

A similar recursive approach would work for the ℓ^p norm of \mathbf{x} , where $p \geq 1$ and

$$\|\mathbf{x}\|_p = \left(\sum_{i=1}^n |x_i|^p \right)^{1/p},$$

if a function $\text{normp}(x, y)$ were available, where

$$\text{normp}(x, y) = (|x|^p + |y|^p)^{1/p},$$

such that unwarranted under/over-flows are avoided, and relative accuracy and monotonicity with respect to $|x|$ and $|y|$ are guaranteed.

For $p = 1$, $\text{norm1}(x, y) = |x| + |y|$, for $p = 2$, $\text{norm2}(x, y) = \text{hypot}(x, y)$. Else, as the first attempt,

$$\text{normp}(x, y) = M (1 + q^p)^{1/p}, \quad M = \max\{|x|, |y|\}, \quad m = \min\{|x|, |y|\}, \quad q = m/M \text{ or } 0 \text{ if } m = 0.$$

Let $z = q^{p/2}$. Then $1 + q^p = 1 + z^2 \approx \text{fma}(z, z, 1)$. With `cr_pow`, the algorithm might be as follows:

$$\begin{aligned} X &= \text{fabs}(x), \quad Y = \text{fabs}(y); \\ M &= \text{fmax}(X, Y), \quad m = \text{fmin}(X, Y); \\ q &= m/M, \quad Q = \text{fmax}(q, 0); \\ z &= \text{cr_pow}(Q, p/2), \quad Z = \text{fma}(z, z, 1); \\ C &= \text{cr_pow}(Z, 1/p); \\ \text{normp}(x, y) &\approx M \cdot C. \end{aligned}$$