uc3m Universidad Carlos III de Madrid

Grado en Ingeniería Informática 2019-2020

Apuntes Cálculo diferencial aplicado

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Parte I

Teoria

1. TABLA: TRANSFORMADA DE LAPLACE

1.
$$\mathcal{L}{f(t) = 1} = F(s) = \frac{1}{s}, \quad s > 0$$

2.
$$\mathcal{L}\{f(t) = e^{at}\} = F(s) = \frac{1}{s-a}, \quad s > a$$

3.
$$\mathcal{L}{f(t) = t^n} = F(s) = \frac{n!}{s^{n+1}}, \quad s > 0; n = 1, 2, 3, \dots$$

4.
$$\mathcal{L}{f(t) = \text{sen}(at)} = F(s) = \frac{a}{s^2 + a^2}, \quad s > 0$$

5.
$$\mathcal{L}{f(t) = \cos(at)} = F(s) = \frac{s}{s^2 + a^2}, \quad s > 0$$

6.
$$\mathcal{L}{f(t) = e^{at} \operatorname{sen}(bt)} = F(s) = \frac{b}{(s-a)^2 + b^2}, \quad s > a$$

7.
$$\mathcal{L}\{f(t) = e^{at}\cos(bt)\} = F(s) = \frac{s-a}{(s-a)^2+b^2}, \quad s > a$$

8.
$$\mathcal{L}{f(t) = t^n e^{at}} = F(s) = \frac{n!}{(s-a)^{n+1}}, \quad s > a; n = 1, 2, 3, \dots$$

9.
$$\mathcal{L}{f(t) = \text{senh}(at)} = F(s) = \frac{a}{s^2 - a^2}, \quad s > |a|$$

10.
$$\mathcal{L}{f(t) = \cosh(at)} = F(s) = \frac{s}{s^2 - a^2}, \quad s > |a|$$

11.
$$\mathcal{L}\left\{(f * g)(t) = \int_0^t f(t - \alpha)g(\alpha)d\alpha\right\} = \int_0^t f(\alpha)g(t - \alpha)d\alpha\right\} = \mathcal{L}\left\{f(t)\right\}\mathcal{L}\left\{g(t)\right\}$$

12.
$$\mathcal{L}\left\{f^{(n)}(t)\right\} = s^n F(s) - s^{n-1} f(0) - s^{(n-2)} f'(0) - \dots - f^{(n-1)}(0); \quad F(s) = \mathcal{L}\left\{f(t)\right\}$$