

Decimal to binary Given an integer N , convert to its binary representation.

Idea: As long as the given number is greater than zero

- ① create a placeholder for the answer.
- ② start a loop and at each iteration.
 - add the result of $(N\%2)$ to result.
 - update N to $N//2$.
- ③ when $N \leq 0$, break out of the loop.

```
def toBinary(N):  
    answer = ""  
    while N > 0:  
        removed = (N%2)  
        // Add the remainder to the answer  
        answer = answer + str(removed)  
        // update N by removing its last digit  
        N = N//2  
    return answer
```

Let's say $N=7$, we want to find its binary representation

N	N%2	answer	N//2	N > 0
7	1	1	$7//2 = 3$	yes
3	$3\%2 = 1$	"1" + "1" = "11"	$3//2 = 1$	yes
1	$1\%2 = 1$	"11" + "1" = "111"	$1//2 = 0$	No, break, return answer

Now, if the goal is to find the representation for all numbers in range of 1 to N, The above function should be called for each integer.

```
def generate(n):
```

```
    answer = []
```

```
    for i in range(1, n+1):
```

```
        // calling toBinary function for each number and saving the result
```

```
        answer.append(toBinary(i))
```

```
    return answer
```

Analysis

def toBinary(N): It can be observed that The growth of This function is depends on integer N and at every Iteration we are reducing by half and we stop when N becomes 1

N=10

$10//2 = 5$

$5//2 = 2$

$2//2 = 1$ stop

N=16

$16//2 = 8$

$8//2 = 4$

$4//2 = 2$

$2//2 = 1$ stop

$$\log_2(16) = \log_2 2^4 = 4$$

$$\log_2(10) = \log_2 2^{3.32} = 3$$

Conclusion: It can observed the above function is a logarithmic function (Runs $\log_2 N$ times)

`def generate(n):` it has a simple for loop and that

runs N times, but inside the loop there is another function

which does $\log_2 N$ operations.

T.C = time complexity

overall T.C = outer loop * inner loop

$$= N * \log_2 N$$

Note: same goes with space complexity.