

To reduce a 5 V signal to 2 V at 500 Hz using a first-order RC low-pass filter, we need to determine the cutoff frequency f_c such that the filter attenuates the signal appropriately.

For a first-order RC low-pass filter, the gain at frequency f is given by:

$$|H(f)| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_c}\right)^2}}$$

We require:

$$|H(500 \text{ Hz})| = \frac{2}{5} = 0.4$$

Solving for f_c :

$$\begin{aligned} 0.4 &= \frac{1}{\sqrt{1 + \left(\frac{500}{f_c}\right)^2}} \\ \sqrt{1 + \left(\frac{500}{f_c}\right)^2} &= \frac{1}{0.4} = 2.5 \\ 1 + \left(\frac{500}{f_c}\right)^2 &= 6.25 \\ \left(\frac{500}{f_c}\right)^2 &= 5.25 \\ \frac{500}{f_c} &= \sqrt{5.25} \approx 2.291 \\ f_c &= \frac{500}{2.291} \approx \boxed{218.3 \text{ Hz}} \end{aligned}$$

Therefore, the filter should be designed with a cutoff frequency of approximately 218 Hz to achieve the desired attenuation at 500 Hz.