

# A Quick Guide for the pbdMPI Package (Ver. 0.2-3)

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**Warning:** The findings and conclusions in this article have not been formally disseminated by the U.S. Department of Energy and should not be construed to represent any determination or policy of University, Agency, and National Laboratory.

This document is written to explain the main functions of **pbdMPI** (Chen *et al.* 2012), version 0.2-3. Every effort will be made to ensure future versions are consistent with these instructions, but features in later versions may not be explained in this document.

Information about the functionality of this package, and any changes in future versions can be found on website: “Programming with Big Data in R” at <http://r-pbd.org/> (Ostrouchov *et al.* 2012).

## 1. Introduction

Our intent is to bring the most common parallel programming model from supercomputing, Single Program Multiple Data (SPMD), to R and enable distributed handling of truly large data. Consequently, **pbdMPI** is intended for batch mode programming with big data (pbd). Unlike **Rmpi** (Yu 2002), **snow** (Tierney *et al.* 2012), or **parallel** (R Core Team 2012), interactive mode is not supported. We think that interaction with a large distributed parallel computing platform is better handled with a client/server relationship, and we are developing other packages in this direction. **pbdMPI** simplifies MPI interaction, but leaves low and mid level functions available for advanced programmers. For example, it is easy to hand communicators to **pbdMPI** from other applications through MPI array pointers. This is intended for integration with other, possibly non-R, parallel software.

Under the SPMD parallel programming model, the identical program runs on every processor but typically works on different parts of a large data set, while communicating with other copies of itself as needed. Differences in execution stem from `comm.rank`, which is typically different on every processor. While on the surface this sounds complicated, after some experience and a new mindset, programming is surprisingly simple. There is no master. There is only cooperation among the workers. Although we target very large distributed computing platforms, SPMD works well even on small multicore platforms.

In the following, we list the main features of **pbdMPI**.

1. Under the SPMD batch programming model, a single program is written, which is spawned by `mpirun`. No spawning and broadcasting from within R are required.
2. S4 methods are used for most collective functions so it is easy to extend them for general R objects.
3. Default methods (like `Robj` functions in **Rmpi**) have homogeneous checking for data type so they are safe for general users.
4. The API in all functions is simplified, with all default arguments in control objects.
5. Methods for array or matrix types are implemented without serialization and un-serialization, resulting in faster communication than **Rmpi**.
6. Basic data types of integer, double and raw in **pbdMPI** are communicated without further checking. This is risky but fast for advanced programmers.

7. Character data type is serialized and communicated by raw type.

System requirements and installation of **pbdMPI** are described next. Section 2 gives a short example for comparing performance of **pbdMPI** and **Rmpi** (Yu 2002). In Section 8, a few quick answers for questions are given. Section ?? provides settings for Windows environments. In Section 3, two examples from **parallel** are shown as SPMD **pbdMPI** programs. Section 4 discusses long vector support and communication in **pbdMPI** as an extension from R. Finally, in Section 5, some simple input and output methods between regular text/csv/csv2 files and `data.frame` are introduced.

## 1.1. System Requirements

**pbdMPI** requires MPI ([http://en.wikipedia.org/wiki/Message\\_Passing\\_Interface](http://en.wikipedia.org/wiki/Message_Passing_Interface)). The package is mainly developed and tested under **OpenMPI** (<http://www.open-mpi.org/>) in xubuntu 11.04 (<http://xubuntu.org/>). The package should also work with MPICH2 (<http://www.mcs.anl.gov/research/projects/mpich2/>) and Microsoft MPI or MS-MPI ([http://msdn.microsoft.com/en-us/library/bb524831\(v=vs.85\).aspx](http://msdn.microsoft.com/en-us/library/bb524831(v=vs.85).aspx)). In addition to unix, **pbdMPI** should also run under other operating systems such as Mac OS X with OpenMPI or Windows 7 with MS-MPI if MPI is installed and launched properly, although we have not tested on multiple machines yet. Please let us know about your experience.

For normal installation, see Sec. 1.2. To build as a static library, which may be required on some large systems, use

Shell Command

```
./configure --enable-static --prefix=${MPI_ROOT}
make
make install
```

where `--enable-static` can build a static library (optional), and `${MPI_ROOT}` is the path to MPI root. Note that the static library is not necessary for **pbdMPI** but may avoid dynamic loading problems.

To make sure your MPI system is working, test with

Shell Command

```
mpiexec -np 2 hostname
```

This should list two host names where MPI jobs are running. Note to use `hostname.exe` with the extension on a Windows system.

## 1.2. Installation and Quick Start

One can download **pbdMPI** from CRAN at <http://cran.r-project.org>, and the intallation can be done with the following commands (using OpenMPI library)

Shell Command

```
tar zxvf pbdMPI_0.1-0.tar.gz
R CMD INSTALL pbdMPI
```

Further configure arguments include

Argument	Default
<code>--with-mpi-type</code>	OPENMPI
<code>--with-mpi-include</code>	<code>\${MPI_ROOT}/include</code>
<code>--with-mpi-libpath</code>	<code>\${MPI_ROOT}/lib</code>
<code>--with-mpi</code>	<code>\${MPI_ROOT}</code>

where `${MPI_ROOT}` is the path to the MPI root. For non-default and unusual installations of MPI systems, the commands may be

#### Shell Command

```
### Under command mode
R CMD INSTALL pbdMPI \
  --configure-args="--with-mpi-type=OPENMPI \
                   --with-mpi=/usr/local "
R CMD INSTALL pbdMPI \
  --configure-args="--with-mpi-type=OPENMPI \
                   --with-mpi-include=/usr/local/ompi/include \
                   --with-mpi-libpath=/usr/local/ompi/lib "
```

See the package source file `pbdMPI/configure` for details.

One can get started quickly with **pbdMPI** by learning from the following six examples.

#### Shell Command

```
### At the shell prompt, run the demo with 2 processors by
### (Use Rscript.exe for windows system)
mpiexec -np 2 Rscript -e "demo(allgather, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript -e "demo(allreduce, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript -e "demo(bcast, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript -e "demo(gather, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript -e "demo(reduce, 'pbdMPI', ask = F, echo=F) "
mpiexec -np 2 Rscript -e "demo(scatter, 'pbdMPI', ask=F, echo=F) "
```

### 1.3. Basic Steps

In the SPMD world, every processor is a worker, every worker knows about all the others, and each worker does its own job, possibly communicating with the others. Unlike the manager/workers style, SPMD is more likely to fully use the computer resources. The following shows typical basic steps of using **pbdMPI**.

1. Initialize. (`init`)
2. Read your portion of the data.
3. Compute. (`send`, `recv`, `barrier`, ...)
4. Communicate results among workers. (`gather`, `allgather`, `reduce`, `allreduce`, ...)

## 5. Finalize. (`finalize`)

In a given application, the Compute and Communicate steps may be repeated several times for intermediate results. The Compute and Communicate steps are more general than the “map” and “reduce” steps of the map-reduce paradigm but similar in spirit. One big difference is that the Communicate step may place the “reductions” on all processors rather than just one (the manager for map-reduce) for roughly the same time cost. With some experience, one can easily convert existing R scripts, and quickly parallelize serial code. **pbdMPI** tends to reduce programming effort, avoid complicated MPI techniques, and gain computing performance.

The major communication functions of **pbdMPI** and corresponding similar functions of **Rmpi** are listed in the following.

<b>pbdMPI</b> (S4)	<b>Rmpi</b>
<code>allgather</code>	<code>mpi.allgather</code> , <code>mpi.allgatherv</code> , <code>mpi.allgather.Robj</code>
<code>allreduce</code>	<code>mpi.allreduce</code>
<code>bcast</code>	<code>mpi.bcast</code> , <code>mpi.bcast.Robj</code>
<code>gather</code>	<code>mpi.gather</code> , <code>mpi.gatherv</code> , <code>mpi.gather.Robj</code>
<code>recv</code>	<code>mpi.recv</code> , <code>mpi.recv.Robj</code>
<code>reduce</code>	<code>mpi.reduce</code>
<code>scatter</code>	<code>mpi.scatter</code> , <code>mpi.scatterv</code> , <code>mpi.scatter.Robj</code>
<code>send</code>	<code>mpi.send</code> , <code>mpi.send.Robj</code>

## 1.4. More Examples

The package source files provide several examples based on **pbdMPI**, such as

Directory	Examples
<code>pbdMPI/inst/examples/test_spm/</code>	main SPMD functions
<code>pbdMPI/inst/examples/test_rmpi/</code>	comparison to <b>Rmpi</b>
<code>pbdMPI/inst/examples/test_parallel/</code>	comparison to <b>parallel</b>
<code>pbdMPI/inst/examples/test_performance/</code>	performance testing
<code>pbdMPI/inst/examples/test_s4/</code>	S4 extension
<code>pbdMPI/inst/examples/test_cs/</code>	client/server examples
<code>pbdMPI/inst/examples/test_long_vector/</code>	long vector examples

where `test_long_vector/` requires to recompile with setting

`pkg_constant.h`

```
#define MPI_LONG_DEBUG 1
```

in `pbdMPI/src/pkg_constant.h`. See Section 4 for details.

Further examples can be found at including:

- “Introduction to distributed computing with pbdR at the UMBC High Performance Computing Facility (Technical Report, 2013).” ([Raim 2013](#))

## 2. Performance

There are more examples for testing performance in `pbdMPI/inst/examples/test_rmpi`. Here, we only show a simple comparison of **pbdMPI** to **Rmpi**. The two scripts are equivalent for **pbdMPI** and **Rmpi**. We run them with two processors and obtain computing times listed below.

Save the following script in `demo_spmd.r` and run it with two processors by

Shell Command

```
mpiexec -np 2 Rscript demo_spmd.r
```

to see the computing time on your platform.

**pbdMPI** R Script

```
### Save this script in "demo_spmd.r".
library(pbdMPI, quietly = TRUE)
init()

time.proc <- list()
time.proc$default <- system.time({
  for(i in 1:1000) y <- allgather(list(x = 1:10000))
  barrier()
})

time.proc$matrix <- system.time({
  for(i in 1:1000) y <- allgather(matrix(1:10000, nrow = 100))
  barrier()
})

comm.print(time.proc, quiet = TRUE)
finalize()
```

Save the following script in `demo_rmpi.r` and run with two processors by

Shell Command

```
mpiexec -np 2 Rscript demo_rmpi.r
```

to see the computing time on your platform.

**Rmpi** R Script

```
### Save this script in "demo_rmpi.r".
library(Rmpi)
invisible(mpi.comm.dup(0, 1))

time.proc <- list()
time.proc$Robj <- system.time({
  for(i in 1:1000) y <- mpi.allgather.Robj(list(x = 1:10000))
  mpi.barrier()
})

time.proc$matrix <- system.time({
```



```

    for(i in 1:1000) y <- mpi.allgather.Robj(matrix(1:10000, nrow =
      100))
    mpi.barrier()
  })

if(mpi.comm.rank(1) == 0) print(time.proc)
mpi.quit()

```

The following shows the computing time of the above two scripts on a single machine with two processors Intel(R) Core(TM) i5-2410M CPU @ 2.30 GHz, xubuntu 11.04 system, and OpenMPI 1.6. The **pbdMPI** is more efficient than **Rmpi** with **list** and **matrix/array** data structures.

#### R Output

```

>> Output from demo_spmd.r
$default
  user  system elapsed
1.680   0.030   1.706

$matrix
  user  system elapsed
0.950   0.000   0.953

>> Output from demo_rmpi.r
$Robj
  user  system elapsed
2.960   0.090   3.041

$matrix
  user  system elapsed
3.120   0.030   3.147

```

### 3. SPMD in Examples from package parallel

We demonstrate how a simple script from **parallel** can be written in batch by using **pbdMPI**. Each time, we first give the version using **parallel** followed by the version using **pbdMPI**. All codes are available in `pbdMPI/inst/examples/test_parallel/`.

**Example 1:** (`mclapply()` originates in **multicore** ([Urbanek 2011](#)))

Save the following script in a file and run with

#### Shell Command

```
Rscript 01_mclapply_par.r
```

to see the computing time on your platform.

#### multicore R Script

```
### File Name: 01_mclapply_par.r
```

```
library(parallel)

system.time(
  unlist(mclapply(1:32, function(x) sum(rnorm(1e7))))
)
```

Now save this script in a file and run with

#### Shell Command

```
mpirun -np 2 Rscript 01_mclapply_spmd.r
```

to see the computing time on your platform.

#### SPMD R Script

```
### File Name: 01_mclapply_spmd.r
library(pbdMPI, quietly = TRUE)
init()

time.proc <- system.time({
  id <- get.jid(32)
  ret <- unlist(lapply(id, function(i) sum(rnorm(1e7))))
  ret <- allgather(ret, unlist = TRUE)
})
comm.print(time.proc)

finalize()
```

The following shows the computing time of the above codes on a single local machine with two cores Intel(R) Core(TM) i5-2410M CPU @ 2.30 GHz, xubuntu 11.04 system, and OpenMPI 1.6. There is not much communication latency in this example since all computings are on one “node” which is also a limitation of **parallel**.

#### R Output

```
>> Test ./01_mclapply_par.r
      user  system elapsed
16.800    0.570   17.419

>> Test ./01_mclapply_spmd.r
COMM.RANK = 0
      user  system elapsed
17.130    0.460   17.583
```

**Example 2:** (`parMM()` originates in **snow** (Tierney *et al.* 2012))

Save the following code in a file and run with two processors

#### Shell Command

```
Rscript 02_parMM_par.r
```

to see the computing time on your platform.

## snow R Script

```
### File Name: 02_parMM_par.r
library(parallel)
cl <- makeCluster(2)

splitRows <- function (x, ncl){
  lapply(splitIndices(nrow(x), ncl), function(i) x[i, , drop = FALSE])
}
parMM <- function (cl, A, B){
  do.call(rbind, clusterApply(cl, splitRows(A, length(cl)),
    get("%*%"), B))
}

set.seed(123)
A <- matrix(rnorm(1000000), 1000)
system.time(replicate(10, A %*% A))
system.time(replicate(10, parMM(cl, A, A)))

stopCluster(cl)
```

Now save this script in a file and run with

## Shell Command

```
mpirun -np 2 Rscript 02_parMM_spmd.r
```

to see the computing time on your platform.

## SPMD R Script

```
### File Name: 02_parMM_spmd.r
library(pbdMPI, quietly = TRUE)
init()

set.seed(123)
x <- matrix(rnorm(1000000), 1000)

parMM.spmd <- function(x, y){
  id <- get.jid(nrow(x))
  do.call(rbind, allgather(x[id,] %*% y))
}
time.proc <- system.time(replicate(10, parMM.spmd(x, x)))
comm.print(time.proc)

finalize()
```

The following shows the computing time of the above code on a single machine with two processors Intel(R) Core(TM) i5-2410M CPU @ 2.30 GHz, xubuntu 11.04 system, and OpenMPI 1.6. **pbdMPI** performs better than **snow** in this example even without communication over network.

## R Output

```
>> Test ./02_parMM_par.r
```

```

    user  system elapsed
12.460   0.170  12.625
    user  system elapsed
 1.780   0.820  10.095

>> Test ./02_parMM_spmd.r
COMM.RANK = 0
    user  system elapsed
  8.84   0.42   9.26

```

## 4. Long Vector and 64-bit for MPI

We add new supports for long vector and communications based on MPI functions to **pbdMPI** since version 0.2-1.

### 4.1. Long Vector for MPI

The current R (3.1.0) uses C structure to extend 32-bit length limitation ( $2^{31} - 1 = 2147483647$  defined as `R_SHORT_LEN_MAX`) to 52-bit length ( $2^{51} - 1 = 4503599627370496$  defined as `R_XLEN_T_MAX`). In general, this is more portable and extensible when 128-bit integer coming on (who know when the day comes ...) However, a vector with elements larger than  $2^{31} - 1$  needs extra effort to be accessed in R. See “R Internals” for details.

The reason is that an integer is 4 bytes in both of x86\_64 system (64-bit) and i386 system (32-bit). Since the capacity of current machine and performance issues, there is no benefit to use 8 bytes for integer. In x86\_64 system, computers or compilers use either `long` or `long long` for pointer address which is in `size_t` for unsigned address or in `ptrdiff_t` for signed address. For example, in GNU C (`gcc`), the flag `-m64` is to use 4 bytes for `int` and 8 bytes for `long` in x86\_64 system.<sup>1</sup>

Therefore, the question is what are the differences of 64-bit and 32-bit system? One of them is “pointer size” which is 8 bytes in x86\_64 machine and it is 4 bytes in i386 machine. This allows computer to lengthen memory and disk space. Note that address is indexed by `long` or `long long` which is no conflict with integer size, and 4 bytes integer is efficient and safe enough for general purpose. For example, `double *a` is a pointer (`a`) pointing to a real scaler (`*a`), but the pointer’s address (`&a`) is in `size_t` (`long` or `long long`) which is 8 bytes in x86\_64 system and is 4 bytes in i386 system.

To deal with long vector, **pbdMPI** uses the same framework as R to build up MPI collective functions. **pbdMPI** follows R’s standard to assume a vector normally has length smaller than `R_SHORT_LEN_MAX` which can be handled by most 32-bit functions. If the vector length is greater than `R_SHORT_LEN_MAX`, then R names this as long vector which also has the maximum `R_XLEN_T_MAX`. The vector length is stored in type `R_xlen_t`. The `R_xlen_t` is `long` if `LONG_VECTOR_SUPPORT` is defined, otherwise it is `int`. R provides several C macro to check, access, and manipulate the vector in `VECSXP` or general `SEXP`. See `Rinternals.h` for details.

The **pbdMPI** first checks if the data size for communication is greater than `SPMD_SHORT_LEN_MAX` or not. If the data is long vector, then **pbdMPI** evokes collective functions to send/receive

<sup>1</sup> Is there a way to have 8 bytes integer? The answer is that it is dependent on compiler.

chunk of data partitioned by `SPMD_SHORT_LEN_MAX` until all chunks are all received/sent. For some MPI collective functions such as `allgather()` and `gather()`, extra space may be allocated for receiving chunks, then the chunks are copied to right memory address by the rank of communicator from the extra space to the receiving buffer.

The reason is that most MPI collective functions rely on arguments for indexing buff types and counting buffer sizes where the types and sizes are both in `int`. `SPMD_SHORT_LEN_MAX` is defined in `pbdMPI/src/spmd.h` and usually is equal to `R_SHORT_LEN_MAX`. Developers may want to use shorter length (such as `SPMD_INT8_LEN_MAX` which is  $2^7 - 1 = 127$ ) for testing without a large memory machine or for debugging without recompiling R with shorter `R_SHORT_LEN_MAX`.

In **pbdMPI**, the implemented MPI collective functions for long vector are `bcast()`, `allreduce()`, `reduce()`, `send()`, `recv()`, `isend()`, `irecv()`, `allgather()`, `gather()`, and `scatter()`. The other MPI collective functions are “NOT” implemented due to the complexity of memory allocation for long vector including `allgatherv()`, `gatherv()`, `scatterv()`, `sendrecv()`, and `sendrecv.replace()`.

Further, **pbdMPI** provides a way to mimic long vector support. Users can set

`pkg_constant.h`

```
#define MPI_LONG_DEBUG 1
```

in `pbdMPI/src/pkg_constant.h` to turn on debugging mode and recompile **pbdMPI**. Then, run examples in `pbdMPI/inst/examples/test_long_vector/` to see how the mimic long vectors are communicated between processors. Also, users can also adjust the length limit of mimic long vector (buffer size) by changing

`spmd.h`

```
#define SPMD_SHORT_LEN_MAX R_SHORT_LEN_MAX
```

in `pbdMPI/src/spmd.h`.

## 4.2. 64-bit for MPI

The remaining question is that does MPI library support 64-bit system? The answer is yes, but users may need to recompile MPI libraries for 64-bit support. The same way as R to enable 64-bit system that MPI libraries may have 8 bytes pointer in order to communicate larger memory or disk space.<sup>2</sup>

For example, the OpenMPI provides next to check if 64-bit system is used.

Shell Command

```
ompi_info -a | grep 'int.* size: '
```

If the output is

Shell Command

```
C int size: 4
```

<sup>2</sup> [http://wiki.chem.vu.nl/dirac/index.php/How\\_to\\_build\\_MPI\\_libraries\\_for\\_64-bit\\_integers](http://wiki.chem.vu.nl/dirac/index.php/How_to_build_MPI_libraries_for_64-bit_integers).

```

C pointer size: 8
Fort integer size: 8
Fort integer1 size: 1
Fort integer2 size: 2
Fort integer4 size: 4
Fort integer8 size: 8
Fort integer16 size: -1

```

then the OpenMPI supports 64-bit system.<sup>3</sup> Otherwise, users may use the next to reinstall OpenMPI as

#### Shell Command

```

./configure --prefix=/path_to_openmpi \
CFLAGS=-fPIC \
FFLAGS="-m64 -fdefault-integer-8" \
FCFLAGS="-m64 -fdefault-integer-8" \
CFLAGS=-m64 \
CXXFLAGS=-m64

```

and remember to reinstall **pbdMPI** as well.

Note that 64-bit pointer may only provide larger size of data, but may degrade hugely for other computing. In general, communication with a large amount of data is a very bad idea. Try to redesign algorithms to communicate lightly such as via sufficient statistics, or to rearrange and load large data partially or equally likely to every processors.

## 5. Simple Input and Output

We add new supports simple data input and output for basic CSV and text files to **pbdMPI** since version 0.2-2.

Two quick demos can simply explain how a dataset can be input and output via **pbdMPI** functions `comm.write.table()` and `comm.read.table()`. The first is

#### Shell Command

```

### Run the demo with 4 processors by
mpiexec -np 4 Rscript -e "demo(simple_io, 'pbdMPI', ask=F, echo=F)"

```

The demo utilizing [iris](#) data ([Fisher 1936](#)) to show simple input and output functions of **pbdMPI** and is summarized as in next.

- 150 rows of `iris` are divided in 4 processors, and processors own 37, 37, 38, and 38 rows of `iris` as a gbd row-block format. i.e. Rank 0 owns row 1 to 37, rank 1 owns row 38 to 74, and so on.
- A text file “iris.txt” is dumped via `comm.write.table()` which sequentially append processor owned row blocks.
- `comm.read.table()` then reads the text file back in memory, and again in a gbd row-block format.

<sup>3</sup> The C integer is still in 4 bytes rather than 8 bytes.

Note that `comm.read.table()` may read a first few lines to predetermine how many lines of the file to read in. This is an approximation and results in unbalance data across processors. In particular, either the highest order rank may own the largest portion of whole dataset, or several higher order ranks may own zero row. So, a call `comm.load.balance()` within `comm.read.table()` is to move rows across processors if necessary. Basically, the reading steps are described as in the next.

1. If file size were less than 5MB, then rank 0 would read in the whole file and scatter rows to other ranks.
2. If file size were large than 5MB, then rank 0 would read in the first 500 lines and estimate total number of records in the file. All ranks sequentially read in the designated records.
3. Call `comm.load.balance()` to balance the data.

The file size limit is controlled by `.SPMD.IO$max.file.size`, and the first few line limit is controlled by `.SPMD.IO$max.test.lines`. Further, users can specify options `nrows` and `skip` to `comm.read.*()` to manually read the file and call `comm.load.balance()` later if needed.

There are several way to distributed or balance data among processors. Currently **pbdMPI** supports 3 formats: `block`, `block0`, and `block.cyclic`. In the above demo, the 150 rows are mainly distributed in (37,37,38,38) which is a `block` format. The second demo shows how to load balance between different formats next.

#### Shell Command

```
### Run the demo with 4 processors by
mpiexec -np 4 Rscript -e "demo(simple_balance, 'pbdMPI', ask=F, echo=F)"
```

In the `block0`, the iris is distributed as (38,38,37,37) row-block of each processor. In the `block.cyclic`, the iris is distributed as (38,38,38,36) row-block of each processor. i.e. Each cycle has 38 rows and one cycle per processor.

See **pbdDEMO** vignettes (Schmidt *et al.* 2013) for more details about “block-cyclic” and “gbd”.

## 6. Simple Pairwise Evaluation

We build some utilities for pairwise evaluation to **pbdMPI** since version 0.2-3.

Evaluating a function on any two data points is a common problems, such as distance, pairwise comparison, and multiple testing problems. Useful functions to solve those problems are

- `comm.as.gbd()`: This function is to turn a common matrix (in all ranks) to a gbd matrix in row major blocks. For example, one may read in data from one rank, then utilizes this function to redistribute data with load balance of all ranks. This is an alternative way to Section 5, but more efficient for small size of data.
- `comm.allpairs()`: This function is mainly to provide indices for all pairs of  $N$  data points. It returns a two columns (i, j) gbd matrix in row major blocks. For example, one may want to evaluate all  $N^2$  pairs of the  $N$  data points. However, in distance context, it provides only indices as in lower-triangular matrix (ordered by row major).

- `comm.dist()`: This function is to compute distance (lower-triangular only) of  $N$  data points as usual `dist()` function, but evaluated on a gbd matrix in row major blocks. The returning can be a common distance matrix (only good for small dataset), or a 3 columns gbd matrix in row major blocks. The columns are  $i$ ,  $j$ , and the value of pair  $(i, j)$ .
- `comm.pairwise()`: This functions is a general extension composed of three functions above that allows users to provide a function `FUN` to evaluate on pairs of data. For example, a distance between two data points  $x$  and  $y$  can be computed via original `dist()` function. So, it can be wrapped as

## R Script

```
dist.pair <- function(x, y, ...){
  as.vector(dist(rbind(x, y), ...))
}
```

for the `FUN` option of `comm.pairwise()`.

This function is also useful for cases that measure of pair  $(i, j)$  differs to that of pair  $(j, i)$ , i.e. non-symmetric measure. If order is matter, then the `FUN` can be evaluated via the options either `pairid.gbd` which can be user defined or simply `symmetric = FALSE`.

Also, we provide some examples in man page. A demo verifies these functions in different ways.

## Shell Command

```
### Run the demo with 4 processors by
mpiexec -np 4 Rscript -e "demo(simple_pairs, 'pbdMPI', ask=F, echo=F)"
```

See **pbdDEMO** vignettes (Schmidt *et al.* 2013) for more statistical examples.

## 7. Windows Systems (MS-MPI)

**pbdMPI** (later than version 0.2-3) supports Windows with Microsoft MPI or MS-MPI ([http://msdn.microsoft.com/en-us/library/bb524831\(v=vs.85\).aspx](http://msdn.microsoft.com/en-us/library/bb524831(v=vs.85).aspx)). Currently, **pbdMPI** is built with 'HPC Pack 2012 R2 MS-MPI Redistributable Package' which is available at <http://http://www.microsoft.com/en-us/download/>. The installation (MSMPISetup.exe) is easily done with a few clicks provided some service packs and Visual C++ runtime are installed correctly. The default environment and path are recommended.

For running MPI and R, users need to set `PATH` to the `mpiexec.exe` and `Rscript.exe`. By default,

## Shell Command

```
### Under command mode, or save in a batch file.
SET R_HOME=C:\Program Files\R\R-3.0.1\
SET MPI_HOME=C:\Program Files\Microsoft MPI\
SET PATH=%MPI_HOME%bin\;%R_HOME%bin\;%PATH%
```



Note that the installation (MSMPISetup.exe) may set several environmental variables including

- MSMPI\_BIN for `mpiexec.exe` and other executable files,
- MSMPI\_INC for header files such as `mpi.h`,
- MSMPI\_LIB32 for 32 bits static libraries such as `msmpi.lib`, and
- MSMPI\_LIB64 for 64 bits static libraries.

These should be useful to verify via R command `Sys.getenv()`.

## 7.1. Install from Binary

The binary packages of **pbdMPI** are available on the website: “Programming with Big Data in R” at <http://r-pbd.org/> or “CRAN” at <http://cran.r-project.org/package=pbdMPI>. Note that different MPI systems require different binaries. The binary can be installed by

Shell Command

```
R CMD INSTALL pbdMPI_0.2-3.zip
```

As on Unix systems, one can start quickly with **pbdMPI** by learning from the following demos. There are six basic examples.

Shell Command

```
### Run the demo with 2 processors by
mpiexec -np 2 Rscript.exe -e "demo(allgather, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript.exe -e "demo(allreduce, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript.exe -e "demo(bcast, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript.exe -e "demo(gather, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript.exe -e "demo(reduce, 'pbdMPI', ask=F, echo=F) "
mpiexec -np 2 Rscript.exe -e "demo(scatter, 'pbdMPI', ask=F, echo=F) "
```

**Warning:** Note that spacing inside `demo` is not working for Windows systems and `Rscript.exe` should be evoked rather than `Rscript`.

## 7.2. Build from Source

**Warning:** This section is only for building binary in 32- and 64-bit Windows system. A more general way can be found in the file `pbdMPI/INSTALL`.

Make sure that R, **Rtools**, and **MINGW** are in the `PATH`. See details on the website “Building R for Windows” at <http://cran.r-project.org/bin/windows/Rtools/>. The environment variable `MPI_HOME` needs to be set for building binaries.

For example, the minimum requirement may be

Shell Command

```
### Under command mode, or save in a batch file.
SET R_HOME=C:\Program Files\R\R-3.0.1\
SET RTOOLS=C:\Rtools\bin\
```

```
SET MINGW=C:\Rtools\gcc-4.6.3\bin\
SET MPI_HOME=C:\Program Files\Miscrosoft MPI\
SET PATH=%MPI_HOME%bin;%R_HOME%;%R_HOME%bin;%RTOOLS%;%MINGW%;%PATH%
```

With a correct PATH, one can use the R commands to install/build the **pbdMPI**:

#### Shell Command

```
### Under command mode, build and install the binary.
tar zxvf pbdMPI_0.2-3.tar.gz
R CMD INSTALL --build pbdMPI
R CMD INSTALL pbdMPI_0.2-3.zip
```

**Warning:** For other **pbdR** packages, it is possible to compile without further changes of configurations. However, only **pbdMPI** is tested regularly before any release.

## 8. FAQs

### 8.1. General

1. **Q:** Do I need MPI knowledge to run **pbdMPI**?  
**A:** Yes, but only the big picture, not the details. We provide several examples in `pbdMPI/inst/examples/test_spmd/` to introduce essential methods for learning MPI communication.
2. **Q:** Can I run **pbdMPI** on my laptop locally?  
**A:** Sure, as long as you have an MPI system. You even can run it on 1 CPU.
3. **Q:** Does **pbdMPI** support Windows clusters?  
**A:** Yes, the released binary currently supports MS-MPI. Currently, **pbdMPI** is built with 'HPC Pack 2012 R2 MS-MPI Redistributable Package' which is available at <http://www.microsoft.com/en-us/download/>. For other MPI systems, users have to compile from source.
4. **Q:** Can I run **pbdMPI** in OpenMPI and MPICH2 together?  
**A:** No, you can have both OpenMPI and MPICH2 installed in your OS, but you are only allowed to run **pbdMPI** with one MPI system. Just pick one.
5. **Q:** Does **pbdMPI** support any interactive mode?  
**A:** No, but yes. **pbdMPI** only considers batch execution and aims for programming with big data that do not fit on desktop platforms. We think that interaction with big data on a big machine is better handled with a client/server interface, where the server runs SPMD codes on big data and the client operates with reduced data representations.

If you really need an interactive mode, such as for debugging, you can utilize **pbdMPI** scripts inside **Rmpi**. **Rmpi** mainly focuses on Manager/Workers computing environments, but can run SPMD codes on workers only with a few adjustments. See the “Programming with Big Data in R” website for details at <http://r-pbd.org/>.

Note that **pbdMPI** uses communicators different from **Rmpi**. Be sure to free the memory correctly for both packages before quitting. `finalize(mpi.finalize = FALSE)` can free the memory allocated by **pbdMPI**, but does not terminate MPI before calling `mpi.quit` of **Rmpi**.

6. **Q:** Can I write my own collective functions for my own data type?  
**A:** Yes, S4 methods allow users to add their own data type, and functions. Quick examples can be found in `pbdMPI/inst/examples/test_s4/`.
7. **Q:** Does **pbdMPI** support long vector or 64-bit integer? **A:** See Section 4.

## 8.2. Programming

1. **Q:** Can I run task jobs by using **pbdMPI**?  
**A:** Yes, it is relatively straightforward for parallel tasks. Neither extra automatic functions nor further command/data communication is required. In other words, SPMD is easier for Monte Carlo, bootstrap, MCMC simulation and statistical analysis for ultra-large datasets. A more efficient way, such as task pull parallelism, can be found in next Q&A.

Example 1:

### SPMD R Script

```
library(pbdMPI, quietly = TRUE)
init()

id <- get.jid(total.tasks)

### Using a loop.
for(i in id){
  ### Put independent task i script here.
}

### Or using apply-like functions.
lapply(id, function(i){
  ### Put independent task i script here.
})

finalize()
```

Note that `id` gets different values on different processors, accomplishing `total.tasks` across all processors. Also note that any data and partial results are not shared across the processors unless communicated.

Example 2:

### SPMD R Script

```
library(pbdMPI, quietly = TRUE)
init()
```

```

### Directly using a loop.
for(i in 1:total.tasks){
  if(i %% comm.size() == comm.rank()){
    ### Put independent task i script here.
  }
}

### Or using apply-like function.
lapply(1:total.tasks, function(i){
  if(i %% comm.size() == comm.rank()){
    ### Put independent task i script here.
  }
})

finalize()

```

2. **Q:** Can I use unblocked send functions, such as `isend()`? Or, does `isend()` truly unblocked?

**A:** The answer is no for **pbdMPI** earlier than version 0.2-2, but it is changed since version 0.2-3. A temporary buffer list `nb.buffer` is used to store all objects being sent by `isend()`. The buffer is created and cumulated in `.pbdMPIEnv`, but released as `wait()` is called. Although this may take some performance and space, this can avoid `gc()` and memory overwrite before actual sending is done.

3. **Q:** Can I run un-barrier task jobs, such as task pull parallelism, by using **pbdMPI**?

**A:** Yes, it is relatively straightforward via **pbdMPI** API function `task.pull()` in SPMD. For example, the next is available in demo which has a user defined function `FUN()` run on workers, and master (rank 0) controls the task management.

#### Shell Command

```
mpiexec -np 4 Rscript -e "demo(task_pull, 'pbdMPI', ask=F, echo=F)"
```

#### SPMD R Script (task\_pull)

```

### Initial.
library(pbdMPI, quietly = TRUE)

### Examples.
FUN <- function(jid){
  Sys.sleep(1)
  jid * 10
}

ret <- task.pull(1:10, FUN)
comm.print(ret)

if(comm.rank() == 0){
  ret.jobs <- unlist(ret)
  ret.jobs <- ret.jobs[names(ret.jobs) == "ret"]
  print(ret.jobs)
}

```

```
### Finish.
finalize()
```

4. **Q:** What if I want to run task push or pull by using **pbdMPI**?

**A:** No problem. As in the two proceeding examples, task push or pull can be done in the same way by using rank 0 as the manager and the other ranks as workers. However, we do not recommend it except perhaps for inhomogeneous computing environments and independent jobs.

5. **Q:** Are S4 methods more efficient?

**A:** Yes and No. S4 methods are a little less efficient than using `switch ... case ...` in C, but most default methods use `raw` with `un-` and `serialize` which may cost 3-10 times more than using `integer` or `double`. Instead of writing C code, it is easier to take advantage of S4 methods to extend to general R objects (`matrix`, `array`, `list`, `data.frame`, and `class ...`) by communicating with basic data types (`integer` and `double`) and avoiding serialization.

6. **Q:** Can I disable the MPI initialization of **pbdMPI** when I call `library(pbdMPI)`?

**A:** Yes, you can set a hidden variable `__DISABLE_MPI_INIT__` in the `.GlobalEnv` before calling `library(pbdMPI)`. For example,

#### SPMD R Script

```
assign("__DISABLE_MPI_INIT__", TRUE, envir = .GlobalEnv)
library(pbdMPI)
ls(all.names = TRUE)
init()
ls(all.names = TRUE)
finalize(mpi.finalize = FALSE)
```

Note that we are *\*NOT\** supposed to kill MPI in the `finalize` step if MPI is initialized by external applications. But some memory allocated by **pbdMPI** has to be free, `mpi.finalize = FALSE` is set above.

To avoid some initialization issues of MPI, **pbdMPI** uses a different way than **Rmpi**. **pbdMPI** allows you to disable initializing communicators when loading the library, and later on you can call `init` to initialize or obtain communicators through `__MPI_APTS__` as in the next question.

7. **Q:** Can **pbdMPI** take or export communicators?

**A:** Yes, the physical memory address is set to the variable `__MPI_APTS__` in the `.GlobalEnv` through a call to `init()`. The variable points to a structure containing MPI structure arrays preallocated while **pbdMPI** is loaded. `pbdMPI/src/pkg_*` provides a mechanism to take or export external/global variables at the C language level.

## 8.3. MPI Errors

1. **Q:** If compilation successful, but load fails with segfault

## Error Message

```

** testing if installed package can be loaded
sh: line 1: 2905 Segmentation fault
'/usr/local/R/3.0.0/intel13/lib64/R/bin/R' --no-save --slave
2>&1 <
/tmp/RtmpGkncGK/file1e541c57190
ERROR: loading failed

*** caught segfault ***
address (nil), cause 'unknown'

```

**A:** Basically, **pbdMPI** and all **pbdR** are tested and have stable configuration in GNU environment. However, other compilers are also possible such as Intel compiler. This message may come from the system of login node does not have a MPI system, MPI system is only allowed to be loaded in computing node, or MPI shared library is not loaded correctly and known to R. The solution is to use extra flag to R **CMD INSTALL -no-test-load pbdMPI\*.tar.gz**, and use **export LD\_PRELOAD=...** as the answer to the next question.

2. **Q:** If installation fails with

## Error Message

```

Error in dyn.load(file, DLLpath = DLLpath, ...) :
  unable to load shared object '/.../pbdMPI/libs/pbdMPI.so':
  libmpi.so: cannot open shared object file: No such file or
  directory

```

**A:** OpenMPI may not be installed in the usual location, so the environment variable **LD\_LIBRARY\_PATH** should be set to the **libmpi.so** path, such as

## Shell Command

```
export LD_LIBRARY_PATH=/usr/local/openmpi/lib:$LD_LIBRARY_PATH
```

where **/usr/local/openmpi/lib** should be replaced by the path to **libmpi.so**. Or, use **export LD\_PRELOAD=...** to preload the MPI library if the library name is not conventional, such as

## Shell Command

```
export LD_PRELOAD=/usr/local/openmpi/lib/libmpi.so:$LD_PRELOAD
```

Another solution may be to use the unix command **ldconfig** to setup the correct path.

3. **Q:** **pbdMPI** installs successfully, but fails at initialization when calling the function **init()** with error message

## Error Message

```

/usr/lib/R/bin/exec/R: symbol lookup error:
/usr/lib/openmpi/lib/openmpi/mca_paffinity_linux.so: undefined
symbol:
mca_base_param_reg_int

```

**A:** The linked library at installation may be different from the runtime library, especially when your system has more than one MPI systems. Since the library at installation is detected by `autoconf` (`configure`) and `automake` (`Makevars`), it can be linked with OpenMPI library, but MPICH2 or LAM/MPI is searched before OpenMPI according to `$PATH`.

Solutions:

- Check which MPI system is your favorite to call. If you use OpenMPI, then you have to link with OpenMPI. Similarly, for MPICH2.
  - Or, only keep the MPI system you do like and drop others.
  - Use `--with-mpi-type` to specify the MPI type.
  - Use `--with-mpi-include` and `--with-mpi-libpath` to specify the right version.
4. **Q:** (Mac) If installs successfully, but fails at initialization with

#### Error Message

```
Library not loaded: /usr/lib/libmpi.0.dylib
```

**A:** Please make sure the GNU compiler, R, OpenMPI, and **pbdMPI** are all built and installed under unified conditions, such as 64-bits environment. 32-bits R may not be able to load 64-bits OpenMPI nor **pbdMPI**.

5. **Q:** (Linux) If OpenMPI `mpiexec` fails with

#### Error Message

```
mca: base: component_find: unable to open
/.../openmpi/lib/openmpi/mca_paffinity_hwloc:
/.../openmpi/lib/openmpi/mca_paffinity_hwloc.so:
undefined symbol: opal_hwloc_topology (ignored)
...
mca: base: component_find: unable to open
/.../openmpi/lib/openmpi/mca_carto_auto_detect:
/.../openmpi/lib/openmpi/mca_carto_auto_detect.so:
undefined symbol: opal_carto_base_graph_get_host_graph_fn
(ignored)
...
```

**A:** The linked MPI library `libmpi.so` may be missing or have a different name. OpenMPI builds shared/dynamic libraries by default and the target file `libmpi.so` is used by `pbdMPI/src/spmd.c` through `#include <dlfcn.h>` and `dlopen(...)` in the file `pbdMPI/src/pkg_dl.c`.

Solutions:

- Check if the path and version of `libmpi.so` are correct. In particular, one may have different MPI systems installed.
- When linking with `libmpi.so` in OpenMPI, one must run/load **pbdMPI** with OpenMPI's `libmpi.so`. The same for LAM/MPI and MPICH2.
- Use `export LD_PRELOAD=$PATH_TO_libmpi.so.*` in command mode.

- Use the file `/etc/ld.so.conf` and the command `ldconfig` to manage personal MPI installation.
- Or, recompile OpenMPI with a static library, and use `libmpi.a` instead.

6. **Q:** (Windows) If OpenMPI `mpiexec` fails with

Error Message

```
ORTE_ERROR_LOG: Error in file ..\..\..\openmpi-1
.6\orte\mca\ess\hnp\ess_hnp_module.c at line 194
...
ORTE_ERROR_LOG: Error in file ..\..\..\openmpi-1
.6\orte\runtime\orte_init.c at line 128
...
```

**A:** Check if the network is unplugged, the network should be “ON” even on a single machine. At least, the status of network interface should be correct.

7. **Q:** (Windows) If MPICH2 `mpiexec` fails with

Error Message

```
c:\>"C:\Program Files\MPICH2\bin\mpiexec.exe" %*
C:\my_script.r
launch failed: CreateProcess(Rscript C:\my_script.r) on
failed, error 2 - The system cannot find the file specified.
```

**A:** Please try to use `Rscript.exe` in windows system.

8. **Q:** For MPICH2 users, if installation fails with

Error Message

```
/usr/bin/ld: libmpich.a(comm_get_attr.o): relocation R_X86_64_32
against `MPIR_ThreadInfo' can not be used when making a shared
object; recompile with -fPIC
libmpich.a: could not read symbols: Bad value
collect2: ld returned 1 exit status
```

**A:** MPICH2 by default does not install a shared library which means `libmpich.so` is missing and **pbdMPI** tries to link with a static library `libmpich.a` instead. Try to recompile MPICH2 with a flag `--enable-shared` and reinstall **pbdMPI** again.

9. **Q:** For MPICH2 and MPICH3 users, if installation fails with

Error Message

```
/usr/bin/ld: cannot find -lopa
collect2: error: ld returned 1 exit status
make: *** [pbdMPI.so] Error 1
ERROR: compilation failed for package 'pbdMPI'
```

**A:** By default, `-lopa` is required for some systems. However, some systems may not have it and can be disabled with a configuration flag when install **pbdMPI**, such as `R CMD INSTALL pbdMPI*.tar.gz --configure-args="--disable-opa"`.



## 8.4. Other Errors

1. **Q:** pbdMPI is linked with pbdPROF (Chen *et al.* 2013) and mpiP (Vetter and McCracken 2001). (i.e. `--enable-pbdPROF` is used in pbdMPI and `--with-mpiP` is used in pbdPROF.) If pbdMPI compilation successful, but load fails with

### Error Message

```
Error : .onLoad failed in loadNamespace() for 'pbdMPI', details:
  call: dyn.load(file, DLLpath = DLLpath, ...)
  error: unable to load shared object 'pbdMPI.so':
  pbdMPI/libs/pbdMPI.so: undefined symbol: _Ux86_64_getcontext
```

**A:** Some prerequisite packages by mpiP is installed incorrectly. Reinstall mpiP by

### R Script

```
./configure --disable-libunwind CPPFLAGS="-fPIC"
-I/usr/lib/openmpi/include" LDFLAGS="-L/usr/lib/openmpi/lib
-lmpi"
```

and followed by reinstall pbdPROF and pbdMPI.

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