National University of Singapore School of Computing CS1010S: Programming Methodology Semester I, 2021/2022

Extra Practice 9

All the best for your finals!

Code Tracing

```
(a) # CS1010S AY17/18 Sem 2 Finals
   def foo(x):
       return lambda y: bar(x) if y % 2 else x
   def bar(y):
       return lambda x: foo(x) if y % 2 else y
   print(foo(2)(3)(4))
(b) # CS1010S AY17/18 Sem 2 Finals
   a = [0, 1, 2]
   a.append(a)
   b = [a[0] + a[1], a[1:2], a[3][3][2]]
   print(b)
(c) # CS1010S AY17/18 Sem 1 Finals
   s = 'Lollapalooza'
   d = \{\}
   for i in range(len(s)):
       d[s[i \% 5]] = s[i]
   print(d)
(d) # CS1010S AY17/18 Sem 2 Finals
   def force(x):
       try:
           return int(x)
       except ValueError:
          return float(x)
       except Exception:
           return "NaN"
   print(force("100"))
   print(force("1.0"))
   print(force("abc"))
```

```
(e) # CS1010S AY19/20 Sem 1 Finals
   def foo(x):
       def baz(y):
           return lambda z: (x, y)[z]
       return lambda x: baz(x)
   print(foo(-1)(0)(1))
(f) # CS1010S AY19/20 Sem 2 Finals
   lst = [[1], [2, 2], [3, 3, 3]]
   def f(lst):
       for i in lst.copy():
           if len(i) < 2:
               i.append(1)
           if sum(i) < 5:
               i.pop()
           else:
               lst.extend(i)
           print(lst)
       return 1st
   print(lst is f(lst))
   print(lst)
(g) # CS1010S AY20/21 Sem 1 Finals
   def wow(n):
       print(n)
       return lambda m: n + m
   def twice(t):
       print('yes')
       return lambda x: t(t(x))
   once = twice(twice)(wow(2))
   print(once(1))
(h) # CS1010FC AY14/15 Special Term I Finals
   a = \{1: 2, 2: 4, 3: 6, 4: 7\}
   for k in a:
       if k % 2 == 1:
           del a[k]
   print(a)
(i) # CS1010X AY16/17 Special Term I Finals
   a = \{(1, 2): 3, (3, 4): 5\}
   for k, v in a.items():
       a[[v, k[0]]] = k[1]
   b = list(a.values())
   b.sort(reverse = True)
   print(b)
```

```
(j) # CS1010S AY17/18 Sem 2 Midterm
    def foo(y):
        return lambda x: x(x(y))
    def bar(x):
        return lambda y: x(y)
    print((bar)(bar)(foo)(2)(lambda x: x + 1))

(k) # CS1010S AY19/20 Sem 1 Midterm
    def foo(x):
        return x(lambda a: a + 1)
    def kung(x):
        return foo(lambda a: a(x))
    print(kung(foo)(9000))
```

Robbing a House

A thief wants to rob a series of houses, but unfortunately, the houses are somehow linked by an alarm system such that he cannot rob two houses side-by-side. Given a list of houses containing the amount of money (in millions) in each house, return the maximum amount the thief can earn.

Sample Tests:

```
>>> rob([3, 1, 4, 10, 2, 2, 9, 8])
23 # 3+10+2+8 = 23
>>> rob([1, 100, 99, 1, 3])
103 # 1+99+3 = 103
```

Number Sum Mania

(CS1010FC AY14/15 Special Term I Finals)

A positive integer $n \ge 2$ can be expressed as the sum of a number of positive integers smaller than n. For example,

```
2 = 1 + 1
3 = 1 + 2
= 1 + 1 + 1
4 = 1 + 3
= 2 + 2
= 1 + 1 + 2
= 1 + 1 + 1 + 1
5 = 1 + 4
= 1 + 1 + 3
= 2 + 3
= 1 + 2 + 2
= 1 + 1 + 1 + 1
```

The function num_sum returns the number of ways that an integer can be expressed as the sum of a number of positive integers. From the above examples, it should be clear that:

```
num_sum(2) = 1
num_sum(3) = 2
num_sum(4) = 4
num_sum(5) = 6
```

- (a) Write the function num_sum. **BIG HINT:** num_sum is extremely similar to count_change which was discussed in lecture.
- (b) Write the function **sum_set** that will return a list of the lists of possible number combinations for the integer sums. **Hint:** Think about how to modify the answer for Part (a).

Sample Execution:

```
>>> sum_set(2)
[[1, 1]]
>>> sum_set(3)
[[1, 1, 1], [2, 1]]
>>> sum_set(4)
[[1, 1, 1, 1], [2, 1, 1], [2, 2], [3, 1]]
>>> sum_set(5)
[[1, 1, 1, 1, 1], [2, 1, 1, 1], [2, 2, 1], [3, 1, 1], [3, 2],
[4, 1]]
```

```
>>> sum_set(6)
[[1, 1, 1, 1, 1], [2, 1, 1, 1, 1], [2, 2, 1, 1], [2, 2, 2],
[3, 1, 1, 1], [3, 2, 1], [3, 3], [4, 1, 1], [4, 2], [5, 1]]
```

(c) Write the function sum_set_product that will return a list of the products of the integer sums produced by sum_set, i.e. multiply together the components of each integer sum. You can assume that you have access to the function sum_set even if you cannot do Part (b).

Sample Execution:

```
>>> sum_set_product(2) # 1x1
[1]

>>> sum_set_product(3) # 1x1x1 and 2x1
[1, 2]

>>> sum_set_product(4)
[1, 2, 3, 4]

>>> sum_set_product(5) # Note that 4x1 = 2x2x1 so 5 elements, not 6
[1, 2, 3, 4, 6]

>>> sum_set_product(6)
[1, 2, 3, 4, 5, 6, 8, 9]
```

(d) Write the function has_prime_sum that will return True for an integer n if it can be expressed as a sum of $\underline{\mathbf{2}}$ prime numbers, or False otherwise. Assume that you have access to the function is_prime that will return True if an integer is prime.

Sample Execution:

```
>>> has_prime_sum(2)
False
>>> has_prime_sum(3)
False
>>> has_prime_sum(4)  # 2+2
True
>>> has_prime_sum(5)  # 2+3
True
>>> has_prime_sum(6)  # 3+3
True
>>> has_prime_sum(11)  # Not possible!
False
```