

Central-limit theorem (Section 9.7)

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In a nutshell, the central-limit theorem states that histograms of sums $X = \sum_{i=1}^N x_i$ of random numbers x_i , drawn from some arbitrary distribution $\Psi(x)$, in the limit of large N always look Gaussian, provided that second moment of $\Psi(x)$ exists.

We first select the number N of random numbers to add and the type of distribution $\Psi(x)$ from which to draw the random numbers. Check out `help random` in MATLAB to find inspiration to extend the selection. Then we fill the array `raw` with $N \times 10^5$ random numbers drawn from the selected distribution.

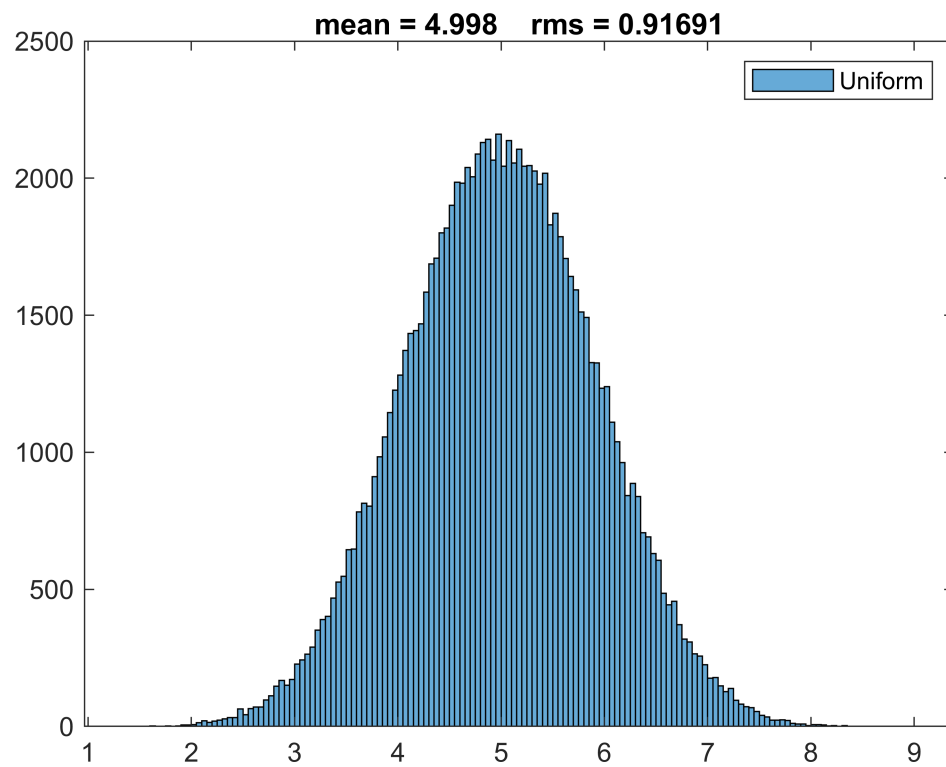
```
clear
N=10; % Slider to set N
distribution="Uniform" % Slider to select the distribution

distribution =
"Uniform"

if distribution == 'Uniform'
    raw=random('unif',0,1,[N,100000]); % uniform between 0 and 1
elseif distribution == 'Exponential'
    raw=random('exp',1,[N,100000]); % exponential with mean=1
elseif distribution == 'Student's t with nu=3'
    raw=random('t',3,[N,100000]); % Student t with nu=3
end
```

Now all we need to do is to sum over the N random numbers in each row of the array `raw` and fill these number into a histogram and display it, after annotating the axes and calculating the mean and rms of the histogram.

```
data=sum(raw,1); % sum over the first index
histogram(data)
title(['mean = ',num2str(mean(data)), '    rms = ',num2str(std(data))]);
legend(distribution)
```



Explore how the mean and the rms change when increasing N for some distributions, but not others. Check out the discussion in Section 9.7 for guidance.