Reparameterization of common distributions

We will work with Torch throughout this notebook.

```
In [ ]: import torch
from torch.distributions import Exponential, Categorical #, ... import the distributions you need here
from torch.nn import functional as F
```

A helper function to visualize the generated samples:

```
import matplotlib.pyplot as plt
def compare_samples (samples_1, samples_2, bins=100, range=None):
    fig = plt.figure()
    if range is not None:
        plt.hist(samples_1, bins=bins, range=range, alpha=0.5)
        plt.hist(samples_2, bins=bins, range=range, alpha=0.5)
    else:
        plt.hist(samples_1, bins=bins, alpha=0.5)
        plt.hist(samples_2, bins=bins, alpha=0.5)
        plt.hist(samples_2, bins=bins, alpha=0.5)
        plt.xlabel('value')
        plt.ylabel('number of samples')
        plt.legend(['direct','via reparameterization'])
        plt.show()
```

Q1. Exponential Distribution

Below write a function that generates N samples from $Exp(\lambda)$.

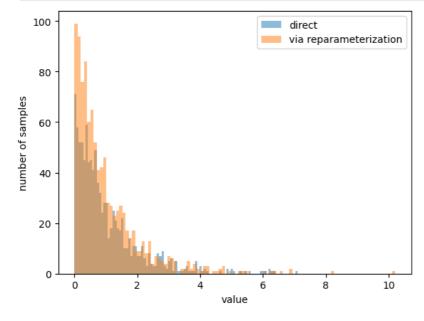
```
In []: def exp_sampler(1, N):
    # insert your code
    samples = Exponential(1).sample((N,))
    return samples # should be N-by-1
```

Now, implement the reparameterization trick:

```
In []:
    def exp_reparametrize(1,N):
        # this function should return N samples via reparametrization,
        # insert your code
        samples = -1/1 *torch.log(1-torch.rand(N,))
        return samples
```

Generate samples for $\lambda=1$ and compare:

```
In []: l = 1  #Lambda
N = 1000
direct_samples = exp_sampler(1, N)
reparametrized_samples = exp_reparametrize(1, N)
direct_samples = direct_samples.detach().numpy()
reparametrized_samples = reparametrized_samples.detach().numpy()
compare_samples(direct_samples, reparametrized_samples)
```



Q2. Categorical Distribution

Below write a function that generates N samples from Categorical (a), where $\mathbf{a} = [a_0, a_1, a_2, a_3]$.

```
In []: def categorical_sampler(a, N):
    # insert your code
    samples = Categorical(a).sample((N,))
    return samples # should be N-by-1
```

Now write a function that generates samples from Categorical (a) via reparameterization:

Generate samples when a = [0.1, 0.2, 0.5, 0.2] and visualize them:

```
In []: a = torch.tensor([0.1,0.2,0.5,0.2])
N = 1000
direct_samples = categorical_sampler(a, N)
reparametrized_samples = categorical_reparametrize(a, N, temp=0.1, eps=1e-20)
direct_samples = direct_samples.detach().numpy()
reparametrized_samples = reparametrized_samples.detach().numpy()
compare_samples(direct_samples, reparametrized_samples)
```

