0}%
2517
     Test{0}{-1}{0}%
     Test{1}{0}{1}%
2518
2519
     \Test{1}{1}{0}%
     \Test{1}{-1}{10}%
2520
2521
     \Test{10}{1}{1}%
2522
     \Test{10}{-1}{100}%
2523
     2524
      \Test{1}{100}{0}%
2525
      \Test{110110110110110}{10}{11011}%
2526
     \Test{110110110110110}{100}{0}%
2527
     \Test{1}{100000}{0}%
2528 \end{qstest}
2529
2530 \begin{qstest}{Profile: Set}{Profile: Set}
2531
     \bitsetSet{abc}{4095}%
2532
     \global\let\BS@global\BS@abc
2533 \end{qstest}
2534
2535 \begin{qstest}{Profile: Get}{Profile: Get}
     \ensuremath{\texttt{dof}}\x{\bitsetGet{global}{4095}}\%
2537 \end{qstest}
2538
2539 \begin{document}
```

```
2540 \end{document} 2541 \langle \text{/test2} \rangle
```

# 4 Installation

#### 4.1 Download

**Package.** This package is available on CTAN<sup>1</sup>:

CTAN:macros/latex/contrib/oberdiek/bitset.dtx The source file.

CTAN:macros/latex/contrib/oberdiek/bitset.pdf Documentation.

**Bundle.** All the packages of the bundle 'oberdiek' are also available in a TDS compliant ZIP archive. There the packages are already unpacked and the documentation files are generated. The files and directories obey the TDS standard.

```
CTAN:install/macros/latex/contrib/oberdiek.tds.zip
```

TDS refers to the standard "A Directory Structure for TEX Files" (CTAN:tds/tds.pdf). Directories with texmf in their name are usually organized this way.

#### 4.2 Bundle installation

Unpacking. Unpack the oberdiek.tds.zip in the TDS tree (also known as texmf tree) of your choice. Example (linux):

```
unzip oberdiek.tds.zip -d ~/texmf
```

Script installation. Check the directory TDS:scripts/oberdiek/ for scripts that need further installation steps. Package attachfile2 comes with the Perl script pdfatfi.pl that should be installed in such a way that it can be called as pdfatfi. Example (linux):

```
chmod +x scripts/oberdiek/pdfatfi.pl
cp scripts/oberdiek/pdfatfi.pl /usr/local/bin/
```

#### 4.3 Package installation

**Unpacking.** The .dtx file is a self-extracting docstrip archive. The files are extracted by running the .dtx through plain-T<sub>E</sub>X:

```
tex bitset.dtx
```

**TDS.** Now the different files must be moved into the different directories in your installation TDS tree (also known as texmf tree):

```
bitset.sty \rightarrow tex/generic/oberdiek/bitset.sty
bitset.pdf \rightarrow doc/latex/oberdiek/bitset.pdf
test/bitset-test1.tex \rightarrow doc/latex/oberdiek/test/bitset-test1.tex
test/bitset-test2.tex \rightarrow doc/latex/oberdiek/test/bitset-test2.tex
test/bitset-test3.tex \rightarrow doc/latex/oberdiek/test/bitset-test3.tex
bitset.dtx \rightarrow source/latex/oberdiek/bitset.dtx
```

If you have a docstrip.cfg that configures and enables docstrip's TDS installing feature, then some files can already be in the right place, see the documentation of docstrip.

<sup>1</sup>ftp://ftp.ctan.org/tex-archive/

#### 4.4 Refresh file name databases

If your  $T_EX$  distribution (te $T_EX$ , mik $T_EX$ , ...) relies on file name databases, you must refresh these. For example, te $T_EX$  users run texhash or mktexlsr.

#### 4.5 Some details for the interested

Attached source. The PDF documentation on CTAN also includes the .dtx source file. It can be extracted by AcrobatReader 6 or higher. Another option is pdftk, e.g. unpack the file into the current directory:

```
pdftk bitset.pdf unpack_files output .
```

Unpacking with LATEX. The .dtx chooses its action depending on the format:

plain-T<sub>E</sub>X: Run docstrip and extract the files.

LATEX: Generate the documentation.

If you insist on using LATEX for docstrip (really, docstrip does not need LATEX), then inform the autodetect routine about your intention:

```
latex \let\install=y\input{bitset.dtx}
```

Do not forget to quote the argument according to the demands of your shell.

Generating the documentation. You can use both the .dtx or the .drv to generate the documentation. The process can be configured by the configuration file ltxdoc.cfg. For instance, put this line into this file, if you want to have A4 as paper format:

```
\PassOptionsToClass{a4paper}{article}
```

An example follows how to generate the documentation with pdfLATEX:

```
pdflatex bitset.dtx
makeindex -s gind.ist bitset.idx
pdflatex bitset.dtx
makeindex -s gind.ist bitset.idx
pdflatex bitset.dtx
```

# 5 History

## [2007/09/28 v1.0]

• First version.

## 6 Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

```
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                                \ensuremath{\mbox{\sc Qehc}} . . . . . . . . . 155, 347, 903, 1061, 1083
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```

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