

Math 201  
Fall 2019  
Midterm1  
10/04/2019  
Time Limit: 50 minutes

Name (Print): \_\_\_\_\_

This exam contains 9 pages (including this cover page) and 4 problems. Check to see if any pages are missing.

***Statement of Ethics***

I agree to complete this exam without unauthorized assistance from any person, materials, or device.

Signature \_\_\_\_\_ Date \_\_\_\_\_

- 1 Fuentes T 1:30 - 2:20 Bloomberg 278
- 2 Quinan T 3:00 - 3:50 Hodson 301
- 3 Quinan T 4:30 - 5:20 Hodson 216
- 4 Luo Th 1:30 - 2:20 Bloomberg 278
- 5 Luo Th 3:00 - 3:50 Maryland 309

Your section number: \_\_\_\_\_

You are required to show your work on each problem on this exam. The following rules apply:

- **Organize your work**, in a reasonably neat and coherent way, in the space provided.
- **No partial credit for any 1 point problem.** A correct answer, unsupported by calculations, explanation, or algebraic work will receive no credit.
- If you need more space, use the back of the pages; clearly indicate when you have done this.
- **Any answer or solution on scratch paper will receive no credit.**

Problem	Points	Score
1	5	
2	5	
3	5	
4	5	
Total:	20	

Do not write in the table to the right.

1. (a) (1 point) For which values of  $a, b, c, d, e$  is the following matrix in reduced row-echelon form?

$$\begin{bmatrix} 1 & a & 2 & 1 & b \\ 0 & 1 & 0 & c & d \\ 0 & 0 & e & 0 & 0 \end{bmatrix}.$$

- (b) (1 point) Let

$$A = \begin{bmatrix} 1 & a & b \\ a & 1 & b \\ a & b & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix},$$

Compute  $AB$ .

(c) (3 points) Consider the equations

$$\begin{cases} x + 2y + 3z &= 4 \\ x + ky + 4z &= 6 \\ x + 2y + (k + 2)z &= 6 \end{cases},$$

where  $k$  is an arbitrary constant. (1) For which values of the constant  $k$  does this system have a unique solution? (1pt) (2) When is there no solution? (1pt) (3) When are there infinitely many solutions? (1pt)

2. (a) (1 point) Find the matrix  $P$  of the orthogonal projection onto the line spanned by  $\vec{w} = (5, 12)$ .

- (b) (2 points) What's the matrix  $A$  of a counterclockwise rotation in  $\mathbb{R}^2$  through the angle  $\frac{\pi}{2}$ ? (1pt) Compute  $A^2$ . (1pt)

- (c) (2 points) Let  $L$  be the line defined by  $2x + y = 0$ , let  $\mathbf{x} = (1, 2)$ , find the reflection of  $\mathbf{x}$  about  $L$ .

3. (a) (2 points) Use Gauss-Jordan elimination to compute  $\text{rref}(A)$ , where  $A = \begin{bmatrix} 1 & 0 & 2 & 4 \\ 0 & 1 & -3 & -1 \\ 3 & 4 & -6 & 8 \\ 0 & -1 & 3 & 4 \end{bmatrix}$ .

(b) (3 points) For which values of the constant  $k$  is the following matrix invertible?

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & k \\ 1 & 4 & k^2 \end{bmatrix}$$

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4. (5 points) Find all the possible solutions of the equation  $A \cdot A^T = I_2$ , where  $A$  is a  $2 \times 3$  matrix,  $A^T$  is the transpose matrix of  $A$ ,  $I_2$  is the  $2 \times 2$  identity matrix.



Please estimate your score. You can also provide your suggestion for the course here.