

## 2. C++ Implementation

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This page first presents a simple PID implementation in C++, then it adds output clamping and integral anti-windup. Finally, it lists the real-world implementation used in the actual microcontroller code.

### Simple implementation

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The following listing gives a very basic implementation of a PID controller in C++. It uses the formulas derived on the previous page.

```
1  #include <cmath>
2
3  /// Very basic, mostly educational PID controller with derivative filter.
4  class PID {
5  public:
6      /// @param kp Proportional gain    @f$ K_p @f$
7      /// @param ki Integral gain        @f$ K_i @f$
8      /// @param kd Derivative gain      @f$ K_d @f$
9      /// @param fc Cutoff frequency    @f$ f_c @f$ of derivative filter in Hz
10     /// @param Ts Controller sampling time @f$ T_s @f$ in seconds
11     /// The derivative filter can be disabled by setting `fc` to zero.
12     PID(float kp, float ki, float kd, float fc, float Ts)
13         : kp(kp), ki(ki), kd(kd), alpha(calcAlphaEMA(fc * Ts)), Ts(Ts) {}
14
15     /// Compute the weight factor  $\alpha$  for an exponential moving average filter
16     /// with a given normalized cutoff frequency `fn`.
17     static float calcAlphaEMA(float fn);
18
19     /// Update the controller with the given position measurement `meas_y` and
20     /// return the new control signal.
21     float update(float reference, float meas_y) {
22         // e[k] = r[k] - y[k], error between setpoint and true position
23         float error = reference - meas_y;
24         // e_f[k] =  $\alpha$  e[k] + (1- $\alpha$ ) e_f[k-1], filtered error
25         float ef = alpha * error + (1 - alpha) * old_ef;
26         // e_d[k] = (e_f[k] - e_f[k-1]) / Ts, filtered derivative
27         float derivative = (ef - old_ef) / Ts;
28         // e_i[k+1] = e_i[k] + Ts e[k], integral
29         float new_integral = integral + error * Ts;
30
31         // PID formula:
32         // u[k] = Kp e[k] + Ki e_i[k] + Kd e_d[k], control signal
33         float control_u = kp * error + ki * integral + kd * derivative;
34
35         // store the state for the next iteration
36         integral = new_integral;
37         old_ef = ef;
38         // return the control signal
39         return control_u;
40     }
41
42 private:
43     float kp, ki, kd, alpha, Ts;
44     float integral = 0;
45     float old_ef = 0;
46 };
47
48 float PID::calcAlphaEMA(float fn) {
49     if (fn <= 0)
50         return 1;
51     //  $\alpha(f_n) = \cos(2\pi f_n) - 1 + \sqrt{\cos(2\pi f_n)^2 - 4 \cos(2\pi f_n) + 3}$ 
52     const float c = std::cos(2 * float(M_PI) * fn);
53     return c - 1 + std::sqrt(c * c - 4 * c + 3);
54 }
```

### Output clamping and anti-windup

---

We can easily modify the code from the previous section to clamp the output of the controller, and to stop the integral from winding up if the output is already saturated:

```

1  /// Very basic, mostly educational PID controller with derivative filter, output
2  /// clamping and integral anti-windup.
3  class PID {
4  public:
5      /* ... */
6
7      /// Update the controller with the given position measurement `meas_y` and
8      /// return the new control signal.
9      float update(float reference, float meas_y) {
10         //  $e[k] = r[k] - y[k]$ , error between setpoint and true position
11         float error = reference - meas_y;
12         //  $e_f[k] = \alpha e[k] + (1-\alpha) e_f[k-1]$ , filtered error
13         float ef = alpha * error + (1 - alpha) * old_ef;
14         //  $e_d[k] = (e_f[k] - e_f[k-1]) / T_s$ , filtered derivative
15         float derivative = (ef - old_ef) / Ts;
16         //  $e_i[k+1] = e_i[k] + T_s e[k]$ , integral
17         float new_integral = integral + error * Ts;
18
19         // PID formula:
20         //  $u[k] = K_p e[k] + K_i e_i[k] + K_d e_d[k]$ , control signal
21         float control_u = kp * error + ki * integral + kd * derivative;
22
23         // Clamp the output
24         if (control_u > max_output)
25             control_u = max_output;
26         else if (control_u < -max_output)
27             control_u = -max_output;
28         else // Anti-windup
29             integral = new_integral;
30         // store the state for the next iteration
31         old_ef = ef;
32         // return the control signal
33         return control_u;
34     }
35
36 private:
37     float kp, ki, kd, alpha, Ts;
38     float max_output = 255;
39     float integral = 0;
40     float old_ef = 0;
41 };

```

## Real-world implementation

In the actual microcontroller code for the motorized fader driver, we make a few changes to the algorithm introduced above:

- We use integer types for the input, setpoint, error and integral.
- For efficiency, the constants  $K_i$  and  $K_d$  are premultiplied/divided by the factor  $T_s$ .
- The output is turned off completely after a given number of cycles of inactivity (no setpoint changes or human interaction), if the error is small enough.

```

38 /// Standard PID (proportional, integral, derivative) controller. Derivative
39 /// component is filtered using an exponential moving average filter.
40 class PID {
41 public:
42     PID() = default;
43     /// @param kp
44     /// Proportional gain
45     /// @param ki
46     /// Integral gain
47     /// @param kd
48     /// Derivative gain
49     /// @param Ts
50     /// Sampling time (seconds)
51     /// @param fc
52     /// Cutoff frequency of derivative EMA filter (Hertz),
53     /// zero to disable the filter entirely
54     PID(float kp, float ki, float kd, float Ts, float f_c = 0,
55         float maxOutput = 255)
56         : Ts(Ts), maxOutput(maxOutput) {
57         setKp(kp);
58         setKi(ki);
59         setKd(kd);
60         setEMACutoff(f_c);
61     }
62
63     /// Update the controller: given the current position, compute the control
64     /// action.
65     float update(uint16_t input) {
66         // The error is the difference between the reference (setpoint) and the
67         // actual position (input)
68         int16_t error = setpoint - input;
69         // The integral or sum of current and previous errors
70         int32_t newIntegral = integral + error;
71         // Compute the difference between the current and the previous input,
72         // but compute a weighted average using a factor  $\alpha \in (0,1]$ 
73         float diff = emaAlpha * (prevInput - input);
74         // Update the average
75         prevInput -= diff;
76
77         // Check if we can turn off the motor
78         if (activityCount >= activityThres && activityThres) {
79             float filtError = setpoint - prevInput;
80             if (filtError >= -errThres && filtError <= errThres) {
81                 errThres = 2; // hysteresis
82                 return 0;
83             } else {
84                 errThres = 1;
85             }
86         } else {
87             ++activityCount;
88             errThres = 1;
89         }
90
91         bool backward = false;
92         int32_t calcIntegral = backward ? newIntegral : integral;
93
94         // Standard PID rule
95         float output = kp * error + ki_Ts * calcIntegral + kd_Ts * diff;
96
97         // Clamp and anti-windup
98         if (output > maxOutput)
99             output = maxOutput;
100         else if (output < -maxOutput)
101             output = -maxOutput;
102         else
103             integral = newIntegral;
104
105         return output;
106     }
107
108     void setKp(float kp) { this->kp = kp; } //< Proportional gain
109     void setKi(float ki) { this->ki_Ts = ki * this->Ts; } //< Integral gain
110     void setKd(float kd) { this->kd_Ts = kd / this->Ts; } //< Derivative gain
111
112     float getKp() const { return kp; } //< Proportional gain
113     float getKi() const { return ki_Ts / Ts; } //< Integral gain
114     float getKd() const { return kd_Ts * Ts; } //< Derivative gain
115
116     /// Set the cutoff frequency (-3 dB point) of the exponential moving average
117     /// filter that is applied to the input before taking the difference for
118     /// computing the derivative term.
119     void setEMACutoff(float f_c) {
120         float f_n = f_c * Ts; // normalized sampling frequency
121         this->emaAlpha = f_c == 0 ? 1 : calcAlphaEMA(f_n);
122     }
123
124     /// Set the reference/target/setpoint of the controller.
125     void setSetpoint(uint16_t setpoint) {
126         if (this->setpoint != setpoint) this->activityCount = 0;
127         this->setpoint = setpoint;
128     }
129     /// @see @ref setSetpoint(int16_t)
130     uint16_t getSetpoint() const { return setpoint; }
131

```

```

132 // Set the maximum control output magnitude. Default is 255, which clamps
133 // the control output in [-255, +255].
134 void setMaxOutput(float maxOutput) { this->maxOutput = maxOutput; }
135 // @see @ref setMaxOutput(float)
136 float getMaxOutput() const { return maxOutput; }
137
138 // Reset the activity counter to prevent the motor from turning off.
139 void resetActivityCounter() { this->activityCount = 0; }
140 // Set the number of seconds after which the motor is turned off, zero to
141 // keep it on indefinitely.
142 void setActivityTimeout(float s) {
143     if (s == 0)
144         activityThres = 0;
145     else
146         activityThres = uint16_t(s / Ts) == 0 ? 1 : s / Ts;
147 }
148
149 // Reset the sum of the previous errors to zero.
150 void resetIntegral() { integral = 0; }
151
152 private:
153     float Ts = 1; //< Sampling time (seconds)
154     float maxOutput = 255; //< Maximum control output magnitude
155     float kp = 1; //< Proportional gain
156     float ki_Ts = 0; //< Integral gain times Ts
157     float kd_Ts = 0; //< Derivative gain divided by Ts
158     float emaAlpha = 1; //< Weight factor of derivative EMA filter.
159     float prevInput = 0; //< (Filtered) previous input for derivative.
160     uint16_t activityCount = 0; //< How many ticks since last setpoint change.
161     uint16_t activityThres = 0; //< Threshold for turning off the output.
162     uint8_t errThres = 1; //< Threshold with hysteresis.
163     int32_t integral = 0; //< Sum of previous errors for integral.
164     uint16_t setpoint = 0; //< Position reference.
165 };

```