

# CharFunTool User Guide

## The Characteristic Functions Toolbox for MATLAB

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**Edited by: Viktor Witkovsky**

**CharfunTool was created in January 2017 by:**

**Viktor Witkovsky**

**and is continuously developing with help of the (still growing) CharFunTool Development Team**

**Current members:**

**Viktor Witkovsky, Geza Wimmer, Tomas Duby, Andrej Gajdoš, Jozef Hanč**

**Former members: Ľudmila Šimková**



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For more information, write to [witkovsky@gmail.com](mailto:witkovsky@gmail.com).

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## Preface

This guide is an introduction to the use of CharFunTool, an open source software package that aims to provide repository of algorithms for computing the characteristic functions and tools for their combinations and numerical inversion.

Application of the exact statistical inference frequently leads to a non-standard probability distributions of the considered estimators or test statistics. Frequently, evaluation of the probability density function (PDF), cumulative distribution function (CDF), and/or the quantile function (QF) is possible from the characteristic function (CF).

In many important situations, derivation of the CFs is more simple than derivation of the PDFs and/or CDFs. In particular, the exact distribution of many estimators and test statistics can be structurally expressed as a linear combination or product of independent random variables with known distributions and characteristic functions as is the case for many standard multivariate test criteria. However, analytical inversion of the characteristic function (if possible) frequently leads to complicated expressions of the corresponding distribution functions, CDF/PDF and the required quantiles.

As we shall illustrate here, for many applications, the method based on simple implementation of the numerical inversion of the characteristic functions is fully sufficient.

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Viktor Witkovsky

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## CharFunTool: The Characteristic Functions Toolbox

The Characteristic Functions Toolbox (CharFunTool) is a MATLAB repository of characteristic functions and tools for their combinations and numerical inversion.

CharFunTool consists of a set of algorithms for evaluating selected characteristic functions and algorithms for numerical inversion of the combined and/or compound characteristic functions, used to evaluate the cumulative distribution function (CDF), the probability density function (PDF), and/or the quantile function (QF).

## Installation

To install, you can either clone the directory with Git or download a .zip file.

- Option 1: Download .zip file

Download a .zip of CharFunTool from

## Inversion algorithms

The toolbox comprises different inversion algorithms, including those based on simple trapezoidal quadrature rule for computing the integrals defined by the Gil-Pelaez formulae, and/or based on using the FFT algorithm for computing the Fourier transform integrals.

### Algorithms for numerical inversion of the characteristic functions

**cf2DistBV**

**cf2DistFFT**

**cf2DistGP**

## Repository of characteristic functions

CharFunTool consists of a set of algorithms for evaluating selected characteristic functions and algorithms for numerical inversion of the combined and/or compound characteristic functions,

### Characteristic functions of general probability distributions

**cf\_ArcsineSymmetric**

cf\_ArcsineSymmetric evaluates the characteristic function of a linear combination (resp. convolution) of independent zero-mean symmetric ARCSINE random variables defined on the interval  $(-1, 1)$ .

**cf\_Beta**

**cf\_BetaNC**

**cf\_BetaSymmetric**

**cf\_Chi**

**cf\_ChiNC**

**cf\_ChiSquare**

**cf\_Exponential**

**cf\_FisherSnedecor**

**cf\_FisherSnedecorNC**

cf\_Gamma  
cf\_GeneralizedExponential  
cf\_Gumbel  
cf\_InverseGamma  
cf\_Laplace  
cf\_MaxwellBoltzmann  
cf\_MaxwellBoltzmannNC  
cf\_Nakagami  
cf\_NakagamiNC  
cf\_Normal  
cf\_Rayleigh  
cf\_RayleighNC  
cf\_Rectangular  
cf\_RectangularSymmetric  
cf\_Rice  
cf\_Stable  
cf\_Student  
cf\_TrapezoidalSymmetric  
cf\_TriangularSymmetric  
cf\_TSPSymmetric  
cf\_Weibull  
cf\_WignerSemicircle

## **Tools for manipulating with the characteristic function**

CharFunTool consists of a set of algorithms for manipulating and combining the characteristic functions.

## **Utility functions**