Intro to Stend Medi

Ex: ferromagnet

Ising Model: 17) chavi

$$H = \sum_{(i,j)} E_{ij} = \sum_{s \in S} s_{is} = \frac{1}{2} \sum_{s \in S} s_{is} = \frac{1}$$

microstate: {si}, sien

macrostate: macro observable E, M

$$M(ss;)) = M$$

micr mouro $ss;s$
 $+ + + | 3$
 $+ - | 1$
 $+ - + | 1$

: tendency of heat flow 154 law: DU = heat + work = Q + W DU = TAS - pay + MAN chempot.

du = TaS - pay + Man. = QUILIBRIUM Equilibilian N= const V= const "commical ensemble nothing (big) chary

Boltzmann distribution

In NVT equilibrium state with overey 5 houre prob

Avoy Everyy: $\langle E \rangle = \sum_{n} E_{n} P(E_{n}) = \sum_{n} E_{n} \frac{1}{2}e^{-\beta E_{n}}$ Sfeaker chem $N: \Omega = 2^{N}$ $\langle E \rangle = \sum_{n} E_{n} P(E_{n}) = \sum_{n} E_{n} \frac{1}{2}e^{-\beta E_{n}}$ Sfeaker chem $N: \Omega = 2^{N}$

$$= \frac{2^{-1} \sum \left(-\frac{9}{9\beta} e^{-\beta E_n}\right)}{n} = -\frac{2^{-1} \frac{9}{9\beta} \sum_{i=1}^{n} \frac{9}{2} \frac{2^{i}}{9\beta}} = -\frac{9 \ln^{2}}{2 \frac{3}{\beta}} = -\frac{9 \ln^{2}}{2 \frac{3}} = -\frac{9 \ln^{2}}{2$$

Z= Ze-BEU & partition function

$$P_{1} = \frac{1}{7}e^{-\beta \overline{E}_{1}}$$

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Relative probabilities between states are governed by the Boltzmann factor of the energy difference between stares.

This applies to any states — micro or macro — as long as the system is in equilibrium.

1) Sing model

$$H = - \mathcal{E} \mathcal{E}_{i,j} \mathcal{E}_{i,j}$$

$$P(\{s; \}) \times e^{-\beta H(\{s; \})}$$

$$\langle H \rangle$$

 $\langle E \rangle = \sum_{skles} E(s; z) e^{\int H(ss, z)}$

regions Sampling process in important

Metropolis algorizmi

- 1) picz Si randomly
- 2) flip spin (trial)

calc. $\Delta E = E' - E$ 3) acceptance $\Delta E <$ DE < 0 DE ZO

4) goto

E': trial

= : current empy

: accept : accept with probe

PHY432 Computational

pacc = min(1, e-BaE) -: g: reject "rejection saupling" ξ: accept ξ ~ Uco,1]

Vieep accepted and rejected steps (= pres.)

= H(trial) - H(auneux) = E'- E

ΔE

$$= -\varepsilon \left(S_{k-1}S_k + S_k S_{k+1} \right) = -\varepsilon S_k \left(S_{k-1}S_{k+1} \right)$$

Periodic hourslavy cord.

$$s_0 \equiv s_N$$

Sk 7 5k=5k (Sh.1+ Sh.1)

Nhy does hetropolis work:
(Markov Chain MC)
1) sequence of moves: moves steer in (i+2)
2) Marrov cord: prob to go from i > k only
depends on i
Hip spin 1 -> 2
orsauc: $E, < E_2 : \Delta E > 0$
accept p & e - BDE _B(E2-E1)
rate of state changes k12 = e
in the opposite dur. 2->1 DECO
accept: 1 $k_{21} = 1$

Equitibrium: DETAILED BALANCE Number of trees = number of transitions = 2 7 1 flux 1->2 flux 1->2 flux 2->2 p, e

probability flux = probability to be in initial state x rate to go from initial to final state

$$p_{1}k_{12} = p_{2}k_{21}$$

Metropolis: gystem etades distribute

Bo/Ensur

The probability ratio will be the Boltzmann factor for ANY states 1 and 2, so the Metropolis procedure will correctly sample from the Boltzmann distribution for all moves that follow the Metropolis criterion (and are "ergodic", i.e., any state can eventually be reached).