
Algorithm 1 LCPSLength(X,Y)

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1:  $n \leftarrow \text{length}[X]$ 
2: for  $i = 1$  to  $n$  do
3:   for  $j = 1$  to  $i$  do
4:     for  $k = 1$  to  $n$  do
5:       for  $\ell = 1$  to  $k$  do
6:         if  $(i = j \text{ or } k = \ell)$  and (either of  $x_i$  or  $x_j$  equals either of  $y_k$  or  $y_\ell$ ) then
7:            $lcps[i, j, k, \ell] = 1$ 
8:         else
9:            $lcps[i, j, k, \ell] = 0$ 
10:        end if
11:      end for
12:    end for
13:  end for
14: end for
15: for  $xLength = 2$  to  $n$  do
16:   for  $yLength = 2$  to  $n$  do
17:     for  $i = 1$  to  $n - xLength + 1$  do
18:       for  $k = 1$  to  $n - yLength + 1$  do
19:          $j = i + xLength$ 
20:          $\ell = k + yLength$ 
21:         if  $x_i = x_j = y_k = y_\ell$  then
22:            $lcps[i, j, k, \ell] = 2 + lcps[i + 1, j - 1, k + 1, \ell - 1]$ 
23:         else
24:            $lcps[i, j, k, \ell] = \max(lcps[i + 1, j, k, \ell], lcps[i, j - 1, k, \ell], lcps[i, j, k + 1, \ell], lcps[i, j, k, \ell - 1])$ 
25:         end if
26:       end for
27:     end for
28:   end for
29: end for
30: return  $lcps$ 
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$$lcps[i, j, k, \ell] = \begin{cases} 0 & i > j \text{ or } k > \ell \\ 1 & (i = j \text{ or } k = \ell) \\ & \text{and} \\ & (\text{either of } x_i \text{ or } x_j \\ & \text{equals} \\ & \text{either of } y_k \text{ or } y_\ell) \\ 2 + lcps[i + 1, j - 1, k + 1, \ell - 1] & (i < j \text{ and } k < \ell) \\ & \text{and} \\ & x_i = x_j = y_k = y_\ell \\ \max(lcps[i + 1, j, k, \ell], lcps[i, j - 1, k, \ell], \\ lcps[i, j, k + 1, \ell], lcps[i, j, k, \ell - 1]) & (i < j \text{ and } k < \ell) \\ & \text{and} \\ & \text{the condition } (x_i = x_j = y_k = y_\ell) \\ & \text{does not hold} \end{cases} \quad (3)$$

The length of an LCPS between X and Y shall be stored at $lcps[1, n, 1, n]$. Since there are $\Theta(n^4)$