

DD2434 - Machine Learning, Advanced Course  
Assignment 1A

Tristan Perrot  
tristanp@kth.se

Étienne Riguet  
riguet@kth.se

November 2023



## 1 Exponential Family

### 1.1 Question 1.1

$$\begin{aligned}
 p(x|\theta) &= h(x) \exp(\eta(\theta) \cdot T(x) - A(\eta)) \\
 &= h(x) \exp(\eta(\lambda) \cdot T(x) - A(\eta(\lambda))) \\
 &= h(x) \exp(\log \lambda \cdot x - A(\log \lambda)) \\
 &= h(x) \exp(\log \lambda \cdot x - \lambda) \\
 &= h(x) \exp(\log \lambda \cdot x) \exp(-\lambda) \\
 &= e^{-\lambda} \frac{\lambda^x}{x!}
 \end{aligned} \tag{1}$$

We can see that the distribution correspond to a Poisson distribution of parameter  $\lambda$ .

## 2 Dependencies in a Directed Graphical Model

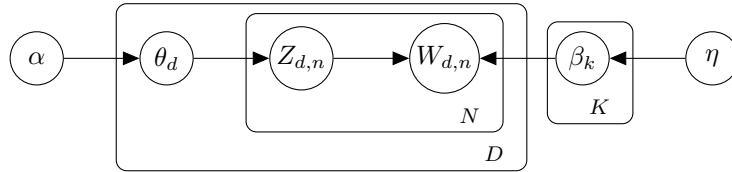


Figure 1: Graphical model of smooth LDA.

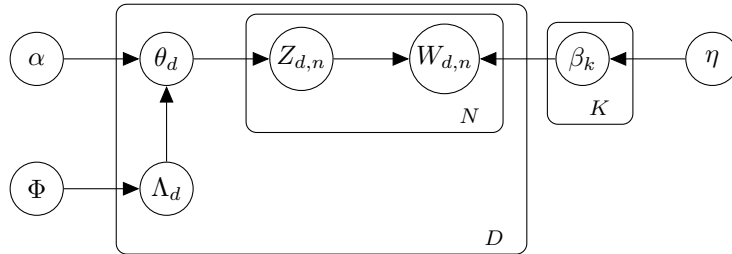


Figure 2: Graphical model of Labeled LDA.