

Screening of Highly Active Hydrogen Evolution Reaction Catalysts: Comparative Analysis of Typical Machine Learning Methods

Warren Wilson College

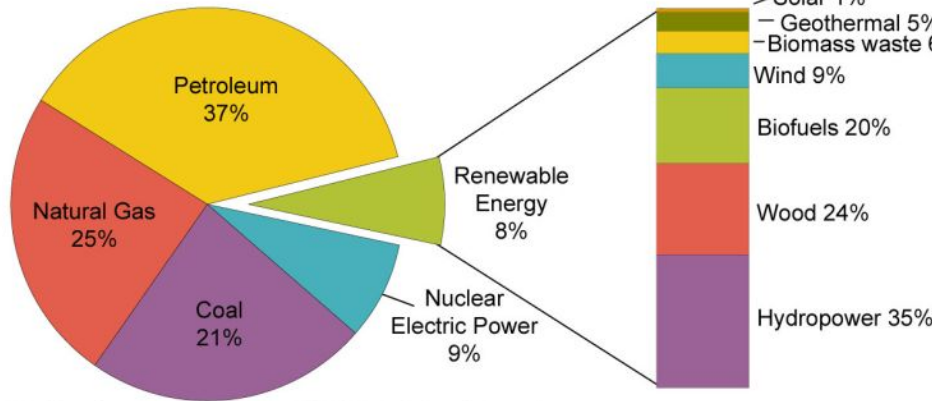
Jordan Mershimer

4/14/2023

The Energy Problem

U.S. Energy Consumption by Energy Source, 2009

Total = 94.578 Quadrillion Btu



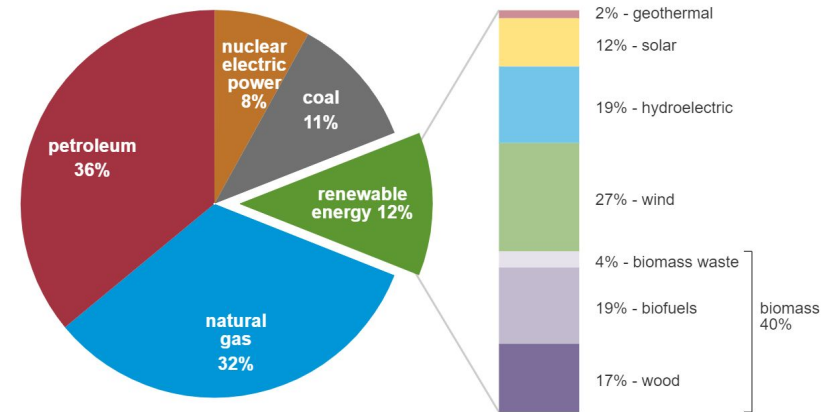
Note: Sum of components may not equal 100% due to independent rounding.

Source: U.S. Energy Information Administration, *Annual Energy Review 2009*, Table 1.3, Primary Energy Consumption by Energy Source, 1949-2009 (August 2010).

U.S. primary energy consumption by energy source, 2021

total = 97.33 quadrillion
British thermal units (Btu)

total = 12.16 quadrillion Btu



Data source: U.S. Energy Information Administration, *Monthly Energy Review*, Table 1.3 and 10.1, April 2022, preliminary data

Note: Sum of components may not equal 100% because of independent rounding.

- Renewable Energy: naturally replenishing but **flow-limited**
- Non-renewable Energy: Will not be replenished for thousands or even millions of years

Energy Storage approaches

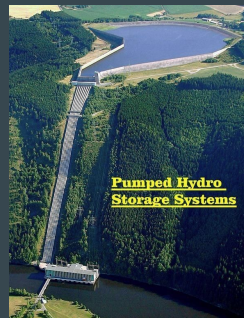
Batteries

- Degrades over time
- Some require rare-earth minerals to manufacture
- Manufacturing process could be detrimental to the environment



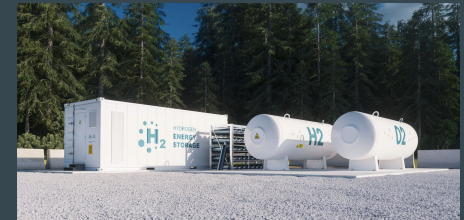
Pumped Storage Hydropower

- Costly to build
- Sizable physical footprint
- Not applicable to all environments



Hydrogen Gas

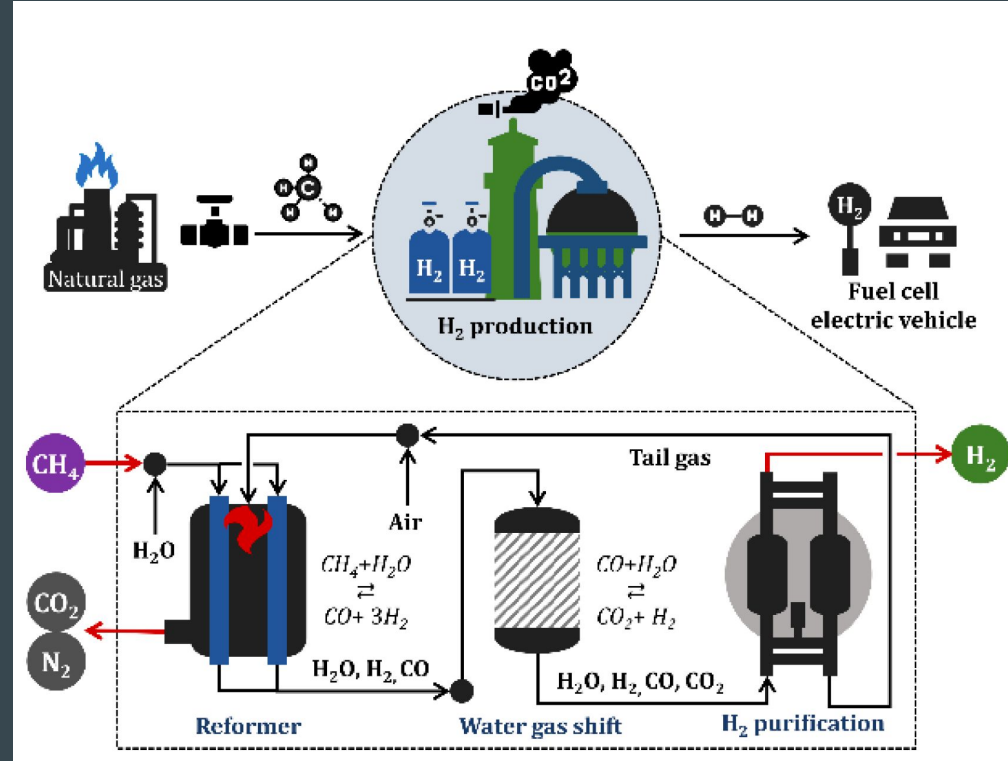
- Can use existing fossil fuel infrastructure
- Produces water when combusted
- Can be stored as liquid, solid, or gas.



Hydrogen gas production

Steam Methane Reforming

- 80-85% of current hydrogen gas produced is by steam methane reforming
- Relies on fossil fuels
- Produces CO_2

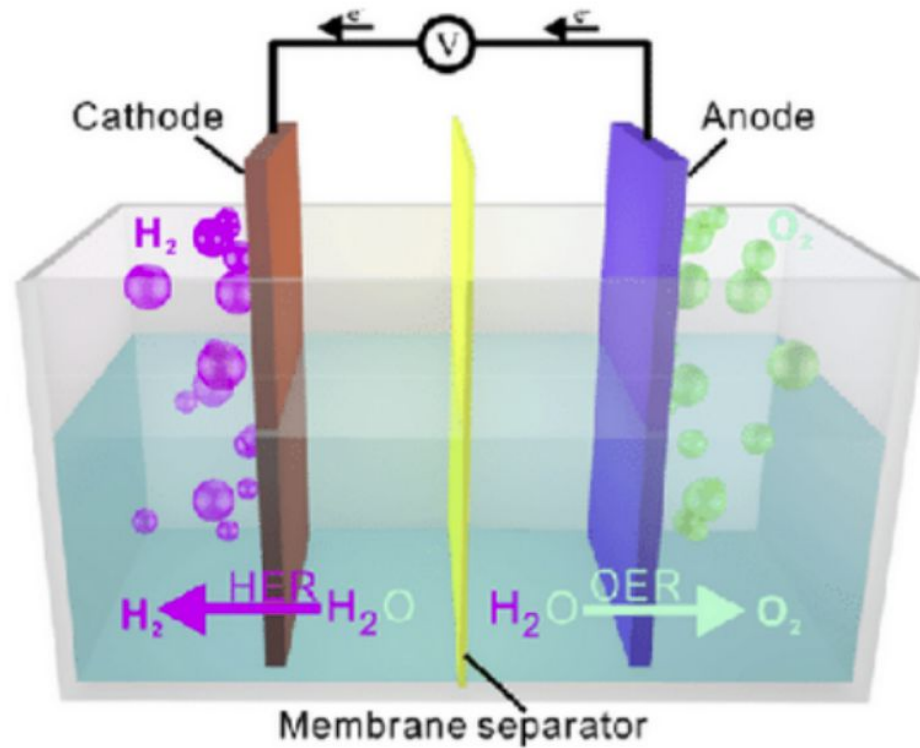


- (13) Barelli, L.; Bidini, G.; Gallorini, F.; Servili, S. Hydrogen Production through Sorption-Enhanced Steam Methane Reforming and Membrane Technology: A Review. *Energy* **2008**, 33 (4), 554–570.
- (14) Simpson, A. P.; Lutz, A. E. Exergy Analysis of Hydrogen Production via Steam Methane Reforming. *Int. J. Hydrog. Energy* **2007**, 32 (18), 4811–4820.

Hydrogen gas production

Water Electrolysis

- Water can be split into hydrogen gas and oxygen through Water Electrolysis.
- This reaction requires an overpotential of energy to occur, reducing the efficiency.
- The most efficient catalysts are composed of noble-metals elements like Pt, Ru, ...



(16) Zhu, J.; Hu, L.; Zhao, P.; Lee, L. Y. S.; Wong, K.-Y. Recent Advances in Electrocatalytic Hydrogen Evolution Using Nanoparticles. *Chem. Rev.* **2020**, *120* (2), 851–918.

(17) Zhao, G.; Rui, K.; Dou, S. X.; Sun, W. Heterostructures for Electrochemical Hydrogen Evolution Reaction: A Review. *Adv. Funct. Mater.* **2018**, *28* (43), 1803291.

Indicator of a good catalyst

Gibbs Free Energy

- The interactions between the catalyst and Hydrogen should be "just right".
- Hydrogen adsorption free energy (ΔG_{H}) close to zero.

Active Sites

- Large number of sites where HER can occur on the surface of the material.

Stable

- Stable in wide range of pH conditions.
- Easy to work with and apply to cathodes.

(22) Lukowski, M. A.; Daniel, A. S.; Meng, F.; Forticaux, A.; Li, L.; Jin, S. Enhanced Hydrogen Evolution Catalysis from Chemically Exfoliated Metallic MoS₂ Nanosheets. *J. Am. Chem. Soc.* 2013, 135 (28), 10274–10277.

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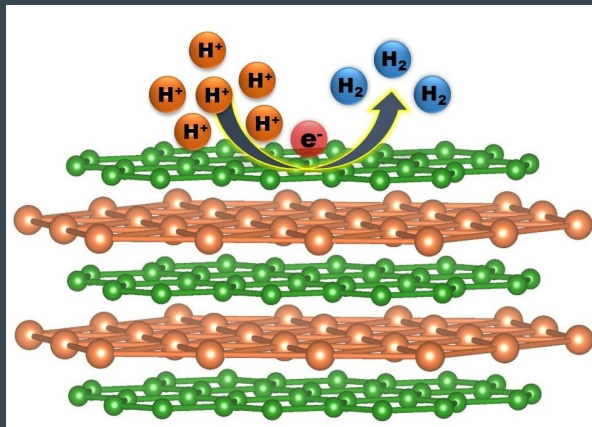
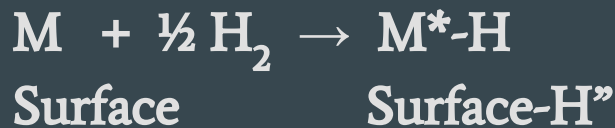
Indicator of a good catalyst

Sabatier principle:

The interactions between the catalyst and Hydrogen should be "just right"; that is, neither too strong nor too weak.



Hydrogen adsorption free energy (ΔG_{H}) close to zero.



Catalyst Progress

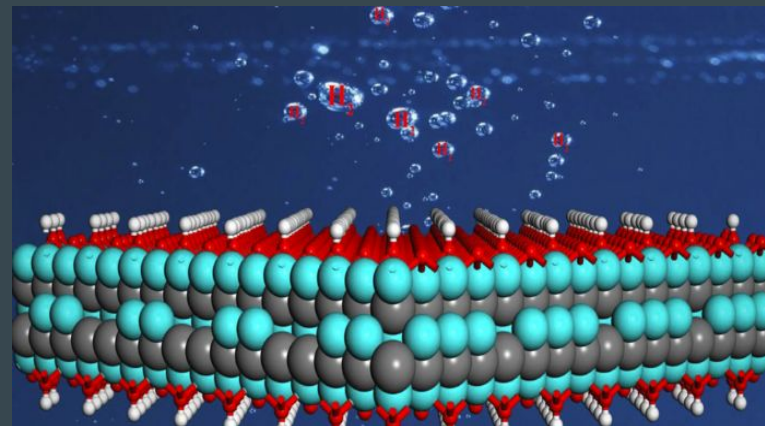
2D materials:

2-dimensional materials offer unique advantages as catalysts.

- Can be uniformly deposited on a cathode
- Large surface area

Current 2D HER catalysts offer some disadvantages..

- Low number of active sites.
- Poor charge-transfer performance
- Unstable under ambient conditions



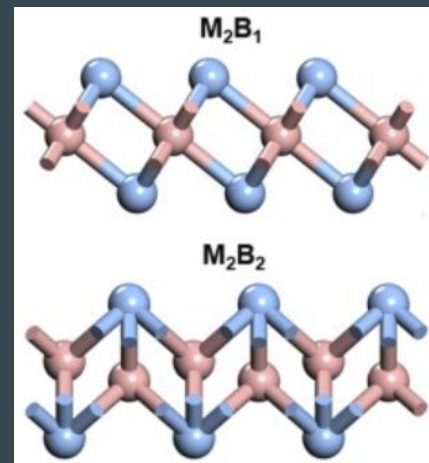
MXenes & MBenes:

2-dimensional materials composed of early transitional metal (M) from 3B, 4B, and 5B on the periodic table and Boron (B) or Nitrogen, Carbon (X).

Details:

- Inexpensive composition
- Not thoroughly explored

3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 9	10 VIII 10
21 Sc Scandium 44.95591	22 Ti Titanium 47.88	23 V Vanadium 50.9415	24 Cr Chromium 51.9961	25 Mn Manganese 54.938	26 Fe Iron 55.847	27 Co Cobalt 58.9332	28 Ni Nickel 58.6934
39 Y Yttrium 88.90585	40 Zr Zirconium 91.224	41 Nb Niobium 92.90638	42 Mo Molybdenum 95.94	43 Tc Technetium 98.9072	44 Ru Ruthenium 101.07	45 Rh Rhodium 102.9055	46 Pd Palladium 106.42
57-71	72 Hf Hafnium 178.49	73 Ta Tantalum 180.9479	74 W Tungsten 183.85	75 Re Rhenium 186.207	76 Os Osmium 190.23	77 Ir Iridium 192.22	78 Pt Platinum 195.08
13 IIIA 3A	14 IVA 4A	15 VA 5A					
5 B Boron 10.811	6 C Carbon 12.011	7 N Nitrogen 14.0074					



Lukowski, M. A.; Daniel, A. S.; Meng, F.; Forticaux, A.; Li, L.; Jin, S. Enhanced Hydrogen Evolution Catalysis from Chemically Exfoliated Metallic MoS₂ Nanosheets. *J. Am. Chem. Soc.* **2013**, *135* (28), 10274–10277.

Gao, G.; O'Mullane, A. P.; Du, A. 2D MXenes: A New Family of Promising Catalysts for the Hydrogen Evolution Reaction. *ACS Catal.* **2017**, *7* (1), 494–500.

Sun, X.; Zheng, J.; Gao, Y.; Qiu, C.; Yan, Y.; Yao, Z.; Deng, S.; Wang, J. Machine-Learning-Accelerated Screening of Hydrogen Evolution Catalysts in MBenes Materials. *Appl. Surf. Sci.* **2020**, *526*, 146522.

Catalyst discovery

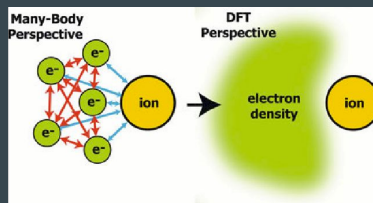
Experimentally

- Synthesizing a single material can take a few days
- Requires lab time, materials, and active work.
- Results are completely accurate



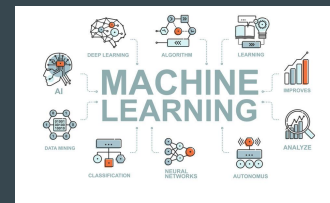
Density Functional Theory

- DFT is a computational method for modeling electronic structures of many-body systems.
- One result can take a few days or more
- Usually very accurate



Machine Learning

- Machine learning is the usage of computer algorithms to predict data.
- Depending on sample size, a model can be generated within seconds.
- Can be quite a complicated process



Project objective:

Compare typical machine learning methods
for Hydrogen Evolution Reaction (HER)
catalyst screening

Focus: MXenes, MBenes

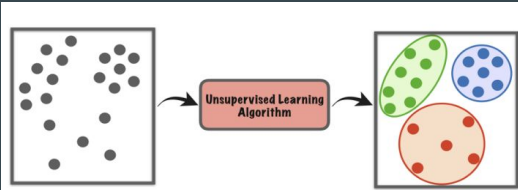
Early Transitional Metals (M). Boron (B), Carbon,
Nitrogen (X). Ratios: 1:1, 1:2, 2:1, 3:4, 5:2.

3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8	9 VIII 9	10 VIII 10
21 Scandium 44.95591	22 Titanium 47.88	23 Vanadium 50.9415	24 Chromium 51.9961	25 Manganese 54.938	26 Iron 55.847	27 Cobalt 58.9332	28 Nickel 58.6934
39 Yttrium 88.90584	40 Zirconium 91.224	41 Niobium 92.90638	42 Molybdenum 95.94	43 Technetium 98.9062	44 Ruthenium 101.07	45 Rhodium 102.9055	46 Palladium 106.42
57-71 Lanthanides	72 Hafnium 178.49	73 Tantalum 180.9479	74 Tungsten 183.84	75 Rhenium 186.207	76 Osmium 190.23	77 Iridium 192.22	78 Platinum 195.08
13 IIIA 3A	14 IVA 4A	15 VA 5A					
5 Boron 10.811	6 Carbon 12.011	7 Nitrogen 14.00644					

Types of machine learning

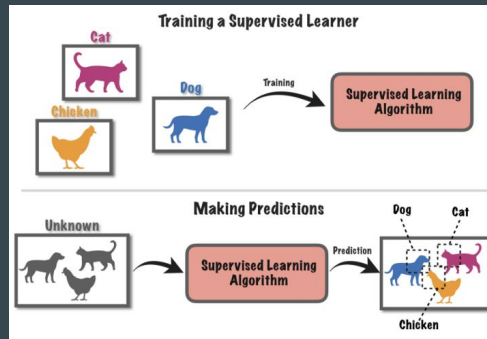
Unsupervised

- No labels
- No feedback
- Find hidden structures or associations in data



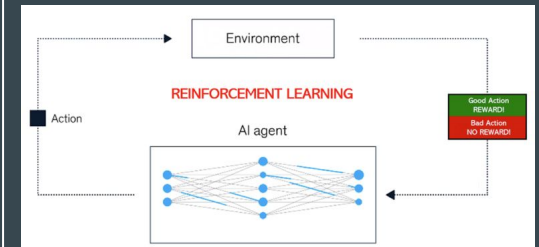
Supervised

- Labeled data
- Direct feedback
- Predict outcomes



Reinforcement

- Decision Process
- Reward System
- Learn series of actions to predict outcome



Methods

Models: Kernel Ridge, Decision Tree, Gaussian Process, Ordinary Least Squares, Multilayer Perceptron, Support Vector Machines, Random forest, Kernel Ridge Cross Validation.

Comparison: Root Mean Squared Error, Model Generation and Prediction Time.

Model Generation (published data.²⁴): $M_n B_m$, $M_n X_m$.
 $n:m = 2:1, 2:2, 2:3, 4:3, 3:2$.
 Various known catalysts.

Materials Predicted: $M_n B_m$, $M_n X_m$.
 $n:m = 1:1, 1:2, 2:1, 3:4, 5:2$.

Training:Testing Split = 75%:25%.
 300 Materials were predicted

Elemental Descriptors	Material Descriptors
M/X Number	Gibbs Free energy
M/X Group	M/X Ratio
M/X Row	
M/X Mass	
M/X Density	
M/X Inter-atomic Distance	
M/X Covalent Radius	
M/X First Ionization Energy	
M/X Electron Affinity	

Methods

Check out the code, modify it, use it.

<https://github.com/Jmersh/NSURS-HER-ML>

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
	Metal Symbol		M Number	X Symbol	X Number	Metal Sym Number	Metal Group	Metal Row	Metal Mass	Metal Density	Metal Inter-atomic Distance	Metal Covalent Radius	Metal First Ionization Energy	Metal Electron Affinity	X Sym Number	X Group	X Row	X Mass	X Density	X Inter-atomic Distance	X Covalent Radius	X First Ionization Energy	X Electron Affinity
IrC	Ir		1	C	1	77	9	6	192.217	22.42	2.423641628	1.41	8.96702	1.5643615	77	14	2	12.0107	2.2	2.085122401	0.76	11.260288	1.262113612
IrC2	Ir		1	C	2	77	9	6	192.217	22.42	2.423641628	1.41	8.96702	1.5643615	77	14	2	12.0107	2.2	2.085122401	0.76	11.260288	1.262113612
Ir2C	Ir		2	C	1	77	9	6	192.217	22.42	2.423641628	1.41	8.96702	1.5643615	77	14	2	12.0107	2.2	2.085122401	0.76	11.260288	1.262113612
Ir3C4	Ir		3	C	4	77	9	6	192.217	22.42	2.423641628	1.41	8.96702	1.5643615	77	14	2	12.0107	2.2	2.085122401	0.76	11.260288	1.262113612
Ir5C2	Ir		5	C	2	77	9	6	192.217	22.42	2.423641628	1.41	8.96702	1.5643615	77	14	2	12.0107	2.2	2.085122401	0.76	11.260288	1.262113612

```
64 for M_MatN2 in M_Mat: # Two for loops are nested together to iterate through each combination of M and X
65     # materials, could use simpler method.
66     for X_MatN2 in X_Mat:
67         ps = pt.elements.symbol # Declare ps as shorthand for longer function
68         pyme = pymatgen.core.periodic_table.Element # Pymatgen implementation
69         MatGenTestCSVWrite.writerow([(M_MatN2 + X_MatN2), M_MatN2, "1", *X_MatN2, "1",
70                                     pyme(M_MatN2).number, pyme(M_MatN2).group, pyme(M_MatN2).row,
71                                     ps(M_MatN2).mass, ps(M_MatN2).density, ps(M_MatN2).interatomic_distance,
72                                     ps(M_MatN2).covalent_radius, pyme(M_MatN2).ionization_energy,
73                                     pyme(M_MatN2).electron_affinity,
74                                     pyme(M_MatN2).number, pyme(X_MatN2).group, pyme(X_MatN2).row,
75                                     ps(X_MatN2).mass, ps(X_MatN2).density, ps(X_MatN2).interatomic_distance,
76                                     ps(X_MatN2).covalent_radius, pyme(X_MatN2).ionization_energy,
77                                     pyme(X_MatN2).electron_affinity)])
78     # Above writes rows of each iteration of the M and X materials along with descriptors such as
79     # mass etc.
```

```
13 def plotdata(model):
14     testdata = pd.read_csv('Models/' + model + '/TestArray.csv')
15     traindata = pd.read_csv('Models/' + model + '/TrainArray.csv')
16     fig, ax = plt.subplots()
17
18     ax.scatter([testdata.iloc[:, 0]], [testdata.iloc[:, 1]], color='blue', marker='o', edgecolors='white', alpha=0.8)
19     ax.scatter([traindata.iloc[:, 0]], [traindata.iloc[:, 1]], color='green', marker='s', edgecolors='white', alpha=0.8)
20     ax.legend(['Testing Data', 'Training Data'])
21     plt.axis([-1.5, 0.5, -1.5, 0.5])
22     plt.title(model + " Pred E vs Actual E", pad=15)
23     plt.xlabel("Predicted  $\delta$ ")
24     plt.ylabel("Actual  $\delta$ ")
25     line = mlines.Line2D([0, 1], [0, 1], color='red', linestyle='dashed')
26     transform = ax.transAxes
27     line.set_transform(transform)
28     ax.add_line(line)
29     circlehighlight = plt.Circle((0, 0), 0.15, color='r', fill=False)
30     plt.gca().add_patch(circlehighlight)
31     plt.savefig('Models/' + model + '/TrainVSTest.png')
32     plt.show()
33
34
```

```
211 # RFR
212 t.start()
213 rfr = RandomForestRegressor(max_depth=20)
214 GenModel(rfr, 1).ReturnArray("RFR")
215 t.stop()
216
217 t.start()
218 GenModel(rfr, 1, p=1).ReturnArray("RFR", p=1)
219 t.stop()
220
```

```
59 plotdata('DTR')
60 plotdata('GPR')
61 plotdata('KRR')
62 plotdata('MLPR')
63 plotdata('OLS')
64 plotdata('RFR')
65 plotdata('RidgeCV')
66 plotdata('SVR')
```

- Kmeans Clustering Intro.py
- KmeansMatRender.py
- LearningModelGen.py
- LearningModelGenBeta.py
- MatGen.py
- MatGenOutput.csv
- MatGenRender.py
- ModelRender.py
- PyPlot Intro.py
- README.md
- TrainData.csv
- TrainDataGen.py
- TrainDataOutput.csv
- TrainingData.csv

- Models
 - DTR
 - MatGenArray.csv
 - RMSEArray.csv
 - RMSEBar.png
 - TestArray.csv
 - TrainArray.csv
 - TrainVSTest.png
 - GPR
 - KRR
 - MLPR
 - OLS
 - RFR
 - RidgeCV
 - SVR



Comparison

We found that Random Forest Regression (RFR) produced the lowest testing RMSE and was chosen to predict our 300 materials.

Models were trained on published training data²⁴.

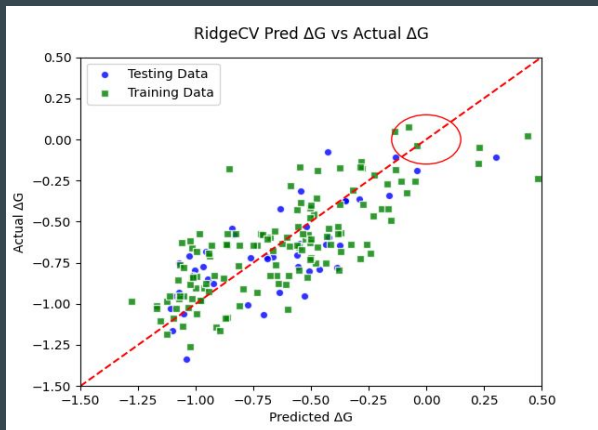
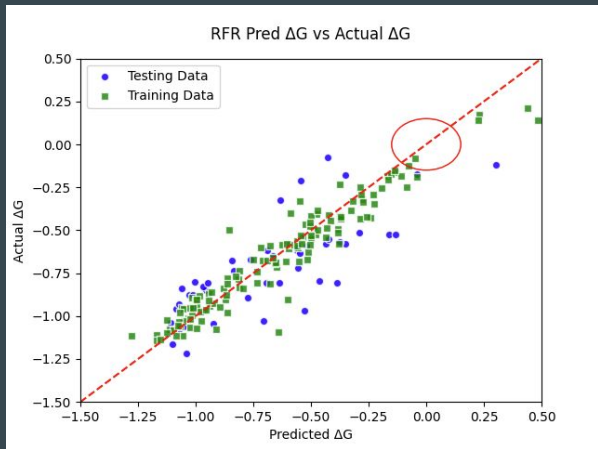
Models are not completely optimized.

	Training RMSE	Testing RMSE	Model Generation Time (s)	Model Prediction Time (s)
OLS	0.2504	0.2798	0.0124	0.0140
GPR	0.2516	0.2722	0.0697	0.0418
KRR	0.2665	0.2810	0.0146	0.0156
RidgeCV	0.2528	0.2727	0.0127	0.0130
SVR	0.3454	0.3469	0.0128	0.0196
DTR	0.0894	0.3304	0.0105	0.0129
<u>RFR</u>	<u>0.1011</u>	<u>0.2702</u>	<u>0.1107</u>	<u>0.1247</u>
MLPR	0.1357	0.2978	1.7014	1.6907

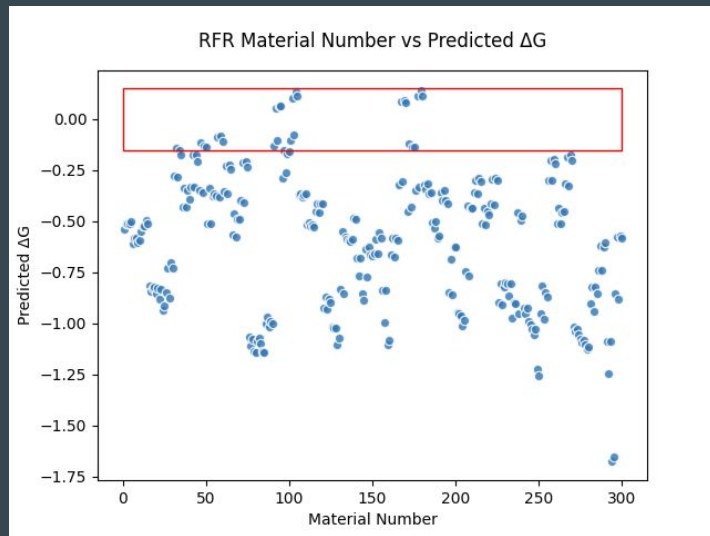
Lower RMSE is better. RMSE Results are averaged over 10 different training/testing split randomizations. Predicted 300 materials.

(24) Sun, X.; Zheng, J.; Gao, Y.; Qiu, C.; Yan, Y.; Yao, Z.; Deng, S.; Wang, J. Machine-Learning-Accelerated Screening of Hydrogen Evolution Catalysts in MBenes Materials. *Appl. Surf. Sci.* **2020**, 526, 146522.

Model Prediction Results



Random Forest Regression (RFR)



Number	Predicted Gibbs Free Energy	Name	Screen
32	-0.13946	RuC2	Yes
34	-0.15172	Ru3C4	Yes
47	-0.11625	CoC2	Yes
49	-0.13134	Co3C4	Yes
91	-0.1281	NiC	Yes
92	0.053562	NiC2	Yes

29 materials were within ± 0.16 eV of 0. Table represents some data. 10-fold reduction.

Summary

- We applied various machine learning models to predict the probability of a list of 300 transition metal borides, carbides, and nitrides being a highly efficient HER catalyst.
- Our results showed that the Random Forest Regression model produced the lowest testing RMSE and was chosen to examine the 300 materials, Out of which 29 materials were predicted to be high-performance HER catalysts.
- Our approach can efficiently identify promising HER catalysts with high accuracy, providing guidance for further experimental and theoretical investigations.
- Future research could include experimental verification of our 29 materials or further research and optimization of our machine learning approach.

Project Team



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Me



Yuemei Zhang, Ph.D.

Head Advisor



Langdon Martin, Ph.D.

Advising Committee



Kim Borges, Ph.D.

Advising Committee

Acknowledgement

Scikit-learn: Machine Learning in Python, Pedregosa et al., JMLR 12, pp. 2825-2830, 2011.



The Matplotlib development team



Shyue Ping Ong, William Davidson Richards, Anubhav Jain, Geoffroy Hautier, Michael Kocher, Shreyas Cholia, Dan Gunter, Vincent Chevrier, Kristin A. Persson, Gerbrand Ceder. Python Materials Genomics (pymatgen) : A Robust, Open-Source Python Library for Materials Analysis. Computational Materials Science, 2013, 68, 314–319. doi:10.1016/j.commatsci.2012.10.028



The pandas development team



Harris, C.R., Millman, K.J., van der Walt, S.J. et al. Array programming with NumPy. Nature 585, 357–362 (2020).

San Diego Supercomputer Center



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- (3) Kaunda, R. B. Potential Environmental Impacts of Lithium Mining. *J. Energy Nat. Resour. Law* **2020**, *38* (3), 237–244.
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