## CS156 – Introduction to Artificial Intelligence Midterm Review

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## **Introduction to Agents**

An agent perceives its environment through sensors and acts upon the environment through actuators.

Turing Test – A test where a human poses a series of questions to the computer and after seeing the responses cannot distinguish the responses from those of a human.

#### **Components Needs to Pass the Turing Test:**

- 1. Natural Language Processing
- 2. Knowledge Representation (i.e. storage paradigm)
- 3. Automated Reasoning
- 4. Machine Learning

**Total Turing Test** – A variant of the Turing Test where the robot passes entirely as a human.

## Additional Requirements Over Standard Turing Test:

- 1. Computer Vision
- 2. Robotics

Rational Agent – For every possible percept sequence, the rational agent selects the action it expects to maximize its performance measure given the information in the percept sequence and whatever built-in knowledge it has.

#### The maximizing action depends on:

- 1. Performance Measure
- 2. Any prior/built-in knowledge of the agent
- 3. Percept sequence to date.
- 4. Set of possible actions.

Percept – An agent's perceptual inputs through sensors at any given instant.

**Percept Sequence** – Set of all percepts to date.

Agent Function: Map from percept sequences to an agent action. Example: An agent action table.

Agents run an agent program. The agent program runs on the agent architecture. The combination of the agent program and agent architecture is called a complete agent.

Cognitive Science: Brings together computer models from Al and experimental techniques from psychology to construct precise and testable theories of the human mind.

#### Task Environment (PEAS)

Performance Measure (P) – Targets/goals	Environment (E) – Objects that interact	Actuators (A) – Tool(s) used by the	Sensors (S) – Tool(s) used by the agent
the agent will try to achieve.	with the agent or the agent interacts with	agent to interact with the environment.	to perceive the environment.

#### **Properties of a Task Environment**

Fully Observable vs. Partially Observable	Deterministic vs. Stochastic	Single-Agent vs. Multi-agent	Episodic vs. Sequential
Can the agent see the entire	Is the next state completely determined	Do objects in the environment need to be	In an episodic environment, the agent's
environment at once (e.g. chess)? If not,	by the current state and the action	treated as other agents? Multi-agent	experience is divided into episodes. In an
it may keep a history of what it has	(chess)? Otherwise it is stochastic (taxi-	environments can be competitive (chess)	episode the agent receives one percept
observed (taxi-driver).	driver).	or cooperative (taxi-driving).	and performs one action (e.g. quality
		Communication between agents is	control robot). In sequential
		possible as is randomized behavior to	environments, current actions affect
		avoid predictability.	future actions.
Static vs. Dynamic	Discrete vs. Continuous	Known versus Unknown	
Does the environment change while the	Time, percepts, and actions divided into	In a known environment, all outcomes of	
agent is making a decision? Chess is	a fixed, finite set (e.g. chess)? A	actions are known. In an unknown	
static while taxi driving is dynamic.	continuous environment is taxi-driving.	environment, the agent needs to figure	
		out how it works to make good decisions.	

#### **Example Episodic Agent**

#### Quality Assurance robot.

- Performance Measure: Fixed minimum and maximum tolerances for a widget. (Example ball board min/max weight, diameter, roundess)
- Environment: Widget (example ball bearing) received for inspection on an input system. Good bin and discard bins.
- Actuator: Arm to place widget in either discard bin or good bin.
- Sensor: Check ball bearing weight, diameter, roundness etc.

#### **Types of Agent Programs**

Simple Reflex Agent – Select actions based off the current percept only. Often defined by condition-action rules (i.e. productions)	Model-Based Reflex Agent – Similar to a Finite State Automata. Uses internal states to keep track of the environment. Updates the internal state based off how the environment evolves independently and how the agent's action affect the environment. This is called the agent model.
Goal Based Agents – A goal is a binary condition (i.e. either met or not met). A goal based agent tries to reach a target goal. Search and planning agents may be goal based agents.	Utility Based Agent – Agent applies a utility function to its performance. Agent tries to maximize its overall utility function.

#### **Additional Definitions**

Problem solving agents deal with atomic	Planning agents deal with factored or	Search – Process of looking over a	Solution – A sequence of actions that
environments (i.e. the environment is	structured environments (i.e. the	sequence of actions.	takes the agent from the initial state to
treated as a single whole and is	environment has attributes/variables		the goal state.
indivisible).	each of which has a value).		

#### Search Problems

#### Classical search problems are deterministic, fully-observable, known, and the solution is a sequence of actions.

<b>Solution:</b> A sequence of actions that takes the agent from the initial state to the goal state.	Root: Initial State Edge/Branches: Actions Node/Vertices: States in the state space Leaf: A node with no children	Node Expansion – Applying all legal actions to the node and generating all successor states.	Frontier or Open List – Set of successor nodes that have not yet been expanded.
Search Strategy: Method for choosing the node on the frontier to next expand.	Repeated State: Any state visited more than once during a search.  Redundant Path: Any two or more paths that go to the same state.	Closed or Explored Set: States that have already been expanded.	Loopy Path – Where a repeated state is expanded causing you not to continue to explore the same section of a graph.

#### **Definitions:**

<b>Uniformed Search</b> – Also known as <b>(Blind Search)</b> is any search that has no information on the search space.	<b>Informed Search</b> – Uses <b>heuristics</b> that inspect the state space to prioritize moves.	Explored Set – Set of all nodes already visited.
Branching Factor (b) – Number of branches/children/successors from a given node. Generally lists as the maximum branching factor.	Depth (d) – Number of branches/children/successors from a given node.	Frontier Set – Set of all nodes available for expansion.

#### A Problem consists of five attributes:

- 1. Initial State
- 2. Set of possible actions (ACTIONS)
- 3. Successor Function/Transitional Model (RESULTS)
- 4. Goal test (TERMINAL-TEST)
- 5. Cost Function

#### Four Ways to Rate/Measure a Search Strategy:

- 1. Completeness If a solution exists, does the algorithm always find it?
- 2. Optimal Is the solution found by the algorithm always optimal (i.e. have the lowest cost).
- 3. Time Complexity Amount of time required by the algorithm to perform the search.4. Space Complexity Amount of memory required by the algorithm to perform the search.
- Memory Queue **Time Complexity** Complete **Optimal** Comments Name Complexity Type Used l is the maximum allowed depth. **Depth Limited Search**  $O(b^l)$ 1. Incomplete if d > l0(l) Nο Nο Stack 2. Can be non-optimal if l > d1. Not complete because of the infinite branching problem (e.g. loop). Yes if the graph is Depth-First Search 0(d)  $O(b^d)$ No Stack 2. Can be considered special case of depth-limited search finite, No with  $l = \infty$ otherwise Always expand left most node that can be expanded. Iterative Deepening  $O(b) + O(b^2) + \cdots$ 0(d) Yes Yes Stack Calls Depth Limited Search algorithm d times  $+ O(b^d) = O(b^{d+1})$ Depth First Search Can be considered a variant of uniform cost search where Yes if each step cost is the same. uniform **Breadth First Search**  $O(b^d)$  $O(b^d)$ Queue Yes Expand the root node and then expand all children of the step root node in the order they are encountered until all nodes cost are expanded or a goal is reached. Variant of Breadth-First Search where two breadth first Yes if searches (one from start and one from the goal) are initiated and carried out simultaneously.  $O\left(b^{\frac{d}{2}}\right)$ uniform  $O\left(b^{\frac{d}{2}}\right)$ **Bidirectional Search** Yes Queue step Generalization of Breadth-First where the root (i.e. initiate state) node is expanded first and nodes are expanded based cost of their non-decreasing distance/cost from the root. Variant of Breadth-First Search where the step cost is not  $O\left(b^{1+\frac{C^*}{\epsilon}}\right)$ Priority uniform.  $O\left(b^{1+\frac{C^*}{\epsilon}}\right)$ **Uniform Cost Search** Yes Yes  $C^*$  - Minimum (optimal) cost to the goal. Queue  $\epsilon$  - Minimum step cost Selects node for expansion based off the one with the lowest **Greedy Best First** heuristic cost. N/A N/A No Nο None Search f(n) = h(n)Can oscillate in a dead end condition. Based off Yes with Based off quality of Priority Α\* quality of Yes heuristic heuristic Queue heuristic conditions Yes if Based off quality of **Recursive Best First** O(d)Yes heuristic Stack Search heuristic

admissible

 $Completeness\ above\ assumes\ the\ branching\ factor\ is\ \textbf{finite}.$ 

Iterative Deepening Depth First Search (also known as Iterative Lengthening Search)

```
def Depth_Limited_Search(node, problem, depth):
                                                                                             if(problem.GOAL_TEST(node)):
def ID_DFS(problem, limit):
                                                                                                  return SOLUTION(node)
     # Incrementally increase the maximum depth
                                                                                             if(depth == 0):
     for maximum depth in range(0, limit):
                                                                                                  return None
          result = Depth_Limited_Search(problem.INITIAL_STATE(),
                                                                                             for action in problem.ACTIONS(node):
                                         problem, maximum_depth)
                                                                                                  child = problem.RESULT(node, action)
          # If solution found return it.
                                                                                                  result = Depth_Limited_Search(child, problem, depth - 1)
          if(result is not None):
                                                                                                  if(result is not None):
                return result
                                                                                                        return result
                                                                                             return None
```

Space Complexity: O(d) since at one time only keeping in memory at most d nodes.

Time Complexity: Depth-Limited-Search is called up to d times. Each call to Depth-Limited-Search takes  $O(b^m)$  time. Given:  $\sum_{i=m}^{n-1}a^i=\frac{a^m-a^n}{1-a}$ , Then  $b+b^2+b^3+\cdots+b^d=O(b^{d+1})$ 

Complete: Yes since all nodes are explored if  $d \leq limit$ 

Optimal: Yes if all steps have uniform cost.

## **Uniform Cost Search (Uniformed Search)**

Uniform cost search explores nodes on the frontier based of a monotonically increase cost function. Hence its evaluation function is:

```
f(n) = c(n) also referred to as f(n) = g(n)
```

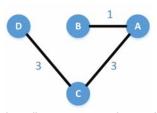
```
def UCS(problem):
     initial_state = problem.INITIAL_STATE()
     priority queue = {}
     explored set = {}
     priority_queue.enqueue(initial_state)
     # Continue until either a solution is found or all nodes explored.
     while( len(priority_queue) > 0):
          node = priority_queue.pop()
          # Must only check AFTER dequeueing the item to ensure it is optimal.
          if(problem.GOAL_TEST(node)): return SOLUTION(node)
          # Add the node to the explored set.
          explored_set.append(result)
          for action in problem.ACTIONS(node):
                result = problem.RESULT(node, action)
                # If not in the priority queue then enqueue it.
                if( result not in priority_queue and result not in explored_set):
                      priority_queue.enqueue(result)
                # Current version of node has lower cost than version in priority queue
                elif( result in priority_queue and result.COST() < priority_queue[result]. COST()):</pre>
                      priority_queue.remove(result)
                     priority_queue.enqueue(result)
     # No path found
     return None
```

Pseudo code for A\* and UCS is the same with the implementation of the COST() method.

#### A\* Algorithm

A* algorithm is a combination of the benefits of Greedy-Best First Search and Uniform Cost Search. Evaluation Function $f(n)$ : $f(n) = g(n) + h(n)$ Also written as: $f(n) = c(n) + h(n)$	Only performs the GOAL-TEST after the node has been dequeued from the priority queue. Similar to Uniform Cost Search.	Derives from Dijkstra's Algorithm.
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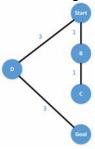
## Example of A\* Performing Better than Greedy Best First Search



Greedy Best First Search Oscillates Between Nodes A and B so it is Incomplete. This graph is solvable by  $A^*$ .

Greedy Best First Search is **memory efficient** since it does not need to remember where it has been.

#### Example of DFS Performing Better than A\*



Heuristic for A\* is Euclidean distance. In this case, A\* adds B then D to the frontier. It next expands B and adds C to the frontier. It next explores C and finds no solutions so it explores D then finds the goal.

#### **Recursive Best-First Search**

This algorithm is **optimal** when the heuristic is **admissible for trees**. The heuristic needs to be **consistent for tree search** to be optimal.

f\_limit/min\_eval\_func\_val – Best alternative path available from the any ancestor of the current node.

#### Simplified Description of Recursive Best First Search

- 1. Start from initial state and set the initial minimum cost of ∞
- 2. Generate all successors of current node. Set successor cost to either current node evaluation function value (f(n)) or the successors evaluation function cost.
- 3. Select successor node with minimum evaluation function (f(n)) cost.
- 4. If current node is a goal state, then return the solution.
- 5. If this cost is more than the current minimum, backtrack to find node with current minimum.
- 6. Extract the evaluation function cost (f(n)) of the second best successor of the current node.
- 7. Recurse using best successor found in step #3 and the minimum of the current minimum cost that was passed to the function and the second best successor of this node. This function results either a solution or None and updates the current best node's evaluation function cost (f(n)).
- 8. If step #7 returned a solution, then return that, otherwise, jump to step #3.

```
# Continues to recurse until current best cost is more than
def RBFS(problem, state, min eval func val):
     # Check if a goal was reached. If so, return it.
     if( problem.GOAL_TEST(state) ):
           return SOLUTION(state)
     # Get set of successors
     for a in problem.ACTIONS(state):
          successors.append(problem.RESULT(state, a))
     # Check a successor exists
     If(len(successors) == 0):
           return None, ∞
     # Update all successor eval function values
     for s in successors:
           s.eval_func_val = max(node.eval_func_val, s.g + s.h)
     while(True):
           # Best successor is a node with min eval cost from successors
           best_successor = node with least eval function value from the successors
           # If the best successor is not better than current best, backtrack to current best
           if(best succesor.eval func value > min eval func value):
```

# May need to recurse back to current level so store second best value for this level.

second\_best\_successor\_eval\_func\_val = Eval func value for second best successor of state
# Run RBFS again from current node with the new min value the minimum of the current

# minimum and the second best successor (i.e. alternative) for this current state/node.

return None, best successor.eval func value

RBFS(problem, best\_successor, min(min\_eval\_func\_val,

result, best\_successor.eval\_func\_val = \

# If solution found, return it. if(result is not None):

return result

#### **Memory Bounded Heuristic Search**

def RECURSIVE DEPTH FIRST SEARCH(problem):

return RDFS(problem, problem.INITIAL\_STATE(), inf)

## Iterative Deepening A\* (IDA\*) Algorithm

Variant of the A\* algorithm that *generally* slower but uses less memory. Sets a maximum total cost (i.e. f(n)) to a starting value of  $\mu$ . In each round, any node whose total cost (i.e. f(n)) is greater than the maximum is ignored. Perform A\* for thresholds:

$$\mu < 2\mu < 3\mu < \cdots$$

```
def IDA_Star(problem, initial_max_cost, maximum_cost):
    current_max_cost = initial_max_cost
    while(current_max_cost < maximum_cost):
        result = A_Star_Search(problem, current_max_cost)
        if(problem.GOAL_TEST(result)):
            return result
            current_maximum_cost += initial_max_cost
        return None</pre>
```

#### Simplified Memory Bounded A\*

Approach to save memory in A\* algorithm. **Procedure:** 

second\_best\_succesor\_eval\_func\_val)

- 1. Perform  $A^*$  until you run out of memory.
- 2. Delete fringe or explored set node with the worst cost.

#### Evaluation Functions f(n) for Three Related Search Algorithms:

Uniform Cost Search: f(n) = c(n)

Greedy Best First Search: f(n) = h(n)

A\* Search Algorithm: f(n) = c(n) + h(n)

A\* algorithm is the only one of the three whose evaluation function estimates the cost of the **total solution**.

**Admissible (Optimistic) Heuristic:** Any heuristic that never over estimates the cost of a solution.

Consistent (Monotonic) Heuristic: For every node, n, every successor, n', that is reached by action, a, then the cost to reach the goal from n is less than or equal to the actual cost to go from n to n' by action a (c(n, a, n')) plus the heuristic cost of n'.

$$h(n) \le c(n, a, n') + h(n')$$

Note: Any heuristic that is consistent is also admissible.

**Example:** Triangle Inequality when the heuristic is straight-line distance.

#### The tree-search version of A\* (i.e. DAG) is optimal if h(n) is admissible, while the graph search version of A\* is optimal if h(n) is consistent.

#### Lemma #1

If h(n) was a consistent heuristic, then the values of f(n) are nondecreasing.

Given a node n' is a successor of n through action a, then:

$$g(n') = g(n) + c(n, a, n')$$

If h(n) is consistent, then:

$$h(n') + c(n, a, n') \ge h(n)$$

Then:

$$g(n') + h(n') + c(n, a, n') \ge g(n) + h(n) + c(n, a, n')$$

$$f(n') + c(n, a, n') \ge f(n) + c(n, a, n')$$

$$f(n') \ge f(n)$$

**Lemma #2:** Whenever A\* selects a node for expansion, the optimal path to that node has been found.

Had lemma #2 not been the case, then there would have been another node n' on the path from the start to n that would have been on the optimal path. Because f(n) is non-decreasing, this node would have had a lower value of f(n) and would be expanded before n in A\*. Hence, this is a contradiction.

#### Combining Lemma #1 and Lemma #2

By Lemma #2: If a goal node is explored, it is the optimal path to that goal node.

By Invariant of A\*: A\* algorithm explores nodes in nondecreasing order of f(n).

By Lemma #1: f(n) is nondecreasing.

Combining Lemma #1, Lemma #2, and Invariant of A\*: Paths to any other unexplored states, including goal states, will have evaluation function values (f(n)) greater than the first one explored. Hence, the optimal path to the first explored goal state is the optimal solution to the entire problem.

Since by lemma #2 A\* returns the optimal path to the first goal state, it returns the optimal path to the entire problem.

## **Choosing a Heuristic**

**Effective Branching Factor** (*b*\*): For a set of *N* moves, it is the equivalent number of uniform branches for a depth *d*. It is a way to quantify the quality of a heuristic.

$$N + 1 = 1 + b + b^{2} + \dots + b^{d}$$

$$N + 1 = \frac{b^{*d+1} - 1}{b^{*d}}$$

Derives from:

$$\sum_{i=m}^{n-1} a^i = \frac{a^m - a^n}{1 - a}$$

Best branch possible factor is 1.

**Relaxed Problem:** A version of the actual problem with fewer restrictions.

An exact solution to a relaxed problem is an admissible heuristic for the original problem.

**Dominating Heuristic:** A heuristic that always has a lower branching factor than another heuristic.

Composite Heuristic: Given a set of admissible heuristics  $\{h_1,h_2,\dots,h_n\}$  none of which is dominating, then the best heuristic is the composite heuristic:

$$h_{composite} = \max\{h_1, h_2, ..., h_n\}$$

**Subproblem:** A reduced version of the actual problem. Admissible heuristics can be derived from the solution to subproblems.

Pattern Database: Stores the exact solution for all versions of a particular subproblem.

To determine the heuristic cost for a version of the subproblem, look up the solution in the database and calculate the heuristic cost.

**Disjoint Patterns:** A problem can be divided into disjoint (i.e. nonoverlapping) subproblems. The disjoint solution to the problem is referred to as a disjoint pattern.

**Disjoint Pattern Database:** Stores solution to disjoint (non-overlapping, non-dependent) subproblems.

Using multiple disjoint subproblems in a disjoint pattern database, you can come up with a composite heuristic by summing the cost to solve each individual subproblem.

#### **Local Search**

**Local search** generally operates using a single **current node** and generally moves to neighbors of that node.

If the local search problem is an **optimization problem**, then it is accompanied by an **objective function** that is to be maximized or minimized.

**Complete Algorithm:** Always finds a solution if it exists.

**Optimal Algorithm:** Always finds a global maximum or minimum.

State Space Landscape: Landscape has a location (i.e. state) and an elevation (utility from the objective function)

### Hill Climbing Algorithm

Local search algorithm that always proceeds to the next successor state with maximum utility. If two successors have the same utility, algorithm randomly chooses between them. Susceptible to local maxima.

Also referred to as **Greedy Local Search**.

#### **Variants of Hill Climbing**

Sideways Move: Allow hill climbing algorithm to move to a state of equal value. Helps to move past flat area in a graph. However, in a plateau, it can lead to an infinite loop so a limit on the number of consecutive sideways moves is common.

**Stochastic Hill Climbing:** Choose a successor state at random with the probability each successor is selected proportional to its utility.

**Hill Climbing with Restarts:** Hill climbing runs from a randomly chosen initial state. If it gets a solution, it returns. Otherwise, it generates another random initial state and repeats the process. Repeated *n* times or until a solution is found.

**Example:** If the probability of finding a solution from an initial state is p, then it is expected  $\frac{1}{n}$  restarts will be required.

See page 122.

```
def HILL CLIMBING WITH RESTART(problem, max restarts):
     while( max restarts > 0):
          max_restarts -= 1
          problem.INITIAL_STATE = problem.RANDOMIZE_STATE()
          result = Hill Climbing(problem)
          if(problem.GOAL TEST(result)):
                return result
     return None
def HILL_CLIMBING(problem):
     current_state = problem.INITIAL_STATE()
     while( True ):
          # Update the previous utility
          best successor = None
          # Iterate through set of possible actions
          for action in state. ACTIONS():
                new_state = problem.RESULTS(state, action)
                if(best_successor is None
                  or problem.UTILITY(new_state) > problem.UTILITY(current_state)):
                     best_successor = new_state
          # Determine if the best successor is better than the current state
          if(problem.UTILITY(best_successor) > problem. UTILITY(current_state)):
                current_state = best_successor
                return current_state
     return None
```

Note: This is a goal based version of Hill Climbing. If you are simply searching for a maximum or minimum, you would need to modify the algorithm to return "current\_state" at the end.

#### **Simulated Annealing**

Can be used for either maximization or minimization problems.

Algorithm is designed to allow the current\_node to move to a worse state with decreasing probability as time progresses.

Probability of Moving to a Lower Value Solution is:

 $P = e^{\frac{\Delta k}{schedule(t)}}$ 

Simulated annealing chooses a random successor.

```
import math
import random
def SIMULATED ANNEALING(problem, schedule, limit, t min):
     current_state = problem.INITIAL_STATE()
     t = 0
     while( True ):
           t += 1
           T = schedule(T)
           if(T < t_min or problem.GOAL_TEST(current_state)):</pre>
                return current_state
           # Get the set of actions.
           actions = current_state.ACTIONS()
           # If no successors possible, terminate
           if(len(actions) == 0):
                return None
           # Randomly select a successor
           a = actions[random.randint(0, len(actions) - 1]
           # Get the successor state
           next_state = problem.RESULT(current_state, a)
           error = problem.UTILITY(next_state) - problem.UTILITY(current_state)
           # If error is positive or probability less than specified number, then update the current state.
           if(error > 0 or random.random() < math.exp( error/ T ):</pre>
                 current_state = next_state
```

Note: This version of the code is a maximization problem. Would need to modify slightly for a minimization problem.

#### **Local Beam Search**

Type of local search.

#### Procedure:

- 1. Begin with k randomly generated states.
- 2. Check if any descendent states at the goal. If so, return state.
- 3. Order all successors from the *k* states and sort them by decreasing performance.
- 4. Choose the best k successors. If any successor has performance measure better than the current best, return to step #2.

The *k* successors are considered a **pool of candidates**. The successors are considered **offspring**.

#### Variant of Local Beam Search

Stochastic Local Beam Search: Choose *k* successors stochastically based off some metric.

#### **Genetic Algorithm**

```
A genetic algorithm is a stochastic beam search algorithm with one key modification:
```

- In local beam search, successors come from modifying a single state (asexual reproduction).
- In genetic algorithm, successors come from combing two parent states (sexual reproduction).

**Population**: Set of *k* solutions. The **initial population** is *k* randomly generated solutions.

Individual: One solution/state in the population.

**Fitness Function:** Evaluation function that rates the quality (i.e. fitness of a solution) generally with general condition that better states have higher fitness function value.

**Crossover:** Process of merging two solution states to form a

Mutation: Random change to a successor solution.

```
def GENETIC_ALGORITHM(problem, FITNESS_FUNCTION, t_max)
     # Generate the population.
     population = problem.GENERATE_POPULATION()
     # Start at time 0.
     while(t < t_max or Not problem.GOAL_TEST(best_solution)):</pre>
          # Increment current time.
          t += 1
          new_population = {}
          best_solution = None
          for i in range(0, problem.POPULATION_SIZE()):
               # Select two parent solutions.
               x = RANDOM_SELECTION(population, FITNESS_FUNCTION)
               y = RANDOM_SELECTION(population, FITNESS_FUNCTION)
               # Merge the two solutions
               child = REPRODUCE(x, y)
               # Mutate on a low probability
               if(random.random() < problem.MUTATION PROBABILITY):</pre>
                    problem.MUTATE(child)
               if(best_solution is None or problem. UTILTY(best_solution) < problem.UTILTY(child)):
                    best_solution = child
               # Add the child solution to the new population.
               new_population.append(child)
          # Set the population to the newly created set.
          population = new_population
     return best solution
def REPRODUCE(x, y):
     # Pick a random cross over point
     crossover point = random.randint(0, len(x) - 1)
     # Crossover the two halves
     return x[0:crossover_point] + y[crossover_point:len(y)]
```

#### 8-Puzzle Goal State:

uzzie Guai Sta		
Х	1	2
3	4	5
6	7	8

## Minimax (Adversarial Search)

Adversarial search problems are those search problems that arise in multiagent, competitive environments. Adversarial search problems are also known as games.

In a zero-sum game, the results for the two players are always equal and opposite.

**Optimal Strategy** – A sequence of contingent decisions that will lead to outcomes as least as good as any other sequence of decisions against an infallible player.

**Perfect Information** – Any situation where an agent has all relevant information with which to make a decision and the results of actions are **deterministic**.

Minimax Value — Utility of being in a current state assuming both players play optimally until the end of the game.

```
H - MINIMAX(s, d) = \begin{cases} UTILITY(p), & \text{if } CUTOFF\_TEST(s, d) \\ \max_{a \in ACTIONS(s)} H - MINIMAX(RESULT(s, a), d), & \text{if } PLAYER(s) \text{ is } MAX \\ \max_{a \in ACTIONS(s)} H - MINIMAX(RESULT(s, a), d), & \text{if } PLAYER(s) \text{ is } MIN \end{cases}
```

#### Initial State in Minimax - 50

Given a state, s, the six key methods used on that state are:

- 1. PLAYER(s) Returns active player for the current state
- 2. ACTIONS() Set of all possible actions/moves that can be made.
- 3. RESULTS(s,a) Given a state, s, and an action a, it returns the successor state. It is also called a Transitional Model.
- 4. CUTOFF\_TEST(s,d) Used in Heuristic minimax. Given a state, s, and a recursive depth, d, it determines if the cutoff condition of either a maximum depth or goal state has been reached.
- 5. TERMINAL\_TEST(s) Used in standard minimax. Given a state, s, this function returns whether a goal state has been met. Terminal states are leaf nodes in the search tree.
- 6. UTILITY(s) Given a state, s, this function returns the state's utility score. It is also called a Utility Function.

Time Complexity with Alpha-Beta Pruning:  $O\left(b^{\frac{d}{2}}\right)$ 

Time Complexity without Alpha-Beta Pruning:  $O(b^d)$ 

```
def Minimax_Algorithm(state, is_max):
     alpha max = -inf
     beta min = inf
     best successor = None
     # Iterate through all possible actions from this state
     for a in state. ACTIONS():
          # Get the successor state
          next state = state.RESULT(state,a)
          # Call heuristic minimax with starting depth 0
          score = H-Minimax(next_state, 0, !is_max,
                            alpha_max, beta_min)
          if(is max and score > alpha max):
                best successor = a
                alpha_max = score
          elif(not is_max and score < beta_min):</pre>
                best successor = a
                beta min = score
     # Return the move with the best score
     return best move
```

```
def H-Minimax(state, depth, is_max, alpha_max, beta_min)
     # p is the reference player for the utility function. Typically max.
    if ( state.CUTOFF-TEST(depth) ):
          return state. UTILITY(p)
    for a in state.ACTIONS():
          next state = state.RESULT(state, a)
          if(is_max):
               # Perform beta pruning
               alpha_max = max(alpha_max, H-Minimax(next_state, depth+1,
                                  not is_max, alpha_max, beta_min))
               if(alpha_max ≥ beta_min):
                     return alpha max
               beta_min = min (beta_min, H-Minimax(next_state, depth+1,
                                not is_max, alpha_max, beta_min))
               # Perform alpha pruning
               if(alpha max ≥ beta min):
                     return beta_min
    # After all actions tested, return score.
    if(is max):
          return alpha_max
    else:
          return beta_min
```

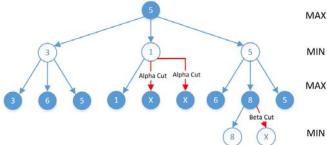
## **Alpha Beta Pruning**

Alpha  $(\alpha)$  – Maximum value found along the path by the MAX player.

**Alpha Cut/Alpha Pruning** – Performed by the **MIN player**. When the MIN player's minimum score is already less than a previous MAX player's maximum score, stop investigating subsequent paths and return the **current minimum score**.

Beta  $(\beta)$  – Minimum value found along the path by the MIN player.

Beta Cut/Beta Pruning – Performed by the MAX player. When the MAX player's maximum score is greater than a previous MIN player's minimum score, stop investigating subsequent paths and return the current maximum score.



Minimax Search Tree Example with Alpha and Beta Cuts.

This is a three move/ply search tree.

#### **Constraint Satisfaction Problem**

Search problems deal with states that are atomic (i.e. indivisible).

Often a state has field variables. Such field values are called a **factored representation** of the problem. A state **solves** a factored representation if each field variable satisfies all constraints on that variable.

A factored representation can allow you to eliminate large areas of the search space by identifying then ignoring variable/value combinations that violate constraints.

A constraint satisfaction problem solution is an assignment of values to variables that satisfies all constraints.

Assignment of values to variables in CSPs is **commutative**. Hence, the order that the values are assigned do not matter. If you consider the problem a search tree, there are at most d children from each node leaving a total of  $d^n$  solutions for a finite domain

#### **Components of a Constraint Satisfaction Problem:**

- 1. X Set of variables  $\{X_1, X_2, X_3, \dots, X_n\}$
- 2. D Set of Domains  $\{D_1, D_2, D_3, \dots, D_n\}$
- 3. C Set of Constraints  $\{C_1, C_2, C_3, \dots, C_n\}$

#### **Optional Definition:**

assignment.

R - Relation of multiple variables  $R(X_i, ..., X_m)$ 

**Definition of a Constraint** 

A constraint is a pair: < scope, relation >

Scope: Tuple of variables that participate in the constraint

**Relation:** A relation that the variables can take on.

**Assignment** – Allocation of values to variables.

Solution: A complete and consistent

**Consistent Assignment** – An assignment of values that does not violate any constraints.

This leads to the term **consistency** which is the **satisfaction of constraints**.

**Complete Assignment** – Every variable is assigned a value.

**Partial Assignment** – Only a subset of variables are assigned a value.

Domain

A variable's domain can be either discrete or continuous. If it is discrete, it can be either finite or infinite (e.g. set of integers).

Simplest CSP Type: Finite, discrete domain

**Constraint Language** 

Defines the allowed relations between variables. It eliminates the need to enumerate allowed value lists.

**Linear Programming Problem:** Continuous CSP with **linear constraint function**(s).

Constraint functions can also be nonlinear.

Constraint Types

 $X = \{X_1, X_2\} \text{ and } D = \{A, B\}$ 

Example Constraint:

 $C = \langle (X_1, X_2), rel \rangle$ 

with

 $rel = \{(A, B), (B, A)\}$ 

**Precedence Constraint:** A

constraint that forces one variable to occur before (i.e. be less than) another variable.

xample:

 $T_1 + d \leq T_2$ 

Disjunctive Constraint: A

constraint that two variables do not overlap (i.e. are not equal):

Example:

 $T_1 + d \le T_2 \text{ or } T_2 + d \le T_1$ 

Absolute Constraint: Any constraint that must be met.

Preference Constraint: A constraint which guides the solution to preferred values.

Problems that optimized preference constraints are called **constraint optimization problems**.

**Unary Constraint** – A constrain involving only a single variable.

**Binary Constraint** – A constrain involving exactly two variables.

**Higher Order Constraint**: A constraint that involves a **fixed** number of variables that is more than two.

All higher order constrains can be reformed as a set of binary constraints.

Global Constraint: A constraint that takes an arbitrary number of variables. It does not need to be all variables. It just needs to be **not fixed** (i.e. arbitrary).

Example: Alldiff

Constraint Graph/CSP Network: Representation of a CSP as a graph. Each node is a variable and the arcs are binary constraints.

**Inference:** Using known/assigned values for a set of variables to select the values for other variables.

Constraint Propagation: Using the constraints to reduce the number of legal values for a variable. This in turn reduces the number of legal values for other variables in a cycle.

Local Consistency: Given a constraint graph, enforcing consistency (i.e. ensuring variables satisfy constraints) locally in each part of the graph leads to invalid values being eliminated throughout the graph.

**Node Consistency** 

Node Consistent Variable – Any variable where every value in the variable's domain satisfies all of its unary constraints in a CSP network.

Node Consistent Network – Any CSP network where all variables are node consistent.

Node consistency can be done as a **preprocessing step** to eliminate invalid values.

#### **Arc Consistency**

Arc Consistent Variable – Any variable where every value in the variable's domain satisfies all of its binary constraints in a CSP network.

Variables are arc-consistent with respect to one another. Example: X being arc consistent with respect to Y does **NOT** imply Y is arc consistent with respect to X.

Arc Consistent Network - Any CSP network where all variables are arc consistent.

#### AC-3 (Arc Consistency Algorithm #3)

Algorithm used to solve for Arc consistency Only possible with finite domains.

#### **Constraints in Arc Consistency Algorithm**

In each iteration of AC-3 algorithm, it only checks the variable being arc-constrained (example in constraint (X,Y), X is being constrained by Y). To have a two directional constraint for X and Y, arc queue would need to contain (X, Y) and (Y, X)

After reducing the domain of X from constraint (X, Y), algorithm needs to recheck any domains that were constrained by X to ensure its domain values are still valid.

#### **Running Time of AC-3 Algorithm**

#### 1. REVISE Function: $O(d^2)$

For each value in the domain of  $X_i$  (up to delements), you iterate overall elements in the domain of  $X_i$ . Hence the running time is:

$$O(d*d) = O(d^2)$$

#### 2. Number of Times REVISE function is Run Per Constraint: O(d)

The REVISE function is run whenever a constraint is popped off the queue. If the domain size is queue, it can be popped off the queue up to d times (once for each element.

#### 3. Number of Constraints: c

#### **Total Running Time:**

$$\mathbf{O}(c) \cdot \mathbf{O}(d) \cdot \mathbf{O}(d^2) = \mathbf{O}(cd^3)$$

```
def AC_3(csp):
     arc_queue = []
     # Add all binary constraints to the queue.
     for b constraint in csp.BINARY CONSTRAINTS:
           arc_queue.append( (b_constraint.X_i, b_constraint.X_j )
     # Iterate until all arcs have been made consistent or an inconsistency is found.
     while(len(arc queue) > 0):
           (X_i, X_j) = arc_queue.pop()
           # Check if the domain of X i is revised.
           if( REVISE(csp, X_i, X_j) ):
                 if(len(X_i) == 0):
                      return False
                 # Only X_i's domain is reduced in function "REVISE" so only check relative to that.
                 # Since X_i's domain is reduced, any variable that is constrained by X_i may need to be reduced
                 for X k in X i.NEIGHBORS() - {X j}:
                      # Only add back to domain if not X j
                      if(X_k != X_j and (X_k, X_i) not in arc_queue):
                            arc_queue.append((X_k, X_i))
     return True
def REVISE(csp, X_i, X_j):
     revised = False # Confirmed in loop
     # Verify all elements in the domain of X_i have a corresponding value in X_j.
     for x in csp.D_i:
           constraining_value_exists = False
           # Iterate through all elements in X_j's domain to see if it constrains x in X_i.
           for y in csp.D_j:
                 if( (x,y) in csp.C(X_i, X_j)) :
                      constraining_value_exists = True
           # If no constraining value exists in X_j, then remove the value from X_i.
           if(not constraining_value_exists):
                 csp.D_i.remove(d)
                 revised = True
     # Return whether the domain of X_i was revised (i.e. reduced)
```

### **Path Consistency**

Path Consistency – A two variable set  $(X_i, X_i)$  are path consistent with respect to a third variable  $X_m$  if for every assignment of values to  $X_i$  and  $X_i$ consistent with the constraint  $\{X_i, X_i\}$ , there is a valid assignment to  $X_m$ that satisfies the constraints  $\{X_i, X_m\}$  and  $\{X_m, X_i\}$ .

#### Origin of the Term "Path Consistency"

Given a two variable set  $\{X_i, X_i\}$  that is path consistent with respect to a variable  $X_m$ , then it is like  $X_m$  is on the path between  $X_i$  and  $X_i$ .

Algorithm to Solve to Check for Path Consistency: PC-2

#### k-Consistency

A CSP is k-consistent if for any set of k-1 variables and for any consistent assignment to those variables, a consistent value can always be assigned to any k-th variable.

Proving k-consistency takes exponential and space in the worst case.

1-consistency is node consistency.

return revised

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2-consistency is arc consistency. Strongly k-consistent: Any CSP that is 1-consistent and 2-consistent and 3-consistent through k-consistent. Hence it is consistent for variable sets of size 1 through k.

Given *n* variables and a CSP that is strongly *n*-consistent, then an assignment of values is possible for this CSP.

Running Time to Solve n-Consistent CSP

## Time Complexity: $O(n^2d)$

Running time derives since for every i-th variable to assign, you must check all i-1 variables for every d elements in the

$$d \cdot \sum_{i=1}^{n} i - 1 = d \cdot \left( \frac{n \cdot (n+1)}{2} - n \right) = O(dn^2)$$

### **Consistency Checks for Global Constraints**

**Global Constraint** – A constraint with

an arbitrary number of variables.

**Example Global Constraint:** Alldiff

#### Alldiff Consistency Algorithm

- 1. Delete a variable that has a singleton domain.
- 2. Remove the value from the domains of all other variables.
- 3. If any singleton domain variables still exists, jump to step #1.
- 4. If a domain has no values or there are more values than there are variables, the Alldiff constraint fails.

#### **Simplified Explanation of Alldiff Consistency Check**

If there are *m* variables and *n* possible values and m > n, then an inconsistency exists.

#### Sudoku

Square grid of n by n cells. All numbers in a row must be unique and all numbers in a column must be unique. For every  $\sqrt{n}$  by  $\sqrt{n}$  subgrid, all numbers must be unique. Each section of the board where all numbers must be unique (e.g. row, column, subgrid) is called a **unit**.

Formal Definition of Sudoku as a CSP:

Variables:  $n^2$  total variables (one for each cell).

**Domain:**  $\{1, 2, 3, ..., n\}$ 

Constraints: 3n Alldiff constraints for each unit.

AC-3 Algorithm can be used to infer the value of cells and to reduce the domains of cells.

#### **CSPs and Backtracking**

Backtracking Search – Variant of Depth First Search where values are assigned to variables until no consistent, legal assignments are possible for a given variable at which point the algorithm backtracks to try to reassign a previous variable to a new value.

**Key Functions in Backtracking Search** 

- 1. SELECT UNASSIGNED VARIABLE
- 2. ORDER\_DOMAIN\_VALUES
- 3. INFERENCE
- 4. BACKTRACK (recursion)

See page 215.

```
def BACKTRACKING SEARCH(csp):
     return BACKTRACK({}, csp)
def BACKTRACK(assignment, CSP):
     # Consistency of all variable assignment checked so if assignment is complete, it is a solution.
     if(csp.COMPLETE_ASSIGNMENT(assignment)) return assignment
     # Select the next variable to assign
     next var = csp.SELECT UNASSIGNED VARIABLE()
     # Order the domain values based off which want to check first
     var_doman = csp.ORDER_DOMAIN_VARIABLES(assignment, next_var)
     # Iterate through all domain values.
     for d in var_domain:
          # Ensure the assignment is consistent.
          if(csp.CONSISTENT_ASSIGNMENT(assignment, d)):
               # Add the variable value to the assignment
               assignment[var_domain] = d
               # Get and apply any inferences
               inferences = csp.INFERENCE(assignment)
               # Only recurse if valid inferences found.
               if(inferences is not None):
                    assignment.APPLY_INFERENCES(inference)
                     result = BACKTRACK(assignment, csp)
                    if( result is not None):
                          return result
                     assignment.REMOVE INFERENCES(inference)
               # Since no solution found using this assignment and variable value
               # remove this variable value from the assignment.
               remove( assignment[var_domain] )
     # No solution found so return None for failure.
     return None
```

#### **Making Backtracking Search More Efficient and Sophisticated**

#### **Variable Ordering**

By selecting a variable most likely to fail earliest, you are prune the search tree and reduce the effective branching factor.

Minimum Remaining Value (MRV), Fail First, Most Constrained Variable Heuristic: Select the variable to assign next that has the smallest inferred domain (i.e. least remaining legal values).

Degree Heuristic: Select the variable for expansion that has the largest number of constraints on other variables. Most commonly used heuristic to select the first variable for assignment.

Degree heuristic can be used as a tie breaker for the more powerful MRV heuristic.

## Value Ordering

Constraining

Least-

Value
Heuristic:
Select the
value that
rules out the
least number
of values for
neighboring
variables in
the graph.

# Interleaving Search and Inference

AC-3 can be used to infer reductions in the search domain both **before and during** search.

Forward Checking – One way to implement "Inference" in Backtracking algorithm. Whenever a variable is assigned, establish arc consistency for it on all unassigned variables. If arc consistency checking was done in preprocessing, forward checking adds no value.

MRV can be combined with forward checking to further prune the search tree.

Chronological Backtracking: Simplest form of backtracking. Revisit the last assigned variable (i.e. most recent decision) before the current variable. If the previous variable does not constrain the current variable, backtracking to only that level is wasteful.

#### **Intelligent Backtracking**

Better to backtrack to a variable that may fix the consistency issue.

**Conflict Set:** Set of value assignments that conflict with a some value for a variable. **Note:** This is value assignments not variables since a variable that can conflict for one value does not conflict for the currently assigned value.

**Backjumping:** Backtracking to the most recent variable in the conflict set.

Variable ordering is fail-first ordering while value ordering is fail-last. This is because when you are trying to fail-first by selecting a variable, the order you inspect the values does not matter as you need to inspect them all anyway. As such, it makes the most sense to inspect the best solutions first in case one of them does actually succeed.

#### **Logical and Knowledge Based Agents**

Knowledge Base (KB) – Central component of a knowledge based agent. Composed of a set of sentences. Similar to a database

Knowledge Representation Language - Formal notation used to express sentences in the knowledge base (KB).

Sentence – Statements that define the knowledge based. They have a specific notation called a syntax and their value (i.e. true or false) is defined by the semantics.

Axiom – A sentence that is taken as given without being derived from other sentences.

Inference – Deriving new sentences from existing sentences.

- Valid Knowledge Base Operations: TELL
  - 2. ASK

1.

**Supporting Knowledge Based Agent Commands:** 

- MAKE PERCEPT SENTENCE 1.
- MAKE ACTION QUERY
- MAKE\_ACTION\_SENTENCE

Background Knowledge - Initial knowledge in the knowledge base.

Four Step Procedure for a Knowledge Based Agent:

- Tell the knowledge base what it perceives.
- Ask the knowledge base it should perform.
- 3. Tell the knowledge base the action it will perform.
- Executive the action.

def KNOWLEDGE BASED AGENT()

# KB is the persistent knowledge base.

# t a time counter initially starting at 0.

TELL( KB, MAKE PERCEPT SENTENCE(t) ) action = ASK(KB, MAKE ACTION QUERY(t)) TELL ( KB, MAKE\_ACTION\_SENTECE(t) )

t += 1 # Increment time

# Return the selected action. return action

Knowledge Level – What the agent knows at a give point in time. Given an agent's knowledge level and goals, you can predict its actions. Declarative Approach - Tell the knowledge base all it needs to know.

Procedural Approach - Procedures for desired behaviors and actions are hard coded into the agent.

#### **Wumpus World**

The knowledge based agent is in an environment consisting of rooms connected by passageways. Some rooms contain bottomless pits while others contain goal. One wumpus lives in the cave in one room. Wumpus eats anyone who enters its room but does not move. Player has one arrow that can kill the wumpus.

#### **Performance Measure**

- +1000 points for getting gold. -1000 points for falling into a pit or eating a wumpus.
- -1 for each action taken. -10 for using an arrow.

#### **Actuators**

Move forward one room. Turn left 90 degrees. Turn right 90 degrees. Shoot the arrow

Climb out (if in starting space)

#### **Sensors**

Stench: A wumpus is in an adjacent room. Breeze: A pit is in an adjacent room. Glitter: Gold is in the player's room Scream: Wumpus is killed.

Bump: Player walks into a wall.

#### Logic

Syntax - Sentence formatting to make all knowledge sentences well formed.

Semantics - Provide meaning to sentences. It defines truth for every possible world.

**Example:** For the sentence, x + y = 4 is true in the world where x = 2 and y = 2. Model - Substitute for the phrase "possible world." A model fixes the truth or falsehood for every relevant sentence.

Satisfaction: Making a sentence true using an allowed model/possible world.

**Example:** If sentence  $\alpha$  is true in model m, then model m satisfies sentence  $\alpha$ .

#### **Entailment**

**Entailment Between Sentences: When one sentence** logically follows from another sentence or set of sentences. It is similar to implies in philosophy.

#### Symbol: ⊨

Given two sentences  $\alpha$  and  $\beta$ , then sentence  $\alpha$  entails the sentence  $\beta$  if and only if:

$$\alpha \vDash \beta \Leftrightarrow \forall M(M(\alpha) \subseteq M(\beta)$$

The knowledge base is a set of sentences. The knowledge base is false in models that conflict with the knowledge base.

Model: Fixes the truth value (i.e. true or false) for each

Atomic Sentence: Simplest type of sentence and contains a

Naming Convention: First letter is capitalized followed by

Positional symbols with fixed meaning: True (always true

Syntax: Defines allowable sentences.

proposition symbol.

Semantics: Defines what a sentence means.

single propositional symbol (i.e. variable)

statement that can be either true of false.

position) and False (always false proposition)

lower case letters and subscripts.

Propositional Symbol: Represents a proposition or

Model Checking: Given a knowledge base, KB, and verify it is a model of  $\alpha$ . Hence:

$$M(KB) \subseteq M(\alpha)$$

Model checking entails enumerating all possible models to determine whenever KB is true that  $\alpha$  is also true. It only works on finite domains.

Logical Inference: Process of drawing conclusions (i.e. new sentences) through entailment.

#### Symbol of Inference: +

Given a knowledge base, KB, and a sentence  $\alpha$ , if an inference algorithm, *i*, inferred  $\alpha$  from *KB* then:

 $KB \vdash_i \alpha$ 

Sound or Truth Preserving Inference Algorithm: Can only derive entailed sentences. Hence it cannot prove any sentence that is wrong.

Example: Model checking is a sound algorithm since it does not work on infinite spaces.

Complete Inference Algorithm: Can derive any entailed sentence. A complete inference algorithm can prove anything that is right.

#### **Syntax**

**Logical Connectives** 

→: Not (Negation)

V: Or (Disjunction). Individual terms are called disjuncts.

Symbols that operate on propositional logic symbols.

A: And (Conjunction). Individual terms are called conjuncts.

⇒: Imply (Implication)

 $\Leftrightarrow$  or  $\equiv$ : Biconditional. "If and only if"

 $A \Rightarrow B$  is True unless A is true and B is false.  $A \Leftrightarrow B$  is true only if A and B are both true or are both false.

If  $A \Rightarrow B$ , then:

- A is the premise or antecedent
- B is the conclusion or consequent.

#### **Valid Sentence**

AtomicSentence := True|False|P|Q|RSentence := AtomicSentence | SentenceComplexSentence := (Sentence) | [Sentence]

| → Sentence

| Sentence \( \text{Sentence} \) | Sentence ∧ Sentence

| Sentence  $\Rightarrow$  Sentence | Sentence  $\Leftrightarrow$  Sentence

#### **Operator Precedence**

 $\neg$ ,  $\lor$ ,  $\land$ ,  $\Rightarrow$ ,  $\Leftrightarrow$ 

## **Inference Proving**

Checking if  $KB \models \alpha$ 

**Model Checking:** Enumerate all the models and check if all for all possible models where KB is that  $\alpha$  is also true. **Model checking is very similar to a truth table.** 

**Theorem Proving:** Using sentences already in the model, apply rules of inference to construct a proof of the desired sentence without consulting models.

**Literal:** In a complex sentence, a literal is either an atomic sentence (i.e. **positive literal**) or its negation (i.e. **negative literal**).

**Logical Connectives:** Used to construct complex sentences out of atomic sentences.

**Logical Equivalence:** Two sentences  $\alpha$  and  $\beta$  that are true in the same set of models. **Notation:**  $\alpha \equiv \beta$ 

Validity: A sentence that is valid (true) in all models.

Tautology: A valid sentence.

#### **Common Logical Equivalences**

Commutative of ∧	$(\alpha \land \beta) \equiv (\beta \land \alpha)$	Commutative of ∨	$(\alpha \vee \beta) \equiv (\beta \vee \alpha)$
Associativity of ∧	$((\alpha \land \beta) \land \gamma) \equiv (\alpha \land (\beta \land \gamma))$	Associativity of ∨	$((\alpha \vee \beta) \vee \gamma) \equiv (\alpha \vee (\beta \vee \gamma))$
<b>Double Negation</b>	$\neg (\neg \alpha) \equiv \alpha$	Contraposition	$(\alpha \Rightarrow \beta) \equiv (\neg \beta \Rightarrow \neg \alpha)$
Implication Elimination	$(\alpha \Rightarrow \beta) \equiv \rightarrow \alpha \lor \beta$	Biconditional Elimination	$(\alpha \Leftrightarrow \beta) \equiv ((\alpha \land \beta) \lor (\neg \alpha \land \neg \beta))$
DeMorgan's Law	$\neg (\alpha \land \beta) \equiv (\neg \alpha \lor \neg \beta)$	DeMorgan's Law	$\neg (\alpha \lor \beta) \equiv (\neg \alpha \land \neg \beta)$
Distributivity of ∧ and ∨	$(\alpha \land (\beta \lor \gamma)) \equiv ((\alpha \land \beta) \lor (\alpha \land \gamma))$	Distributivity of ∧ and ∨	$(\alpha \vee (\beta \wedge \gamma)) \equiv ((\alpha \vee \beta) \wedge (\alpha \vee \gamma))$
Modus Ponens	$(\alpha, \alpha \Rightarrow \beta) \equiv \beta$	Modus Tollens	$(\neg \beta, \alpha \Rightarrow \beta) \equiv \neg \alpha$
And Elimination	$(\alpha \land \beta) \Rightarrow \alpha$		

**Satisfiability:** A sentence that can be made true with some model. For a finite environment, satisfiability can be by enumerating all possible models and seeing if any leads to the statement being true. CSP consistency checking is a type of satisfiability problem.

**Validity and Satisfiability:** A sentence is valid if and only if its negation is not satisfiable.

**Reduction ad absurdum/Proof By Reduction/Proof by Contradiction**: Given a logical expression, assume the opposite of the expression and determine if it is satisfiable.

**Example:**  $(\alpha \land \beta)$  is true in the model:  $M = \{\alpha = True, \beta = True\}$ 

**Proof:** A chain of conclusions that leads to the establishing some statement following from the knowledge base.

#### **Example**

Consider a situation where four light switches on a control panel. Define a knowledge base for this system with conditions defined in **Part A** and **Part B**.

#### **Definition:**

 $S_1$ : Propositional symbol for the first switch and is true if the switch is on and false otherwise.

S<sub>2</sub>: Propositional symbol for the second switch and is true if the switch is on and false otherwise.

 $S_3$ : Propositional symbol for the third switch and is true if the switch is on and false otherwise.

S4: Propositional symbol for the fourth (i.e. last) switch and is true if the switch is on and false otherwise.

Part A: The first and last switches are never both on.

$$\neg (S_1 \land S_4)$$
  
$$\neg S_1 \lor \neg S_4$$

Part B: At least one switch must be on.

$$S_1 \vee S_2 \vee S_3 \vee S_4$$

## **Python Review**

#### **Python Basics**

**Command Line Call to Run Python:** python filename.py **Python File Extension:** \*.py

**Command to Print to Console:** print "Hello World!" Printing without Inserting a Newline: Use "," (Comma)

**Command to Get Last Result:** \_ (Underscore) Example: >>> 2/3 + 7.9 >>> print \_ + 1 # prints 8.9

**Valid Python Operators:** +, \*, -, /, \*=, /=, -=, +=, %, ==, != // (Integer Division), \*\* (Power)

Math Functions:

math.exp( value ): e^value random.randint(n,m): Integer  $n \le x \le m$ random.random(): Float  $0 \le x < 1$ 

**Invalid Operators:** 

++, --

**Minimum and Maximum Value:** 

Use the % symbol similar to C/C++

inf, -inf

Conditionals: if( expr ): # Do something elif( expr ): # Do something

# Do something

is, and, or, not **Boolean Literals:** True, False

print "Hello World",

**Boolean Arithmetic:** 

**Check Membership in List:** 

File IO: f = open("filename.txt", "w") line = f.readline() f.close()

# Iterate over a file line by line for line in open("my\_file.txt"): #Do something

**Formatted Printing:** 

print "%3d %0.2f" % (10, .9799) # Prints "10 0.98"

**Python String Manipulation** 

**Python String Implementation** Immutable list of characters.

**String Concatenation:** 

**Converting from a String:** 

int("38") float("46.456")

Converting to a String:

str(7)

repr(32.9)

**Substring Manipulation** 

Use [] like a list with the first character index 0 a = "Hello World" print a[4] # Prints "o" print a[:5] # Prints "Hello" print a[6:] # Prints "World" print a[3:8] # Prints "lo Wo"

**Checking for Substring:** 

Use the *in* operator: if( "hello" in "hello world"): print "It's in there."

**Get Index of Substring:** x = "hello world".index("llo") print x # Prints "2"

#### **Element Containers**

List (Array) Basics:

+ (plus sign)

Able to hold data of different types in the same list including other lists. Uses [] x =[ 5, 4, "hello", "world" ] print x[1] # Prints "4" print x[1:] # Prints "[4, "hello", "world"]" print x[0:2] # Prints "[4, 5]" y = [3, 2], [1, 0]print y[1][0] # Prints 1

**Nested (Two-Dimensional) Lists:** 

y = [[3, 2], [1, 0]]print y[1][0] # Prints 1 **Concatenating Lists:** x = [1, 2, 3]y = [4, 5]z = x + v

print z # Prints "[1, 2, 3, 4, 5]"

List Length: Use len()

x = [1, 2, 5, 10]print len(x) # Prints "4"

**Extracting List Properties:** max( list ) - Gets Maximum Value in List

min( list ) - Gets Maximum Value in List

Tuple:

Immutable list. Created used () parenthesis.

**Accessing Tuple Elements:** 

c = (4, 5)print c[1] # Prints "5" a, b = c # a = 4 and b = 5

**Creating a Tuple:** 

a = (1, 2, 3) # Tuple of size 3 b = (x, y) # Tuple made of two variables c = "Hello", "World" # Tuple of size 2 d = () # Empty Tuple e = "yo", # Tuple of size 1 f = ("yo", ) # Equal to e g = (d, ) # Tuple of empty tuple ((), )

Sets:

Unordered collection of unique elements. x = set([3, 6, 9, 2])my\_set = set("goodness") print my set # Prints ["g", "o", "d", "n", "e", "s"] with no duplicates Frozenset:

An immutable set. x = frozenset([4, 5, 6])

**Set Operations:** 

| Union, & Intersection, - Difference, ^ Symmetric Difference (XOR)

Dictionary:

Associative Array (i.e. hash table). Uses {} curly brackets. person ={ "name": "bob". "age": "27", "sex": "Male"

print person["name"] # prints "Bob" **Deleting from a Dictionary:** del person["name"]

**Dictionary Membership Test:** 

Use the keyword "in" if( "name" in person ): print person["name"] # Prints "bob"

**Accessing Tuple Elements:** 

person.kevs() # Gets all dict keys person.values() # Gets all dict values person.len() # Gets all dict length

**Looping and Iteration** 

While Loop:

while( expr ): # Do something For Loop:

for x in [2, 4, 5, 6, 9]: print x for y in range(1, 10): print y # Only prints 9 lines range:

Iterable object in Python. range(0, 10) - Creates list of 0 to 9 in steps of 1 range(10) – Starting 0 not needed. Same as range(0,10) range(0, 5, 2) - Starts 0 and steps by 2 until 5 range(7, 2, -1) - Starts at 7 and decrements by 1 until 3

range vs. xrange:

range creates an array that Python iterates over. This is memory inefficient. xrange acts like a real for loop without the memory overhead of range.

**Iterable Objects in Python:** 

set, frozenset List, Tuple Dictionary key File (open("filename") String (letter by letter) Generator

#### **Functions**

```
Creating a Function:
Keyword: def
def my_func(params):
 # Do something
Keyword to Return: return
Supports Recursion: Yes
Taking an Arbitrary Number of Input Variables
Keyword: *args
def my_function(*args):
```

```
Scope:
Default scope in python is local.
def print_i():
 i = 4
 print i
print_i() # Prints "4"
print I # Prints "5"
```

```
Keyword to Add to Global Scope:
global
def assign_i():
 global i
 i = 3
```

```
Storing a Function in a Variable:
def print i()
 i = 4
 print i
a = print_i
a() # Prints "4"
```

```
Anonymous Function:
Keyword: lambda
g = lambda x: x**3
print g(10) # Prints "1000"
h = lambda y, z: z + 2*y
print h(2, 3) # Prints "8"
def make_adder(n):
  return lambda z: z+n
f = make adder(2)
print f(3) # Prints "5"
print f(6) # Prints "8"
g = make adder(4)
print f(3) # Prints "7"
print f(6) # Prints "10"
LAMBDA NEVER HAS A RETURN
```

## Generator

Uses the yield construct and the object method next.

Allows you to get a sequence of objects in a dedicated routine.

```
def countdown(n):
     while(n > 0):
           yield n
           n -= 1
```

# Creates the function call as object but does NOT run it yet x = countdown(3)

```
print x.next() # First runs "countdown(3)" then prints "3"
print x.next () # Prints "2"
print x.next () # Prints "1"
```

#### Coroutine

Uses the yield construct and the object method send and next.

Allows you to pass a sequence of values one at a time to a function (e.g. log file printer)

```
def print_matches(text):
     print "Trying to find text: " + text
      while(True):
            line = (yield)
            if(text in line):
                 print line
```

# Creates the function call as object but does NOT run it yet x = print\_matches("hello") x.next() # Runs to first yield. print x.send("lalalala") # Prints nothing print x. send ("hello world") # Prints "hello world"

#### Classes

```
class ClassName(inherited class1, inherited closs2):
     # Class variables
     class name = "Class Name"
     # Constructor
     def init (self):
          self.attribute1 = 1
          self.attribute2 = [3, 4]
          self.length value = 1
     # Called without parenthesis for methosd
     @property
     def length(self)
          return self.length_value
     # Called by ClassName.static_method(arg)
     @staticmethod
     def print_class_name()
          print class_name
             Calling Supercass Methods
Option #1
super(SuperClassName, self).methodName(variables)
Option #2
 _ClassName__method_name(variables)
```

**Invoking a Class Constructor:** Use the class name followed by two paranethesis. Example for class "Stack":

Example: my\_stack = Stack()

#### **Class Special Methods:**

name Always preceded and proceeded by two underscores.

@property: Class methods that do not require parenthesis when called. Typically return an object or primitive.

Static Method: @staticmethod Called using the class name not an object name.

#### Example:

pass

ClassName.static method()

Inheritance and Classes: Python class can inherit multiple classes.

#### **Class and Inheritance Functions:**

- type(variable name): Returns a formatted string of object's class name.
- isinstance(variable\_name, ClassName): Returns True if variable is of type ClassName, False otherwise.

Example: isinstance(my\_stack, Stack) returns True.

issubclass(SubclassName, ClassName): Returns true if SubclassName is a subclass of ClassName.

Example: issubclass(Stack, object) returns True.

#### **Abstract Classes**

Requires the import: from abc import ABCMeta, abstractmethod, abstractproperty

# Required first line for abstract class \_\_meta\_class\_\_ = ABCMeta

@abstractmethod

def my\_method(args): pass

@abstractproperty def my\_method(args): pass

**Abstract classes do NOT inherit** ABCMeta.

#### **Exceptions**

```
Format for an Exception
try:
     pass
except ErrorTypeName as error object:
     # Catches only error of type ErrorName
     pass
except:
     # Catches all exceptions
finally:
     # Always run
     pass
```

```
Creating Your Own Exception
```

```
class MyException(exception):
     def init (self, errno, msg):
          self.args = (errno, msg)
          self.errno = errno
          self.msg = msg
class MyException2(exception):
```

Use the raise keyword

raise MyException(404, "Access Forbidden")

**Throwing an Exception** 

#### Modules, Importing, and the sys Toolset

#### Importing From a Module with Normal Namespace Syntax: import filename

Filename is the python filename without the file extension (.py). When importing in this fashion, it uses the file name as the namespace for the functions/classes in that file.

Example: Python file div.py has a function called divide that divides to integers.

import div

print div.divide(4,2)

Importing From a Module with a New Namespace

Syntax: import filename as namespace Use a custom namespace name for

Example: Python file div.py has a function called divide that divides to integers. New namespace is named "foo"

import div as foo print foo.divide(4,2)

#### sys - Common System Functions

import sys

**Command Line Arguments:** 

svs.argv

**Quitting Python:** 

sys.exit(0)

Printing to the Console (Substitute for print): sys.stdout("Hello World")

**Getting User Input from the Console:** input = sys.stdin.readline()

### **Function to Add Set of Integers** Passed by Command Line

import sys

```
def sum command line args()
     input_args = sys.argv
     sum = 0
     try:
          # Skip element one since module name
          for i in range(1, len(input_args)):
               sum += int(input_args[i])
          print "Input argument not an integer"
```

sys.exit(0) # Print the sum to the console.

**Unit Testing** 

print "The sum of the input arguments is: ", print sum\_command\_line\_args()

#### **Documentation String**

Documentation String: First statement of a module, class, or function.

**Extracting Documentation String for a Function, Class, or Module:** 

Use the method \_\_doc\_\_

**Example:** A function exists called fact. To print its documentation string, call:

print fact. doc

**Accessing Documentation String Outside a Python Program** 

Example: Function fact exists in module MyModule.py

Interpretative Mode:

import(MyModule) help(MyModule.fact)

**Command Line:** 

pydoc MyModule.fact

## Included in **Documentation String**.

**Module Name: doctest** 

Unit Test Function Name: testmod()

Format:

>>> function\_name(args)

result

Example:

def multiply(a, b):

>>> multiply (0, 1) >>> multiply (2, 1) >>> multiply (3, -1)

-3

return a \* b

doctest.testmod()

#### **Setting Up doctest in Supporting Modules**

```
# Check to see if this module is main
if( __name__ == 'main'):
     # Import doctest module then run testmod()
     import doctest
```

## **Benefits of Python**

Good string and list processing functionality which minimizes awkward additional	Scripted/interpreted coding available for testing
coding.	
Higher order function support (e.g. functions can take other functions as arguments)	Syntax is comparable to other languages.
Good set of built-in libraries.	Wide range of free libraries and projects to build off.
People outside AI use it so others can appreciate your code.	

## **Special Notes**

#### Python:

- 1. Do not forget colons in Python code including after function definitions, for, while, and if statements.
- 2. Do not forget to call imports in Python code for modules such as math, random, and sys.
- 3. Printing a formatted string of numbers can be written:

print "%3d %0.2f" % (10, .9799) # Prints 10 with a preceding space and 0.98

4. It is possible to have Tuples of size 0 by doing:

x = ()

5. It is possible to have Tuples of size 1 by doing:

x = "Hello World", x = ("Hello World".)

6. For an abstract class, you need the line:

\_\_metaclass\_\_ = ABCMeta

#### **General Agents:**

- 7. Components Needs to Pass the Turing Test:
  - a. Natural Language Processing
  - b. Knowledge Representation (i.e. storage paradigm)
  - c. Automated Reasoning
  - d. Machine Learning
- 8. Cognitive Science: Brings together computer models from AI and experimental techniques from psychology to construct precise and testable theories of

#### the human mind.

- 9. Agent Function Maps percept sequence to agent action.
- 10. Simple Reflex Agent Select actions based off the current percept only. Often defined by condition-action rules (i.e. productions)
- 11. Goal Based Agents A goal is a binary condition (i.e. either met or not met). A goal based agent tries to reach a target goal. Search and planning agents may be goal based agents.
- 12. Problem solving agents deal with atomic environments (i.e. the environment is treated as a single whole and is indivisible).

#### Search:

- 13. In Recursive Best First Search code, remember to do the Goal Test at the beginning of the function and to check if the successors list is empty after creating it.
- 14. Effective Branch Factor: b\* Equivalent branch factor if the search tree was modelled as a balanced tree (i.e. where the number of children for each node is equivalent for all nodes).

#### **Constraint Satisfaction:**

- 15. Node Consistent Variable Any variable where every value in the variable's domain satisfies all of its unary constraints in a CSP network.
- 16. In AC-3, only excluding the current paired variable are expanded.
- 17. Local Consistency: Given a constraint graph, enforcing consistency (i.e. ensuring variables satisfy constraints) locally in each part of the graph leads to invalid values being eliminated throughout the graph.
- 18. Path Consistency A two variable set  $(X_i, X_j)$  are path consistent with respect to a third variable  $X_m$  if for every assignment of values to  $X_i$  and  $X_j$  consistent with the constraint  $\{X_i, X_j\}$ , there is a valid assignment to  $X_m$  that satisfies the constraints  $\{X_i, X_m\}$  and  $\{X_m, X_i\}$ .
- 19. Interleaving Search and Inference AC-3 can be used to infer reductions in the search domain both before and during search.
- 20. Forward Checking One way to implement "Inference" in Backtracking algorithm. Whenever a variable is assigned, establish arc consistency for it on all unassigned variables. If arc consistency checking was done in preprocessing, forward checking adds no value.
- 21. **Minimum Remaining Value (MRV), Fail First, Most Constrained Variable Heuristic:** Select the variable to assign next that has the smallest inferred domain (i.e. least remaining legal values).

#### **Logic and Logic Agents**

- 22. Declarative Programming: Provide information to the agent on information it needs to know and it figures out how to achieve the solution. De Procedural approach: Teach the agent how to do certain actions and it uses that information to figure out a solution to what you intend for it to do.
- 23. Background Knowledge Initial knowledge in the knowledge base.
- 24. Inference Deriving new sentences from existing sentences.
- 25. Logical Connectives: Used to construct complex sentences out of atomic sentences.
- 26. Theorem Proving: Using sentences already in the model, apply rules of inference to construct a proof of the desired sentence without consulting models.
- 27. Entailment Between Sentences: When one sentence logically follows from another sentence or set of sentences. It is similar to implies in philosophy.
- 28. Logical Inference: Process of drawing conclusions (i.e. new sentences) through entailment. Symbol of Inference:  $\vdash$  Given a knowledge base, KB, and a sentence  $\alpha$ , if an inference algorithm, i, inferred  $\alpha$  from KB then:  $KB \vdash_i \alpha$
- 29. Sound or Truth Preserving Inference Algorithm: Can only **derive** entailed sentences. Hence it cannot prove any sentence that is wrong. Example: Model checking is a sound algorithm since it does not work on infinite spaces.
- 30. Complete Inference Algorithm: Can derive any entailed sentence. A complete inference algorithm can prove anything that is right.
- 31. Literal: In a complex sentence, a literal is either an atomic sentence (i.e. positive literal) or its negation (i.e. negative literal).
- 32. Proof: A chain of conclusions that leads to the establishing some statement following from the knowledge base.

**General:**  $\sum_{i=m}^{n-1} a^i = \frac{a^m - a^n}{1-a}$