



Geophysical Research Letters

## *Supporting Information for*

# **Imaging the Hydrothermal System of Kirishima Volcanic Complex, Japan with L-band InSAR Time Series**

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## Introduction

*Table S1 summarizes the used satellite SAR data information and configurations used in the stack processing. Table S2 summarizes the impact of the minimum free surface height on the fitted source parameters. Table S3 lists the configurations used for parameter optimization of the modeling. Table S4 lists the parameter of the optimal solution from geodetic modeling and their 95% confidence intervals.*

21       *Fig. S1 shows the network configuration of interferometric pairs used in the stack*  
22    *processing. Fig. S2-S4 show the temporal coherence, estimated DEM errors and noise level in terms*  
23    *of residual phase root mean squares of the InSAR time series analysis.*

24       *Fig. S5-S8 show the displacement time-series of the Kirishima volcanic complex from the*  
25    *four orbits (ALOS and ALOS-2, ascending and descending) in the line-of-sight direction after all the*  
26    *phase corrections. Fig. S9-S10 show the displacement time-series of the Shinmoe-dake crater from*  
27    *ALOS-2 ascending and descending orbits estimated without interferograms after the 2017*  
28    *Shinmoe-dake eruption.*

29       *Fig. S11 demonstrates the impact of the two extra steps after the MintPy routine workflow*  
30    *on the displacement estimation for time periods of interest. Fig. S12 shows the thickness of the lava*  
31    *dome extruded from the 2011 Shinmoe-dake eruption estimated using the DEM error.*

32       *Fig. S13-S15 show displacement map of Kirishima during the three representative time*  
33    *periods from ascending/descending and their decomposition in quasi-horizontal/vertical direction.*

34       *Fig. S16 shows the displacement due to ash/tephra deposition from the 2017 Shinmoe-dake*  
35    *eruption. Fig. S17 shows the pre-eruptive inflation, co-eruptive deflation and ash/tephra deposition*  
36    *from the 2011 Shinmoe-dake eruption.*

37       *Fig. S18-S19 show the subsampling result of InSAR displacement as the input of geodetic*  
38    *modeling. Fig. S20-S23 show the joint probability density distribution among all free parameters of*  
39    *the geodetic modeling. Fig. S24 shows the residual between the observed and predicted*  
40    *displacement from geodetic modeling for the expanded inflation at Iwo-yama after Dec 2017.*

41

<i>Satellite</i>	<i>ALOS</i>		<i>ALOS-2</i>	
<i>Orbit direction</i>	<i>ascending</i>	<i>descending</i>	<i>ascending</i>	<i>descending</i>
<i>Track</i>	424	73	131	23
<i>Frame</i>	620-630	2970-2980	620	2970
<i>Start date</i>	2006-06-24	2007-01-07	2014-09-30	2015-02-09
<i>End date</i>	2011-04-07	2011-04-20	2019-07-02	2019-08-19
<i>Number of acquisitions</i>	29	21	36	49
<i>Number of interferograms</i>	225	115	204	341
<i>Max perpendicular baseline [m]</i>	1800	1800	200	200
<i>Max temporal baseline [day]</i>	1800	1800	400	400
<i># of looks in range direction</i>	4	4	8	8
<i># of looks in azimuth direction</i>	10	10	10	10
<i>power spectral filter strength (Goldstein &amp; Werner, 1998)</i>	0.5	0.5	0.5	0.5

42      **Table S1.** SAR dataset information with parameters used in InSAR stack processing. To form the  
 43      ALOS interferograms, we oversample the SAR images which are acquired in fine beam dual-  
 44      polarization mode with 14 MHz bandwidth to 28 MHz, the bandwidth of fine beam single  
 45      polarization mode.

46

Finite sphere (McTigue, 1987)								
Min free surface hgt. (MFSH) [m]	Points below MFSH		Latitude [°]	Longitude [°]	Depth [m]	Radius [m]	$\Delta P/\mu$ [10 <sup>-2</sup> ]	$\Delta V$ [10 <sup>3</sup> m <sup>3</sup> ]
	Perc.	Height incr. [m] avg. [min, max]						
None	0%	0	31.9469 ± 0.0001	130.8531 ± 0.0001	150 (1162) ± 10	40 <sup>#</sup> ± 7	4.3 ± 1.7	8.7 ± 1.1
1250	11%	49 [0, 237]	31.9469 ± 0.0001	130.8531 ± 0.0001	150 (1162) ± 10	40 <sup>#</sup> ± 8	<b>4.4<sup>#</sup></b> ± 1.9	<b>8.8</b> ± 1.1
1300	59%	32 [0, 287]	<b>31.9468</b> ± 0.0001	130.8531 ± 0.0001	<b>165 (1148)</b> ± 10	40 <sup>#</sup> ± 17	<b>5.7<sup>#</sup></b> ± 5.5	<b>11.8</b> ± 1.5

CDM (Nikkhoo et al., 2016)											
MFSH [m]	Latitude [°]	Longitude [°]	Depth [m]	$\omega_x$ [°]	$\omega_y$ [°]	$\omega_z$ [°]	$a_x$ [m]	$a_y/a_x$	$a_z/a_x$	opening [m]	$\Delta V$ [10 <sup>3</sup> m <sup>3</sup> ]
1250	31.9470 ± 0.0001	130.8532 ± 0.0001	130 (1184) ± 10	5 ± 2	-8 ± 2	0 <sup>fix</sup> ± 2	60 ± 10	1.2 ± 0.4	1.0 ± 0.2	0.28 ± 0.10	13 ± 2
1300	31.9470 ± 0.0001	130.8532 ± 0.0001	<b>130 (1181)</b> ± 10	5 ± 2	-8 ± 2	0 <sup>fix</sup> ± 2	60 ± 10	1.2 ± 0.3	<b>1.1</b> ± 0.2	<b>0.30</b> ± 0.08	<b>15</b> ± 2

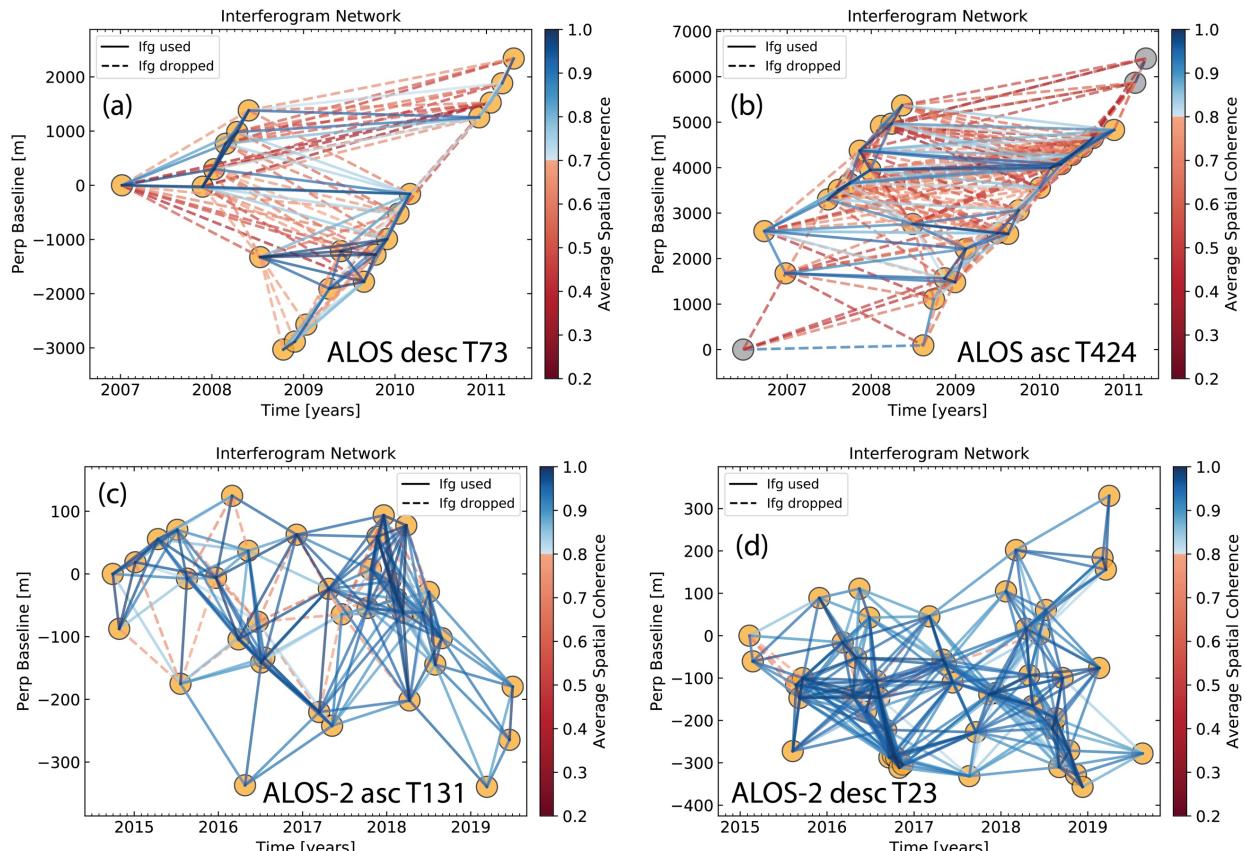
47 **Table S2.** Impact of the minimum free surface height (MFSH) constraint on the source parameter  
48 estimation at Iwo-yama during 2015-2017 (Fig. 2k-o). We use both the finite sphere model (McTigue,  
49 1987; does not require positive depths) and the CDM solution (Nikkhoo et al., 2016; do require  
50 positive depths) with different MFSH settings. Differences are highlighted in bold. Check Table S4 for  
51 detailed explanation of parameters and equations for volume change. Conclusions are: **1)** Between  
52 the finite sphere results without MFSH and with MFSH of 1250 m, the difference is negligible due to  
53 the low percentage (11%) of affected data points. Thus, we expect negligible impact at Shinmoe-  
54 dake during 2008-2010 and during 2015-2017 due to the similar low percentage (<=12%) and far-  
55 field locations (Fig. S18) of affected data points. **2)** Considering the similar CDM results with MFSH  
56 of 1250 m and of 1300 m, we conclude the impact of MFSH is negligible for Iwo-yama during 2015-  
57 2017. **3)** Comparing the finite sphere results without MFSH and with MFSH of 1300 m, the depth  
58 increase (15 m) is much smaller than the average height increase (32 m). Similarly, for Iwo-yama  
59 during 2015-2017 with the average height increase of 56 m for 77% of the data points (Fig. S19), we  
60 except less than 56 m of estimated depth increase, which is well within the reported 95% confidence  
61 interval of 100 m.

Shinmoe-dake					
		2008-2010		2015-2017	
		ascending	descending	ascending	descending
<i>Reference point [°]</i>		[130.88; 31.91]			
<i>Bounding box in WNES [°]</i>		[130.85; 31.94; 130.91; 31.88]			
<i>Remove constant offset</i>		yes		yes	
<i>Remove ramp</i>		no		no	
<i>Structural function</i>	<i>sill [m<sup>2</sup>]</i>	3.7e-05	2.8e-05	5.0e-05	4.4e-05
	<i>range [m]</i>	1300	2100	1460	940
	<i>nugget [m]</i>	1.1e-06	6.7e-06	6.8e-06	7.3e-06
<i>Quadtree sampling</i>	<i>max var [m<sup>2</sup>]</i>	0.002 <sup>2</sup>	0.0025 <sup>2</sup>	0.0035 <sup>2</sup>	0.0035 <sup>2</sup>
	<i>end level</i>	15	15	7	7
	<i>min pixel #</i>	3	3	15	15
	<i>WNES [°]</i>	[130.865; 31.925; 130.900; 31.900]		[130.865; 31.925; 130.900; 31.900]	
<i>Grid sampling</i>	<i>step [m]</i>	750		1500	
<i>min free surface height [m]</i>		1100		1100	
Iwo-yama					
		2015-2017		2017-2019	
		ascending	descending	ascending	descending
<i>Reference point [°]</i>		[130.853; 31.947]			
<i>Bounding box in WNES [°]</i>		[130.832; 31.960; 130.870; 31.935]			
<i>Remove constant offset</i>		yes		yes	
<i>Remove ramp</i>		no		yes	
<i>Structural function</i>	<i>sill [m<sup>2</sup>]</i>	3.6e-05	3.1e-05	9.5e-05	13e-05
	<i>range [m]</i>	1060	860	1800	2100
	<i>nugget [m]</i>	8.0e-06	6.7e-06	5.9e-06	6.6e-07
<i>Quadtree sampling</i>	<i>max var [m<sup>2</sup>]</i>	0.006 <sup>2</sup>	0.0075 <sup>2</sup>	0.0045 <sup>2</sup>	0.0040 <sup>2</sup>
	<i>end level</i>	15	15	9	9
	<i>min pixel #</i>	1	1	2	2
	<i>WNES [°]</i>	[130.842; 31.954; 130.862; 31.941]		[130.840; 31.954; 130.862; 31.940]	
<i>Grid sampling</i>	<i>step [m]</i>	600		600	
<i>min free surface height [m]</i>		1300		1300	

- 62 **Table S3.** Configurations for parameters optimization used in the GBIS software. Related to section  
 63 6. Sill, range and nugget are the three parameters used to describe the exponential fit to the  
 64 experimental variogram calculated from the InSAR observation.

Time period	Latitude [°]	Longitude [°]	Depth [m]	$\omega_X$	$\omega_Y$	$\omega_Z$	$a_X$	$a_Y/a_X$	$a_Z/a_X$	opening [m]	$\Delta V$ [ $10^3 m^3$ ]	Source shape
<i>Shinmoe-dake (1,421 m a.s.l.)</i>												
2008-2010	31.9125 ± 0.0006	130.8845 ± 0.0004	620 (800) ± 50	-19 ± 12	12 ± 9	18 ± 15	190 ± 80	0.8 ± 0.7	1.4 ± 0.7	-0.26 ± 0.15	-124 ± 26	prolate ellipsoid
2015- 2017	31.9111 ± 0.0011	130.8828 ± 0.0013	730 (693) ± 210	0 <sup>fix</sup>	0 <sup>fix</sup>	0 <sup>fix</sup>	200 <sup>#</sup> ± 100	1 <sup>fix</sup>	1 <sup>fix</sup>	0.30 ± 0.19	146 ± 95	sphere
<i>Iwo-yama (1,313 m a.s.l.)</i>												
2015- 2017	31.9470 ± 0.0001	130.8532 ± 0.0001	130 (1181) ± 10	5 ± 2	-8 ± 2	0 <sup>fix</sup>	60 ± 10	1.2 ± 0.5	1.1 ± 0.2	0.30 ± 0.08	15 ± 2	sphere
2017-2019	31.9464 ± 0.0003	130.8530 ± 0.0002	340 (970) ± 100	0 <sup>fix</sup>	0 <sup>fix</sup>	0 <sup>fix</sup>	380 ± 80	0.3 ± 0.3	0.2 ± 0.4	0.16 <sup>#</sup> + 0.14 ± 0.08	76 ± 39	sphere + horizontal cigar

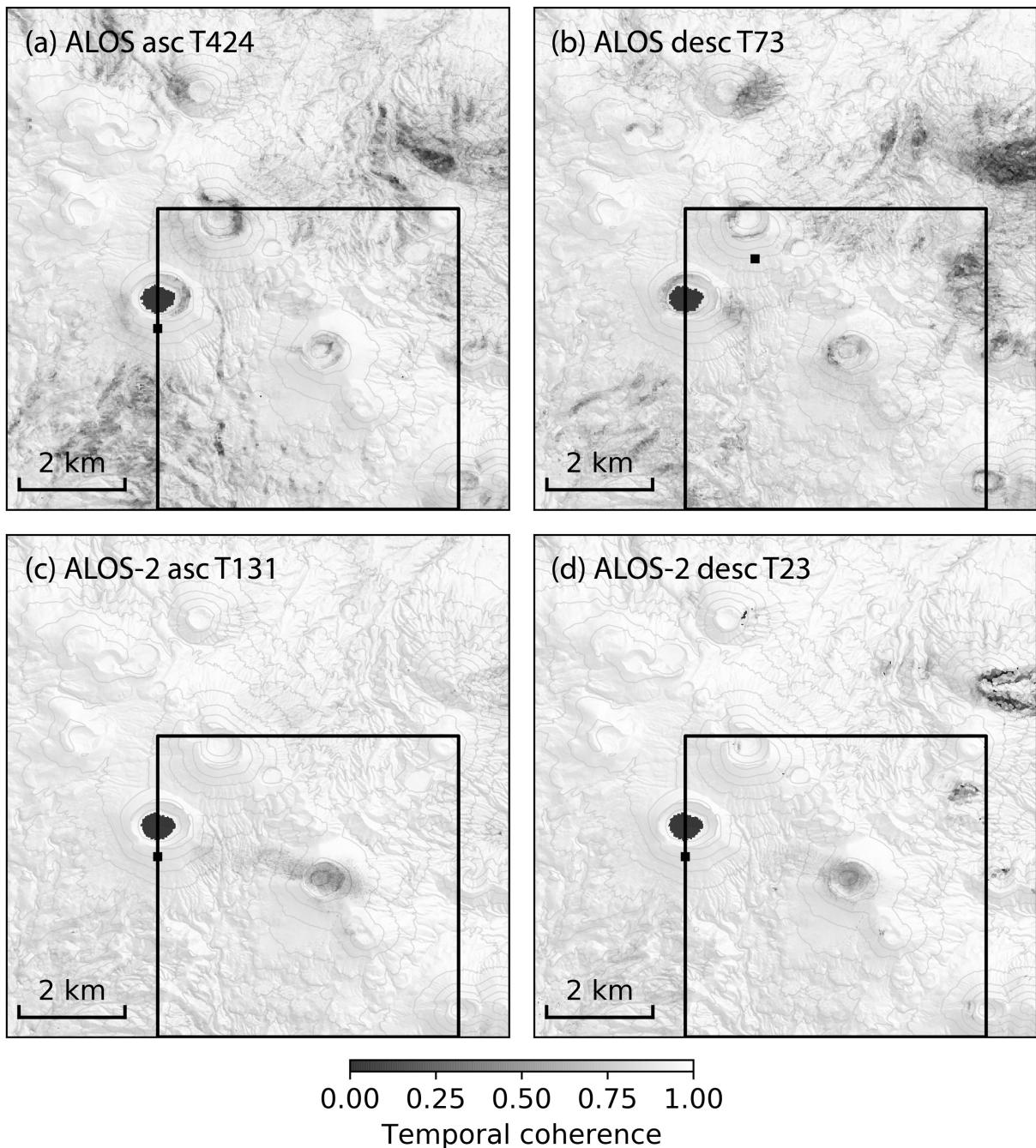
65     **Table S4.** Parameters of the CDM models for two periods at Shinmoe-dake and Iwo-yama as given  
66     by the maximum *a posteriori* probability solution with 95% confidence intervals. Depth of the model  
67     centroid is reported as below the summit (rounded to the nearest 10 m; and above the mean sea  
68     level).  $\omega_i$  and  $a_i$ ,  $i = X, Y, Z$  are the rotation angle (rounded to the nearest 1°; positive for clockwise)  
69     and length of the semi-axis along the  $i$ -axis (rounded to the nearest 10 m), respectively. Opening is  
70     the uniform opening on all three segments.  $\Delta V$  is the cavity volume change in  $10^3 m^3$  with:  $\Delta V = 4 \cdot$   
71      $(a_X a_Y + a_Y a_Z + a_X a_Z) \cdot \mu$  for the CDM (Nikkhoo et al., 2016) and  $\Delta V = \Delta P / \mu \cdot \pi r^3$  for the finite  
72     sphere (McTigue, 1987), where  $\mu$  is the opening and  $r$  is the radius. <sup>#</sup>not-converged parameters.  
73



74

75 **Figure S1.** Network configurations of interferograms stacks. Line colors represent the average  
 76 spatial coherence of the interferogram calculated over the area of interest around Shinmoe-dake  
 77 (marked by black squares in Fig. S2). Dashed lines represent the interferograms excluded during the  
 78 time-series analysis due to low coherence.

79

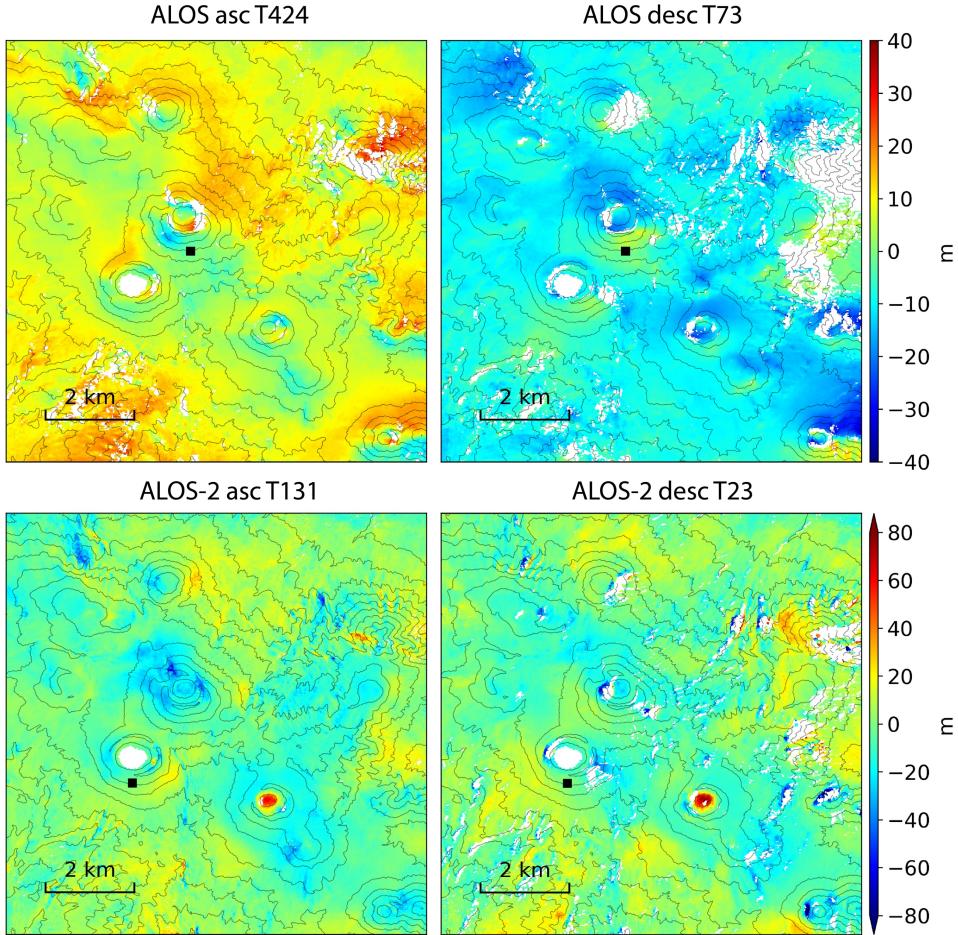


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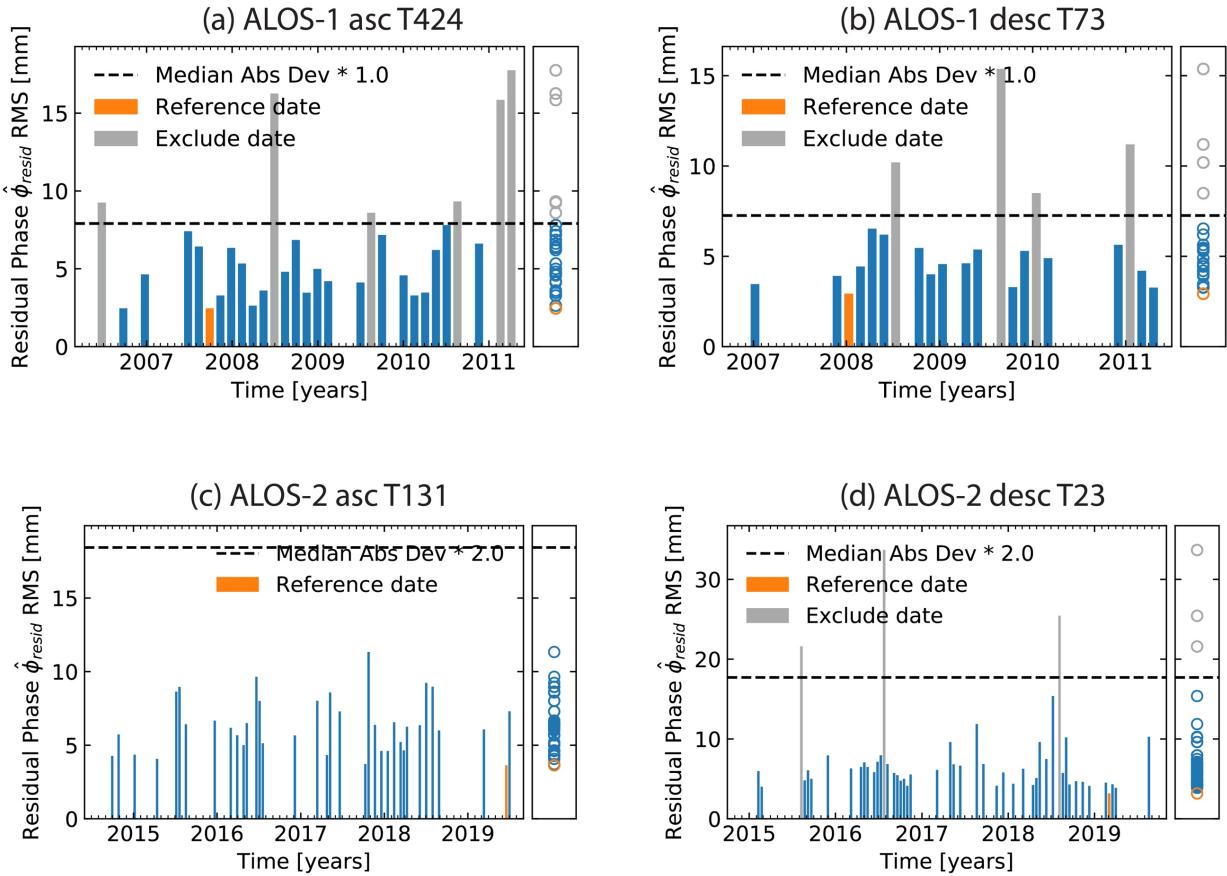
81 **Figure S2.** Temporal coherence of all four datasets from the routine MintPy workflow. Black  
82 squares: the custom area of interest used for the coherence-based network modification (Fig. S1).

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84

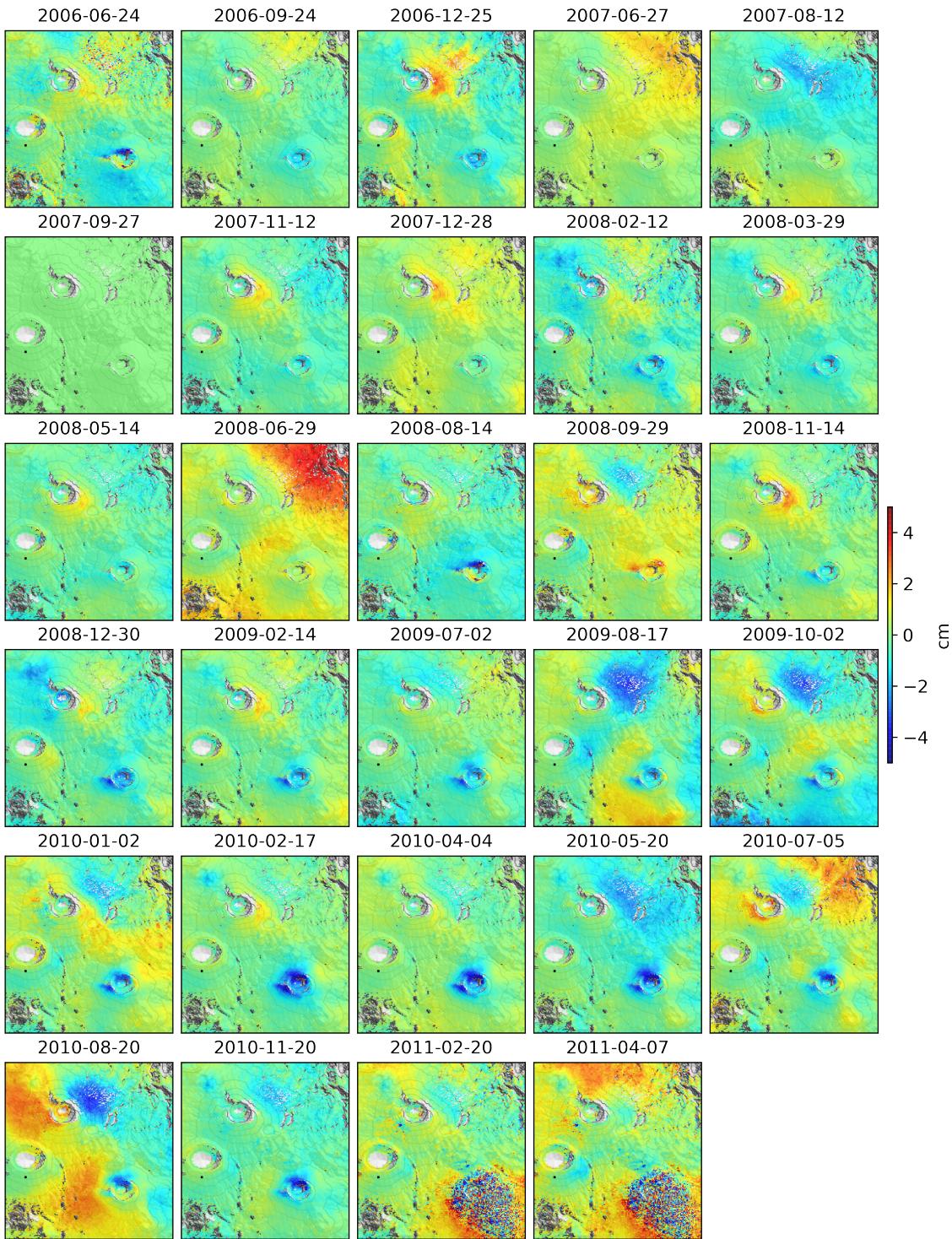


85 **Figure S3.** Estimated DEM error of all four datasets based on the method by Fattah & Amelung  
 86 (2013) from acquisitions before the 2011 and 2017 eruptions. Black squares: reference points.  
 87 Contour lines in every 100 m. In the ALOS-2 estimates, the 60-80 m DEM error at Shinmoe-dake  
 88 crater represents the lava dome generated from the 2011 eruption. In the ALOS estimates, the  
 89 opposite sign of the DEM error (+/- 10 m on average) between the ascending and descending orbits  
 90 reflects a horizontal shift between the coregistered SLC stack and the DEM. Since the same DEM is  
 91 used for all datasets and the ALOS-2 estimates are normal as expected, we believe this horizontal  
 92 shift is originated from the ALOS coregistered SLC stack due to improper geometry handling of the  
 93 ISCE-2 software during SAR focusing. Possible causes include inaccurate starting range re-  
 94 estimation during the range padding of the native-doppler focusing, inaccurate time tag (only to  
 95 the closest millisecond), assumption in the focusing of no hidden offset in azimuth, transmit and  
 96 receive time misuse. Nevertheless, this shift should not affect the displacement time-series after the  
 97 DEM error correction.



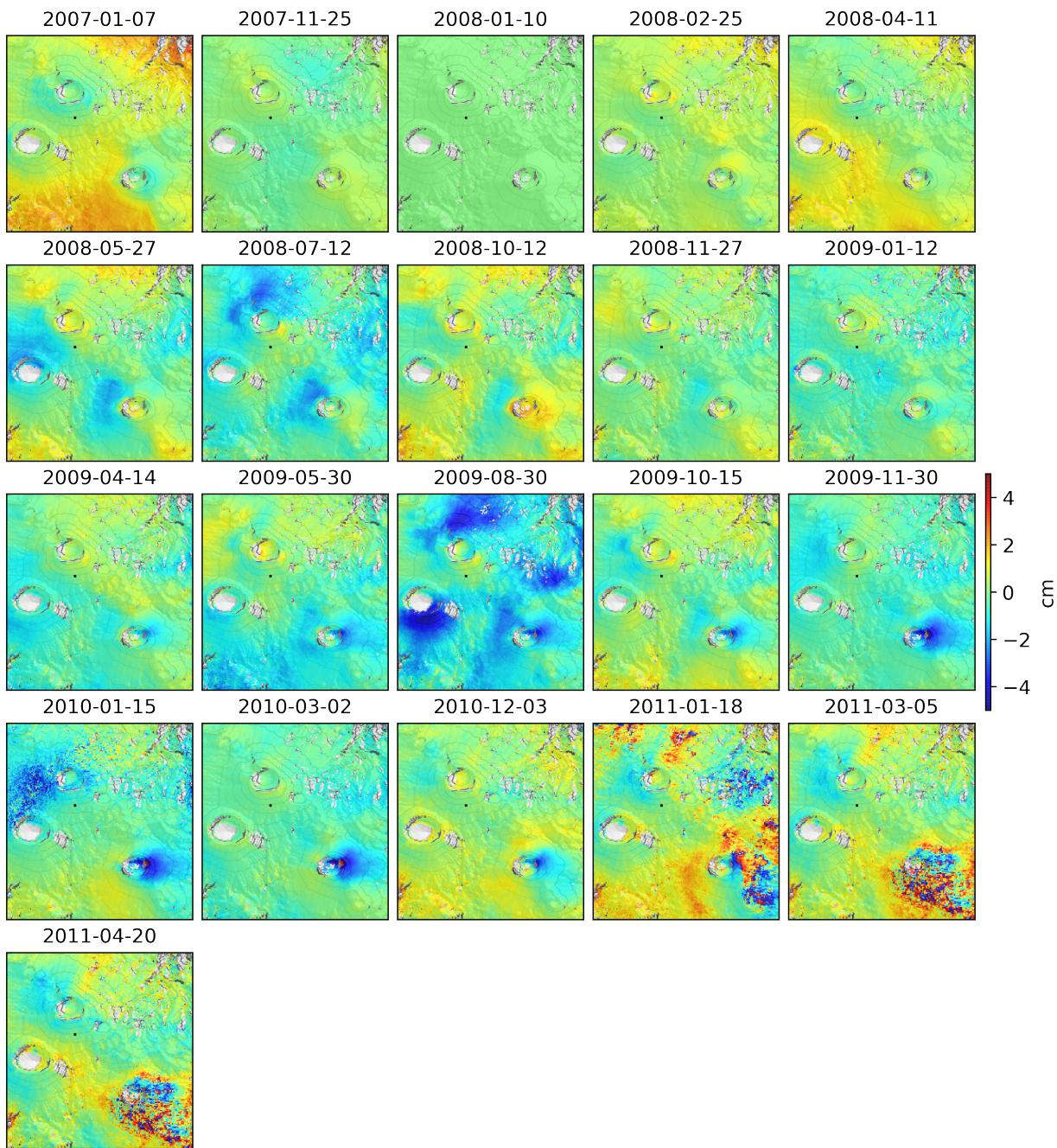
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99 **Figure S4.** Residual phase root mean squares (RMS) time-series with noisy acquisitions. The orange  
100 bar indicates the acquisition with minimum residual phase RMS and the optimal reference date for  
101 each dataset. The gray bars indicate acquisitions with residual phase RMS larger than the  
102 predefined threshold (dashed black lines), thus, considered as noisy and excluded during the  
103 average velocity estimation.



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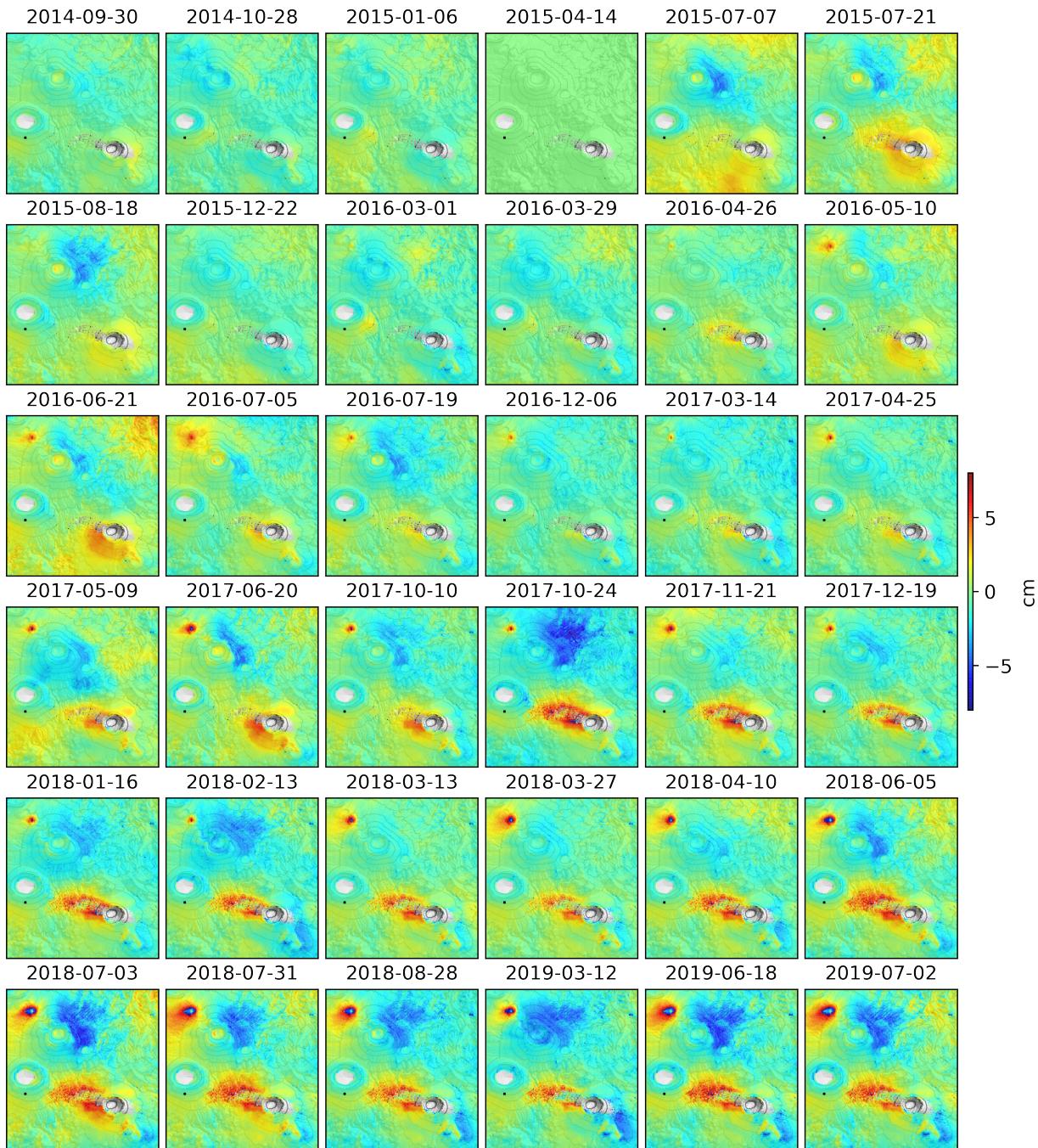
105 **Figure S5.** LOS displacement time-series of Kirishima from ALOS ascending track 424. Positive  
106 value for motion toward the satellite. Data are wrapped into [-5, 5) cm for display. Black squares:  
107 reference points. Contour lines in every 100 m.



108

109 **Figure S6.** LOS displacement time-series of Kirishima from ALOS descending track 73. Positive  
 110 value for motion toward the satellite. Data are wrapped into [-5, 5) cm for display. Black squares:  
 111 reference points. Contour lines in every 100 m.

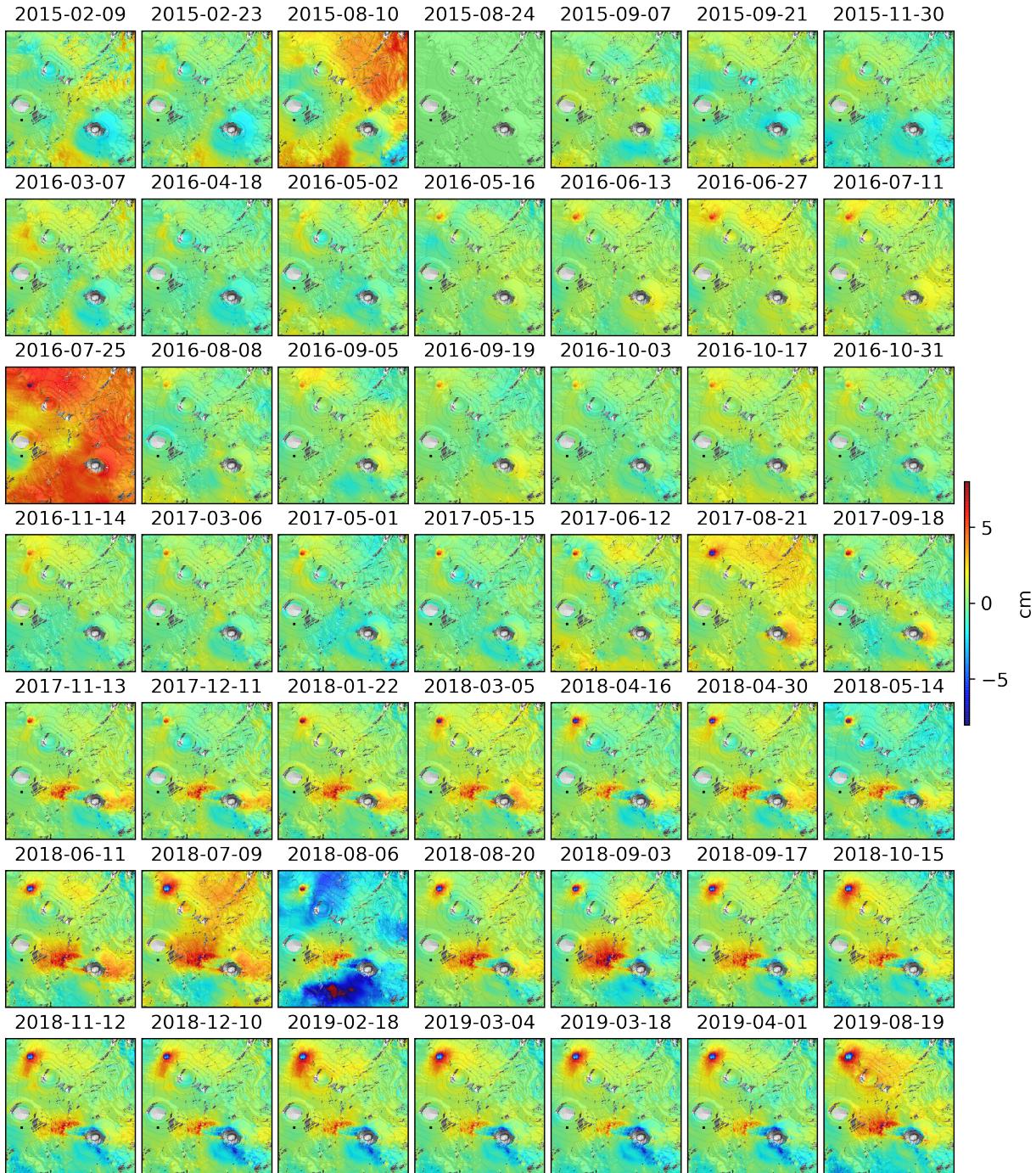
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113

114 **Figure S7.** LOS displacement time-series of Kirishima from ALOS-2 ascending track 131. Positive  
 115 value for motion toward the satellite. Data are wrapped into [-8, 8) cm for display. Black squares:  
 116 reference points. Contour lines in every 100 m.

117



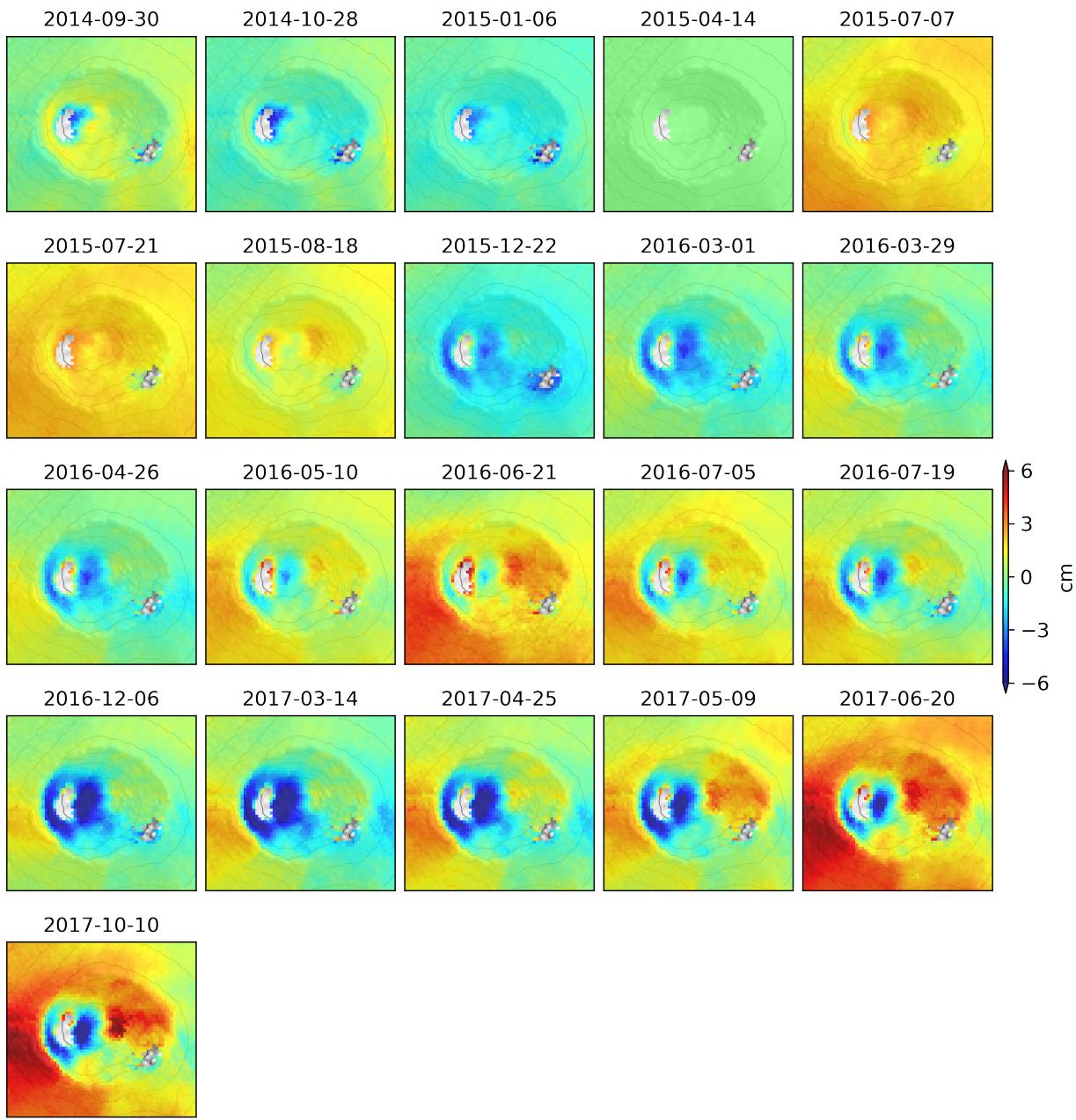
118

119 **Figure S8.** LOS displacement time-series of Kirishima from ALOS-2 descending track 23. Positive

120 value for motion toward the satellite. Data are wrapped into [-8, 8) cm for display. Black squares:

121 reference points. Contour lines in every 100 m.

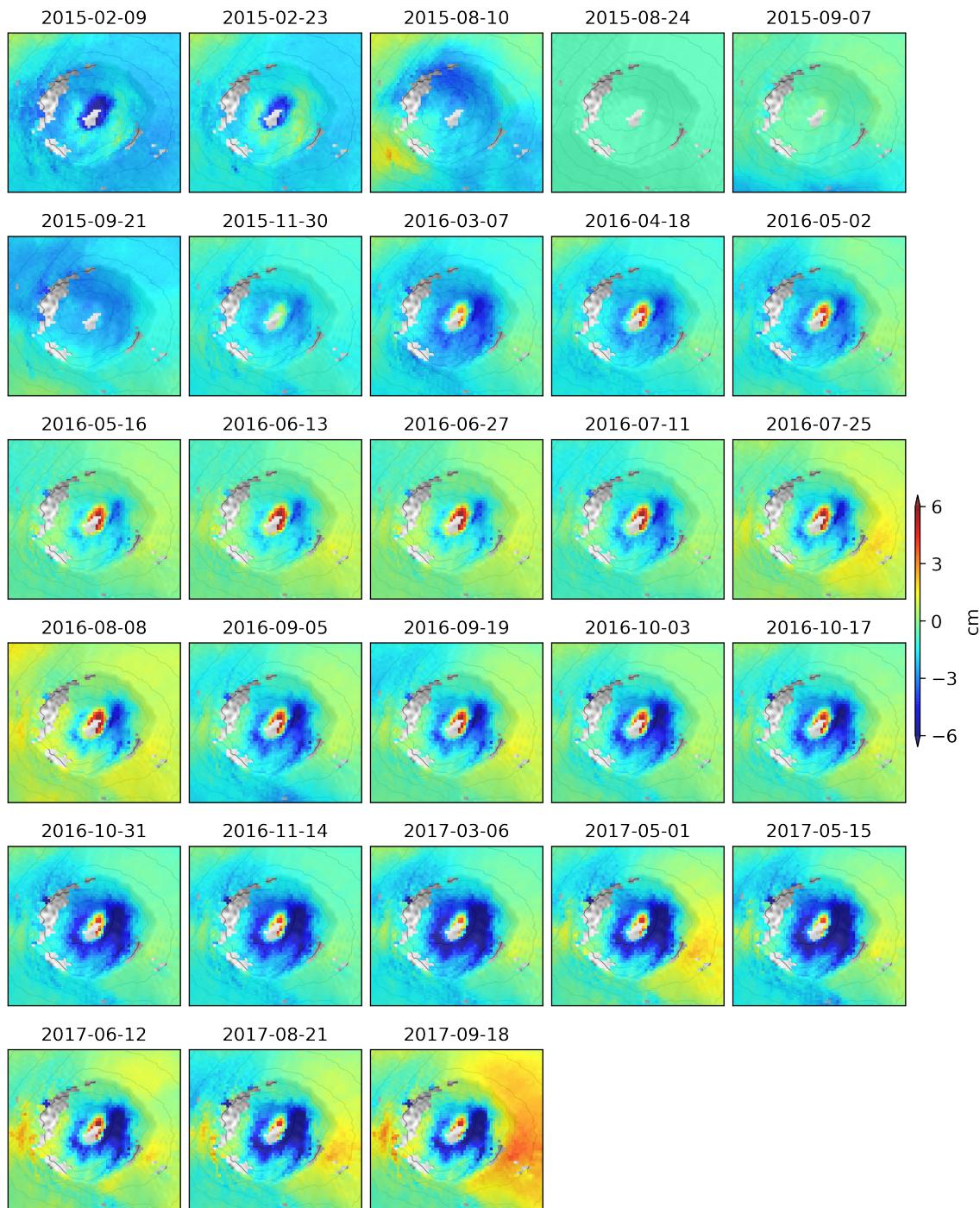
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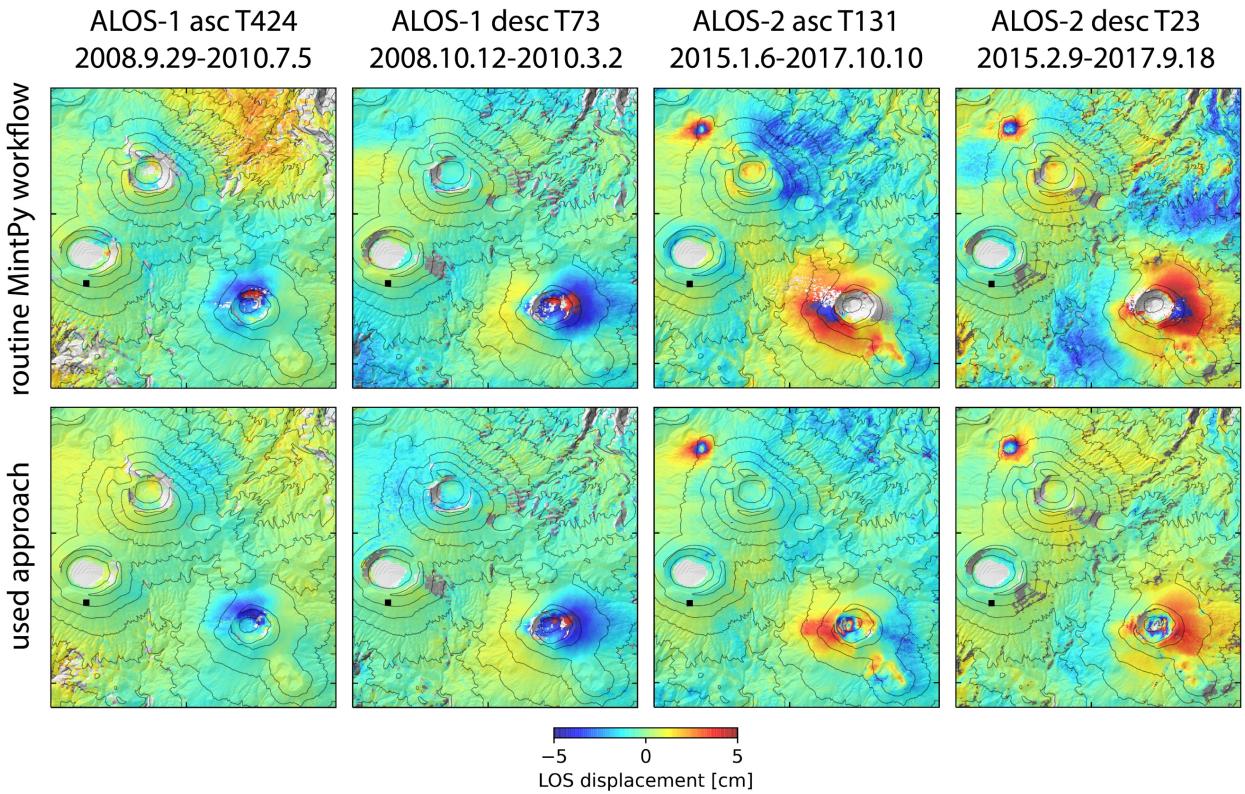
124 **Figure S9.** LOS displacement time-series of Shinmoe-dake crater [ $E130.877^\circ$  -  $E130.889^\circ$ ,  $N31.906^\circ$   
125 -  $N31.917^\circ$ ] before the October 2017 eruption from ALOS-2 ascending track 131. Positive value for  
126 motion toward the satellite. Contour lines in every 50 m. Reference point is outside of the map extent  
127 ( $E130.877^\circ$  -  $E130.889^\circ$ ,  $N31.906^\circ$  -  $N31.917^\circ$ ) at [ $E130.894^\circ$ ,  $N31.921^\circ$ ].

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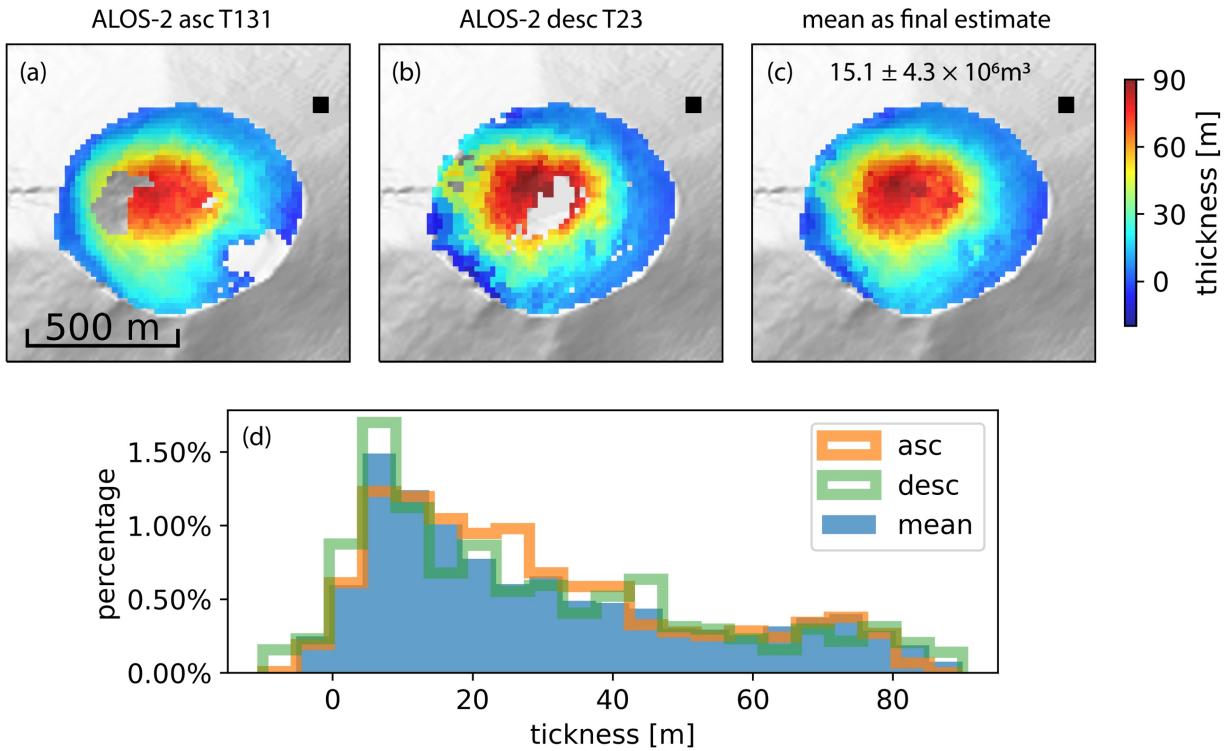
130 **Figure S10.** LOS displacement time-series of Shinmoe-dake crater before the October 2017  
 131 eruption from ALOS-2 descending track 23. Positive value for motion toward the satellite. Contour  
 132 lines in every 50 m. Reference point is outside of the map extent ( $E130.877^\circ - E130.889^\circ, N31.906^\circ -$   
 133  $N31.917^\circ$ ) at [ $E130.894^\circ, N31.921^\circ$ ].



134

135 **Figure S11.** Comparison between two approaches to estimate LOS displacements. Top panel:  
 136 differential displacements between two acquisitions from displacement time-series using the  
 137 routine MintPy workflow. Bottom panel (used approach): displacements converted from the linear  
 138 velocity of the time periods of interest, estimated from the displacement time-series after additional  
 139 network modification by excluding interferograms with acquisitions after the 2011 and 2017  
 140 eruptions. Positive value for motion toward the satellite. Contour lines in every 100 m.

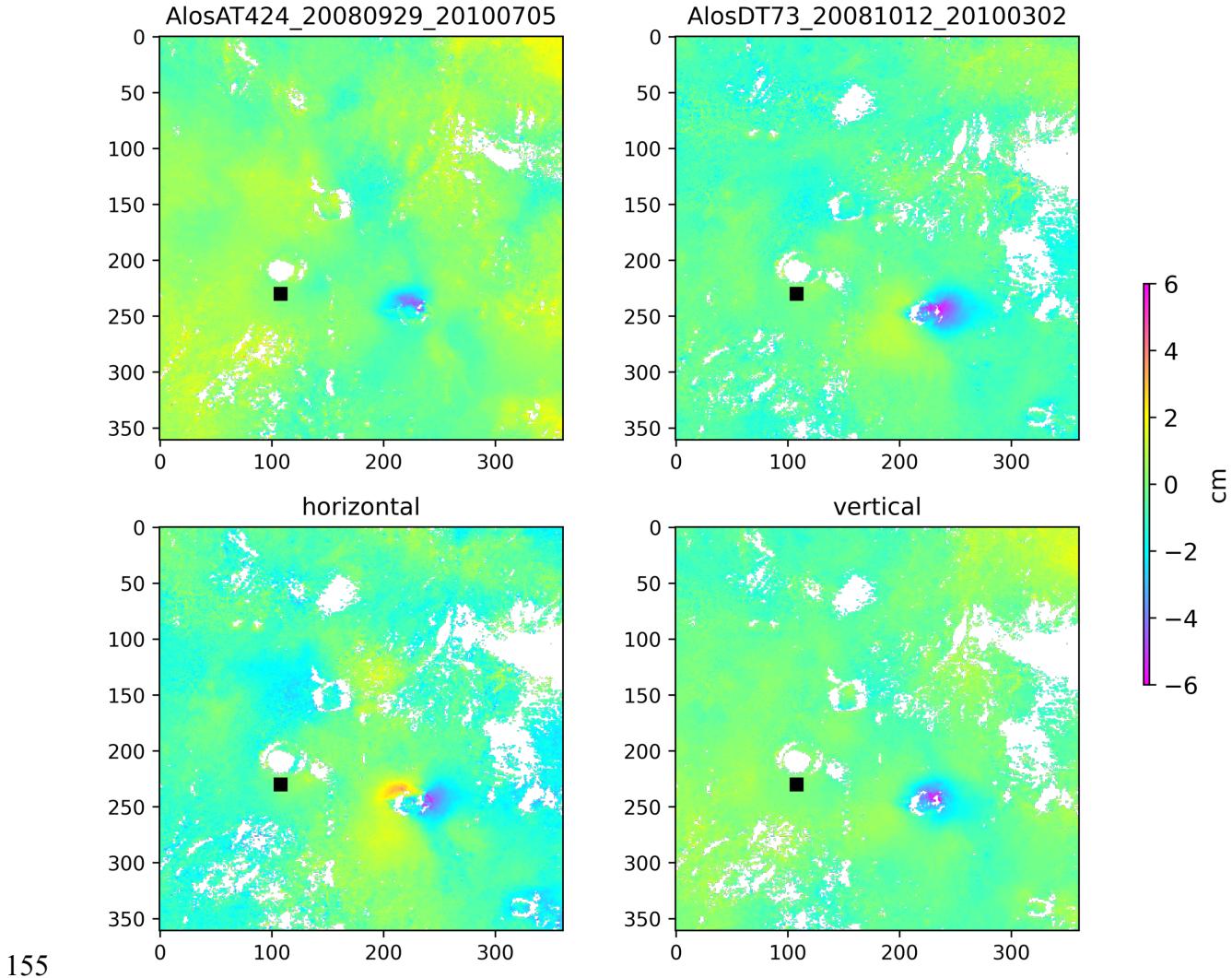
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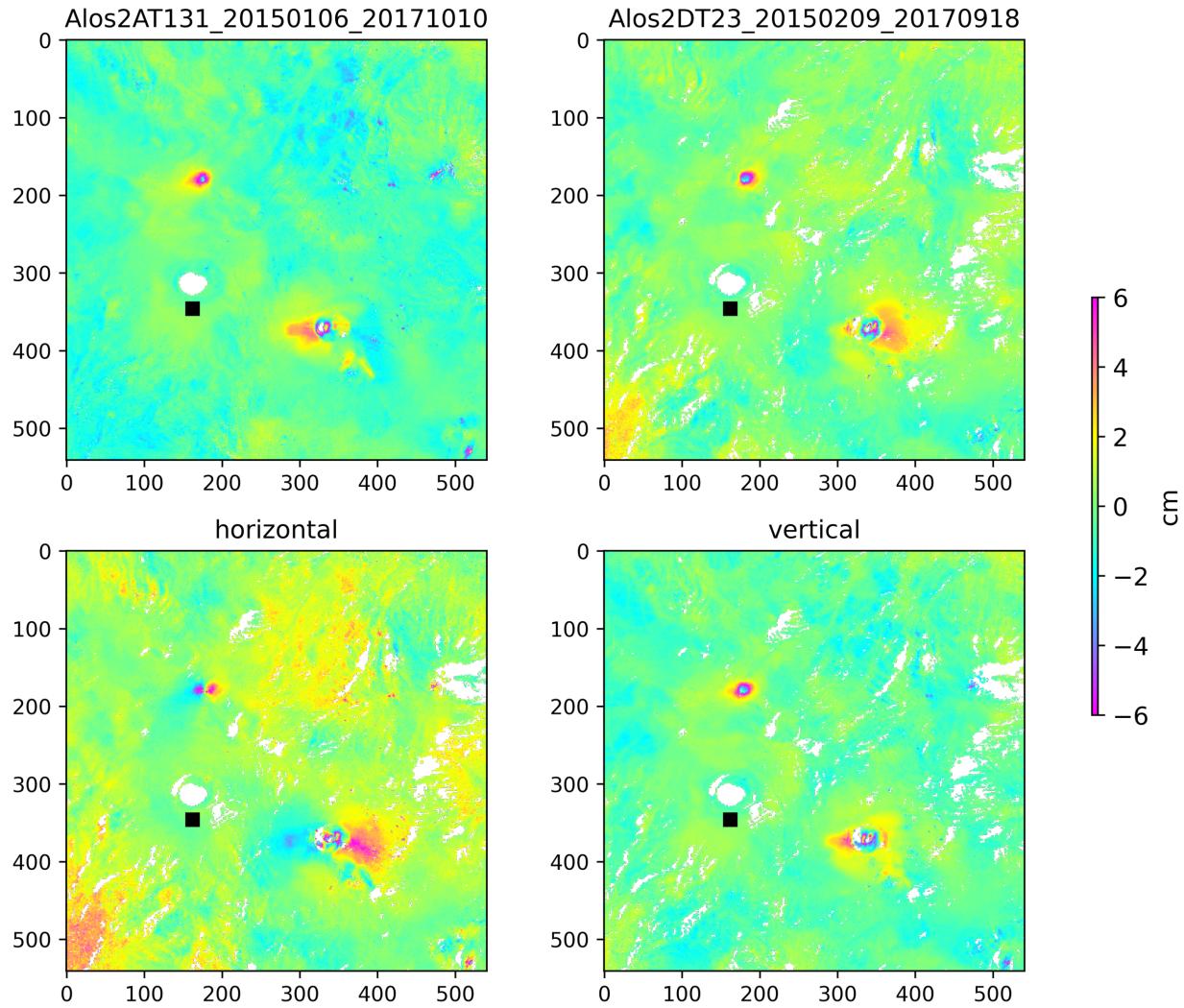
143 **Figure S12.** Lava dome thickness at the Shinmoe-dake crater due to the 2011 eruption estimated  
 144 from the ALOS-2 DEM error estimates (Fig. S3 lower panel). (a-b) Thickness estimates from ALOS-2  
 145 ascending and descending orbits, respectively. (c) Average of (a-b). (d) Histogram of (a-c). We use a  
 146 common local reference point (black square) to align the relative DEM error to the Shinmoe-dake  
 147 crater. A high temporal coherence threshold (0.95) is used to discard noisy pixels, resulting in the  
 148 masked-out areas in (a-b). Both ascending and descending estimates are used to get the mean  
 149 estimate and fill the masked-out areas. The remaining masked-out areas (4 pixels) are filled with the  
 150 nearest data. The estimated volume of the lava dome is  $15.1 \pm 4.3 \times 10^6 \text{ m}^3$  with three-sigma  
 151 intervals. This estimate is similar to Ozawa & Kozono (2013;  $15.4 \times 10^6 \text{ m}^3$ ) using SAR intensity  
 152 simulation from TerraSAR-X image of 1 February 2011, but lower than Shimono et al. (2011;  
 153  $19 \times 10^6 \text{ m}^3$ ) using single-pass SAR interferometry from airborne SAR data of 7 February 2011.

154



156 **Figure S13.** Deflation at Shinmoe-dake during the 2008-2010 eruptions. Top panel: LOS  
 157 displacement from ALOS ascending track 424 and descending track 73, respectively. Positive value  
 158 for motion toward the satellite. Bottom panel: quasi-east-west and quasi-vertical displacement  
 159 decomposed from the top panel. Positive value for motion toward the east and uplift. Data are  
 160 wrapped into [-6, 6) cm for display. Related to Fig. 1d.

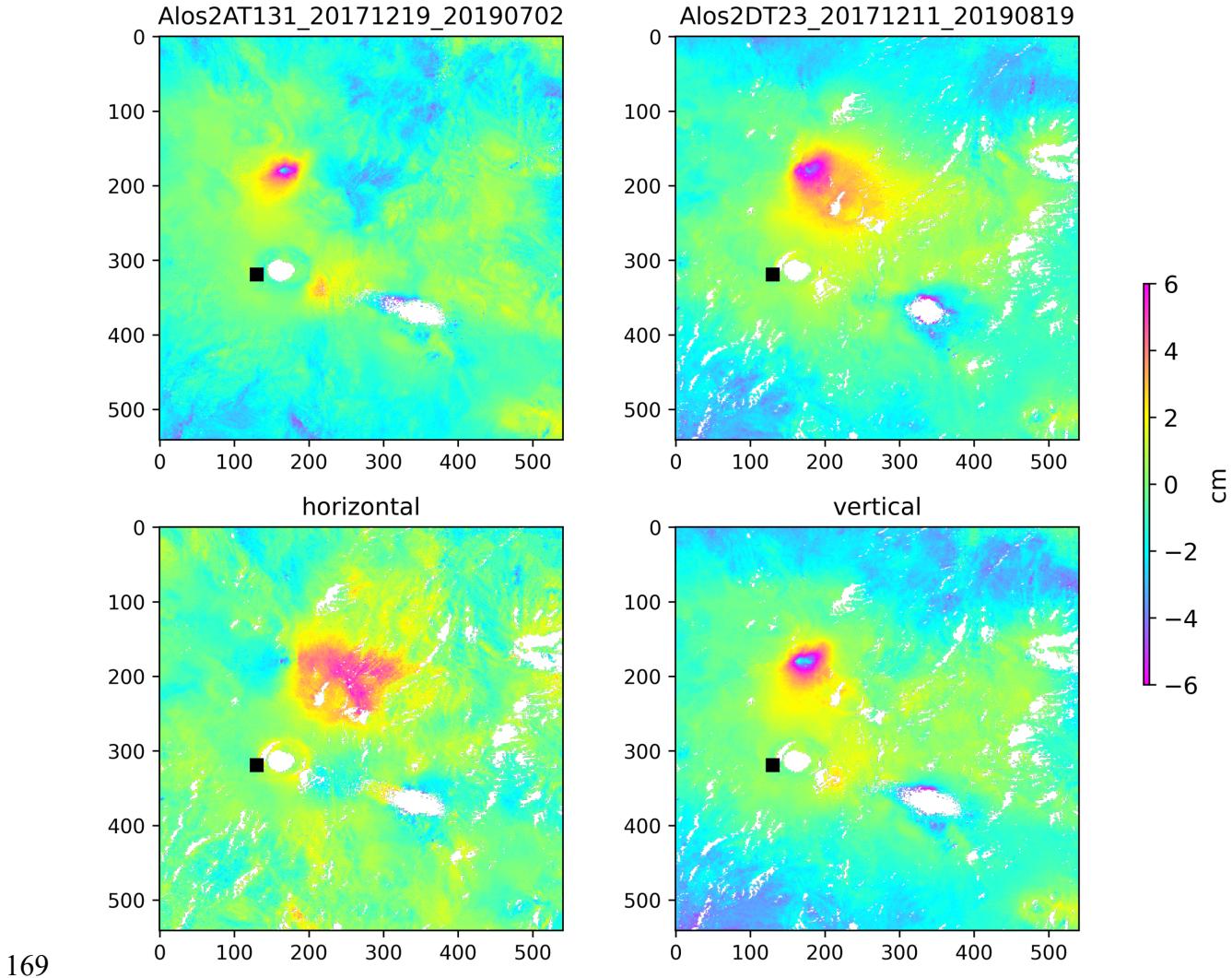
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162

163 **Figure S14.** Inflation at Shinmoe-dake and Iwo-yama before the October 2017 eruption. Top panel:  
 164 LOS displacement from ALOS-2 ascending track 131 and descending track 23, respectively. Positive  
 165 value for motion toward the satellite Bottom panel: quasi-east-west and quasi-vertical  
 166 displacement decomposed from the top panel. Positive value for motion toward the east and uplift.  
 167 Data are wrapped into [-6, 6) cm for display. Related to Fig. 1e.

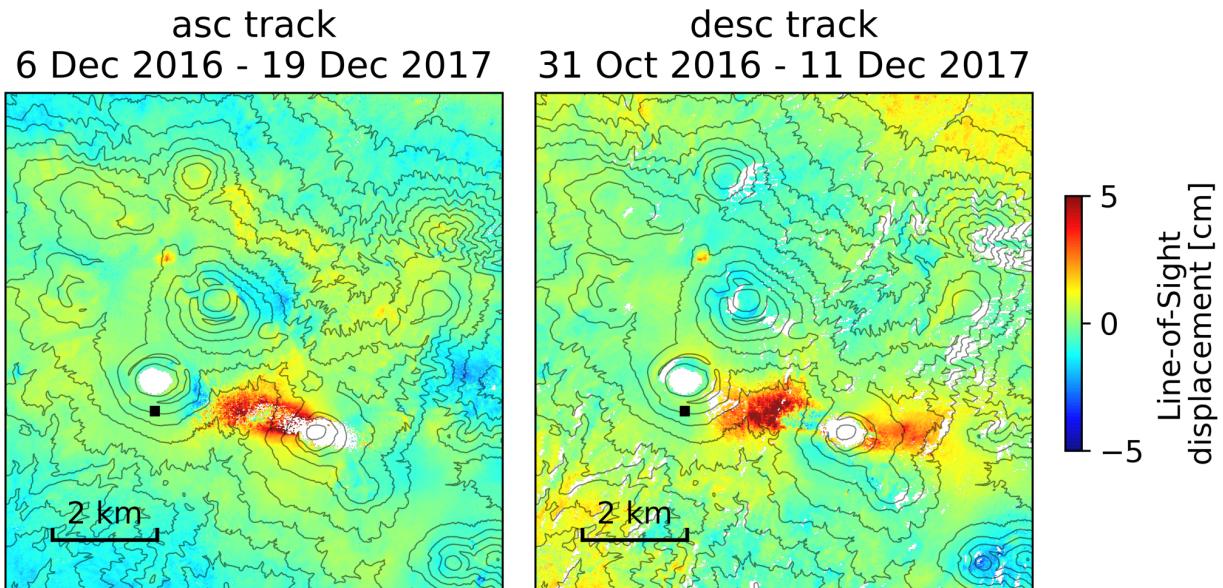
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169

170 **Figure S15.** Deflation at Shinmoe-dake and inflation at Iwo-yama after December 2017. Top panel:  
 171 LOS displacement from ALOS-2 ascending track 131 and descending track 23, respectively. Positive  
 172 value for motion toward the satellite. Bottom panel: quasi-east-west and quasi-vertical  
 173 displacement decomposed from the top panel. Positive value for motion toward the east and uplift.  
 174 Data are wrapped into [-6, 6) cm for display. Related to Fig. 1f.

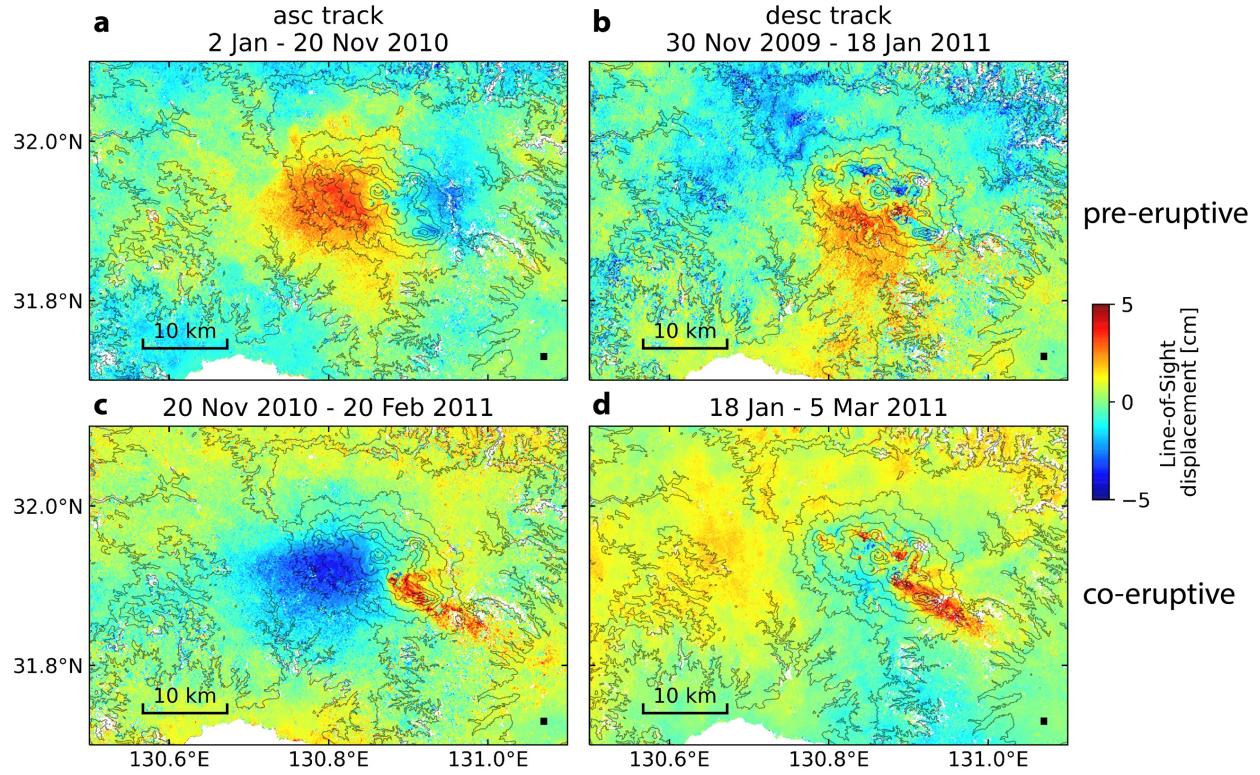
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176

177 **Figure S16.** Ash/tephra deposition from the October 2017 Shinmoe-dake eruption. Left and right:  
 178 ALOS-2 ascending track 131 and descending track 23, respectively. Positive values indicate motion  
 179 toward the satellite. Black squares: reference points. Contour lines in 100 m.

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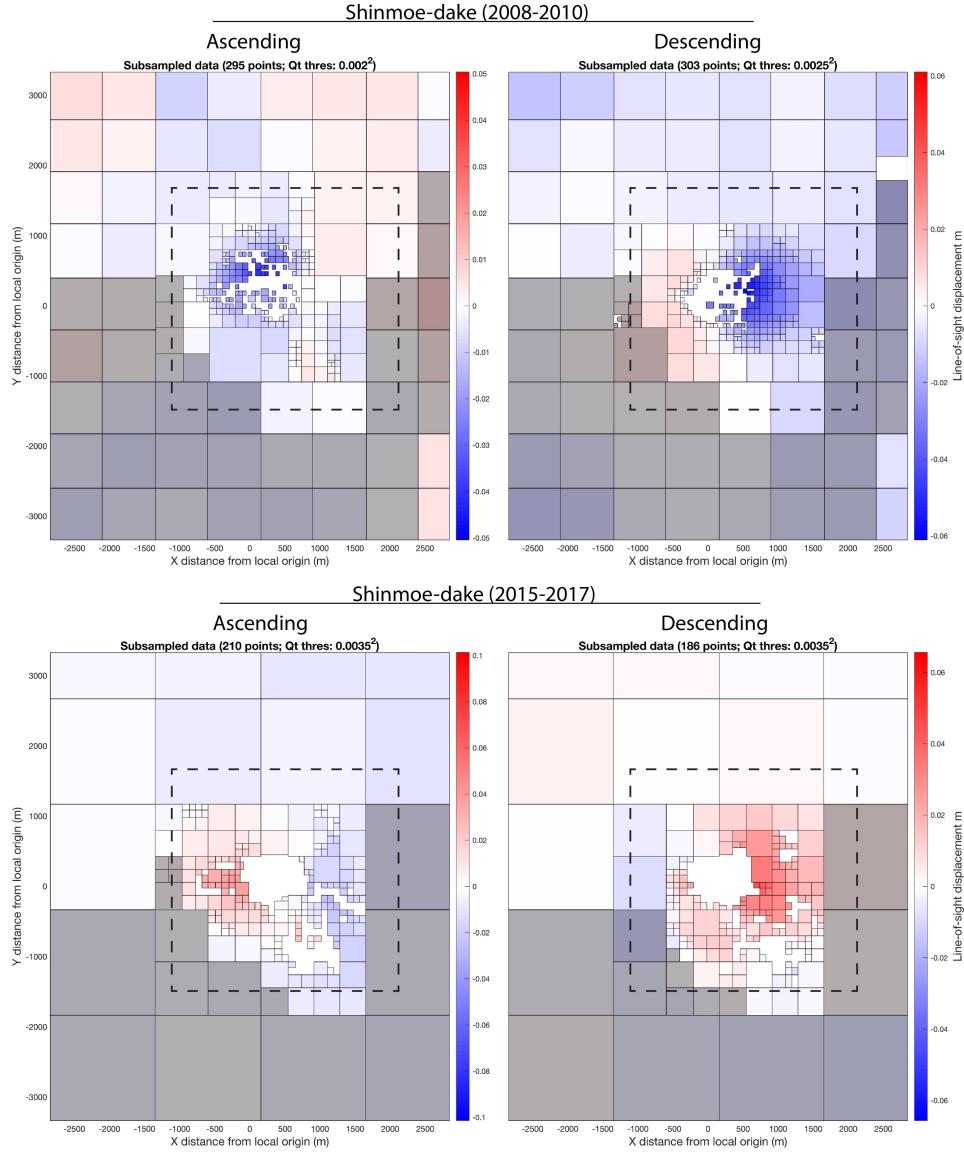


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182 **Figure S17.** Pre-/co-eruptive deformation of the 2011 Shinmoe-dake eruption. Left and right: ALOS  
 183 ascending track 424 and descending track 73, respectively. Positive values indicate motion toward  
 184 the satellite. Black squares: reference points. Contour lines in 200 m. Red long tail pattern in (c-d):  
 185 ash/tephra deposition from the eruption.

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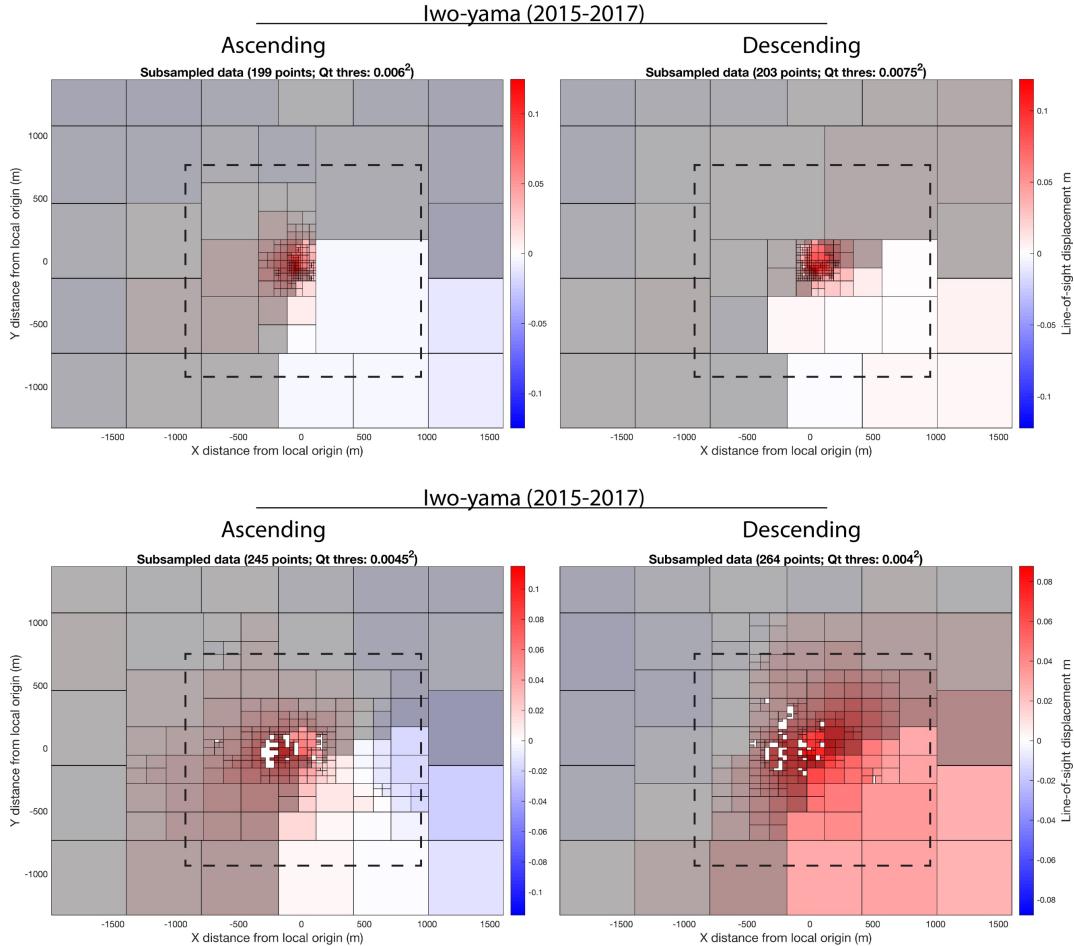
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189 **Figure S18.** Subsampled LOS displacement at Shinmoe-dake from ALOS and ALOS-2 ascending  
 190 and descending orbits. Positive value for motion toward the satellite. Black dashed rectangle  
 191 represents Fig. 3a-i coverage. We apply a minimum free surface height constraint of 1,100 m  
 192 (shaded grids). This affects 74 (with an average / min / max height increase of 119 / 7 / 343 m) out  
 193 of 598 points (12%) for the 2008-2010 period; and 30 (with an average / min / max height crease of  
 194 82 / 1 / 273 m) out of 396 points (8%) for the 2015-2017 period.

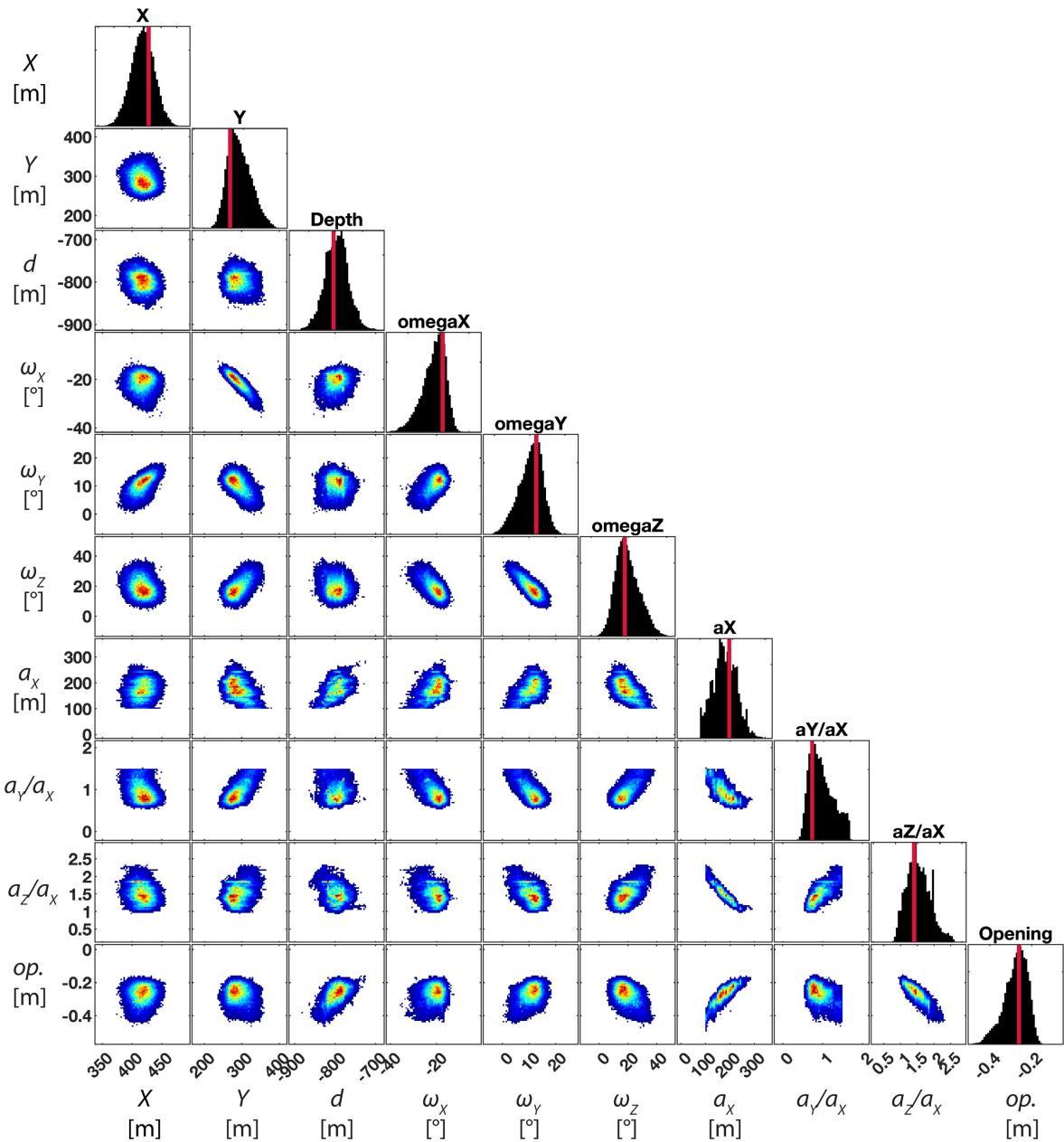
195



196

197 **Figure S19.** Subsampled LOS displacement data at Iwo-yama from ALOS-2 ascending and  
 198 descending orbits. Positive value for motion toward the satellite. Black dashed rectangle represents  
 199 Fig. 3k-s coverage. We apply a minimum free surface height constraint of 1,300 m (shaded grids).  
 200 This affects 239 (with an average / min / max height increase of 32 / 0 / 287 m) out of 402 points  
 201 (59%) for the 2015-2017 period; and 394 (with an average / min / max height crease of 56 / 0 / 287  
 202 m) out of 509 points (77%) for the 2017-2019 period.

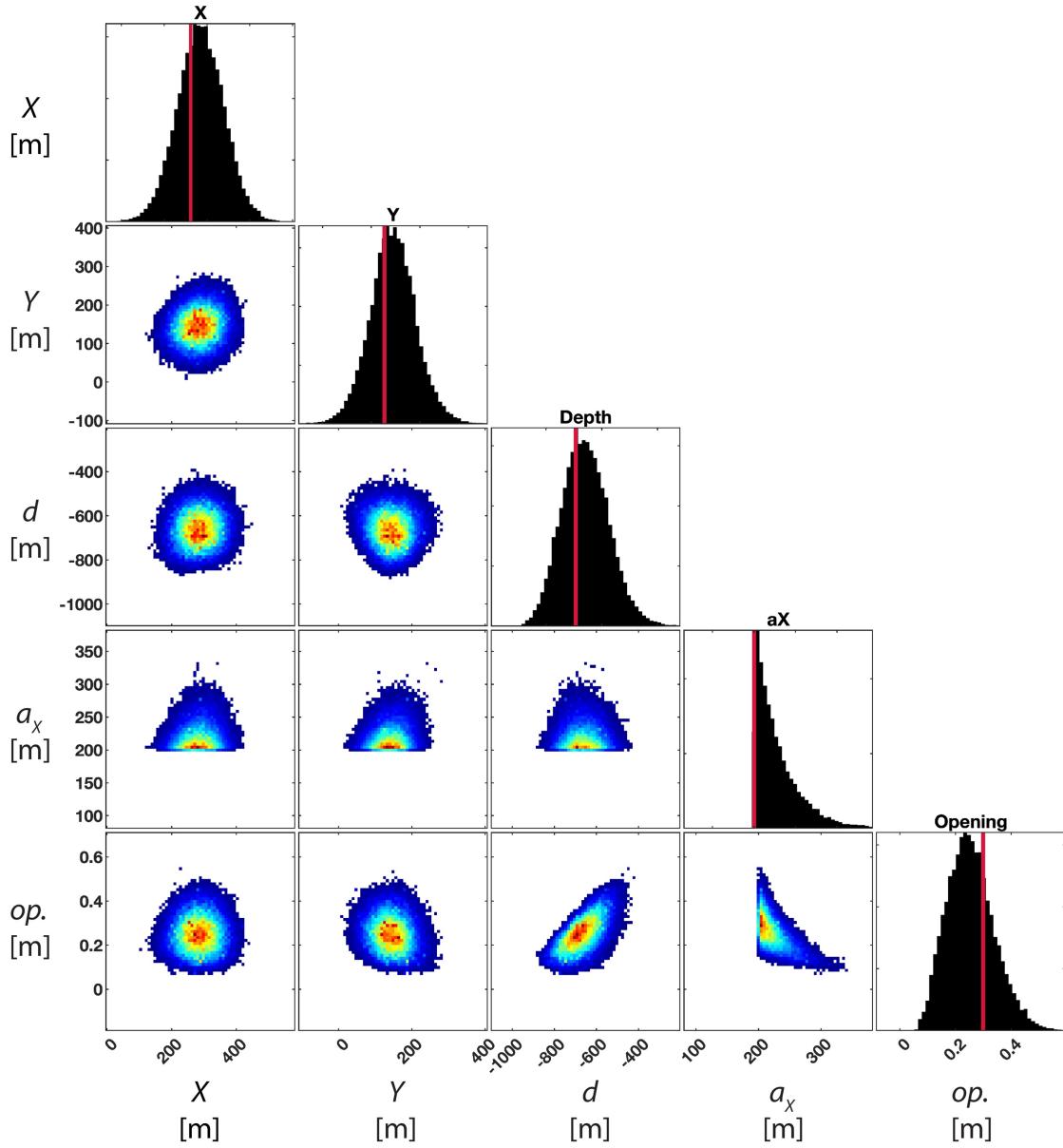
203



204

205 **Figure S20.** Marginal posterior probability distributions of the CDM parameters for the deflation  
 206 between the 2008-2010 phreatic eruptions at Shinmoe-dake. Black bars in the diagonal: posterior  
 207 probability distribution for each parameter. Red lines: maximum *a posteriori* probability (optimal)  
 208 solution.  $\omega_i$  and  $a_i, i = X, Y, Z$  are the rotation angle (positive for clockwise) and length of the  
 209 semi-axis along the  $i$ -axis, respectively. Related to Fig. 2a-e.

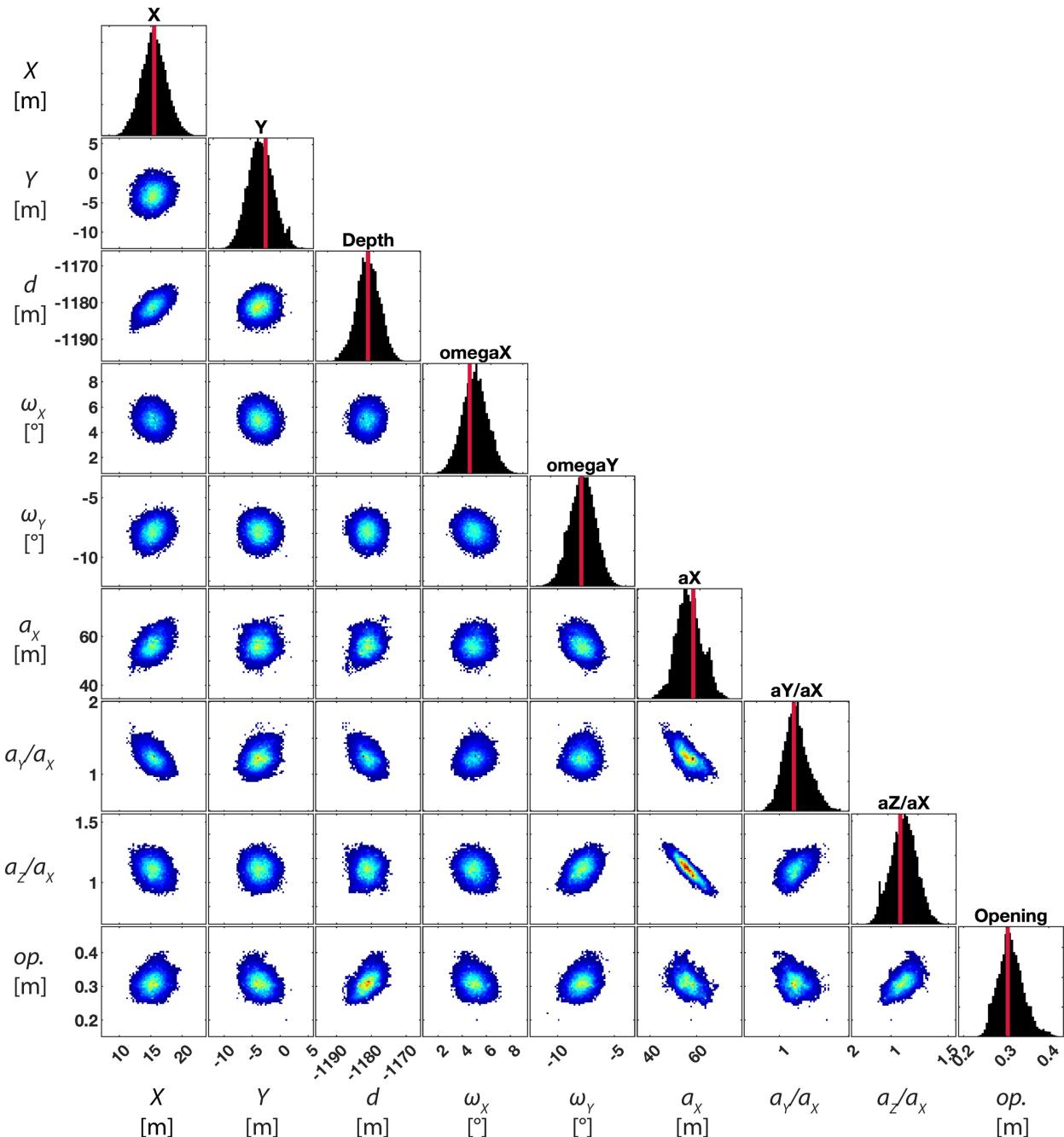
210



211

212 **Figure S21.** Marginal posterior probability distributions of CDM parameters for the pre-eruptive  
 213 inflation of the 2017 magmatic eruption at Shinmoe-dake. Fixed parameters are not shown. Black  
 214 bars in the diagonal: posterior probability distribution for each parameter. Red lines: maximum a  
 215 posteriori probability (optimal) solution. Related to Fig. 2f-j.

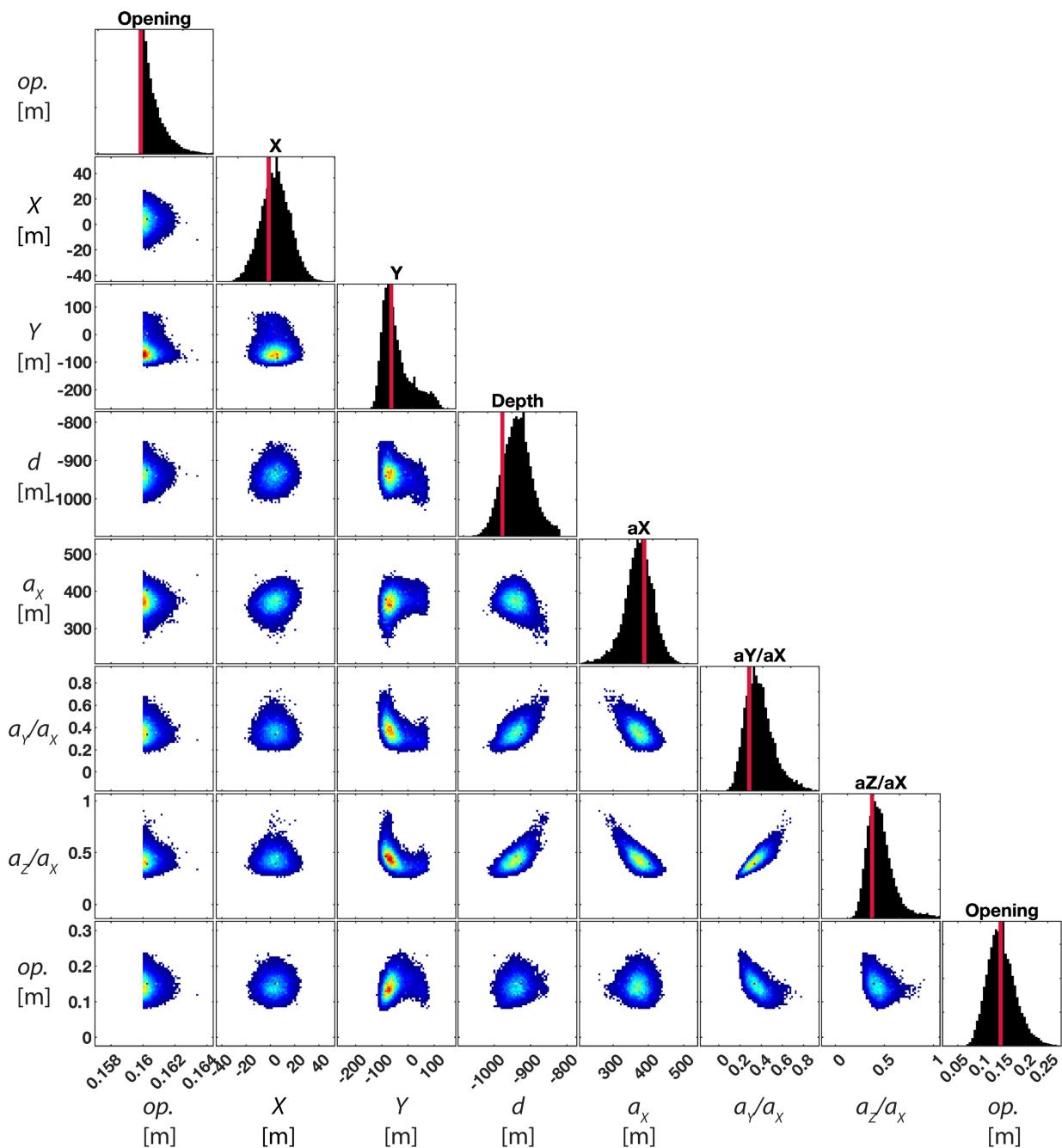
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217

218 **Figure S22.** Marginal posterior probability distributions of CDM parameters for the inflation before  
 219 October 2017 at Iwo-yama. Fixed parameters are not shown. Black bars in the diagonal: posterior  
 220 probability distribution for each parameter. Red lines: maximum a posteriori probability (optimal)  
 221 solution. Related to Fig. 2k-o.

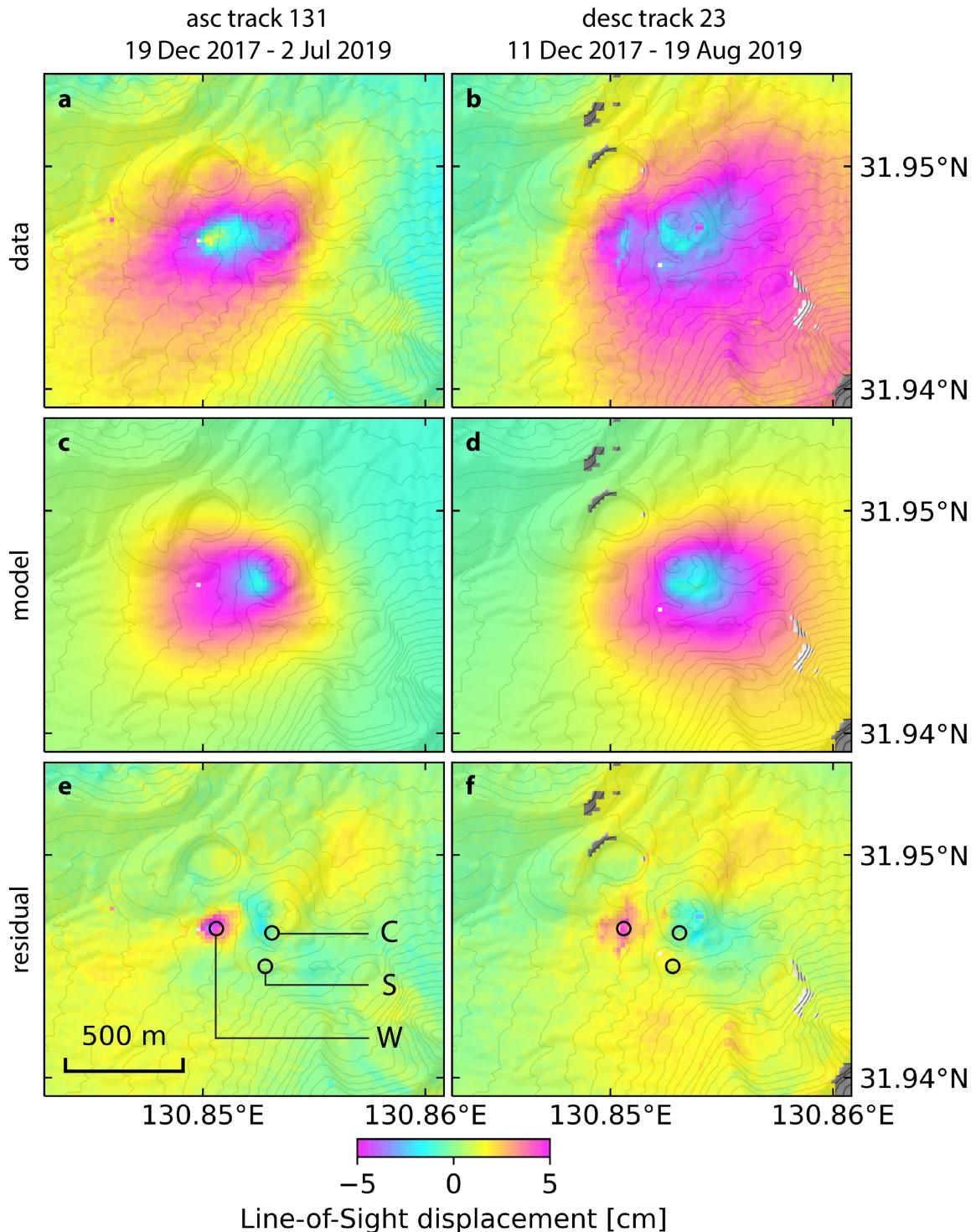
222



223

224 **Figure S23.** Marginal posterior probability distributions of two CDMs parameters for the expanded  
 225 inflation after December 2017 at Iwo-yama. Fixed parameters are not shown. Black bars in the  
 226 diagonal: posterior probability distribution for each parameter. Red lines: maximum a posteriori  
 227 probability (optimal) solution. Related to Fig. 2p-t.

228



229

230 **Figure S24.** Residual between the observed and predicted displacement from two CDMs at two-  
 231 yama after December 2017. Contour lines in 20 m. Point C, S and W are the same as in Fig. 1. Positive  
 232 values for motion toward the satellite. Related to Fig 1g and 2p-t.