

CS 482/682 – Machine Learning

TEST 2

Chapter 4- Data Preprocessing., Ch5-Non Linear Models

Your Name: **KEY**

1. (3 points) Given the following dataset, provide the revised data table by using one hot encoding for the categorical data. For the numeric column Test-Ch1 use standard scalar i.e make the mean 0 and standard deviation 1. For Test-Ch8 use Min-Max scaling.

Test-Ch1	Test-Ch8	Sex
2	8	Male
8	9	Female
7	8	Female
3	5	Male
10	3	Female

SOLUTION

Mean ([2 8 7 3 10]) = $30/5 = 6$

Standard deviation of (2 8 7 3 10]) = $\text{sqrt}(((-4)^2 + 2^2 + 1^2 + (-3)^2 + 4^2)/5) = \text{sqrt}(((-4)^2 + 2^2 + 1^2 + (-3)^2 + 4^2)/5) = \text{sqrt}((16+4+1+9+16)/5) = \text{sqrt}(46/5) = \text{sqrt}(9.2) = 3.03$

Min ([8 9 8 5 3]) = 3

Max ([8 9 8 5 3]) = 9

Range ([8 9 8 5 3]) = $9-3 = 6$

(TestCh1-mean)/std_dev	(TestCh8-Min)/Range	Sex_male	Sex_Femal	
$-4/3.03 = -1.32$	$5/6=.83$	1	0	
$2/3.03 = .66$	$6/6=1$	0	1	
$1/3.03 = .33$	$5/6=.83$	0	1	
$-3/3.03=-.99$	$2/6=.33$	1	0	
$4/3.03=1.32$	$0/6=0$	0	1	

2. (2 points) An SVM model was developed for a binary classification problem in which there are three predictors. The two classes are Class 1 (target value is 1) and Class 2 (target value is -1) The values of margin points (support vectors, SV1, SV2 and SV3), the values of weights α_i for the margin points are given along with bias term

$$\beta_0 = -2$$

Support Vector Number	Support Vector Value	Target Value	α_i
SV1	(2,2,1)	-1	1.00
SV2	(-1,-2,2)	1	.3
SV3	(-2,-1,3)	1	.6

Classify the unknown data $u = (-2, -4, -1)$ as either Class 1 or Class 2.

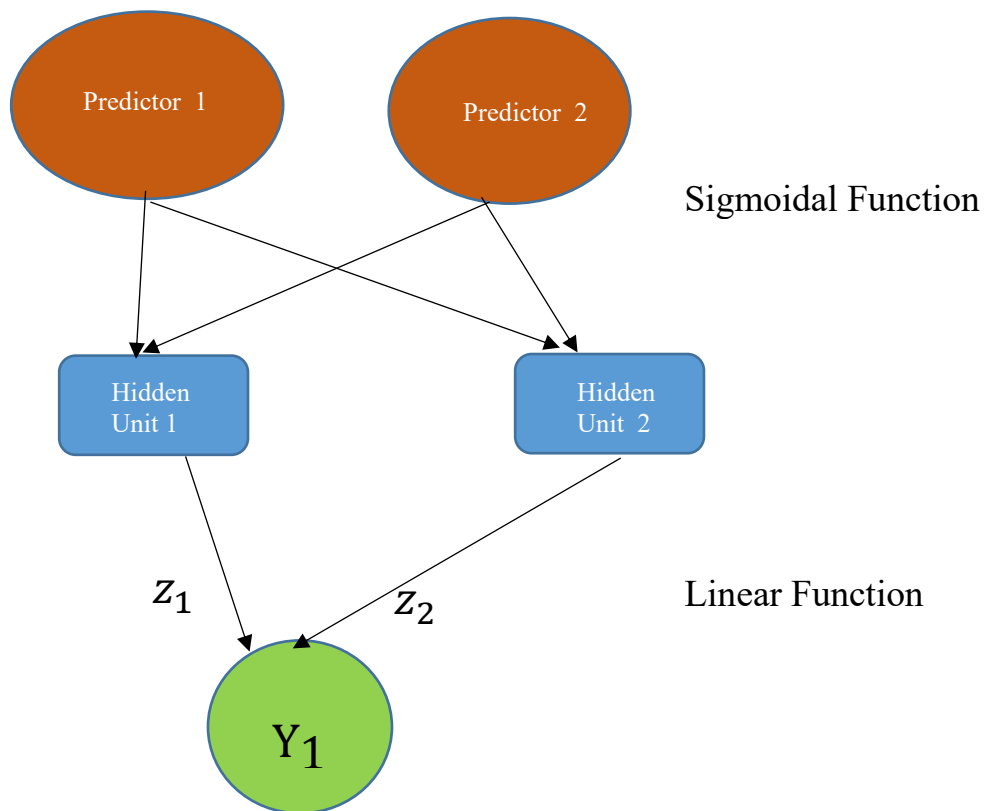
$$\begin{aligned}
 D(u) &= -2 + [(2,2,1) * (-2,-4,-1)^T * (-1) * 1 + (-1,-2,2) * (-2,-4,-1)^T * 1 * (.3) + (-2,-1,3) * (-2,-4,-1)^T \\
 &\quad (1) * (.6)] = \\
 &= -2 + (-4-8-1) * (-1) + (2+8-2) * (.3) + (4+4-3) * (.6) = -2 + 13 + 2.4 + 3.0 = \\
 &11 + 2.4 + 3.0 = 11 + 5.4 = 16.4 > 0
 \end{aligned}$$

Therefore the unknown point belongs to Class 1

3. (4 +1 = 5 points) A neural network with 2 hidden units is shown in the figure below for a regression problem, Assume the following values for hidden units 1 and 2 and the outcome unit Y_1 .

$$\alpha_1 = (\alpha_{01}, \alpha_{11}, \alpha_{21}) = (1, 1, 0) \quad \alpha_2 = (\alpha_{02}, \alpha_{12}, \alpha_{22}) = (1, 0, 1)$$
$$\beta_1 = (\beta_{01}, \beta_{11}, \beta_{21}) = (1, 1, 1)$$

- a) Find the prediction Y_1 made by the outcome unit for the input data with predictor values [2 3].
- b) If the correct outcome is 5, calculate the absolute value of the error in the prediction.



$$\begin{aligned} \text{a) } z_1 &= \sigma(u_1) \text{ where } u_1 = \alpha_{01} + x_{11} * \alpha_{11} + x_{12} \alpha_{21} = 1 + 1 * 2 + 0 * 3 = 3 \\ z_2 &= \sigma(u_2) \text{ where } u_2 = \alpha_{02} + x_{11} * \alpha_{12} + x_{12} \alpha_{22} = 1 + 0 * 2 + 1 * 3 = 4 \end{aligned}$$

$$\sigma(4) = 1/(1+e^4) = 1/(1+54.59) = 1/55.59 = 0.0183$$

$$Y_1 = \beta_{01} + z_1 * \beta_{11} + z_2 \beta_{21} = 1 + 1 * .0474 + 1 * .0183 = 1.0657$$

$$\text{b) Absolute value of error: } |5 - 1.0657| = 3.93$$

4. (5 points) (CS-682 Students ONLY) : Given the learning rate is .4 use the equations below to find the update of α 's and β 's in the problem above after finding the predicted value for [2 3] and the correct outcome being 5. Note that x' stands for transpose of x in the equations below.

$$\frac{\partial R_i}{\partial \beta_{km}} = -2(y_{ik} - f_k(x_i))g'_k(\beta_k^T z_i)z_{mi},$$

$$\frac{\partial R_i}{\partial \alpha_{m\ell}} = -\sum_{k=1}^K 2(y_{ik} - f_k(x_i))g'_k(\beta_k^T z_i)\beta_{km}\sigma'(\alpha_m^T x_i)x_{i\ell}.$$

$$\beta_{km}^{(r+1)} = \beta_{km}^{(r)} - \gamma_r \sum_{i=1}^N \frac{\partial R_i}{\partial \beta_{km}^{(r)}},$$

$$\alpha_{m\ell}^{(r+1)} = \alpha_{m\ell}^{(r)} - \gamma_r \sum_{i=1}^N \frac{\partial R_i}{\partial \alpha_{m\ell}^{(r)}},$$

$$g_k(T) = \frac{e^{T_k}}{\sum_{\ell=1}^K e^{T_\ell}}.$$

$$\sigma(u) = \frac{1}{1 + e^u}$$