

Reparameterization of common distributions

We will work with Torch throughout this notebook.

```
In [ ]: import torch
from torch.distributions import Exponential, Categorical, Gumbel #, ... import the distributions you need here
from torch.nn import functional as F
```

A helper function to visualize the generated samples:

```
In [ ]: import matplotlib.pyplot as plt
def compare_samples(samples_1, samples_2, bins=100, range=None):
    fig = plt.figure()
    if range is not None:
        plt.hist(samples_1, bins=bins, range=range, alpha=0.5)
        plt.hist(samples_2, bins=bins, range=range, alpha=0.5)
    else:
        plt.hist(samples_1, bins=bins, alpha=0.5)
        plt.hist(samples_2, bins=bins, alpha=0.5)
    plt.xlabel('value')
    plt.ylabel('number of samples')
    plt.legend(['direct', 'via reparameterization'])
    plt.show()
```

Q1. Exponential Distribution

Below write a function that generates N samples from $Exp(\lambda)$.

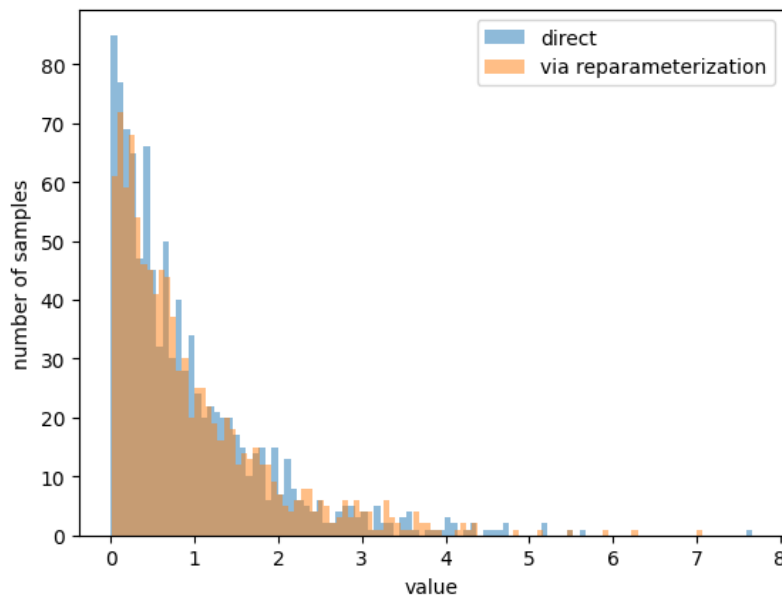
```
In [ ]: def exp_sampler(l, N):
    # insert your code
    samples = Exponential(l).sample((N,))
    samples = torch.reshape(samples, (-1,))
    return samples # should be N-by-1
```

Now, implement the reparameterization trick:

```
In [ ]: def exp_reparametrize(l, N):
    # this function should return N samples via reparametrization,
    # insert your code
    samples = -1/l * torch.log(1-torch.rand(N,))
    samples = torch.reshape(samples, (-1,))
    return samples
```

Generate samples for $\lambda = 1$ and compare:

```
In [ ]: l = 1 #Lambda
N = 1000
direct_samples = exp_sampler(l, N)
reparametrized_samples = exp_reparametrize(l, N)
compare_samples(direct_samples, reparametrized_samples)
```



Q2. Categorical Distribution

Below write a function that generates N samples from Categorical (**a**), where $\mathbf{a} = [a_0, a_1, a_2, a_3]$.

```
In [ ]: def categorical_sampler(a, N):  
    # insert your code  
    samples = Categorical(a).sample((N,))  
    samples = torch.reshape(samples, (-1,))  
    return samples # should be N-by-1
```

Now write a function that generates samples from Categorical (**a**) via reparameterization:

```
In [ ]: # Hint: approximate the Categorical distribution with the Gumbel-Softmax distribution  
def categorical_reparametrize(a, N, temp=0.1, eps=1e-20): # temp and eps are hyperparameters for Gumbel-Softmax  
    # insert your code  
    samples = Gumbel(0,1).sample((N,a.shape[0]))  
    samples = F.softmax((samples + torch.log(a+eps))/temp, dim=1)  
  
    with torch.no_grad():  
        samples = torch.argmax(samples, dim=1)  
  
    samples = torch.reshape(samples, (-1,))  
    return samples # make sure that your implementation allows the gradient to backpropagate
```

Generate samples when $\mathbf{a} = [0.1, 0.2, 0.5, 0.2]$ and visualize them:

```
In [ ]: a = torch.tensor([0.1,0.2,0.5,0.2])  
N = 1000  
direct_samples = categorical_sampler(a, N)  
reparametrized_samples = categorical_reparametrize(a, N, temp=0.1, eps=1e-20)  
compare_samples(direct_samples, reparametrized_samples)
```

