

Infix, Postfix, Prefix Notations

operand: The character or the number that the operation is going to be done on.

Ex: 1 'a' 100 'abc'

operator: A symbol that is going to represent an operation to be done on an operand.

Ex: + - * / ^

Expression: A sequence of operands and operations that when evaluated, produces a single value.

Ex: $4 + 2 = 6$

Diagram labels: 'operand' points to 4, 'operand' points to 2, 'value' points to 6. 'operator' points to +.

$2 + 4 * 2 / 2 = 6$

Diagram labels: 'operand' points to 2, 'operand' points to 4, 'operand' points to 2, 'operand' points to 2, 'value' points to 6. 'operator' points to +, 'operator' points to *, 'operator' points to /.

Infix, Postfix, Prefix Notations are used to represent mathematical expressions, but the order of operands, operators are different in each of them.

Infix: operators are placed between the operands

operand1 operator operand2
4 + 2

Postfix: operators are placed after the operands.

operand1 operand2 operator
4 2 +

Prefix: operators are placed before the operands.

operator operand1 operand2
+ 4 2

All of the above notations means the same thing, $4 + 2 = 6$

Advantages: Prefix and postfix don't need to follow precedence or associative rule.

operator	Associative Rule	Precedence
\wedge	Right to left	Highest
$*, /$	Left to right	Higher
$+, -$	Left to right	Lowest

Precedence: It shows which operation should be done first; an operator with highest precedence should be performed first.

Associative: It specifies from which direction the operations should be performed.

Examples

Precedence: $4 + 2/2 = 5$

Associative ($L \rightarrow R$): $8 + 2 - 9 = 1$

Associative ($R \rightarrow L$): $2 \wedge 1 \wedge 10$

$$1 \wedge 10 = 1$$

$$2 \wedge 1 = 1$$

Infix to Postfix Conversion: parenthesis all the operands around the operators.

start converting to postfix from operators with highest priority

Ex: $x + y * z \Rightarrow (x + (y * z)) \Rightarrow (x + (yz*)) \Rightarrow xyz*+$

Ex: $(x + y) * z \Rightarrow ((x + y) * z) \Rightarrow ((xy+) * z) \Rightarrow xy+z*$

Infix to Prefix Conversion:

- parenthesise every expression

- start conversion from the operators with highest precedence

Ex: $x + y * z \Rightarrow (x + (y * z)) \Rightarrow (x + (*yz)) \Rightarrow +x*yz$

Ex: $(x + y) * z \Rightarrow ((x + y) * z) \Rightarrow ((+xy) * z) \Rightarrow *+xyz$

