

Transferring from orbit to intermediate orbit.

$$\frac{-GMe m}{2r_1} + \frac{1}{2} m v^2 = \frac{-GMe m}{r_1 + r_2}$$

$$2 \left(\frac{GMe}{2r_1} - \frac{GMe}{r_1 + r_2} \right) = v^2$$

$$\sqrt{\frac{GMe}{r_1}} \sqrt{\frac{r}{r_1 + r_2}} = V_1$$

$$\Rightarrow \Delta V_1 = \sqrt{\frac{GMe}{r_1}} \left(\sqrt{\frac{r}{r_1 + r_2}} - 1 \right)$$

for transforming from intermediate orbit.

$$\frac{-GMe m}{r + r_2} + \frac{1}{2} m v^2 = \frac{-GMe m}{2r_2}$$

$$\Delta V_2 = \sqrt{\frac{GM}{r}} \left(1 - \sqrt{\frac{2r_2}{r_1 + r_2}} \right)$$

$$\Delta V_{\text{total}} = \Delta V_1 + \Delta V_2$$

$$= \sqrt{\frac{GM}{r_2}} \left(\sqrt{\frac{2r}{r_1 + r_2}} - 1 \right) + \sqrt{\frac{GM}{r_2}} \left(1 - \sqrt{\frac{2r}{r_1 + r_2}} \right)$$

On putting value of geostationary orbit

$$r_1 = 38000 \text{ Km} = 42200 \text{ km}$$

$$r_2 = 36000 \text{ Km} = 42450 \text{ km}$$

$$(\Delta V_{\text{total}})_1 = \Delta V_1 + \Delta V_2 = 9.07 \text{ m/s}$$

Similarly on putting values for transferring b/w
geostationary & ~~graveyard~~ orbit low earth
orbit

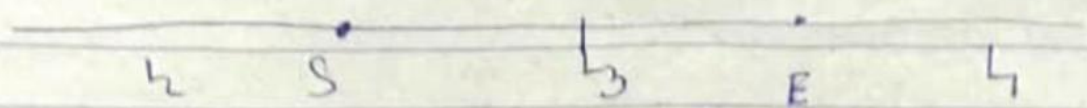
$$r_1 = 3800 + R_e = 42200$$

$$r_2 = 24000 + R_e = 68000$$

$$\left(\Delta V_{\text{total}} \right)_{\text{LEO}} = -3856 \text{ m/s}$$

$$\Delta V_{\text{total}} > (\Delta V)_{\text{geo}}$$

We would transfer to ~~graveyard~~
orbit



∴ for an equipotential region
 $V = \text{constant}$

$$\Rightarrow \frac{dV}{dx} = 0 \Rightarrow F = 0$$

$$\Rightarrow (F_G)_S + (F_G)_E = F_{\text{centrifugal force}} = F_c$$

For L1 region

$$\frac{G M_S}{(x+r_1)^2} + \frac{G M_E}{(x-r_2)^2} = G \frac{(M_S + M_E)}{R_{SE}^3} x$$

$$r_1 = \text{Distance of sun from COM} = \frac{M_E}{M_S + M_E} R$$

$$r_2 = \text{Distance of earth from COM} = \frac{M_S}{M_S + M_E} R$$

Putting the value of M_E , M_S and R

$$G M_S (x+r_1)^{-2} R^3 + G M_E (x-r_2)^{-2} R^3 = G (M_S + M_E) x$$

$$\Rightarrow M_S (x-r_1)^{-2} + M_E (x+r_2)^{-2} R^3 = (M_S + M_E) x$$

⑦

Putting
given $L_1 = R \left(1 + \left(\frac{m_E/m_S}{3} \right)^{1/3} \right)$

Putting L_1 in eqⁿ L_1 and checking whether
 L_1 satisfies eqⁿ 1 or not

$$L_1 \approx 1.5 - 1.515 \times 10^{11} \text{ km}$$

Putting it in eqⁿ 1

$$\text{eqⁿ ①} \approx 0$$

$\rightarrow L_1$ satisfies eqⁿ ①

Similarly for L_2

eqⁿ ②

$$\frac{GM_S}{(x-r)^2} - \frac{GM_E}{(x+r)^2} - \frac{G(M_S+M_E)}{R^2} x = 0$$

$$\Rightarrow -M_S(x-r)^2 R^3 + GM_E(x+r)^2 R^3 = (M_S+M_E)xR^3$$

$$\Rightarrow \text{for } L_2 = 1.48 \times 10^{11} \text{ km} \quad L_2 = \left(1 - \left(\frac{m_E}{3m_S} \right)^{1/3} \right) R$$

Putting L_2 in eqⁿ ②

$$L_2 \text{ in eqⁿ ②} \approx 0$$

$\Rightarrow L_2$ satisfies eqⁿ ②

for L_3

$$\frac{G M_2}{(a-r)^2} - \frac{h^2 \omega}{(a-r)^2} = \frac{G M_2}{(a-r)^2} \lambda \quad \text{--- (3)}$$

$$L_3 = -1.5000187 \times 10^{11} \quad L_3 = -R \left(1 + \frac{S}{h} \right)$$

So for further $L_3 = \text{in eq (3)}$

$$e_4^h(5) = 0$$

$\Rightarrow L_3$ satisfies eq (3)

$$\Rightarrow R \left(1 + \frac{S M_2}{h} \right)$$

3) The fig. illustrate how a spacecraft can achieve an extraordinary Δv using a gravity orbit. It changes the direction of probe motion in such a way that the velocity components (due to the relative motion w.r.t the sun & jupiter) add up at an obtuse angle as probe reaches jupiter from the plane. This manoeuvre would require an enormous amount of propellant, the planet's absence.