

# Musical patterns for prediction

Bachelor Project

Sebastian VELEZ DE VILLA

Supervised by M. Andrew MCLEOD

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## Abstract

Repetitions play a central role in music, whether they be repeated themes, harmonies or even rhythms. They can differ in many ways: vertically, by shifting the notes up or down, time-dilated, by slowing or accelerating them, or just slightly different, with ornamentation or removed notes, for example. We, humans, can easily recognise those patterns. However, this task becomes incredibly difficult to implement algorithmically, as music is subjective, and thus non deterministic: its perception can vary from an individual to the other. This paper aims at describing two ways of finding such repetitions, and how to use them to generate a continuation of a piece, given the first few notes, also called the “prime”. For discovery, string-based and translation-based approaches were used. Markov chains, where the next state depends only on the previous state, were employed for generation. This research aims at finding a solution to the first subtask of MIREX 2019: Patterns for Prediction, and at improving the already existing Markov chains approach. The results show a great improvement with both string-based and translation-based solutions, with the latter showcasing the most promising results. However, even if the generated notes are closer to the true continuations than the baseline, it still lacks some creativity, as the model only creates patterns or notes that already exist in the prime.

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# 1 Introduction

This project focuses on the first subtask of the MIREX 2019: Patterns for Prediction task ([9]), whose goal is to develop algorithms that take a short excerpt (called the prime) of music and produce a continuation: some notes that will follow the prime.

The main challenge for this task was to develop a robust way to find patterns in music. By “robust”, I mean an algorithm that could find repeated sequences that would be considered very similar by human listeners: it could be a repeated theme played at a higher pitch, or one played slower, or with a different rhythm. This trivial task for humans can become very cumbersome to implement for a computer, but not impossible. A basic way to find perfect matches would be to compare all subsets of the short excerpt with the whole set, and count how many times each one of them appears in the prime. This solution definitely works, but is slow, and doesn’t work when the patterns are not exact. It is often the case that themes, or important parts of the music, are repeated, but usually those themes slightly change throughout the piece. In other words, finding perfect matches is feasible, but does not find all the patterns.

In this work, I take existing algorithms for pattern detection ([11], [13]), and apply them (with some changes) to the task of music generation.

Such models already exist, and AIs are becoming the state of the art for this task ([14], [15]). I decided to work with statistics, and more specifically, Markov chains, because I wanted to learn something new, and different from what we can see nowadays. I also wanted to prove that a simpler model can still perform well, and produce convincing continuations.

In order to find such patterns, I decided to follow two approaches: a string-based approach, which finds exact patterns, and a translation-based approach, which finds exact patterns, as well as vertically shifted patterns. Consider the sequence “1 2 3 4 2 3 4 5” consisting of eight states. The string-based solution would only find the pattern “2 3 4”, whereas the translation-based algorithm would find the pattern “1 2 3 4”, knowing that it is shifted up by one to obtain “2 3 4 5”.

As we will see below, those two approaches perform pretty well against other models, but still lack some creativity. I decided to only work with monophonic music, but the algorithms described below could be extended to polyphonic music.

## 2 Related work

### 2.1 AI approaches

Various implementations of AI for music generation have been developed over the years. One of them, the “Music Transformer” ([1]) (built for a different task!) could be promising. This proposed architecture is based on the Transformer ([4]), which relies heavily on the concept of attention. The latter was first proposed by D. Bahdanau, K. Cho and Y. Bengio in 2014 ([3]), and by M.-T. Luong, H. Pham and C. D. Manning in 2015 ([5]). Attention models, as opposed to sequence-to-sequence models, pass down all hidden states from the encoder to the decoder, and give a certain score to each hidden state, so that the decoder focuses more on certain parts of the input sequence. This approach was first used for translation, where not all words in a sentence have the same importance, and was afterwards adapted for music generation. The goal is to produce music with long-term structure which, as opposed to Markov chains (described below), can generate the next notes depending not only from the previous state, but from the piece as a whole, disregarding patterns. As most AIs, it needs a lot of training based on existing data, whereas my models only need to analyse the prime. However, it is meant to work on both monophonic and polyphonic datasets.

Another approach that seems quite interesting is “MidiNet” ([15]), a convolutional generative adversarial network. It could also work on the MIREX 2019: Patterns for Prediction, as it can generate a continuation given a prime. The team tested the produced outputs with a few participants,

and asked them to rank the generations based on three questions: how pleasing, how real and how interesting. The users were told that some results were composed by humans, although all were created by a machine, to avoid bias. The results show that “MidiNet” outperforms attention-based models in all three categories. This solution also disregards patterns, and need a lot of training.

## 2.2 Statistical approach

A lot of my work was inspired by T. Collins, R. Laney, A. Willis and P. H. Garthwaite’s work ([12]). In this paper, they discuss how a computer can generate music using statistics. The basic idea uses Markov chains, i.e., a succession of states, where each state only depends on the previous one.

A simple music generation algorithm can be extended from that idea ([12]): generate the next note given only the previous note. Here’s an example:



Figure 1: Simple melody

To calculate the probabilities for each state, a possible algorithm could be formulated in the following way: create a transition matrix, and for each note, count how many times it is being followed by all the notes, and divide by the number of times that note appears (disregarding the last note which, by definition, doesn’t have a next state). As a result, this would generate the following table:

Pitch class	C	D	E	F	G
C	0.25	0.5	0.25	0	0
D	0	0	1.0	0	0
E	0.5	0	0	0.5	0
F	0	0	0	0	1.0
G	0	0	1.0	0	0

Table 1: Transition matrix of Figure 1

The previous transition matrix should be read line then column: "D is followed by E with probability 1.0", for example. This table can then be used to generate the next notes, by taking the last state, here G, and just reading the table with the probabilities for the next note. See subsection 3.3 for the cases where the last note is unique. Suppose we want to generate four notes, a possible output would be: "E C E F". This simple generation algorithm can thus only generate states that appear in the prime sequence (i.e. the input), and only transitions that already exist (we can never have a C followed by a G, and we can never have a B, for example). There is therefore no notion of creativity or musical structure in this case, only repetitions of what already exists. To a human listener, most of the outputs from this algorithm do not sound good. However, it is fast, and can run in  $\mathcal{O}(n+k)$ , where  $n$  is the length of the sequence, and  $k$  is the number of generated states.

In the example I provided, a first-order Markov model was used to generate pitches, but it can also be extended for durations, or pairs of pitches and durations.

In order to improve this basic model, they propose a solution based on pattern discovery and pattern inheritance. A pattern (or motive) is basically a set of notes which is repeated, shifted, or time-dilated in the piece. In Figure 1, a pattern would be "C D E C", as it is repeated twice.

### 3 Design and implementation

#### 3.1 Input format

The algorithms take monophonic sequences of midi notes, which are tuples of pitch, onset, duration and velocity attributes. Before the detection of patterns and generation, each prime is transformed so that it does not include rests, making both more straightforward. The pitches and onsets remain unchanged, only the durations are updated, so that each note ends when the next note starts. When generating the next states, the starting time becomes the offset of the previous note. Both algorithms transform that updated sequence into a list of pitch and, depending on the algorithm used, either the duration (string-based) or the onset of the notes (translation-based).

#### 3.2 Pattern detection

Based on the pattern idea discussed in [12], I wanted to test two different ways of finding such patterns in monophonic pieces, and compare the results with the simple case algorithm described in [subsection 2.2](#):

1. Exact non-overlapping non-shifted patterns (String-based).
2. Non-overlapping (possibly-) shifted patterns (Translation-based).

##### 3.2.1 String-based pattern recognition

In the former case, the program uses a string-based approach, and finds exact patterns, which is defined as a sequence of notes that have the same pitches and duration, that appears at least twice in the score. A pattern detected by this algorithm for [Figure 1](#) would be the first four notes. This method can obtain results in  $\mathcal{O}(n^2)$ .

##### 3.2.2 Translation-based pattern recognition

In the latter case, the program uses translation vectors: it tries to find the maximum translatable pattern, i.e., a pattern that can be shifted either vertically or horizontally in the score. As opposed to the string-based approach, this method uses onsets instead of duration, which is needed to calculate the translation vectors, described below. This algorithm is based on **SIA**, described in [11].

To make things simple, I will go step by step over this algorithm with the simple case scenario of [Figure 1](#). For each note, calculate its translation vector with all the other future notes in the sequence: let  $n$  and  $m$  be two notes, with onsets and pitches, then the translation vector would be a 2-d vector, equal to  $\begin{pmatrix} m.onset - n.onset \\ m.pitch - n.pitch \end{pmatrix}$ . This would result in the following table for the first two measures, where the table should be read starting with columns and then rows (e.g. note  $\begin{pmatrix} 0.0 \\ 72 \end{pmatrix}$  can be transformed into  $\begin{pmatrix} 0.25 \\ 74 \end{pmatrix}$  by adding the vector  $\begin{pmatrix} 0.25 \\ 2 \end{pmatrix}$ ):

(Onset, pitch)	(0.0, 72)	(0.25, 74)	(0.5, 76)	(0.75, 72)	(1.0, 72)	(1.25, 74)	(1.5, 76)	(1.75, 72)
(0.0, 72)	-	-	-	-	-	-	-	-
(0.25, 74)	(0.25, 2)	-	-	-	-	-	-	-
(0.5, 76)	(0.5, 4)	(0.25, 2)	-	-	-	-	-	-
(0.75, 72)	(0.75, 0)	(0.5, -2)	(0.25, -4)	-	-	-	-	-
(1.0, 72)	(1.0, 0)	(0.75, -2)	(0.5, -4)	(0.25, 0)	-	-	-	-
(1.25, 74)	(1.25, 2)	(1.0, 0)	(0.75, -2)	(0.5, 2)	(0.25, 2)	-	-	-
(1.5, 76)	(1.5, 4)	(1.25, 2)	(1.0, 0)	(0.75, 4)	(0.5, 4)	(0.25, 2)	-	-
(1.75, 72)	(1.75, 0)	(1.5, -2)	(1.25, -4)	(1.0, 0)	(0.75, 0)	(0.5, -2)	(0.25, -4)	-

Table 2: Translation vectors of the first two measures of [Figure 1](#), uncoloured non-empty cells are unique.

Then for each translation vector that appears at least twice in the table, create a sequence of notes which have this vector in their column. Sorting them by length would result in:

- 
- $\begin{pmatrix} 0.25 \\ 2 \end{pmatrix}$ :  $\begin{pmatrix} 0.0 \\ 72 \end{pmatrix}$ ,  $\begin{pmatrix} 0.25 \\ 74 \end{pmatrix}$ ,  $\begin{pmatrix} 1.0 \\ 72 \end{pmatrix}$  and  $\begin{pmatrix} 1.25 \\ 74 \end{pmatrix}$ .
  - $\begin{pmatrix} 1.0 \\ 0 \end{pmatrix}$ :  $\begin{pmatrix} 0.0 \\ 72 \end{pmatrix}$ ,  $\begin{pmatrix} 0.25 \\ 74 \end{pmatrix}$ ,  $\begin{pmatrix} 0.5 \\ 76 \end{pmatrix}$  and  $\begin{pmatrix} 0.75 \\ 72 \end{pmatrix}$ .
  - $\begin{pmatrix} 0.5 \\ 4 \end{pmatrix}$ :  $\begin{pmatrix} 0.0 \\ 72 \end{pmatrix}$  and  $\begin{pmatrix} 1.0 \\ 72 \end{pmatrix}$ .
  - ...
  - $\begin{pmatrix} 1.25 \\ 2 \end{pmatrix}$ :  $\begin{pmatrix} 0.0 \\ 72 \end{pmatrix}$  and  $\begin{pmatrix} 0.25 \\ 74 \end{pmatrix}$ .

Then the patterns are filtered to keep only those which are continuous, like the second one in the enumeration above, and unlike the first one.

So as an example, the first four notes can be shifted by four beats to obtain the last four notes, which corresponds to the second element in the aforementioned enumeration, and to the purple cells in [Table 2](#). This whole process can take  $\mathcal{O}(n^2)$ , but is slower than the string-based approach.

### 3.3 Special cases

For both string-based and translation-based, when a note appears only once, only at the end of the prime, or is not part of any pattern, it is considered as a pattern, making it easier for the generation. In the case where the last note is unique, the probabilities for the next pattern (or note, in the simple algorithm case) are set according to the normalised histogram of the prime, which corresponds to the probability of each pattern (or note) appearing in the whole set, regardless of its position.

### 3.4 Generation

Once the patterns are found, both algorithms work in the same way: they transform the sequence of notes into a sequence of patterns, and apply a first-order Markov model on this transformed sequence to generate, not the next notes, but the next patterns. Then, the program translates back this sequence of patterns into a sequence of midi notes, i.e., a list of tuples with pitch, onset, duration and velocity attributes, the latter being always set to 100. Note that the velocity was never used, as the goal of this project was to generate written pieces.

### 3.5 Smoothing

These algorithms only produce transitions that already exist in the prime sequence. To solve this problem, I decided to use some sort of additive smoothing. First, produce the transition matrix, as in [Table 1](#). Then, multiply each probability by some number  $\alpha$  (I decided to set  $\alpha = 0.9$ ), and then distribute the remaining  $1 - \alpha$  among all the states, according to their normalised histogram (the unigram probability of each state). For example, for [Figure 1](#), it would be (with values rounded to the fourth decimal):

C	D	E	F	G
0.2857	0.1429	0.2857	0.1429	0.1429

Table 3: Normalised histogram of [Figure 1](#)

This approach would ensure that some states appear more than others, and would create transitions that don't exist in the prime, resulting in some "creativity". Taking this into account, this would result in the following transition matrix for [Figure 1](#):



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Pitch class	C	D	E	F	G
C	0.25357	0.46429	0.25357	0.01429	0.01429
D	0.02857	0.01429	0.92857	0.01429	0.01429
E	0.47857	0.01429	0.02857	0.46429	0.01429
F	0.02857	0.01429	0.02857	0.01429	0.91429
G	0.02857	0.01429	0.92857	0.01429	0.01429

Table 4: Transition matrix of Figure 1 with additive smoothing

The values in the table above have been rounded to the fifth decimal. The continuation would be produced in the same way as previously described, but taking these new values into account. This idea can also be applied (and was applied for the evaluation) to the two pattern recognition algorithms.

## 4 Evaluation

The evaluation of the continuation could be done manually, but these would take a lot of time, and would lack objectivity, as music is intrinsically differently perceived by everyone. Instead, an automatic evaluation was used, available at [9]. The dataset used for both generation and evaluation is composed of two parts, the prime, from which a continuation will be generated, and the true continuation, which will be compared with the outputs of the two algorithms. The dataset was a subset of the Lakh MIDI dataset ([10]), which was specially prepared for this MIREX task.

The evaluation was done in two different ways ([9]): with a cardinality score, and with a pitch score.

### 4.1 Cardinality score

The cardinality score is defined as  $CS(\mathbf{P}, \mathbf{Q}) = \max_{t \in \mathbf{T}} |\{q \forall q \in \mathbf{Q} \mid (q + t) \in \mathbf{P}\}|$ , where  $\mathbf{P}$  and  $\mathbf{Q}$  are two-dimensional sets of onset and pitch,  $\mathbf{P}$  being the true continuation,  $\mathbf{Q}$  being the algorithmic continuation, and  $t \in \mathbf{T}$  being the vector that maximises the cardinality score.  $\mathbf{T}$  is defined as  $\mathbf{T} = \{p - q \forall p \in \mathbf{P}, q \in \mathbf{Q}\}$ , and represents the set of all translation vectors that transform an algorithmically generated note into a note from the true continuation. In other words, a higher score reflects how similar two continuation are in their shape, meaning that they are independent of shifts in time and pitch. From there, three methods of measurements can be computed:

1. The recall, which is the number of correctly predicted notes, divided by the length of the true continuation (we have  $-1$  because at least one note can be translated into a note of the true sequence, and we want the recall to be in  $[0, 1]$ ):  $\text{Recall} = \frac{CS(\mathbf{P}, \mathbf{Q}) - 1}{|\mathbf{P}| - 1}$ . The higher the better.
2. The precision, which is the number of correctly predicted notes, divided by the length of the algorithmically generated continuation (same convention applies):  $\text{Precision} = \frac{CS(\mathbf{P}, \mathbf{Q}) - 1}{|\mathbf{Q}| - 1}$ .
3. The F1 measure, which is the harmonic mean of the two previous methods.

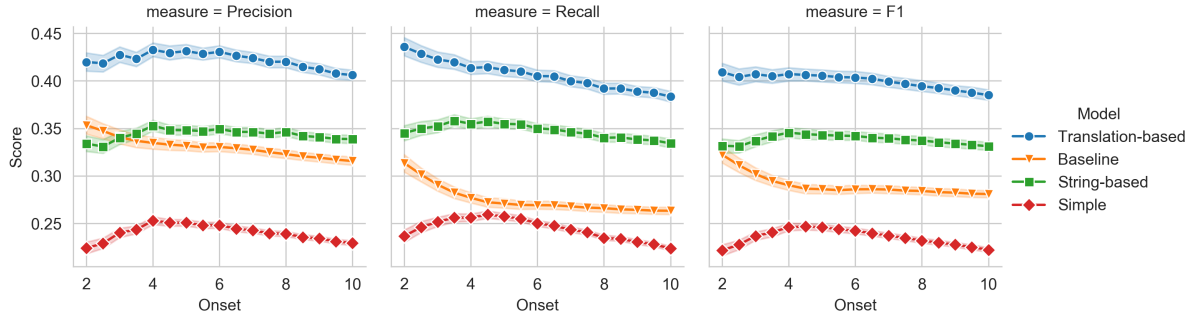


Figure 2: Cardinality scores for the three models described above and the baseline.

The x-axis represents the onset times of the true continuation after the end of the prime, and is clipped to 10 beats: the notes generated after the tenth beat are disregarded.

We observe that the simple first-order Markov model performs pretty badly, which can be expected. However, we notice a great improvement in the recall measure with the two pattern recognition algorithms (translation-based and string-based). This means that the continuation produced is closer in some sense, i.e., has a more similar shape, than the baseline, to the true continuation. Generally, all get worse as time goes on, but the simple and string-based algorithms have humps at 4 beats (on the x-axis).

## 4.2 Pitch score

The problem with the cardinality score is that it is pitch invariant: if the generated continuation is equal to the true continuation but shifted vertically, it would get a perfect score (of 1), as we can translate the whole sequence of notes with only one translation vector. The pitch score is used to solve this. It is the comparison of the normalised histograms of the true and generated continuations (an example of a normalised histogram is given in Table 3). This process is repeated disregarding the octaves (mod 12 pitches).

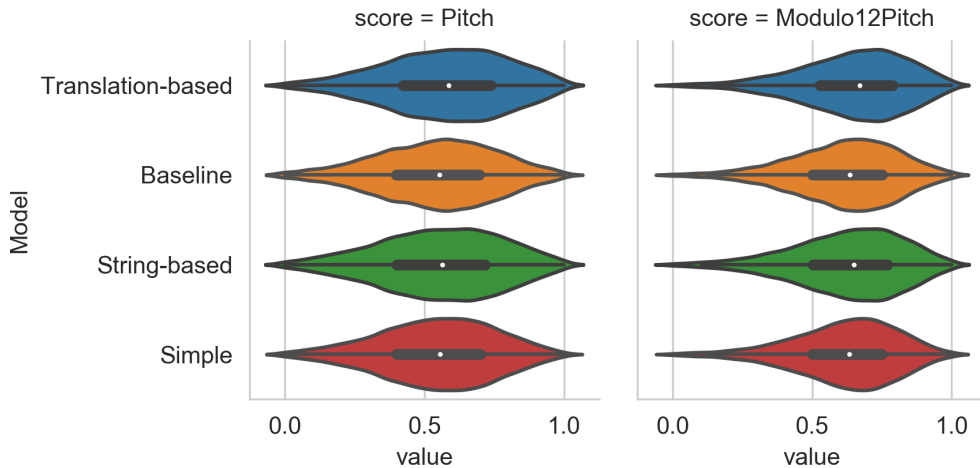


Figure 3: Pitch scores for the three models described above and the baseline.

All of them are pretty similar:

	Pitch		
	mean	median	std
Model			
Baseline	0.542	0.555	0.211
Simple	0.544	0.556	0.206
String-based	0.553	0.565	0.220
Translation-based	0.574	0.588	0.218

Figure 4: Pitch scores.

	Modulo12Pitch		
	mean	median	std
Model			
Baseline	0.616	0.635	0.188
Simple	0.618	0.633	0.185
String-based	0.627	0.650	0.196
Translation-based	0.647	0.670	0.192

Figure 5: Mod12 pitch scores.

We notice however that the translation-based continuation is again, better. The higher the score, the higher the similarity in distribution of the pitches between the true and the generated continuations. The fact that this score is just above 0.5 means that the distributions are similar to the ones of the true continuations, but far from equal.

### 4.3 Interpretation of the evaluation’s results

The results shown in the pictures can vary from one execution to the other, as the generations are based on some randomness. However, the patterns discovered will always be deterministic.

### 4.4 Comparison with an example

In order to compare the results, let’s take the following piece, and see what the three algorithms produce as a continuation, as well as their corresponding cardinality and pitch scores:



Figure 6: MIDI sample taken from the MIREX 2019: Patterns for prediction dataset [9]. In red, the patterns found by the string-based algorithm. In green, the patterns found by the translation-based one.

- Simple algorithm without pattern recognition:



- String-based pattern recognition algorithm:



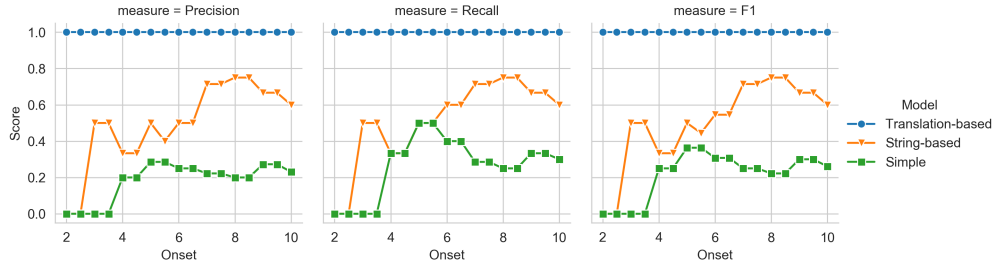
- Translation-based pattern recognition algorithm:



We can observe that in the last two cases, some patterns from the prime are repeated, whereas it is not the case for the simple algorithm without pattern recognition. The fact that some elements are not repeated makes the generation look totally random, so less likely to be correct. Here is the true continuation of [Figure 6](#):



Which gives us the following cardinality scores:



As shown in the graph, the translation-based approach obtains a perfect score for this prime, meaning that the generated continuation has exactly the same shape as the true continuation. The string-based algorithm performs slightly better than the simple model. Concerning the pitch scores, we obtain the following means: **0.143** for the simple algorithm, **0.621** for string-based and **1.000** for translation-based. Thus, if we have both a higher cardinality and pitch scores, then we can consider the continuation as better. Note that these values might change between different executions, as the results depend on some randomness.

The produced outputs from the best version, the translation-based approach, heavily depend on the structure of the prime. It has to be repetitive, i.e. contain patterns (either vertically or horizontally shifted, but not time-dilated), and long enough to detect multiple patterns, to add some variety. If the prime doesn't respect one of these conditions, then the generated continuation will be poor, like in the example below:



Figure 7: "Castle in the sky" theme, composed by Joe Hisaishi. In red, the patterns found by the string-based approach, in green, the ones found by the translation-based algorithm.

And the three continuations:

- Simple algorithm without pattern recognition:



- String-based pattern recognition:



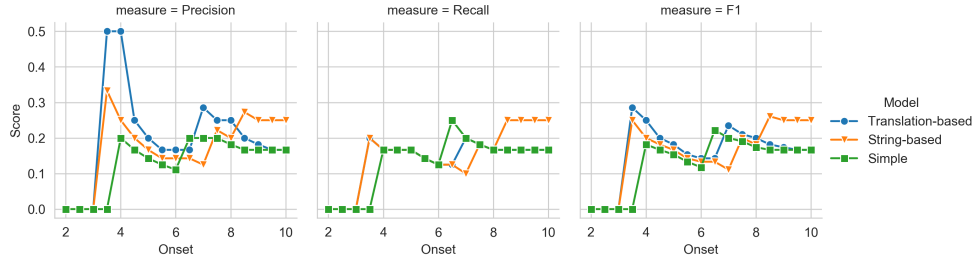
- Translation-based pattern recognition:



And the true continuation is:



Which gives pitch scores of **0.308**, **0.308** and **0.231**, for the simple algorithm, string-based and translation-based, respectively, and those cardinality scores:



We can observe that all three generations are completely different from the true continuation, because the prime is not repetitive enough, and the true continuation is original, which is not handled by any of the algorithms. We can also see that the patterns found by both algorithms are either comprised of only one or a few notes, which is very different compared to the other example. Taking into account the pitch scores and cardinality scores, the values are pretty low, which confirms that the continuation is not great.

## 5 Conclusion

Overall, the two pattern-based algorithms work well when the true continuation contains a repetition of a known pattern, i.e., a pattern that has already appeared at least twice in the prime. It performs badly when the continuation is new, as the algorithms do not have a notion of creativity. Although these algorithms can perform pretty well as we saw in [section 4](#), further work can be done. Each solution I provided was an improvement of the previous version, and improvements over the last version can still be made, by adding non-exact patterns to the translation vectors approach. For example, the two patterns "C D E C" and "C D C C" could be considered as similar, as most of the notes are equal. Another approach would be to use a second-order Markov model, i.e., where the next state depends on the two previous states.

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Similar algorithms for polyphonic music can be developed, as well as AI-based solutions, which could be combined with statistical models. Future work could try to inject creativity into the generated sequences by adding more noise to the unknown states, or just give non-zero probabilities to new notes or patterns. Overall, this statistical approach is great for repetitive pieces, but certainly lacks creativity, which remains a central piece of composition.

The code for this work is available online<sup>1</sup>.

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<sup>1</sup><https://github.com/v1ruso/BachelorProject>