

$i1 = \text{temp}$

$o1 = \text{how happy I am}$

$$h_1 = \text{NLU}(w_1 \cdot i_1 + b_1)$$

NLU = non-linear unit

$$o_1 = h_1 w_2 + b_2$$

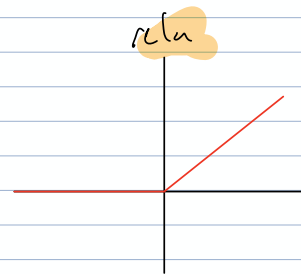
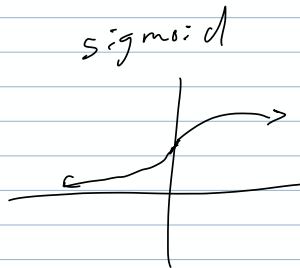
$$f(x) = \frac{1}{1 + e^{-x}} \quad (\text{sigmoid})$$

Ex

$$h_1 = \text{Relu}(w_1 \cdot i_1 + b_1)$$

$$o_1 = h_1 w_2 + b_2$$

$$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{otherwise} \end{cases} \quad (\text{relu})$$



$$i_1 = 3$$

$$w_1 = 4$$

$$b_1 = -13$$

$$w_2 = 6$$

$$b_2 = 7$$

$$\text{relu}(4 \cdot 3 - 13) = 0 = h_1$$

temp	happiness
60	-100
74	100
3	-200

$$o_1 = w_2 + b_2 = 7$$

1. Make network (choose NLU's, hidden layers)

(b) randomly initialize w 's, b 's

2. Choose a loss function

$$\text{MSE} = \frac{1}{2} (\hat{y} - y)^2$$

- outputs a scalar

3. Backprop

$$h_i = \text{ReLU}(w_i \cdot i + b_i)$$

$$o_i = h_i w_2 + b_2$$

$$L = \frac{1}{2} (o_i - y)^2$$

$$\frac{\partial o_i}{\partial w_2} = h_i$$

$$\frac{\partial o_i}{\partial b_2} = 1$$

$$\frac{\partial L}{\partial o_i} = o_i - y$$

$$= 7 - (-200)$$

$$= 207$$

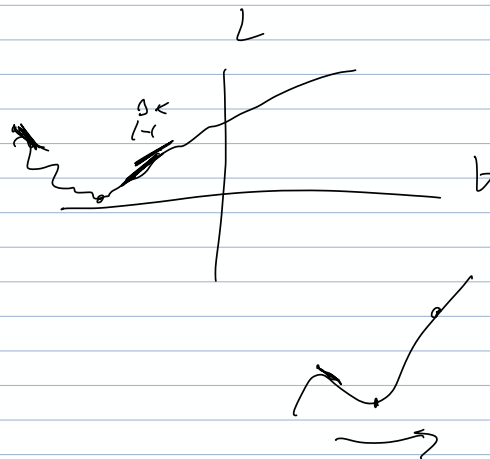
$$L = \text{MSE} = 207^2$$

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial o_i} \cdot \frac{\partial o_i}{\partial w_2}$$

$$= 207 \cdot 0 = 0$$

$$\frac{\partial L}{\partial b_2} = \frac{\partial L}{\partial o_i} \cdot \frac{\partial o_i}{\partial b_2}$$

$$= 207 \cdot 1 = 207$$



- We should decrease b to decrease L (if $\frac{\partial L}{\partial b_2} > 0$)

- $\uparrow b_2$ to $\downarrow L$ (if $\frac{\partial L}{\partial b_2} < 0$)

$$b_2' = b_2 - \frac{\partial L}{\partial b_2} \cdot \Sigma$$

$$\Sigma = \text{learning rate} \\ = 1e^{-3}$$

q

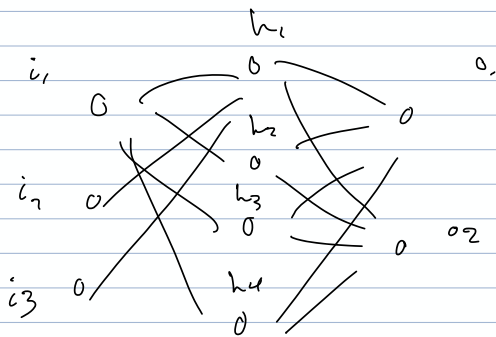
$$\frac{\partial o_1}{\partial h_1} = w_2$$

$$\frac{\partial L}{\partial h_1} = \frac{\partial L}{\partial o_1} \cdot \frac{\partial o_1}{\partial h_1}$$

$$= 207.6$$

$$\frac{\partial h_1}{\partial b_1} =$$

$$\frac{\partial L}{\partial h_1} \cdot \frac{\partial h_1}{\partial b_1} = \frac{\partial L}{\partial b_1}$$



$$h_1 = \text{ReLU}(w_{i_1, h_1} \cdot i_1 + w_{i_2, h_1} \cdot i_2 + w_{i_3, h_1} \cdot i_3 + b_{h_1})$$

↑
MLP