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"Brian Beckman: Don't Fear the Monad"

Available on Youtube [2].

Dr. Beckman, astrophysicist and senior software engineer, begins with a basic introduction to functional programming as a concept. Most notably, he focuses on the concept of functions as being **replaceable** by table-lookups.

1.1 Outline (7:50)

- 1. Functions
- 2. Monoids
- 3. Functions
- 4. Monads

1.2 Notation (8:25)

From "imperative" to functional notation:

- $int \ x = x \in int$
- x :: int
- int f(int x)
- $f :: int \rightarrow int$

Given type variable $a: \forall a$

- A x
- x :: a
- static A f < A > (A x)
- f :: a →a

1.2.1 Composition

Given:

in imperative style function composition might appear as: f(g(a)) or in reverse: g(f(a)).

In functional style, function application appears as: g a and composition can be shown as: f(g a). Parenthesis are necessary due to partial application being left associative. For example, f h g is applied as though (f h) g.

It is also possible to use a composition operator, \circ , to imply composition: (f \circ g) a. So, given the above 1.2.1, we can deduce:

```
h = (f \circ g) \ a = f \circ g
h :: a \to a
```

This does confuse the concepts of a as argument and a as type, but the point remains clear, I think.

1.3 Monoids (20:40)

In abstract algebra, a branch of mathematics, a monoid is an algebraic structure with a single associative binary operation and an identity element.

Monoids are studied in semigroup theory, because they are semigroups with identity. a.

 a Wikipedia

A Monoid is a Set with:

- 1. an associative binary operator (generally composition)
- 2. an identity value

The operator need not be commutative.

In a programming context, a Monoid guarantees type-consistency over function composition.

1.4 Monads (30:39)

Given:

```
x :: a
f :: a \rightarrow M a
g :: a \rightarrow M a
g :: a \rightarrow M a
```

M is described as a "Type Constructor."

Again, Dr. Beckman is using a to represent both a value of type a as well as the type itself a. Here he introduced the *Monad* "bind" operator: >>=, which he likes to call "shove":

```
f:: a \to M a g:: a \to M a f:: a \to M a
```

The reason to preserve symmetry in the above expression is that the desired expression is "bracketed" as: $\lambda a \to [(fa)>>=\lambda a \to (ga)]$ because the bind operator has type:

```
(\gt)=) :: Monad m \Rightarrow m \ a \rightarrow (a \rightarrow m \ b) \rightarrow m \ b
```

That is, >>= accepts a Monad (M a) and returns a function from a \rightarrow M a.

The functions f, and g live in a Monoid. M a (the data) lives in a Monad.

(>>=) is the analog of function composition and, therefore, obeys the rules of a *Monoid*. Including associativity and identity.

In a Monad, identity is—in Haskell-written as:

```
return :: Monad m \Rightarrow a \rightarrow m a
```

Extended to non-uniform types:

```
g :: a \rightarrow Mb

f :: b \rightarrow Mc

\lambda a \rightarrow (g \ a) >>= \lambda b \rightarrow (f \ b) :: a \rightarrow Mc

g >>= \lambda b \rightarrow (f \ b)
```

The Maybe Monad

2.1 As Described by Computerphile [1]

```
-- Type and 2 type constuctors: Val and Div
data Expr = Val Int | Div Expr Expr

-- Val 1
-- Div (Val 6) (Val 2)

unsafe_eval :: Expr → Int
unsafe_eval (Val n) = n
unsafe_eval (Div x y) = div (eval x) (eval y)

-- eval (Div (Val 6) (Val 2))
```

What if Div is passed zero? The program will crash. So, error-checking is necessary.

Abstracting the pattern of case checking Maybe values can be represented as:

```
Without 'do' notation

eval' :: Expr \rightarrow Maybe Int
eval' (Val n) = return n
eval' (Div x y) =

eval' x>>= (\lambda n \rightarrow 0)
eval' y>>= (\lambda m \rightarrow 0)
safediv n m)

With 'do' notation

eval'' :: Expr \rightarrow Maybe Int
eval'' (Val n) = return n
eval'' (Div x y) = do
n \leftarrow eval'' x
m \leftarrow eval'' y
safediv n m
```

Other Monads

The Monad type [3, p. 402]:

Monad comes with some default definitions:

```
m \gg k = m \gg \lambda_{\perp} \rightarrow k
fail s = \text{error } s
```

From this definition it can be seen that >> acts like >>=, except that the value returned by the first argument is discarded rather than being passed to the second argument. [3, p. 403]

3.1 The Identity Monad [3, p. 404]

The identity monad takes a type to itself with definitions:

```
m >>= f = f m
return = id
```

3.2 Definition of Maybe

3.3 The List Monad

```
instance Monad [] where
  xs >>= f = concat (map f xs)
  return x = [x]
  fail s = []
```

Lists are, in fact, themselves instances of Monad.

```
fmap :: Functor f \Rightarrow (a \rightarrow b) \rightarrow f \ a \rightarrow f \ b

\langle > \Rightarrow \rangle :: Monad m \Rightarrow m \ a \rightarrow (a \rightarrow m \ b) \rightarrow m \ b

map :: (a \rightarrow b) \rightarrow [a] \rightarrow [b]
```

Parsec

4.1 Using Parsec [4, Ch. 16]

```
import Text.ParserCombinators.Parsec
```

Input type is a sequence of characters, i.e., a Haskell *String*. *String* is the same as [*Char*]. The return value is [[*String*]]; a list of a list of Strings. We'll ignore *st* for now.

The do block implies a Monad. GenParser is a parsing monad.

many is a higher-order function that passes input repeatedly to the function passed as its argument. It collects the return values and treturns them in a list.

```
csvFile :: GenParser Char st [[String]]
csvFile =
  do result ← many line
  eof
  return result
```

A line is a list of cells followed by eol.

```
line :: GenParser Char st [String]
line =
  do result ← cells
    eol
    return result
```

```
cells :: GenParser Char st [String]
cells =
  do first ← cellContent
   next ← remainingCells
  return (first : next)
```

The choice operator, <|>, tries the parser on the left and tries The parser on the right if the left consumes no input.

```
remainingCells :: GenParser Char st [String]
remainingCells =
  (char ',' >> cells) <|> (return [])
```

```
cellContent :: GenParser Char st String cellContent = many (noneOf ",\lambdan")
```

```
eol :: GenParser Char st Char eol = char '\lambdan'
```

```
\begin{array}{l} \textit{parseCSV} :: \textbf{String} \rightarrow \textbf{Either} \ \textit{ParseError} \ [[\textbf{String}]] \\ \textit{parseCSV} \ \textit{input} = \textit{parse} \ \textit{csvFile} \ "(unknown)" \ \textit{input} \end{array}
```

Bibliography

- [1] Sean Riley and Professor Graham Hutton, Computerphile: What is a Monad?, YouTube, November 2017.
- [2] Dr. Brian Beckman, Don't Fear the Monad, YouTube, November 2012.
- [3] Simon Thompson, *The Craft of Functional Programming*, Pearson, Edinburgh Gate, England, Second Edition, 1999.
- [4] Bryan O'Sullivan, Don Stewart, and John Goerzen Real World Haskell O'Reilly Media 2008.