



+ Código + Texto

RAM Disco



## Trabalhando com a biblioteca Numpy

```
[1] import numpy as np
[2] #características do dataset
#7 anos e 3 meses de dados
7*12+3
87
[3] #dadas as características acima preciso gerar um array para excluir a primeira coluna de strings
colunas_dataframe = np.arange(1,88,1)
colunas_dataframe
array([ 1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16, 17,
       18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34,
       35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51,
       52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68,
       69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85,
       86, 87])
[4] dados = np.loadtxt('apples_ts.csv', delimiter=',', usecols=colunas_dataframe)
dados
```

45.85 , 49.25 , 48.14 , 49.18 , 49.49 , 49.83 ,
49.14 , 63.21 , 61.2 , 60.34 , 62.2 , 74.2 ,
75.32 , 75.92 , 72.89 , 74.85 , 92.19 , 99.7 ,
182.78 , 92.67 , 90.63 , 83.31 , 75.5 , 74.6 ,
76.94 , 83.04 , 80.74 , 80.29 , 82.82 , 86.29 ,
87.41 , 85.1 , 78.08 , 76.06 , 69.23 , 69.04 ,
64.48 , 65.73 , 67.2 , 70.25 , 82.59 , 92.12 ,
100.82 , 95.23 , 89.51 , 82.84 , 82.3 , 83.76 ,
84.72 , 83.91 , 99.14 , 101.6 , 113.03 , 119.54 ,
118.09 , 107.32 , 82.6 , 77.4 , 71.77 , 71.25 ,
71.35 , 73.62 , 76.2 , 74.15 , 75.67 , 79.2 ,
80.85 , 85.33 , 75.02 , 77.95 , 78.98 , 76.55 ,
74.89 , 70. , 81.53 ],
[ 62.55 , 62.73 , 63.43 , 63.83 , 66.06 , 69.22 ,
72.07 , 69.31 , 65.18 , 62.13 , 64.17 , 65.5 ,
66.85 , 68.38 , 68.77 , 69.32 , 69.77 , 70.17 ,
70.76 , 75.16 , 74.86 , 71.47 , 76.08 , 82.11 ,
94.63 , 98.54 , 97.84 , 94.54 , 97.88 , 97.73 ,
100.89 , 104.88 , 104.39 , 101.9 , 98.99 , 99.42 ,
106.37 , 113.89 , 114.78 , 115.6 , 115.89 , 117.66 ,
118.27 , 114.19 , 101.81 , 91.62 , 90.15 , 90.55 ,
92.3 , 91.75 , 92. , 92.57 , 100.28 , 114.33 ,
122.17 , 117.83 , 112.49 , 93.7 , 97.17 , 95.64 ,
102.21 , 107.58 , 110.48 , 117.73 , 122.07 , 128.58 ,
131.12 , 127.08 , 110.99 , 97.43 , 92.05 , 93.21 ,
98.58 , 100.23 , 102.09 , 101.73 , 107.28 , 115.35 ,
123.03 , 123.08 , 109.71 , 97.22 , 95.75 , 97.09 ,
98.18 , 103.1 , 110.6 ],
[ 48.26 , 51.01 , 50.91 , 53.94 , 61.27 , 65.44 ,
56.51 , 53. , 43.87 , 42.12 , 43.98 , 44.66 ,
47.73 , 52.31 , 56.8 , 51.15 , 54.63 , 55.8 ,
57.31 , 53.81 , 55.5 , 52.95 , 53.29 , 54.86 ,
71.72 , 74.36 , 78.25 , 78.63 , 77.06 , 81.52 ,
84.12 , 83.33 , 66.98 , 62.04 , 59.79 , 66.06 ,
71.99 , 76.79 , 80.98 , 89.18 , 92.71 , 94.85 ,
99.18 , 86.33 , 71.94 , 67.18 , 62.98 , 69.45 ,
67.56 , 67.92 , 68.4 , 67.97 , 76.33 , 95.79 ,
112.36 , 82.03 , 73.83 , 66.12 , 63.24 , 63.98 ,
69.1 , 70.04 , 80.03 , 87.92 , 97.07 , 106.52 ,
108.93 , 95.17 , 74.31 , 62.63 , 69.92 , 70.58 ,
74.63 , 78.69 , 81.82 , 82.36 , 89.44 , 102.01 ,
116.12 , 92.06 , 82.7 , 66.62 , 68.11 , 73.48 ,
82.04 , 81.19 , 95.05 ],
[ 71.25 , 71.35 , 70.9 , 71.92 , 72.91 , 74.39 ,
73.1 , 70.24 , 69.12 , 68.98 , 68.58 , 69.5 ,
70.14 , 70.58 , 70.78 , 72.78 , 72.84 , 74.74 ,
76.43 , 81.2 , 82.04 , 79.67 , 81.25 , 85.88 ,
91.35 , 101.32 , 102.45 , 98.18 , 105.1 , 104.85 ,
111.48 , 118.51 , 118.92 , 109.87 , 105.22 , 105.45 ,

```
115.61 , 116.61 , 120.39 , 119.2 , 119.92 , 120.57 ,
123.37 , 121.39 , 118.16 , 108.84 , 100.78 , 99.92 ,
100.65 , 98.92 , 100.31 , 96.41 , 101.24 , 118.7 ,
133.29 , 130.31 , 122.4 , 104.98 , 107.54 , 110.74 ,
110.51 , 111.46 , 113.42 , 118.15 , 114. , 124.91 ,
126.06 , 123.3 , 111.61 , 98.82 , 97.47 , 103.01 ,
189.36 , 104.79 , 105.09 , 103.16 , 106.52 , 121.68 ,
125.32 , 123.41 , 108.48 , 98.73 , 96.25 , 100.12 ,
101.29 , 102.81 , 108.53 ]])
```

```
[5] #diferença entre Lista e Array em Python
import numpy as np

# cria uma lista
lista = [1, 2, 3, 4, 5]

# transforma a lista em um array Numpy
array = np.array(lista)

print("Lista: ", lista)
print("Array: ", array)

Lista: [1, 2, 3, 4, 5]
Array: [1 2 3 4 5]
```

```
[6] import time

# cria uma lista com 1000000 elementos
lista = list(range(1000000))

# transforma a lista em um array Numpy
array = np.array(lista)

# começa a cronometrar o tempo para a operação com a lista
start_time = time.time()

# realiza a operação de elevar ao quadrado cada elemento da lista
lista_quadrado = [i**2 for i in lista]

# para o cronômetro
list_time = time.time() - start_time

# começa a cronometrar o tempo para a operação com o array
start_time = time.time()

# realiza a operação de elevar ao quadrado cada elemento do array
array_quadrado = array**2

# para o cronômetro
array_time = time.time() - start_time

print("Tempo da operação com a lista: ", list_time)
print("Tempo da operação com o array: ", array_time)
```

```
Tempo da operação com a lista: 0.320446252822876
Tempo da operação com o array: 0.003691434860229492
```

```
[7] dados.ndim
```

```
2
```

```
[8] dados.size
```

```
522
```

```
[9] dados.shape
```

```
(6, 87)
```

```
[10] #transposição
dados_transpostos = dados.T
dados_transpostos
```

```
[ 6.2015, 97.29 , 99.7 , 97.73 , 81.52 , 104.85 ],
[ 7.2015, 98.64 , 102.78 , 100.89 , 84.12 , 111.48 ],
[ 8.2015, 104.26 , 92.67 , 104.88 , 83.33 , 118.51 ],
[ 9.2015, 102.63 , 90.63 , 104.39 , 66.98 , 118.92 ],
[ 10.2015, 98.64 , 83.31 , 101.9 , 62.04 , 109.87 ],
[ 11.2015, 97.17 , 75.5 , 98.99 , 59.79 , 105.22 ],
[ 12.2015, 98.09 , 74.6 , 99.42 , 66.06 , 105.45 ],
[ 1.2016, 103.07 , 76.94 , 106.37 , 71.99 , 115.61 ],
[ 2.2016, 110.26 , 83.04 , 113.89 , 76.79 , 116.61 ],
[ 3.2016, 110.84 , 80.74 , 114.78 , 80.98 , 120.39 ],
[ 4.2016, 112.28 , 80.29 , 115.6 , 89.18 , 119.2 ],
[ 5.2016, 111.1 , 82.82 , 115.89 , 92.71 , 119.92 ],
[ 6.2016, 110.06 , 86.29 , 117.66 , 94.85 , 120.57 ],
[ 7.2016, 113.7 , 87.41 , 118.27 , 99.18 , 123.37 ],
[ 8.2016, 112.88 , 85.1 , 114.19 , 86.33 , 121.39 ],
[ 9.2016, 102.08 , 78.08 , 101.81 , 71.94 , 118.16 ],
[ 10.2016, 95.54 , 76.06 , 91.62 , 67.18 , 108.84 ],
[ 11.2016, 91.33 , 69.23 , 90.15 , 62.98 , 100.78 ],
[ 12.2016, 89.99 , 69.04 , 90.55 , 69.45 , 99.92 ],
[ 1.2017, 91.44 , 64.48 , 92.3 , 67.56 , 100.65 ],
```

```
[ 2.2017, 93.51 , 65.73 , 91.75 , 67.92 , 98.92 ],
[ 3.2017, 93.6 , 67.2 , 92. , 68.4 , 100.31 ],
[ 4.2017, 93.78 , 70.25 , 92.57 , 67.97 , 96.41 ],
[ 5.2017, 98.91 , 82.59 , 100.28 , 76.33 , 101.24 ],
[ 6.2017, 121.76 , 92.12 , 114.33 , 95.79 , 118.7 ],
[ 7.2017, 129.6 , 100.82 , 122.17 , 112.36 , 133.29 ],
[ 8.2017, 127.9 , 95.23 , 117.83 , 82.03 , 130.31 ],
[ 9.2017, 114.55 , 89.51 , 112.49 , 73.83 , 122.4 ],
[ 10.2017, 101.88 , 82.84 , 93.7 , 66.12 , 104.98 ],
[ 11.2017, 99.09 , 82.3 , 97.17 , 63.24 , 107.54 ],
[ 12.2017, 103.35 , 83.76 , 95.64 , 63.98 , 110.74 ],
[ 1.2018, 106.58 , 84.72 , 102.21 , 69.1 , 110.51 ],
[ 2.2018, 108. , 83.91 , 107.58 , 70.04 , 111.46 ],
[ 3.2018, 114.95 , 99.14 , 110.48 , 80.03 , 113.42 ],
[ 4.2018, 121.17 , 101.6 , 117.73 , 87.92 , 118.15 ],
[ 5.2018, 122.48 , 113.03 , 122.07 , 97.07 , 114. ],
[ 6.2018, 127.58 , 119.54 , 128.58 , 106.52 , 124.91 ],
[ 7.2018, 131.89 , 118.09 , 131.12 , 108.93 , 126.06 ],
[ 8.2018, 129.36 , 107.32 , 127.08 , 95.17 , 123.3 ],
[ 9.2018, 104.26 , 82.6 , 110.99 , 74.31 , 111.61 ],
[ 10.2018, 93.45 , 77.4 , 97.43 , 62.63 , 98.82 ],
[ 11.2018, 92.93 , 71.77 , 92.05 , 69.92 , 97.47 ],
[ 12.2018, 96.15 , 71.25 , 93.21 , 70.58 , 103.01 ],
[ 1.2019, 99.1 , 71.35 , 98.58 , 74.63 , 109.36 ],
[ 2.2019, 103. , 73.62 , 100.23 , 78.69 , 104.79 ],
[ 3.2019, 103.31 , 76.2 , 102.09 , 81.82 , 105.09 ],
[ 4.2019, 103.01 , 74.15 , 101.73 , 82.36 , 103.16 ],
[ 5.2019, 107.37 , 75.67 , 107.28 , 89.44 , 106.52 ],
[ 6.2019, 116.91 , 79.2 , 115.35 , 102.01 , 121.68 ],
[ 7.2019, 125.29 , 80.85 , 123.03 , 116.12 , 125.32 ],
[ 8.2019, 123.94 , 85.33 , 123.08 , 92.06 , 123.41 ],
[ 9.2019, 113.03 , 75.02 , 109.71 , 82.7 , 108.48 ],
[ 10.2019, 102.19 , 77.95 , 97.22 , 66.62 , 98.73 ],
[ 11.2019, 97.83 , 78.98 , 95.75 , 68.11 , 96.25 ],
[ 12.2019, 101.07 , 76.55 , 97.09 , 73.48 , 100.12 ],
[ 1.202 , 103.44 , 74.89 , 98.18 , 82.04 , 101.29 ],
[ 2.202 , 108.23 , 70. , 103.1 , 81.19 , 102.81 ],
[ 3.202 , 110.28 , 81.53 , 110.6 , 95.05 , 108.53 ]])
```

✓ [11] `dados = dados_transpostos[:,0]`

`dados.shape`

(87,)

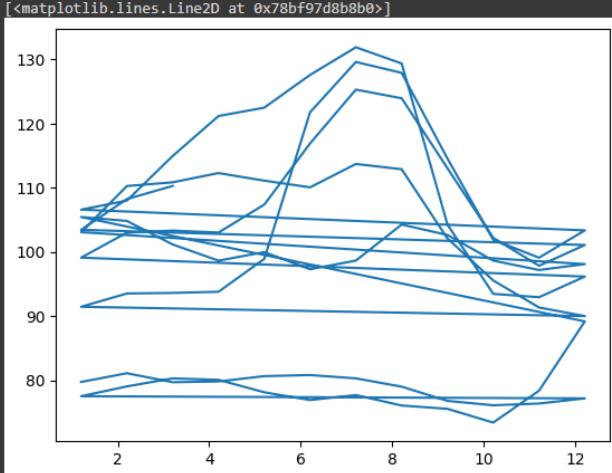
✓ [12] `precos = dados_transpostos[:,1:6]`

`precos.shape`

(87, 5)

✓ [13] `import matplotlib.pyplot as plt`

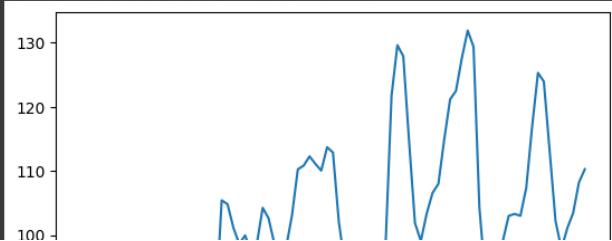
✓ [14] `plt.plot(dados, precos[:,0])`

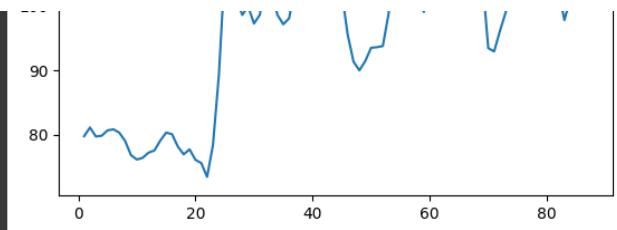


✓ [15] `dados = np.arange(1, 88, 1)`  
`plt.plot(dados, precos[:,0])`

#eu não estou mais trabalhando com valores de datas na variável "dados"  
#simplesmente gerei um array para servir de base de plotagem para o eixo x.

[<matplotlib.lines.Line2D at 0x78bf94c1d4b0>]





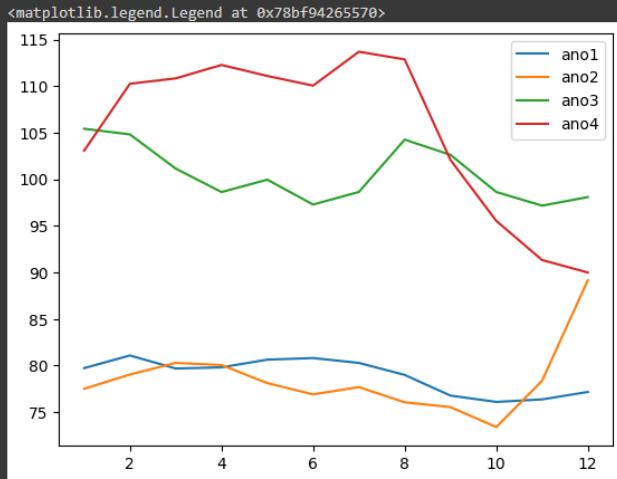
```

✓ [16] Moscow = precos[:,0]
      Kaliningrad = precos[:,1]
      Petersburg = precos[:,2]
      Krasnodar = precos[:,3]
      Ekaterinburg = precos[:,4]

✓ [17] # segmentando por ano para comparações sazonais
      Moscow_ano1 = Moscow[0:12]
      Moscow_ano2 = Moscow[12:24]
      Moscow_ano3 = Moscow[24:36]
      Moscow_ano4 = Moscow[36:48]

✓ [18] plt.plot(np.arange(1,13,1), Moscow_ano1)
      plt.plot(np.arange(1,13,1), Moscow_ano2)
      plt.plot(np.arange(1,13,1), Moscow_ano3)
      plt.plot(np.arange(1,13,1), Moscow_ano4)
      plt.legend(['ano1', 'ano2', 'ano3', 'ano4'])

```



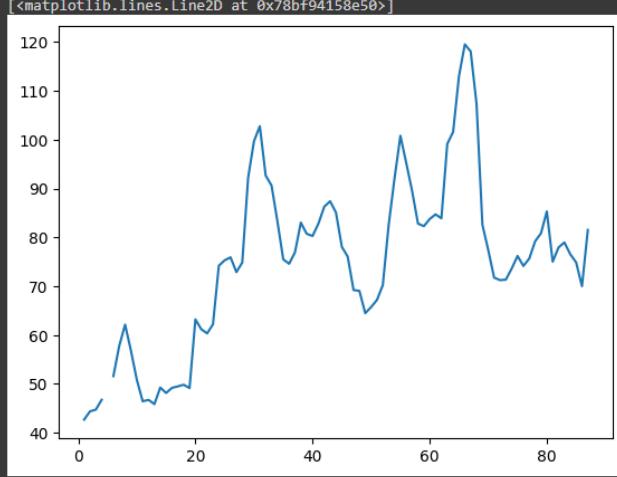
```

✓ [19] np.array_equal(Moscow_ano3, Moscow_ano4)
      False

✓ [20] np.allclose(Moscow_ano1, Moscow_ano2, 0.01)
      False

✓ [21] plt.plot(datas, Kaliningrad)

```



```

✓ [22] Kaliningrad

```

```
array([ 42.67, 44.37, 44.73, 48.75, nan, 51.59, 57.8 , 62.14,
       56.76, 58.85, 46.43, 46.73, 45.85, 49.25, 48.14, 49.18,
       49.49, 49.83, 49.14, 63.21, 61.2 , 60.34, 62.2 , 74.2 ,
       75.32, 75.92, 72.89, 74.85, 92.19, 99.7 , 102.78, 92.67,
       90.63, 83.31, 75.5 , 74.6 , 76.94, 83.04, 80.74, 80.29,
       82.82, 86.29, 87.41, 85.1 , 78.08, 76.06, 69.23, 69.04,
       64.48, 65.73, 67.2 , 70.25, 82.59, 92.12, 100.82, 95.23,
       89.51, 82.84, 82.3 , 83.76, 84.72, 83.91, 99.14, 101.6 ,
      113.03, 119.54, 118.09, 107.32, 82.6 , 77.4 , 71.77, 71.25,
      71.35, 73.62, 76.2 , 74.15, 75.67, 79.2 , 80.85, 85.33,
      75.02, 77.95, 78.98, 76.55, 74.89, 70. , 81.53])
```

```
[23] sum(np.isnan(Kaliningrad))
```

```
1
```

```
[24] (Kaliningrad[3]+Kaliningrad[5])/2
```

```
49.17
```

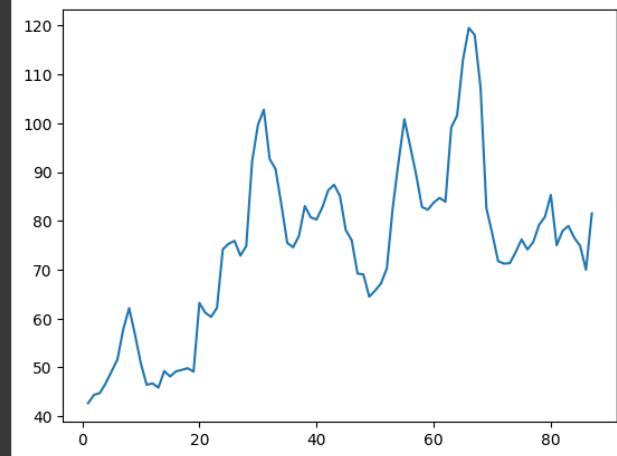
```
[25] #ou
np.mean([Kaliningrad[3], Kaliningrad[5]])
```

```
49.17
```

```
[26] #substituindo o NaN
Kaliningrad[4] = np.mean([Kaliningrad[3], Kaliningrad[5]])
```

```
[27] plt.plot(datas, Kaliningrad)
```

```
[<matplotlib.lines.Line2D at 0x78bf941c5f90>]
```



```
[28] np.mean(Moscow)
```

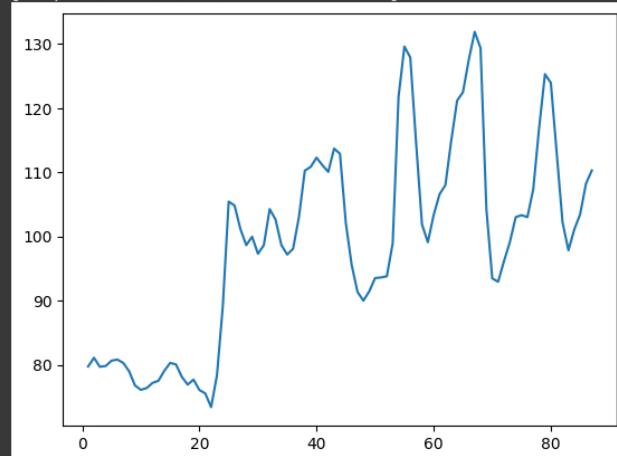
```
98.79781609195402
```

```
[29] np.mean(Kaliningrad)
```

```
74.5506896551724
```

```
[30] # ajustando uma reta para os preços
# coeficiente angular: y = ax + b, onde o y é o preço, a é o coeficiente angular e b o coeficiente linear.
plt.plot(datas, Moscow)
```

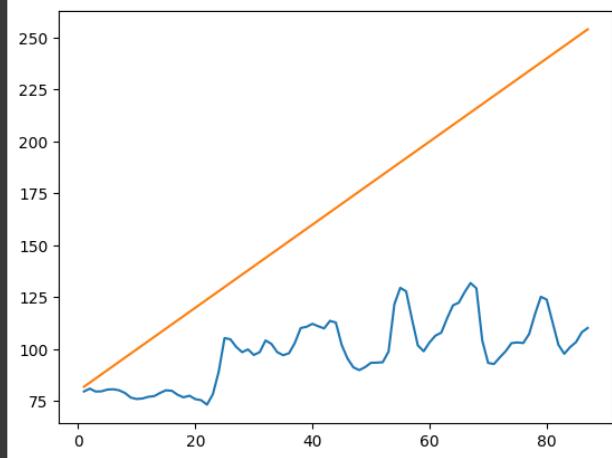
```
[<matplotlib.lines.Line2D at 0x78bf94064580>]
```



```
[31] # apenas supondo valores para as variáveis x e y
```

```
x = datas  
y = 2*x + 80  
  
plt.plot(datas, Moscow)  
plt.plot(x, y)
```

```
[<matplotlib.lines.Line2D at 0x78bf940cd9c0>]
```



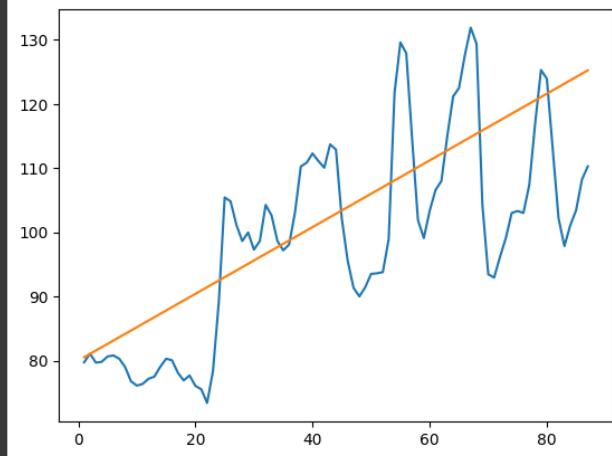
```
✓ [32] # eu preciso ajustar a reta aos meus dados  
# para isso eu subtraio Moscow de y e elevo ao quadrado para eliminar os números negativos  
# após a elevação ao quadrado, eu terei números muito grandes, então é necessário um ajuste com soma.  
  
np.sqrt(np.sum(np.power(Moscow - y, 2)))
```

```
749.2329171225728
```

```
✓ [33] # refazendo os cálculos com outros valores de reta
```

```
y = 0.52*x + 80  
plt.plot(datas, Moscow)  
plt.plot(x, y)
```

```
[<matplotlib.lines.Line2D at 0x78bf9412b670>]
```



```
✓ [34] np.sqrt(np.sum(np.power(Moscow - y, 2)))  
110.48504740461489
```

```
✓ [35] # refazendo o mesmo cálculo com função do numpy  
np.linalg.norm(Moscow - y)
```

```
110.48504740461489
```

#### ▼ Adendo: Cópia ou Referência de arrays?

```
✓ [36] # Cópias referenciadas: alteração em uma, altera outra  
preco_imoveis = np.array([10000,120000,11000,200000])  
preco_imoveis_sao_paulo = preco_imoveis
```

```
✓ [37] preco_imoveis[0] = 120000
```

```
✓ [38] preco_imoveis_sao_paulo
```

```
array([120000, 120000, 11000, 200000])
```

```

✓ [39] # Cópias não referenciadas
preco_imoveis = np.array([10000,120000,11000,200000])
preco_imoveis_sao_paulo = np.copy(preco_imoveis) # <---
preco_imoveis[0] = 12000
preco_imoveis_sao_paulo

array([ 10000, 120000, 11000, 200000])

```

▼ continuando...

```

✓ [40] # trabalhando com os dados reais de preços
Y = Moscow
x = datas
n = np.size(Moscow)

```

```

✓ [41] (x**2).shape
(87,)

```

```

✓ [42] # escrevendo a fórmula do coeficiente angular
a = (n*np.sum(x*Y) - np.sum(x)*np.sum(Y)) / (n*np.sum(x**2) - np.sum(x)**2)

```

```

✓ [43] # escrevendo a fórmula do coeficiente linear
b = np.mean(Y) - a*np.mean(x)

```

```

✓ [44] y = a*x + b

```

```

✓ [45] np.linalg.norm(Moscow-y)
101.7969539992751

```

▼ exercício de plotagem de círculo

```

✓ [46] # Gerar uma sequência de valores de x de -1 a 1
x = np.arange(-1, 1, 0.0001)

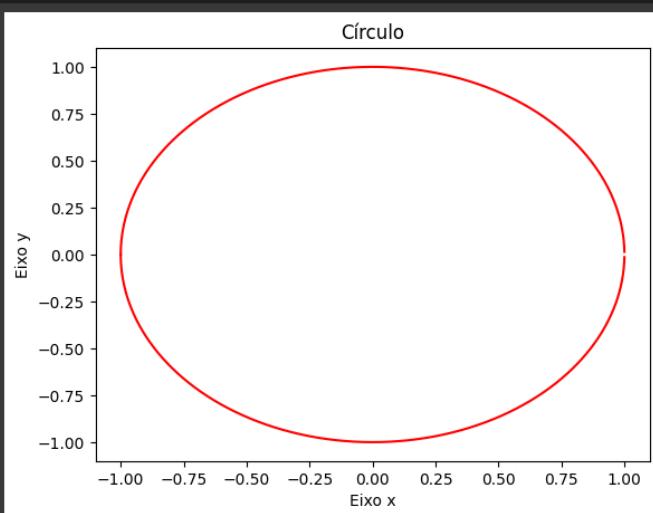
# Implementação da fórmula
y1 = np.sqrt(1 - x**2)
y2 = -np.sqrt(1 - x**2)

# Plotar o gráfico com as duas partes do círculo
plt.plot(x, y1, 'r')
plt.plot(x, y2, 'r' )

# Adicionar o título do gráfico e os rótulos dos eixos x e y
plt.title("Círculo")
plt.xlabel("Eixo x")
plt.ylabel("Eixo y")

# Exibir o gráfico
plt.show()

```



▼ continuando com regressão liner

```

✓ [49] # plotagem da regressão linear calculada corretamente
Y = Moscow
x = datas
n = np.size(Moscow)

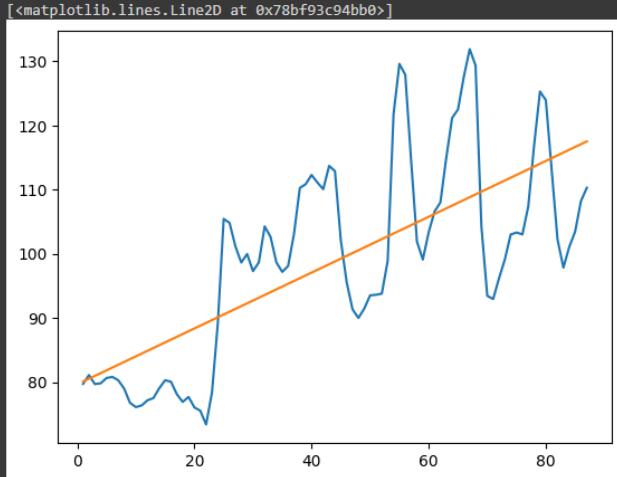
(x**2).shape

```

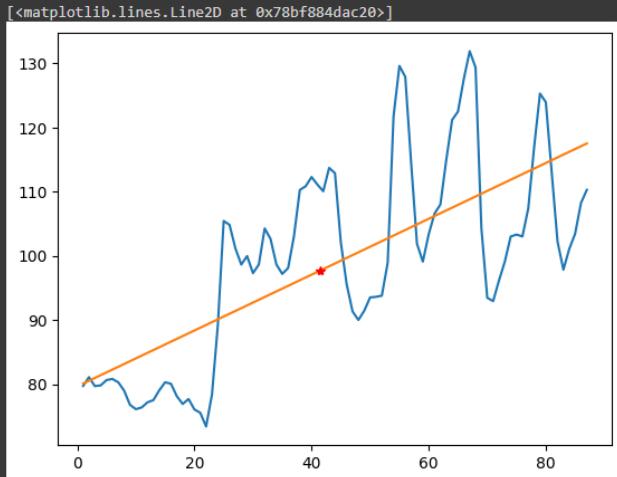
```

a = (n*np.sum(x*Y) - np.sum(x)*np.sum(Y)) / (n*np.sum(x**2) - np.sum(x)**2)
b = np.mean(Y) - a*np.mean(x)
y = a*x + b
plt.plot(datas, Moscow)
plt.plot(x, y)

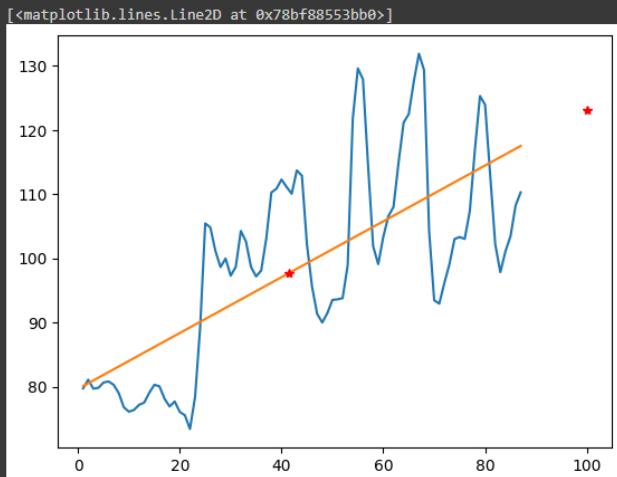
```



✓ [51] # para plotar apenas um ponto no gráfico  
plt.plot(datas, Moscow)  
plt.plot(x, y)  
plt.plot(41.5, 41.5\*a+b, '\*r')



✓ [52] # projetando a reta para previsão de valores  
plt.plot(datas, Moscow)  
plt.plot(x, y)  
plt.plot(41.5, 41.5\*a+b, '\*r')  
#altero valores para 100 (máximo 87)  
plt.plot(100, 100\*a+b, '\*r')



▼ trabalhando com aleatoriedade

```
[53] # gerando números inteiros aleatórios  
np.random.randint(low=40, high=100, size=100)
```

```
array([55, 52, 62, 80, 98, 96, 84, 91, 90, 58, 63, 83, 90, 72, 51, 63, 77,  
57, 79, 82, 52, 55, 52, 81, 54, 97, 82, 40, 82, 44, 77, 48, 75, 68,  
62, 62, 72, 84, 43, 72, 72, 79, 76, 86, 73, 99, 45, 47, 41, 78, 70,  
53, 51, 44, 90, 58, 59, 80, 87, 90, 86, 93, 44, 56, 49, 94, 41, 78,  
49, 68, 93, 91, 79, 92, 54, 50, 49, 69, 85, 70, 89, 92, 68, 49, 42,  
82, 60, 45, 85, 66, 73, 56, 58, 79, 84, 88, 71, 76, 40, 89])
```

✓ [54] # gerando números float aleatórios  
np.random.uniform(low=0.10, high=0.90, size=100)

```
array([0.80184047, 0.28105119, 0.63495476, 0.14638628, 0.26925898,  
0.82874877, 0.71296087, 0.20745547, 0.24686278, 0.43598836,  
0.25458102, 0.11836423, 0.30123979, 0.70811736, 0.85461215,  
0.37981964, 0.34363767, 0.89442305, 0.20976168, 0.132793 ,  
0.68627765, 0.28155431, 0.57164003, 0.82233307, 0.63662586,  
0.88361555, 0.1275358 , 0.21503829, 0.43798102, 0.43798976,  
0.65869389, 0.86752676, 0.5623516 , 0.1877705 , 0.45047816,  
0.13017819, 0.46212497, 0.31086822, 0.28443036, 0.35099549,  
0.26999819, 0.8069876 , 0.51539028, 0.33754001, 0.12068728,  
0.47693865, 0.47756444, 0.78028976, 0.66468176, 0.68768448,  
0.88741179, 0.10582072, 0.74690756, 0.25145515, 0.44113542,  
0.68488001, 0.45558659, 0.89373706, 0.69543613, 0.50562004,  
0.71311167, 0.13691203, 0.33958534, 0.42852394, 0.43559358,  
0.21777936, 0.19887186, 0.60000471, 0.19801875, 0.44357298,  
0.62318445, 0.52131239, 0.55098368, 0.87665377, 0.71631875,  
0.47218768, 0.374013 , 0.33008675, 0.10941211, 0.43602839,  
0.12693923, 0.63166349, 0.49670593, 0.49353516, 0.17374747,  
0.8158285 , 0.13581216, 0.27852468, 0.52559458, 0.29711451,  
0.6764442 , 0.45839564, 0.46296011, 0.23522712, 0.89441771,  
0.30057862, 0.28805054, 0.57561912, 0.14947784, 0.85646977])
```

✓ [55] # testando coeficiente angular com esses números aleatórios  
coef\_angulares = np.random.uniform(low=0.10, high=0.90, size=100)

✓ [56] for i in range(100):  
 print(np.linalg.norm(Moscow - (coef\_angulares[i]\*x+b)))

```
135.42711409580505  
117.43401249964366  
203.53196228325183  
150.2465219585277  
124.02717506416148  
116.99994953870367  
106.40189123489117  
141.22452698758542  
174.18919891216316  
166.5807465821204  
180.0419120004132  
102.69896628407006  
137.40722484664536  
149.78000729876882  
156.2792804299463  
122.97447302040547  
108.60076609596442  
189.32451223756152  
148.645877977689  
162.11415266404893  
146.80453481493868  
154.28840741591068  
104.10086590276241  
107.14991814644899  
170.85680975976726  
101.8473372786546  
130.7506771111329  
161.29663487137086  
138.8712054568994  
214.77656758718618  
214.39275969269042  
112.05731790544765  
126.7505940237295  
138.46146653854564  
116.41469892903108  
226.8553473843902  
106.30570467009734  
206.76672753657496  
131.3493810071654  
102.9284919091172  
171.46955632279372  
124.56741483049458  
145.8665080784717  
113.26190824079261  
145.70431190004  
115.16977350999927  
106.45200903790047  
103.63107476456527  
207.47279650331646  
107.93878382436365  
240.27576000337613  
213.63632679176465  
161.25215371799004  
164.68851130066915  
106.39346726861051  
106.87991347005214
```

```
226.04261426590512
174.88522121325357
```

```
✓ [58] # agregando esses valores a um array
norma = np.array([])

for i in range(100):
    norma = np.append(norma, np.linalg.norm(Moscow - (coef_angulares[i]*x+b)))

norma

array([147.10101138, 101.8165657, 172.01403888, 147.99170917,
       156.86381528, 223.69121172, 141.07902887, 193.35045219,
       148.04348404, 130.00445928, 143.97411878, 134.59639439,
       136.07395798, 180.3292952, 179.10964793, 104.17723111,
       135.90188801, 119.46407591, 102.03555771, 167.86744578,
       217.05444629, 155.04579349, 101.84307135, 159.10522417,
       130.20979449, 173.32242094, 151.97406227, 177.70750684,
       163.17110361, 189.89989274, 102.27580584, 185.4974683,
       110.81321053, 183.26271362, 131.33557346, 186.26862509,
       148.63307053, 119.07003563, 143.20540066, 126.19084886,
       129.44787843, 176.62857077, 135.4271141, 117.4340125,
       203.53196228, 150.24652196, 124.02717506, 116.99994954,
       106.48189123, 141.22452699, 174.18919891, 166.58874658,
       180.041912, 182.69996628, 137.48722485, 149.7800873,
       156.27928043, 122.97447302, 108.6007661, 189.32451224,
       148.64507798, 162.11415266, 146.88453481, 154.28840742,
       104.1808659, 187.14991815, 170.85680976, 181.84733728,
       130.75067711, 161.29663487, 138.87120546, 214.77656759,
       214.39275969, 112.05731791, 126.75059402, 138.46146654,
       116.41469893, 226.85534738, 106.30570467, 206.76672754,
       131.34938101, 182.92849191, 171.46955632, 124.56741483,
       145.86650888, 113.26198824, 145.7043119, 115.16977351,
       106.452000904, 183.63107476, 207.4727965, 107.93878382,
       240.27676, 213.63632679, 161.25215372, 164.6885113,
       106.39346727, 186.87991347, 226.04261427, 174.88522121])
```

```
✓ [59] # testando o coeficiente angular em qualquer posição do array
coef_angulares[1]
```

```
0.4394309162204504
```

```
[60] #reprodutibilidade - SEED
#travando a aleatoriedade gerada
```

```
np.random.seed(16)
np.random.uniform(low=0.10, high=0.90, size=100)
```

```
array([0.27863286, 0.51853067, 0.54056117, 0.13648156, 0.38858307,
       0.27846475, 0.65098093, 0.23098514, 0.15625989, 0.85280869,
       0.5509451, 0.16239387, 0.67811241, 0.22676174, 0.30022505,
       0.3347898, 0.65728857, 0.47141127, 0.27204971, 0.45746181,
       0.196703, 0.83414961, 0.55315706, 0.47761545, 0.35165314,
       0.13457258, 0.70195593, 0.53461524, 0.71375234, 0.73235901,
       0.1577771, 0.62777267, 0.14263947, 0.64801956, 0.45468077,
       0.47439692, 0.62884747, 0.65197331, 0.31066359, 0.18918315,
       0.71703556, 0.752911386, 0.21171328, 0.5624054, 0.37253942,
       0.28577239, 0.258915, 0.31719262, 0.88148221, 0.27234318,
       0.38512593, 0.11471996, 0.59343222, 0.28432431, 0.69388139,
       0.56740017, 0.436088284, 0.66740227, 0.87763642, 0.74803129,
       0.44452414, 0.86618288, 0.13820648, 0.68622544, 0.64053316,
       0.52160413, 0.55358996, 0.6783562, 0.64608268, 0.73625014,
       0.19027642, 0.25933011, 0.67705538, 0.41509386, 0.37134832,
       0.22275655, 0.18045921, 0.42579769, 0.56633237, 0.69257642,
       0.79628867, 0.87322093, 0.46445188, 0.4203384, 0.33915157,
       0.76268805, 0.82787294, 0.71290934, 0.15465183, 0.58482122,
       0.85137291, 0.18171413, 0.88203161, 0.38535098, 0.62334973,
       0.19822857, 0.86908175, 0.62094514, 0.84934225, 0.82786184])
```

```
✓ [62] # se reproduzir o código sem o seed na sequência, não haverá a trava de aleatoriedade.
np.random.uniform(low=0.10, high=0.90, size=100)
```

```
array([0.48500983, 0.75450251, 0.54784106, 0.76580928, 0.58895348,
       0.39720625, 0.73190595, 0.56491178, 0.65877136, 0.14779337,
       0.25141208, 0.41854883, 0.68964221, 0.54177352, 0.29256499,
       0.82760739, 0.12016638, 0.33253592, 0.26049265, 0.39180554,
       0.80770835, 0.64889924, 0.2117912, 0.25004344, 0.13198589,
       0.25282076, 0.24318745, 0.3496539, 0.60106379, 0.67387554,
       0.20459079, 0.53295927, 0.7685072, 0.39100571, 0.54835399,
       0.51866898, 0.55469996, 0.82228867, 0.32118238, 0.58094439,
       0.10000356, 0.13371557, 0.35243667, 0.5738667, 0.12206297,
       0.41098732, 0.7171872, 0.10437215, 0.76597854, 0.69531581,
       0.68564233, 0.72599325, 0.83940319, 0.56335324, 0.22198688,
       0.67077979, 0.38743239, 0.81998321, 0.77250465, 0.66381904,
       0.20114065, 0.408399719, 0.41808924, 0.78874839, 0.82689583,
       0.4938446, 0.54418544, 0.13484602, 0.23471086, 0.61582527,
       0.47289357, 0.15476097, 0.18279763, 0.18108401, 0.3607793,
       0.57480171, 0.74450387, 0.6925472, 0.36622843, 0.15841153,
       0.1559766, 0.22795023, 0.56458643, 0.33814918, 0.60044662,
       0.16047333, 0.61879717, 0.32293671, 0.21905367, 0.86895804,
       0.77228641, 0.19000994, 0.41917446, 0.15702624, 0.8490132,
       0.75373905, 0.56289373, 0.84475328, 0.48509605, 0.18019447])
```

```
✓ [65] np.random.seed(84)
coef_angulares = np.random.uniform(low=0.10, high=0.90, size=100)
norma = np.array([])
```

```

for i in range(100):
    norma = np.append(norma, np.linalg.norm(Moscow - (coef_angulares[i]*x+b)))
norma
array([173.90151233, 103.45241986, 121.75367289, 128.97173036,
       238.69504078, 149.16590195, 137.73123242, 118.54419212,
       101.79720981, 149.04689147, 112.88225228, 105.8049351 ,
       230.82444742, 111.69795952, 134.56525693, 110.93209631,
       204.12484481, 196.82117307, 221.88687726, 156.13691854,
       125.51272174, 136.46474504, 165.39506278, 240.68784732,
       104.52254473, 188.75637903, 131.2292927 , 128.94885341,
       234.70773582, 147.01799832, 113.7418054 , 116.94496221,
       109.58257043, 187.09546548, 145.00728041, 182.83818792,
       148.95017242, 186.12371866, 107.8915778 , 132.45242448,
       144.8736358 , 143.54772697, 240.23793834, 113.74604121,
       116.01191029, 152.02977343, 174.72333708, 141.8068161 ,
       101.93467119, 183.01538109, 169.59787792, 128.13083711,
       105.06648948, 181.83421597, 102.53716362, 113.63850533,
       219.96993004, 117.37921502, 182.70217805, 146.69612581,
       178.64742004, 132.25425967, 109.74998636, 186.49825034,
       104.98272763, 133.73791912, 182.82613374, 235.49081818,
       179.79275527, 228.72013359, 184.2584889 , 114.02435937,
       124.95415977, 187.42082714, 105.18421164, 102.1005486 ,
       135.72717949, 187.19212075, 114.07766563, 225.76351056,
       103.96340568, 118.21130391, 109.96158846, 181.54233309,
       114.09828878, 118.61778913, 224.37792949, 153.50523694,
       185.44994519, 117.35423938, 151.19534147, 118.44720795,
       112.26379208, 104.60483872, 123.8587347 , 111.40038324,
       102.05294074, 150.97459646, 108.76787533, 107.97542886])

```

```

[66] #salvando dados
dados = np.column_stack([norma, coef_angulares])

[67] dados.shape
(100, 2)

```

dados

```

[1.16944962e+02, 3.1538503e-01],
[1.09582570e+02, 3.49353446e-01],
[1.07095465e+02, 3.64798675e-01],
[1.45007280e+02, 2.16664750e-01],
[1.82838188e+02, 7.56607337e-01],
[1.40950172e+02, 2.28893954e-01],
[1.06123719e+02, 4.98674696e-01],
[1.07091578e+02, 3.64825163e-01],
[1.32452424e+02, 2.55873812e-01],
[1.44873636e+02, 2.17062053e-01],
[1.43547727e+02, 6.49380794e-01],
[2.48237938e+02, 8.95695282e-01],
[1.13746041e+02, 3.27895663e-01],
[1.16011910e+02, 5.52953548e-01],
[1.52029773e+02, 1.96246038e-01],
[1.74723337e+02, 1.34690357e-01],
[1.41806816e+02, 2.26281568e-01],
[1.01934671e+02, 4.46411433e-01],
[1.03015381e+02, 4.01772345e-01],
[1.69597878e+02, 1.48141097e-01],
[1.281308837e+02, 5.99869975e-01],
[1.05066489e+02, 4.90237320e-01],
[1.01834216e+02, 4.29372898e-01],
[1.02537164e+02, 4.61227883e-01],
[1.13638585e+02, 5.42087557e-01],
[2.19969930e+02, 8.47855493e-01],
[1.17379215e+02, 3.11531216e-01],
[1.82702178e+02, 1.14143458e-01],
[1.46696126e+02, 6.58730132e-01],
[1.78647420e+02, 7.45874224e-01],
[1.32254260e+02, 6.13874257e-01],
[1.09749986e+02, 5.22003253e-01],
[1.86498250e+02, 7.65890838e-01],
[1.04982728e+02, 3.80887466e-01],
[1.33737919e+02, 2.51650906e-01],
[1.82826134e+02, 1.13827615e-01],
[2.35498810e+02, 8.84579966e-01],
[1.79792755e+02, 7.48819153e-01],
[2.28720134e+02, 8.68636214e-01],
[1.84258489e+02, 1.10184840e-01],
[1.14024359e+02, 3.26492005e-01],
[1.24954160e+02, 2.81855776e-01],
[1.87420827e+02, 1.02185763e-01],
[1.05184212e+02, 3.79168955e-01],
[1.02100549e+02, 4.51851906e-01],
[1.35727179e+02, 2.45224309e-01],
[1.07192121e+02, 5.06261248e-01],
[1.14877666e+02, 3.26241845e-01],
[2.25763511e+02, 8.61637911e-01],
[1.03963406e+02, 4.79881898e-01],
[1.18211304e+02, 3.08031447e-01],
[1.09961588e+02, 3.47209860e-01],
[1.81542333e+02, 1.17103490e-01],
[1.14098289e+02, 3.26145185e-01],
[1.18617789e+02, 3.06347578e-01],
[2.24377929e+02, 8.58350258e-01],
[1.53505237e+02, 6.78345791e-01],
[1.85449945e+02, 7.63240042e-01],
[1.17354239e+02, 5.58766835e-01],

```

```
[68] np.savetxt('dados.csv', dados, delimiter=',')
```

