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Algorithms Lab

Exercise - Diet

100 1000

The economical crisis came and people in a poor country of Theirlands do have hardly enough money to feed themselves. The government decided to help them by designing a cheap, yet sufficient, diet for all its citizens. There are some constraints on the diet that need to be fulfilled for a long-term normal functioning of the human body, as for instance a daily intake of between around 1500 and 2500 kilocalories, some minimal amounts of vitamins, antioxidants and some other nutrients which are considered "generally healthy" – and much more. You can describe all these constraints in the form "the daily amount of x should be between a and b". These constraints slightly differ from person to person and are exactly determined by voluntary-unpaid doctors in the country.

What the government wants from you is a program that, given the constraints for an individual and the food which is available in the area where the individual lives, calculates the cheapest diet (that means amounts of each product such that the total amounts of each nutrient fulfills the prescribed conditions; these amounts do not need to be integral - it is possible to consume any fractional amount of a product in a day). They understand though, that it is an uneasy task on such a short notice and will for now be happy with an alpha version which only calculates the price of a cheapest diet.

Input The input file consists of several test cases. Each of them starts with a line containing two integers n and m ($1 \le n \le 40$ and $1 \le m \le 100$). The following n lines describe the nutrients. The ith of these lines contains two integers \min_i and \max_i , the minimal and maximal daily amount of the ith nutrient. The next m lines describe the foods. Each of them contains an integer price of a unit of the jth product, p_j , and another n integers $C_{j,1} \dots C_{j,n}$ describing the amounts of nutrients $1 \dots n$ in a unit of product j. All the above integer values are in absolute value smaller than 2^{20} . The input is terminated by a line 0 0.

All the numbers on a single line are separated by a single space and there are no trailing whitespaces at the end of a line.

Output The output for each testcase is a line containing a single number c, the cost of the cheapest diet rounded down to an integer. If there is no diet fulfilling the criteria, output the line No such diet. No trailing spaces at the end of the line are allowed.

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Sample Input

1500 < 512x < 2500

1 1
1500 2500

2 512
2 3
1000 < 2000

1000 < 10x + 40y + 50z < 1000
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10 450 10

5 50 40

7 100 50

2 3

1000 2000

100 1000

10 450 10

5 50 40

6 100 50

2 1

1 10

1 10

1 20 1

0 0
```

Sample Output

5 30 28 No such diet.