

2. C++ Implementation

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This page first presents a simple PID implementation in C++, then it adds output clamping and integral anti-windup. Finally, it lists the real-world implementation used in the actual microcontroller code.

Simple implementation

The following listing gives a very basic implementation of a PID controller in C++. It uses the formulas derived on the previous page.

```
1  #include <cmath>
2
3  /// Very basic, mostly educational PID controller with derivative filter.
4  class PID {
5  public:
6      /// @param kp Proportional gain    @f$ K_p @f$
7      /// @param ki Integral gain        @f$ K_i @f$
8      /// @param kd Derivative gain      @f$ K_d @f$
9      /// @param fc Cutoff frequency     @f$ f_c @f$ of derivative filter in Hz
10     /// @param Ts Controller sampling time @f$ T_s @f$ in seconds
11     /// The derivative filter can be disabled by setting `fc` to zero.
12     PID(float kp, float ki, float kd, float fc, float Ts)
13         : kp(kp), ki(ki), kd(kd), alpha(calcAlphaEMA(fc * Ts)), Ts(Ts) {}
14
15     /// Compute the weight factor  $\alpha$  for an exponential moving average filter
16     /// with a given normalized cutoff frequency `fn`.
17     static float calcAlphaEMA(float fn);
18
19     /// Update the controller with the given position measurement `meas_y` and
20     /// return the new control signal.
21     float update(float reference, float meas_y) {
22         // e[k] = r[k] - y[k], error between setpoint and true position
23         float error = reference - meas_y;
24         // e_f[k] =  $\alpha$  e[k] + (1- $\alpha$ ) e_f[k-1], filtered error
25         float ef = alpha * error + (1 - alpha) * old_ef;
26         // e_d[k] = (e_f[k] - e_f[k-1]) / Ts, filtered derivative
27         float derivative = (ef - old_ef) / Ts;
28         // e_i[k+1] = e_i[k] + Ts * e[k], integral
29         float new_integral = integral + error * Ts;
30
31         // PID formula:
32         // u[k] = Kp e[k] + Ki e_i[k] + Kd e_d[k], control signal
33         float control_u = kp * error + ki * integral + kd * derivative;
34
35         // store the state for the next iteration
36         integral = new_integral;
37         old_ef = ef;
38         // return the control signal
39         return control_u;
40     }
41
42 private:
43     float kp, ki, kd, alpha, Ts;
44     float integral = 0;
45     float old_ef = 0;
46 };
47
48 float PID::calcAlphaEMA(float fn) {
49     if (fn <= 0)
50         return 1;
51     //  $\alpha(f_n) = \cos(2\pi f_n) - 1 + \sqrt{\cos(2\pi f_n)^2 - 4 \cos(2\pi f_n) + 3}$ 
52     const float c = std::cos(2 * float(M_PI) * fn);
53     return c - 1 + std::sqrt(c * c - 4 * c + 3);
54 }
```

Output clamping and anti-windup

We can easily modify the code from the previous section to clamp the output of the controller, and to stop the integral from winding up if the output is already saturated:

```

1  /// Very basic, mostly educational PID controller with derivative filter, output
2  /// clamping and integral anti-windup.
3  class PID {
4  public:
5      /* ... */
6
7      /// Update the controller with the given position measurement `meas_y` and
8      /// return the new control signal.
9      float update(float reference, float meas_y) {
10         // e[k] = r[k] - y[k], error between setpoint and true position
11         float error = reference - meas_y;
12         // e_f[k] =  $\alpha$  e[k] + (1- $\alpha$ ) e_f[k-1], filtered error
13         float ef = alpha * error + (1 - alpha) * old_ef;
14         // e_d[k] = (e_f[k] - e_f[k-1]) / T_s, filtered derivative
15         float derivative = (ef - old_ef) / Ts;
16         // e_i[k+1] = e_i[k] + T_s e[k], integral
17         float new_integral = integral + error * Ts;
18
19         // PID formula:
20         // u[k] = K_p e[k] + K_i e_i[k] + K_d e_d[k], control signal
21         float control_u = kp * error + ki * integral + kd * derivative;
22
23         // Clamp the output
24         if (control_u > max_output)
25             control_u = max_output;
26         else if (control_u < -max_output)
27             control_u = -max_output;
28         else // Anti-windup
29             integral = new_integral;
30         // store the state for the next iteration
31         old_ef = ef;
32         // return the control signal
33         return control_u;
34     }
35
36 private:
37     float kp, ki, kd, alpha, Ts;
38     float max_output = 255;
39     float integral = 0;
40     float old_ef = 0;
41 };

```

Real-world implementation

In the actual microcontroller code for the motorized fader driver, we make a few changes to the algorithm introduced above:

- We use integer types for the input, setpoint, error and integral.
- For efficiency, the constants K_i and K_d are premultiplied/divided by the factor T_s .
- The output is turned off completely after a given number of cycles of inactivity (no setpoint changes or human interaction), if the error is small enough.

```

38 /// Standard PID (proportional, integral, derivative) controller. Derivative
39 /// component is filtered using an exponential moving average filter.
40 class PID {
41 public:
42     PID() = default;
43     /// @param kp
44     /// Proportional gain
45     /// @param ki
46     /// Integral gain
47     /// @param kd
48     /// Derivative gain
49     /// @param Ts
50     /// Sampling time (seconds)
51     /// @param fc
52     /// Cutoff frequency of derivative EMA filter (Hertz),
53     /// zero to disable the filter entirely
54     PID(float kp, float ki, float kd, float Ts, float f_c = 0,
55         float maxOutput = 255)
56         : Ts(Ts), maxOutput(maxOutput) {
57         setKp(kp);
58         setKi(ki);
59         setKd(kd);
60         setEMACutoff(f_c);
61     }
62
63     /// Update the controller: given the current position, compute the control
64     /// action.
65     float update(uint16_t input) {
66         // The error is the difference between the reference (setpoint) and the
67         // actual position (input)
68         int16_t error = setpoint - input;
69         // The integral or sum of current and previous errors
70         int32_t newIntegral = integral + error;
71         // Compute the difference between the current and the previous input,
72         // but compute a weighted average using a factor  $\alpha \in (0,1]$ 
73         float diff = emaAlpha * (prevInput - input);
74         // Update the average
75         prevInput -= diff;
76
77         // Check if we can turn off the motor
78         if (activityCount >= activityThres && activityThres) {
79             float filtError = setpoint - prevInput;
80             if (filtError >= -errThres && filtError <= errThres) {
81                 errThres = 2; // hysteresis
82                 return 0;
83             } else {
84                 errThres = 1;
85             }
86         } else {
87             ++activityCount;
88             errThres = 1;
89         }
90
91         bool backward = false;
92         int32_t calcIntegral = backward ? newIntegral : integral;
93
94         // Standard PID rule
95         float output = kp * error + ki_Ts * calcIntegral + kd_Ts * diff;
96
97         // Clamp and anti-windup
98         if (output > maxOutput)
99             output = maxOutput;
100         else if (output < -maxOutput)
101             output = -maxOutput;
102         else
103             integral = newIntegral;
104
105         return output;
106     }
107
108     void setKp(float kp) { this->kp = kp; } //< Proportional gain
109     void setKi(float ki) { this->ki_Ts = ki * this->Ts; } //< Integral gain
110     void setKd(float kd) { this->kd_Ts = kd / this->Ts; } //< Derivative gain
111
112     float getKp() const { return kp; } //< Proportional gain
113     float getKi() const { return ki_Ts / Ts; } //< Integral gain
114     float getKd() const { return kd_Ts * Ts; } //< Derivative gain
115
116     /// Set the cutoff frequency (-3 dB point) of the exponential moving average
117     /// filter that is applied to the input before taking the difference for
118     /// computing the derivative term.
119     void setEMACutoff(float f_c) {
120         float f_n = f_c * Ts; // normalized sampling frequency
121         this->emaAlpha = f_c == 0 ? 1 : calcAlphaEMA(f_n);
122     }
123
124     /// Set the reference/target/setpoint of the controller.
125     void setSetpoint(uint16_t setpoint) {
126         if (this->setpoint != setpoint) this->activityCount = 0;
127         this->setpoint = setpoint;
128     }
129     /// @see @ref setSetpoint(int16_t)
130     uint16_t getSetpoint() const { return setpoint; }
131

```

```

132     /// Set the maximum control output magnitude. Default is 255, which clamps
133     /// the control output in [-255, +255].
134     void setMaxOutput(float maxOutput) { this->maxOutput = maxOutput; }
135     /// @see @ref setMaxOutput(float)
136     float getMaxOutput() const { return maxOutput; }
137
138     /// Reset the activity counter to prevent the motor from turning off.
139     void resetActivityCounter() { this->activityCount = 0; }
140     /// Set the number of seconds after which the motor is turned off, zero to
141     /// keep it on indefinitely.
142     void setActivityTimeout(float s) {
143         if (s == 0)
144             activityThres = 0;
145         else
146             activityThres = uint16_t(s / Ts) == 0 ? 1 : s / Ts;
147     }
148
149     /// Reset the sum of the previous errors to zero.
150     void resetIntegral() { integral = 0; }
151
152 private:
153     float Ts = 1;          ///< Sampling time (seconds)
154     float maxOutput = 255;  ///< Maximum control output magnitude
155     float kp = 1;          ///< Proportional gain
156     float ki_Ts = 0;       ///< Integral gain times Ts
157     float kd_Ts = 0;       ///< Derivative gain divided by Ts
158     float emaAlpha = 1;    ///< Weight factor of derivative EMA filter.
159     float prevInput = 0;    ///< (Filtered) previous input for derivative.
160     uint16_t activityCount = 0; ///< How many ticks since last setpoint change.
161     uint16_t activityThres = 0; ///< Threshold for turning off the output.
162     uint8_t errThres = 1;   ///< Threshold with hysteresis.
163     int32_t integral = 0;   ///< Sum of previous errors for integral.
164     uint16_t setpoint = 0;  ///< Position reference.
165 };

```