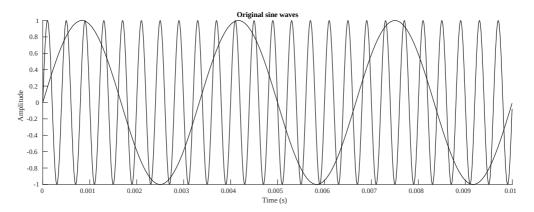
Filtering in MATLAB

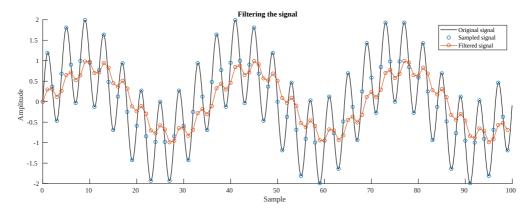
Pieter F

We can use MATLAB to visualize the effects of the filter. The scripts used can be found at the bottom of the page.

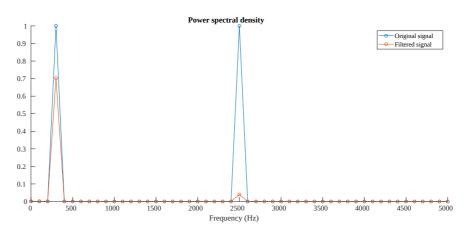
First, we generate a test signal that consists of two sine waves.



Then we apply the filter to it and plot the result. You can clearly see how the high-frequency sine wave is attenuated. Also note the phase shift between the original and the filtered signal: the red curve is delayed slightly, it is shifted to the right.



Finally, we can apply a fast fourier transform to inspect the frequency content.



Attenuation of first sine wave (30 Hz) = -1.53 dB Attenuation of second sine wave (250 Hz) = -13.97 dB

You can hear the difference for yourself:

Original Filtered

Audio

It can be used on music as well:

Original Filtered

Code

Sine Wave Code

```
%% Visualization
 1
       close all;
                              % Close all open figures
 3
       alpha = 0.25; % Filter factor of 1/4
       f s = 10000;
                               % 10 kHz sample frequency
% First sine wave with a frequency of 300 Hz
       f 1 = 300;
       f_2 = 2500;
                                % Second sine wave with a frequency of 2.5 kHz
10
       samples = 100; % Calculate/plot 100 samples
11
       n = linspace(0, samples-1, samples); % Generate a vector with sample numbers t = n / f_s; % Generate a vector with time
12
13
       \begin{array}{lll} sine\_1 &= sin(2*pi*f\_1*t); & \text{ Calculate the (sampled) sine waves} \\ sine\_2 &= sin(2*pi*f\_2*t); \\ signal &= (sine\_1 + sine\_2); & \text{ Mix the two sine waves togethe} \\ \end{array}
15
16
                                                       % Mix the two sine waves together
18
                                           \% Coefficients of the numerator of the transfer function \% Coefficients of the denominator of the transfer function
19
       b = alpha;
20
       a = [1, -(1-alpha)];
21
       filtered = filter(b, a, signal);
                                                        % Filter the signal
22
                                                       % Create a version with ten times more samples
23
       oversample continuous = 20;
       % to display the smooth, continuous signal samples_continuous = oversample_continuous * samples;
24
25
      26
27
28
29
30
       signal_continuous = (sine_1_continuous + sine_2_continuous);
31
32
      % Plot the two original sine waves
33
       figure('pos',[0,0,1200,400]);
34
       hold on:
      plot(t_continuous, sine_1_continuous, 'k');
plot(t_continuous, sine_2_continuous, 'k');
title('Original sine waves');
xlabel('Time (s)');
35
36
37
38
39
       ylabel('Amplitude');
40
      % Plot the continuous signal, the sampled version and the filtered output
41
42
       figure('pos',[0,0,1200,400]);
43
      hold on;
      noid on;
plot(n_continuous, signal_continuous, 'k');
plot(n, signal,'o');
plot(n, filtered,'-o');
title('Filtering the signal');
xlabel('Sample');
ylabel('Amplitude');
legend('Original signal','Sampled signal','Filtered signal');
44
45
46
47
49
50
51
52
      \mbox{\%} Apply a fast fourier transform and plot the spectra of the
      % original signal and of the filtered output figure('pos',[0,0,1000,400]);
53
54
55
       hold on;
56
       f = linspace(0, samples-1, samples)*f_s/samples;
      f = linspace(0, samples-1, samples)*f_s/samples;
original_spectrum = (abs(fft(signal))*2/samples).^2;
filtered_spectrum = (abs(fft(filtered))*2/samples).^2;
plot(f(1:1+samples/2), original_spectrum(1:1+samples/2),'-o');
plot(f(1:1+samples/2), filtered_spectrum(1:1+samples/2),'-o');
title('Power spectral density');
xlabel('Frequency (Hz)');
legend('Original signal','Filtered signal');
57
58
59
60
61
62
63
64
      % Calculate the attenuation of the two sine waves
65
      f_1_index = f_1*samples/f_s+1;
66
67
      A_1 = filtered_spectrum(f_1_index) / original_spectrum(f_1_index);
      A_1_dB = 10*\log_{10}(A_1);

fprintf('Attenuation of first sine wave (%.0f Hz) = %.02f dB\n', f_1, A_1_dB);
68
69
70
71
       \begin{array}{ll} f\_2\_index = f\_2*samples/f\_s+1; \\ A\_2 = filtered\_spectrum(f\_2\_index) \ / \ original\_spectrum(f\_2\_index); \end{array} 
72
      A_2_{dB} = 10*log10(A_2);
fprintf('Attenuation of second sine wave (%.0f Hz) = %.02f dB\n', f_2, A_2_dB);
74
75
       \% Open the filter visualization tool
77
       fvtool(b, a, 'Fs', f_s);
78
79
      %% WAV export
80
       samples = f_s*2;  % 2 seconds of audio
81
            linspace(0, samples-1, samples); % Generate a vector with sample numbers n / f_s; % Generate a vector with time
83
       t = n / f_s;
84
       \begin{array}{lll} sine\_1 = sin(2*pi*f\_1*t); & \text{\% Calculate the (sampled) sine wave } sine\_2 = sin(2*pi*f\_2*t); \\ signal = (sine\_1 + sine\_2)/2; & \text{Mix the two sine waves together} \end{array}
                                                 % Calculate the (sampled) sine waves
85
86
87
89
       filtered = filter(alpha,[1,-(1-alpha)], signal); % Filter the signal
90
       audiowrite('original.wav',signal,f_s);
audiowrite('filtered.wav',filtered,f_s);
                                                                      % Export as audio
92
```

Audio Code