

Inertial Measurement Units I



Gordon Wetzstein
Stanford University

EE 267 Virtual Reality

Lecture 9

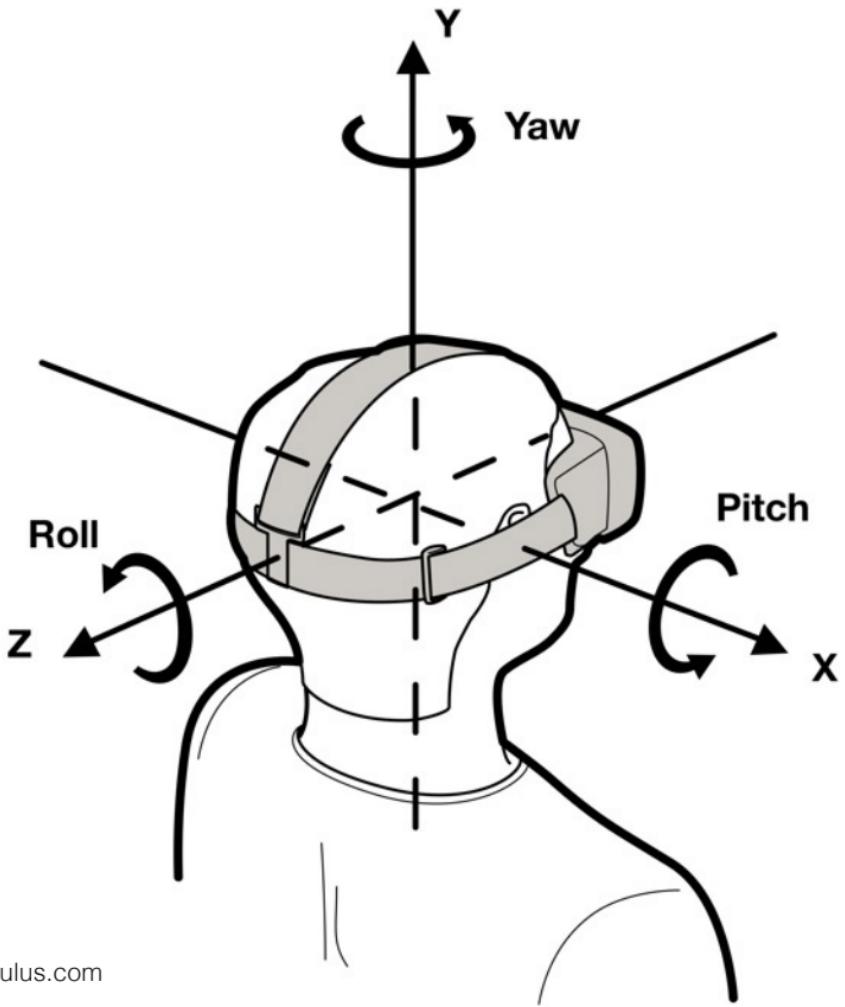
stanford.edu/class/ee267/

Logistics

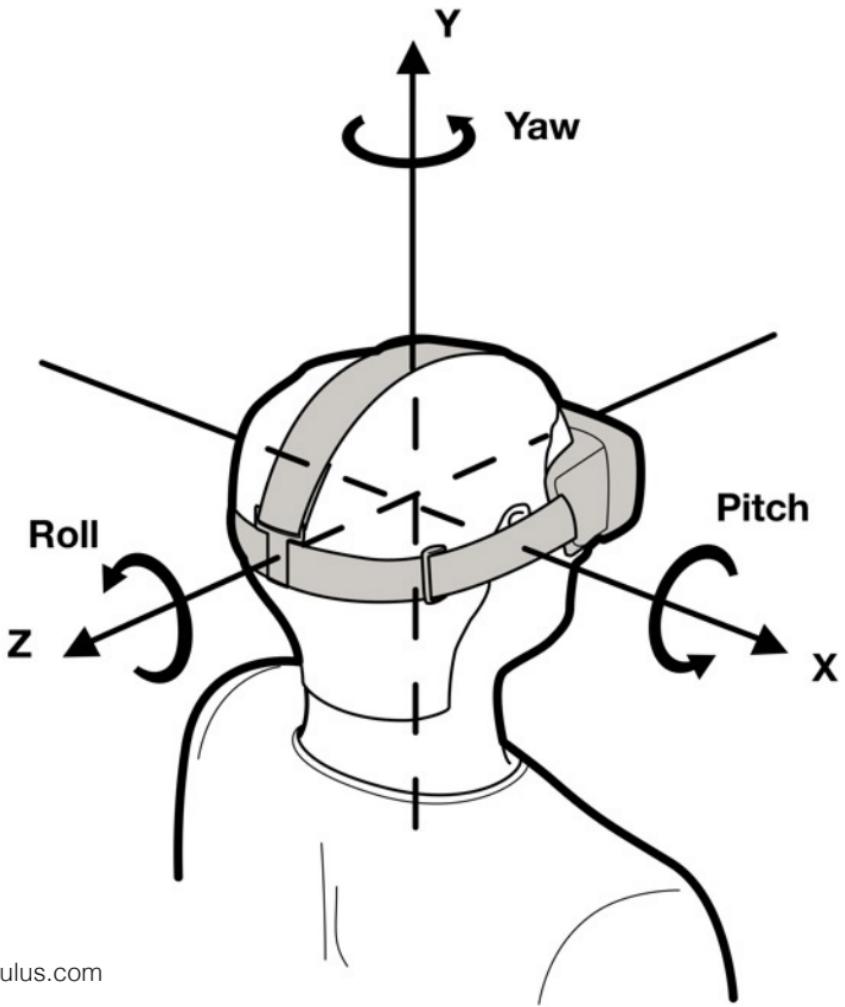
- Project proposal due this Fri

Lecture Overview

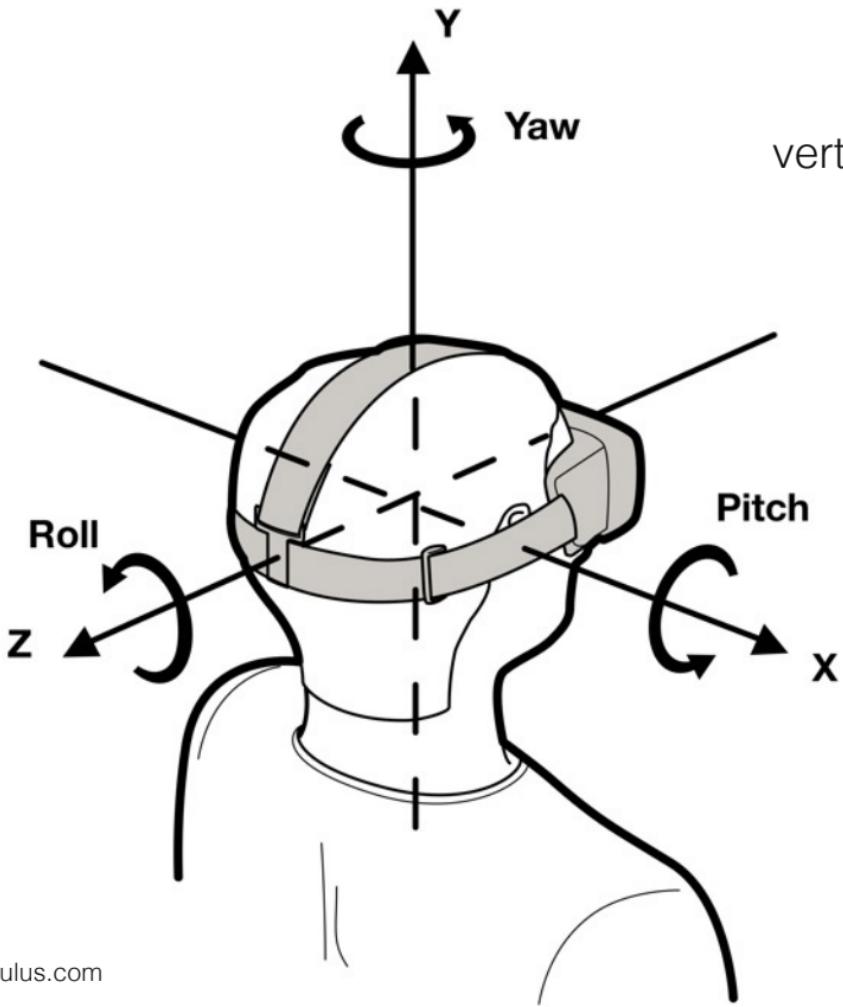
- coordinate systems (world, body/sensor, inertial, transforms)
- overview of inertial sensors: gyroscopes, accelerometers, and magnetometers
- gyro integration aka *dead reckoning*
- orientation tracking in *flatland*
- pitch & roll from accelerometer
- overview of VRduino



- primary goal: track orientation of head or other device
- orientation is the rotation of device w.r.t. world/earth or *inertial* frame
- rotations are represented by Euler angles (yaw, pitch, roll) or quaternions



- orientation tracked with IMU models relative rotation of sensor/body frame in world/inertial coordinates
- example: person on the left looks up → pitch=90° or rotation around x-axis by 90°
- similarly, the world rotates around the sensor frame by -90° (inverse rotation)



from lecture 2:

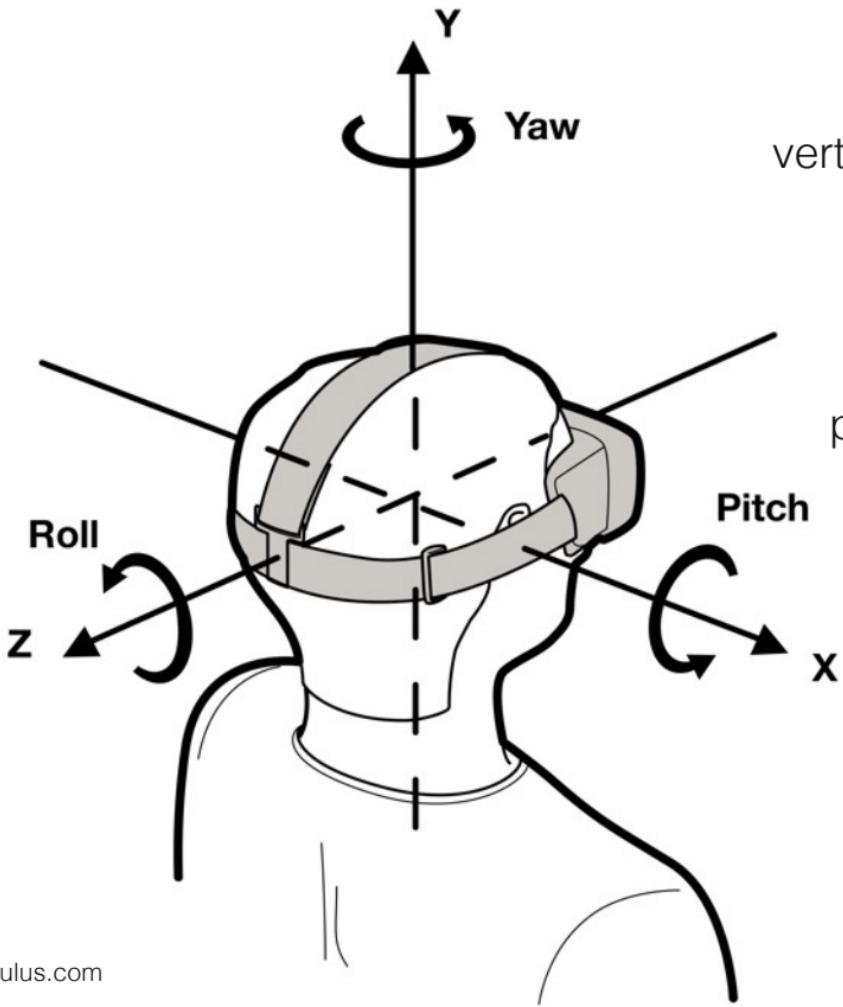
vertex in clip space



$$v_{clip} = M_{proj} \cdot M_{view} \cdot M_{model} \cdot v$$

vertex



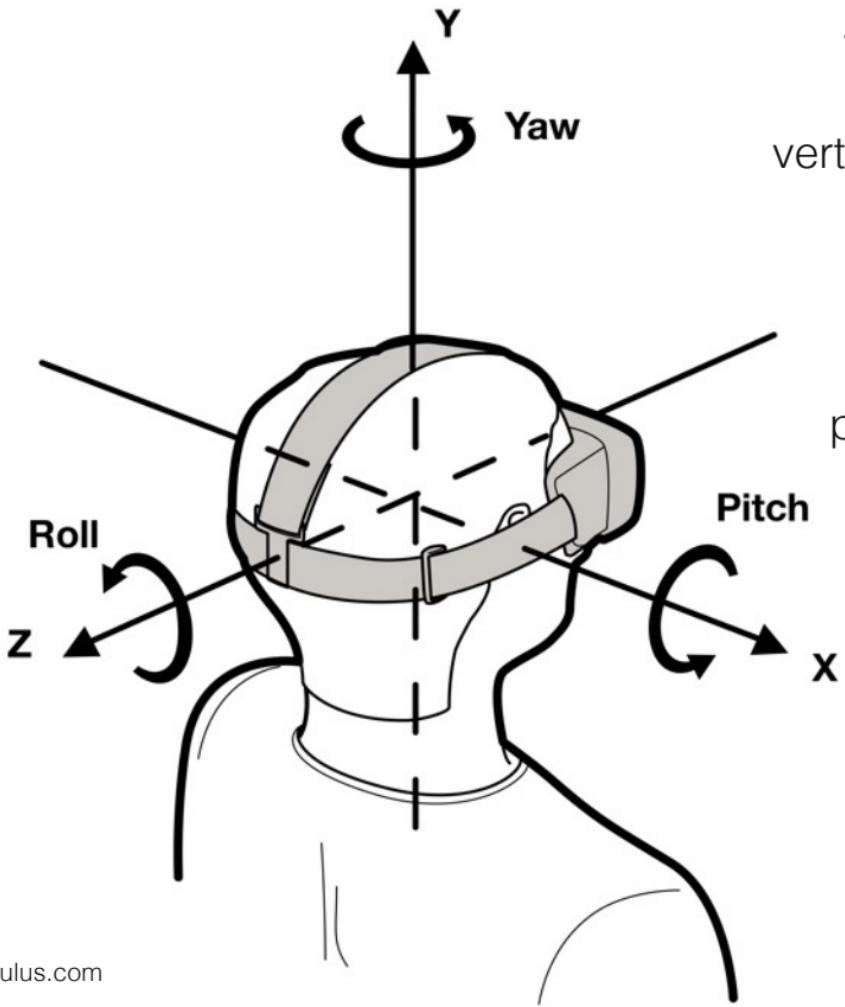


from lecture 2:

vertex in clip space

$$v_{clip} = M_{proj} \cdot M_{view} \cdot M_{model} \cdot v$$

↓
projection matrix view matrix model matrix
↑ ↑ ↑
vertex



from lecture 2:

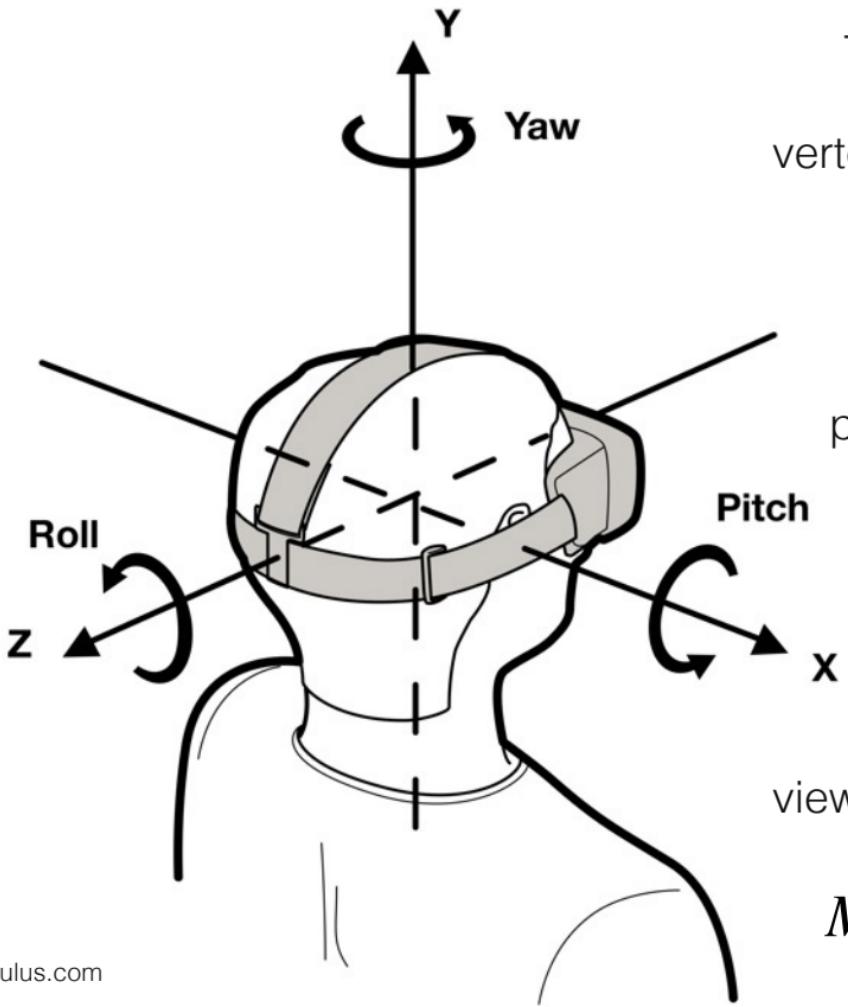
vertex in clip space

$$v_{clip} = M_{proj} \cdot M_{view} \cdot M_{model} \cdot v$$

↓ ↑ ↑ ↓
projection matrix view matrix model matrix vertex

rotation translation

$$M_{view} = R \cdot T(-eye)$$



from lecture 2:

vertex in clip space

$$v_{clip} = M_{proj} \cdot M_{view} \cdot M_{model} \cdot v$$

projection matrix

view matrix

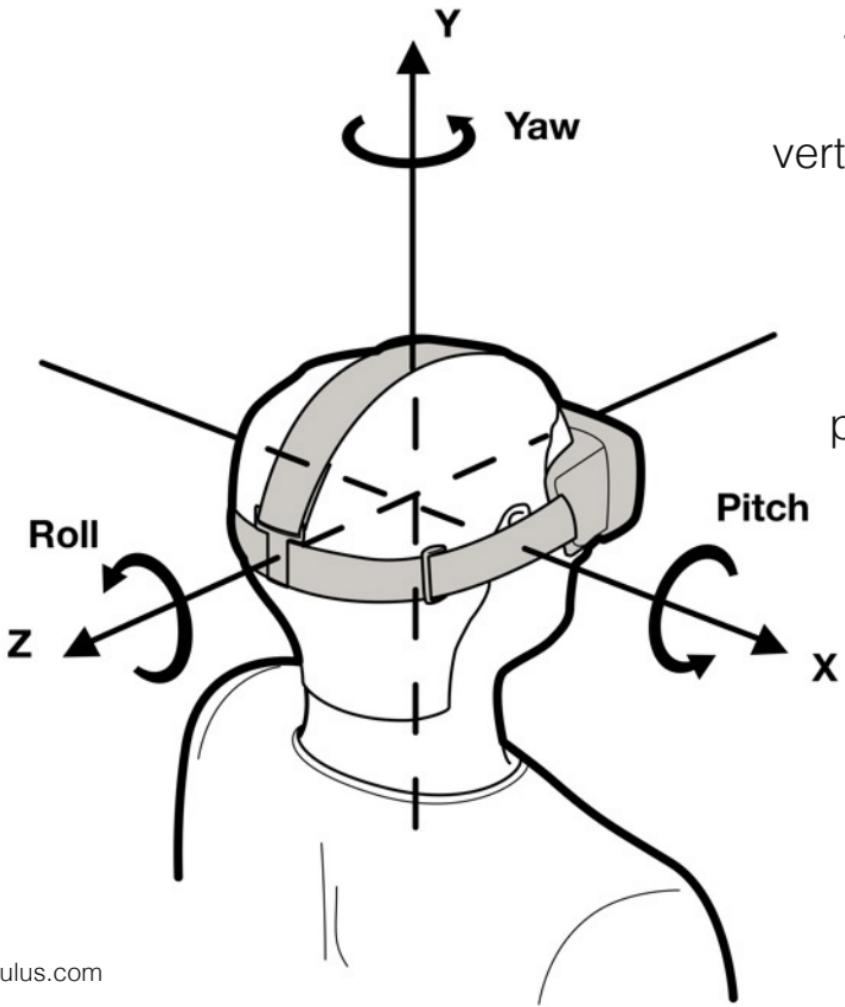
model matrix

rotation translation

$$M_{view} = R \cdot T(-eye)$$

view matrix for stereo camera:

$$M_{view}^{stereo} = T\left(\pm\frac{ipd}{2}, 0, 0\right) \cdot R \cdot T(-eye)$$



from lecture 2:

vertex in clip space

$$v_{clip} = M_{proj} \cdot M_{view} \cdot M_{model} \cdot v$$

projection matrix

view matrix

model matrix

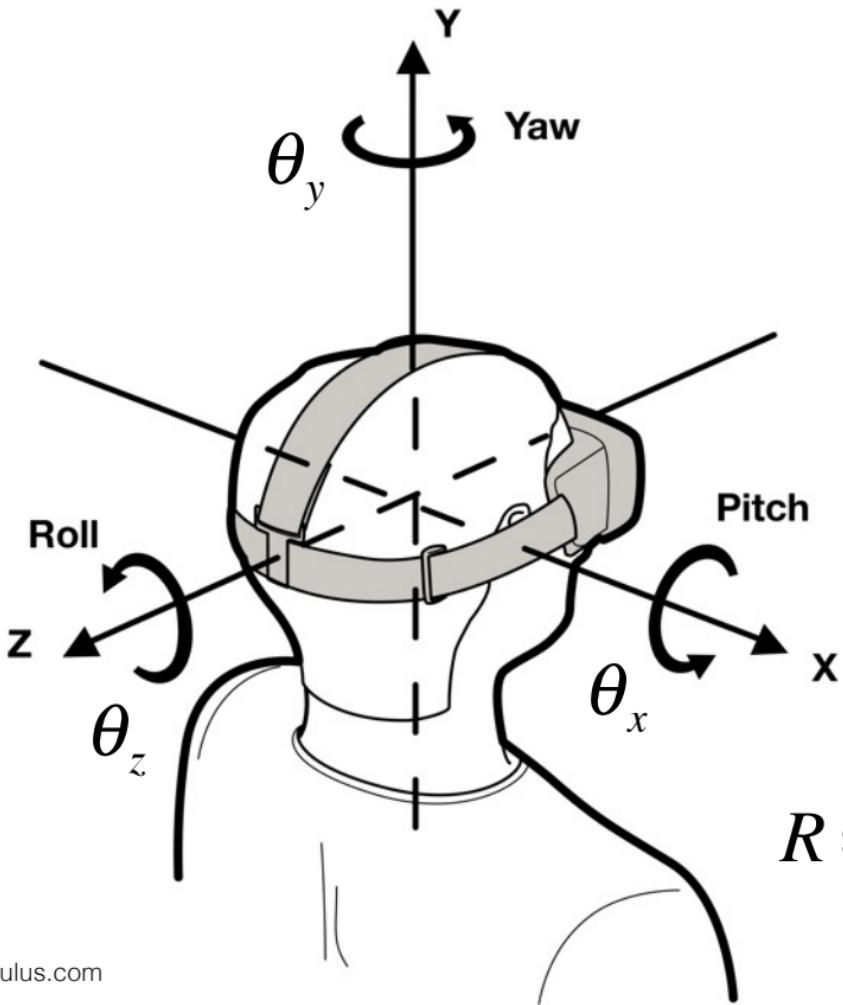
rotation translation

$$M_{view} = R \cdot T(-eye)$$

↑
↑

sensor/body
frame

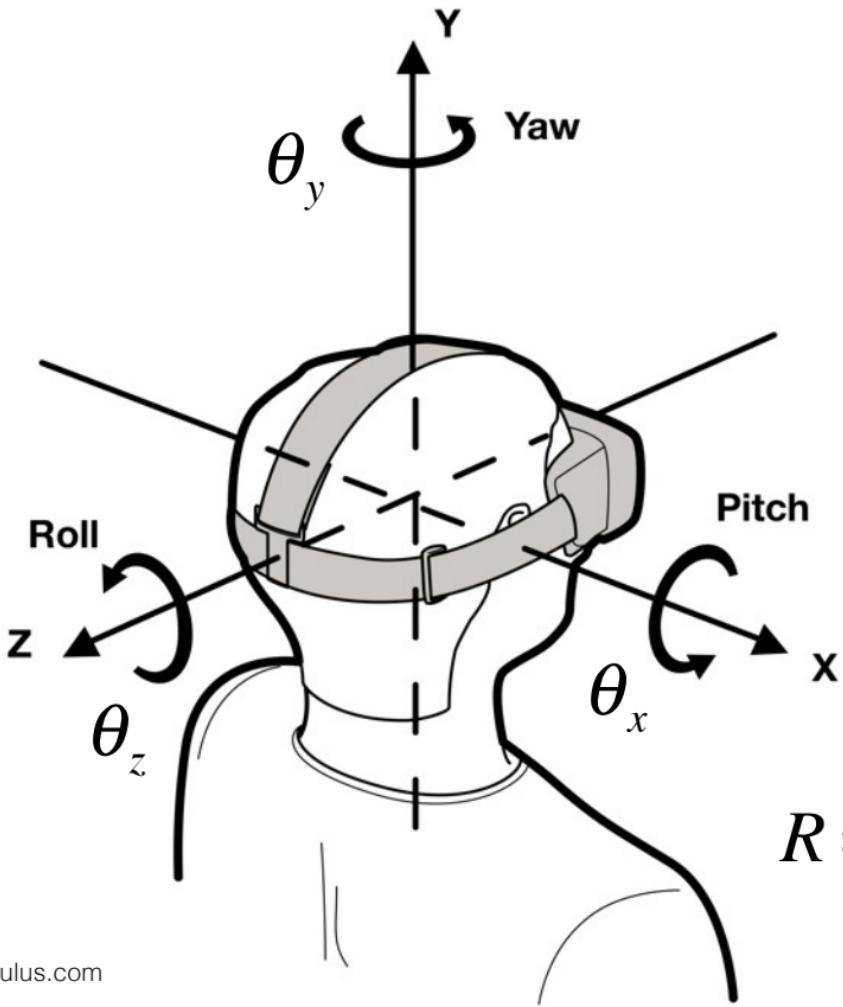
world/inertial
frame



rotation translation

$$M_{view} = R \cdot T(-eye)$$
$$R = R_z(-\theta_z) \cdot R_x(-\theta_x) \cdot R_y(-\theta_y)$$

order of rotations (world to body)



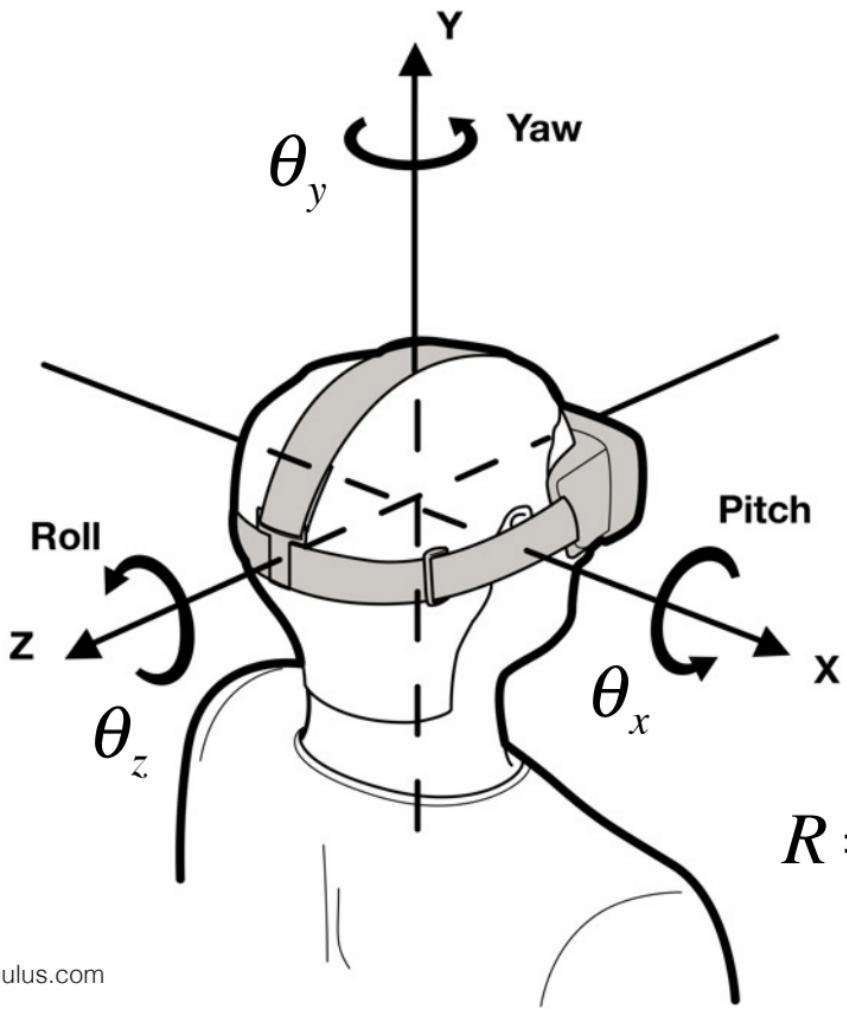
- this representation for a rotation is known as *Euler angles*

- need to specify order of rotation, e.g. yaw-pitch-roll

$$R = R_z(-\theta_z) \cdot R_x(-\theta_x) \cdot R_y(-\theta_y)$$

order of rotations (world to body)

ATTENTION!



- Euler angles are usually a terrible idea for orientation tracking with more than 1 axis
- one of several reasons:
rotations are not commutative

$$R = R_z(-\theta_z) \cdot R_x(-\theta_x) \cdot R_y(-\theta_y)$$

order of rotations (world to body)

What do Inertial Sensors Measure?

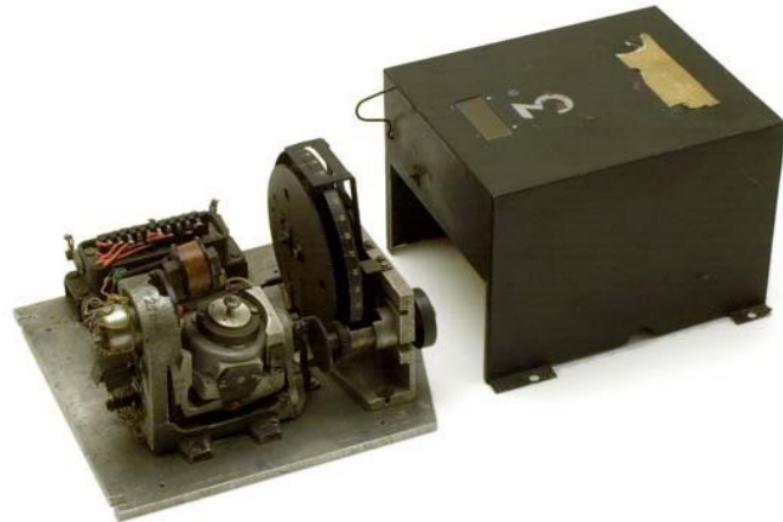
- gyroscope measures angular velocity $\tilde{\omega}$ in degrees/sec
- accelerometer measures linear acceleration \tilde{a} in m/s²
- magnetometer measures magnetic field strength \tilde{m} in uT
(micro Tesla) or Gauss → 1 Gauss = 100 uT

What do Inertial Sensors Measure?

- gyroscope measures angular velocity $\tilde{\omega}$ in degrees/sec
 - accelerometer measures linear acceleration \tilde{a} in m/s²
 - magnetometer measures magnetic field strength \tilde{m} in uT
(micro Tesla) or Gauss $\rightarrow 1$ Gauss = 100 uT
- ALL MEASUREMENTS TAKEN IN
SENSOR/BODY COORDINATES!**

History of Gyroscopes

- critical for inertial measurements in ballistic missiles, aircrafts, drones, the mars rover, pretty much anything that moves!

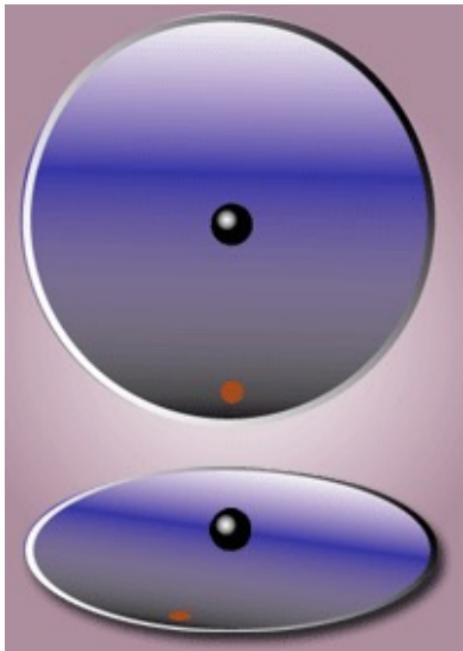


WWII era gyroscope used in the V2 rocket

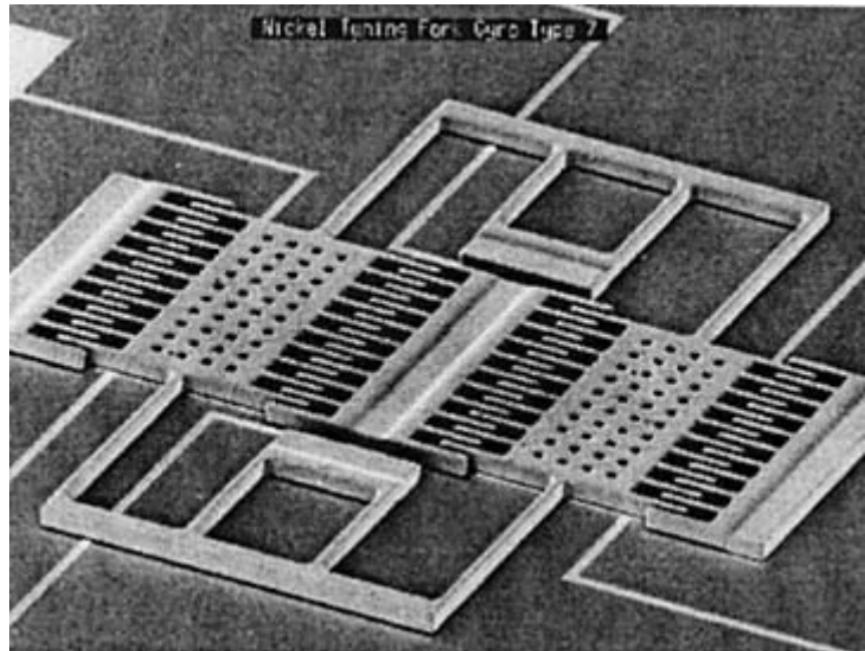
MEMS Gyroscopes

- today, we use microelectromechanical systems (MEMS)

Coriolis Force

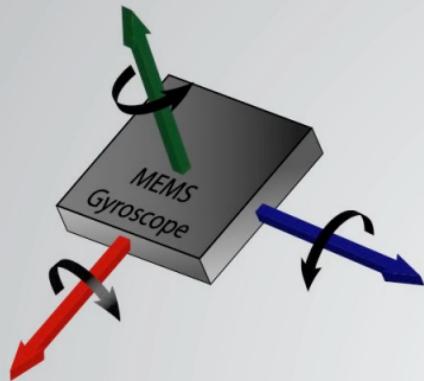


wikipedia



quora.com

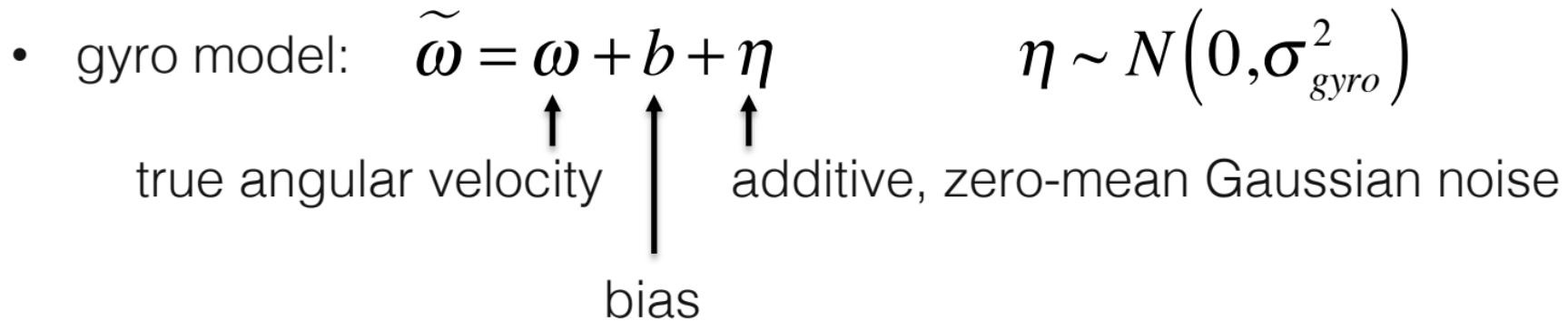
MEMS Gyroscope



Gyroscopes

- gyro model: $\tilde{\omega} = \omega + b + \eta$

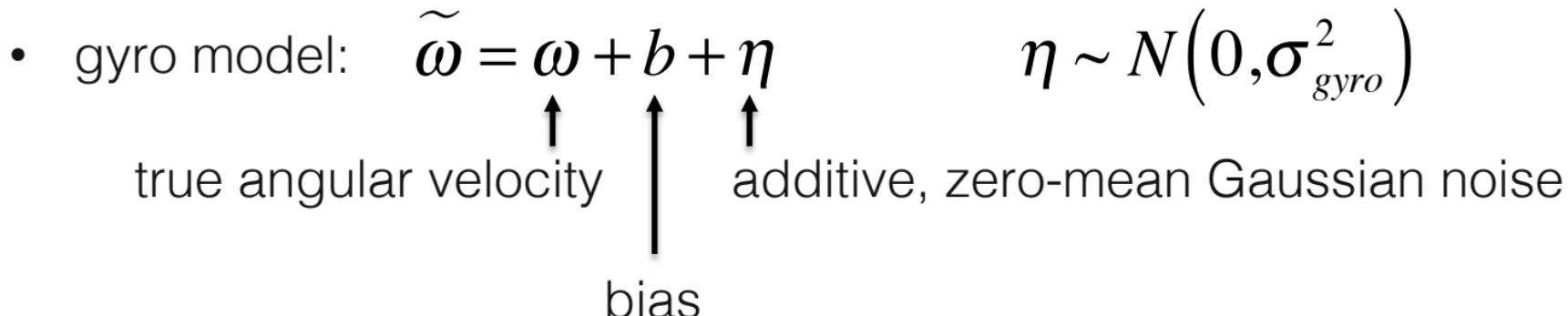
Gyroscopes

- gyro model: $\tilde{\omega} = \omega + b + \eta$ $\eta \sim N(0, \sigma_{gyro}^2)$


↑ ↑ ↑

true angular velocity bias additive, zero-mean Gaussian noise

Gyroscopes

- gyro model: $\tilde{\omega} = \omega + b + \eta$ $\eta \sim N(0, \sigma_{gyro}^2)$


The diagram illustrates the gyro model equation $\tilde{\omega} = \omega + b + \eta$. Three vertical arrows point upwards from the terms to their labels: the first arrow points to ω with the label "true angular velocity"; the second arrow points to b with the label "bias"; the third arrow points to η with the label "additive, zero-mean Gaussian noise".
- 3 DOF = 3-axis gyros that measures 3 orthogonal axes, assume no crosstalk
- bias is temperature-dependent and may change over time; can approximate as a constant
- additive measurement noise

Gyroscopes

- from gyro measurements to orientation – use Taylor expansion

$$\theta(t + \Delta t) \approx \theta(t) + \frac{\partial}{\partial t} \theta(t) \Delta t + \varepsilon, \quad \varepsilon \sim O(\Delta t^2)$$

Gyroscopes

- from gyro measurements to orientation – use Taylor expansion

have: angle at
last time step

have:
time step

$$\theta(t + \Delta t) \approx \theta(t) \downarrow + \frac{\partial}{\partial t} \theta(t) \Delta t + \varepsilon, \quad \varepsilon \sim O(\Delta t^2)$$

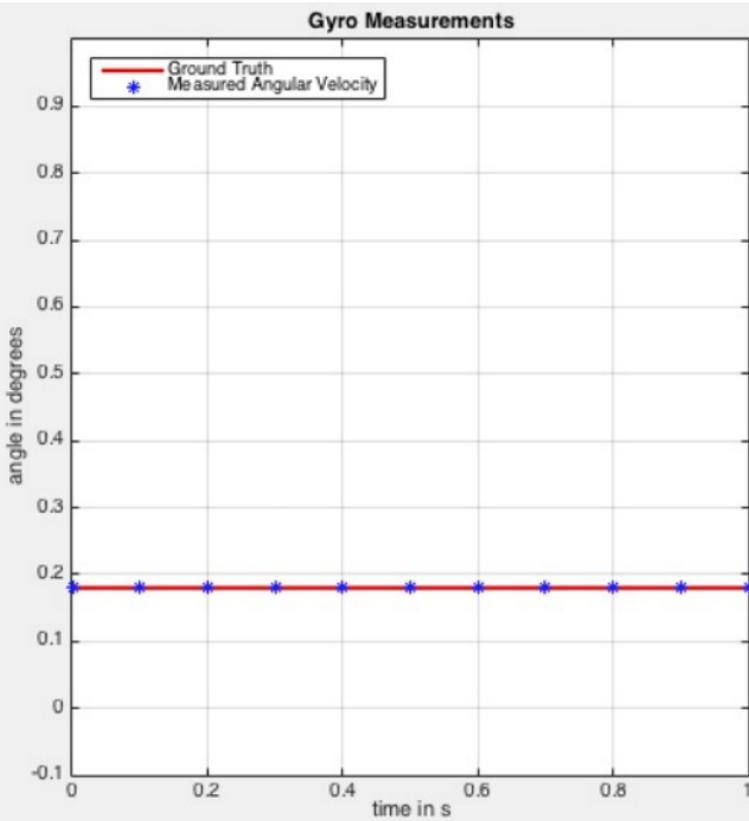
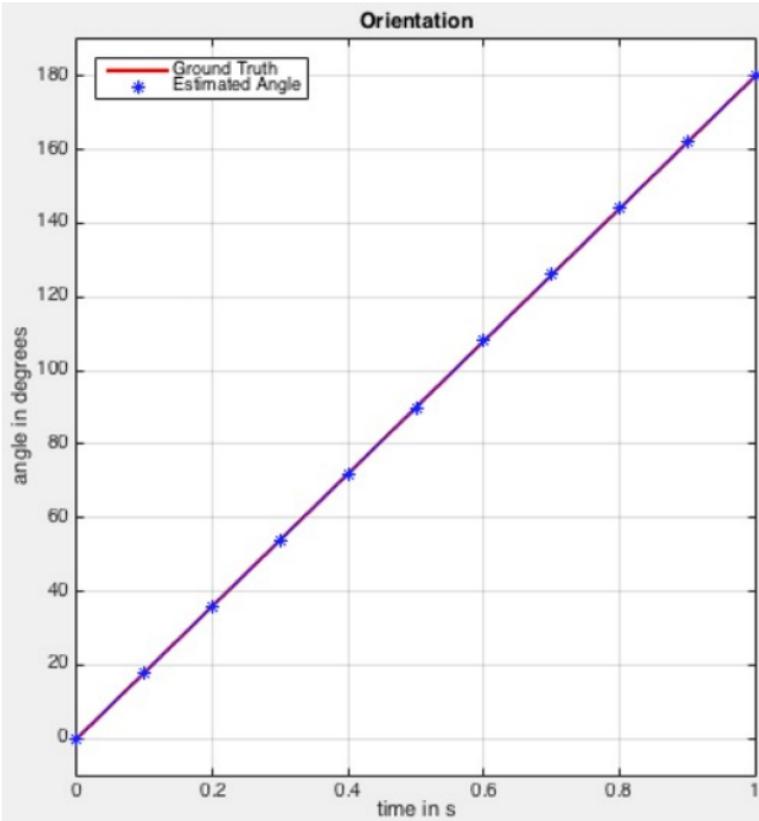
want: angle at
current time step

$= \omega$

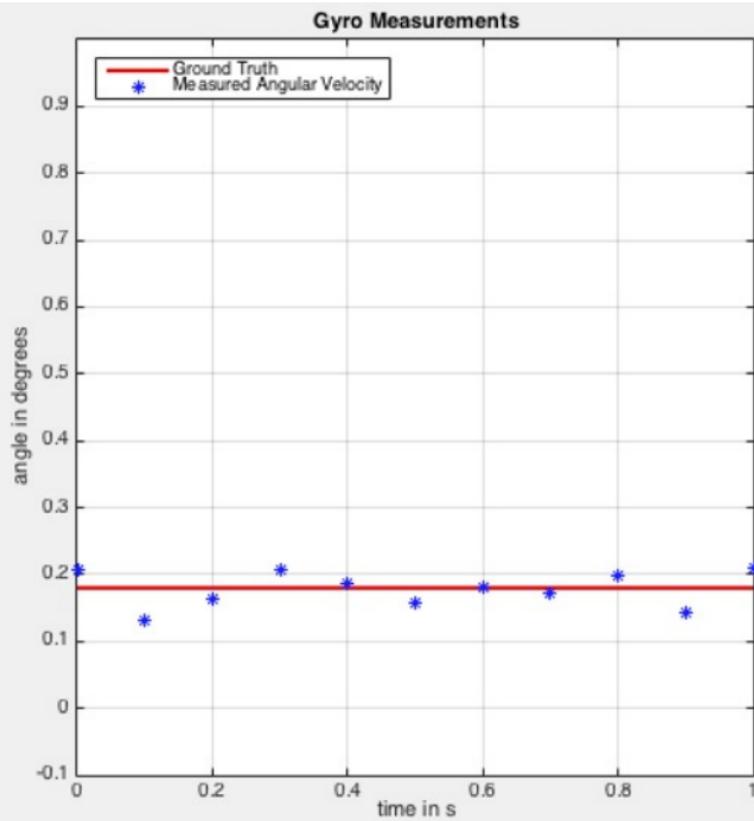
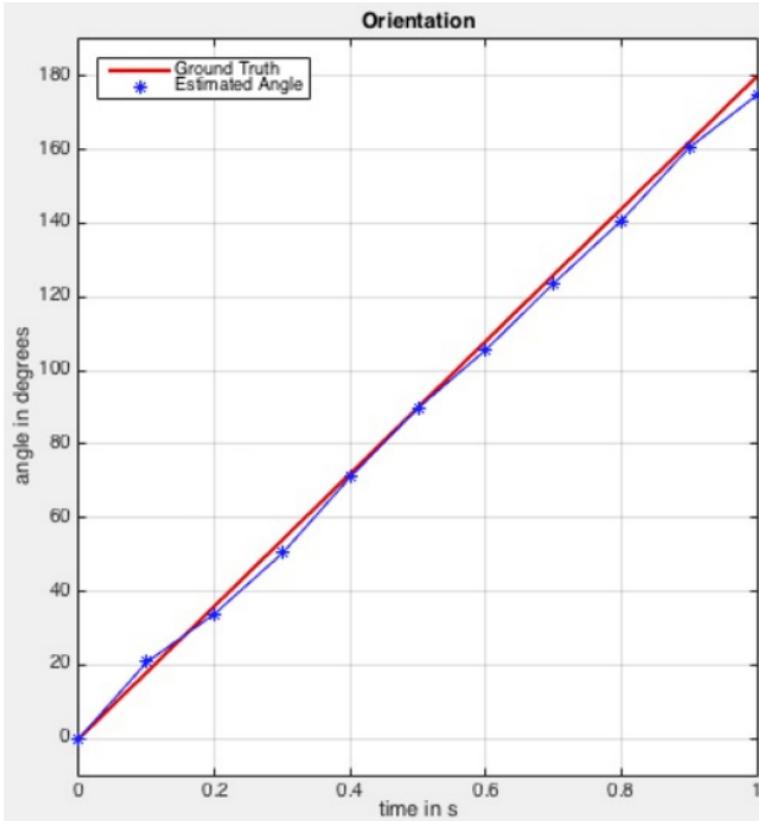
↑
approximation error!

have: gyro measurement
(angular velocity)

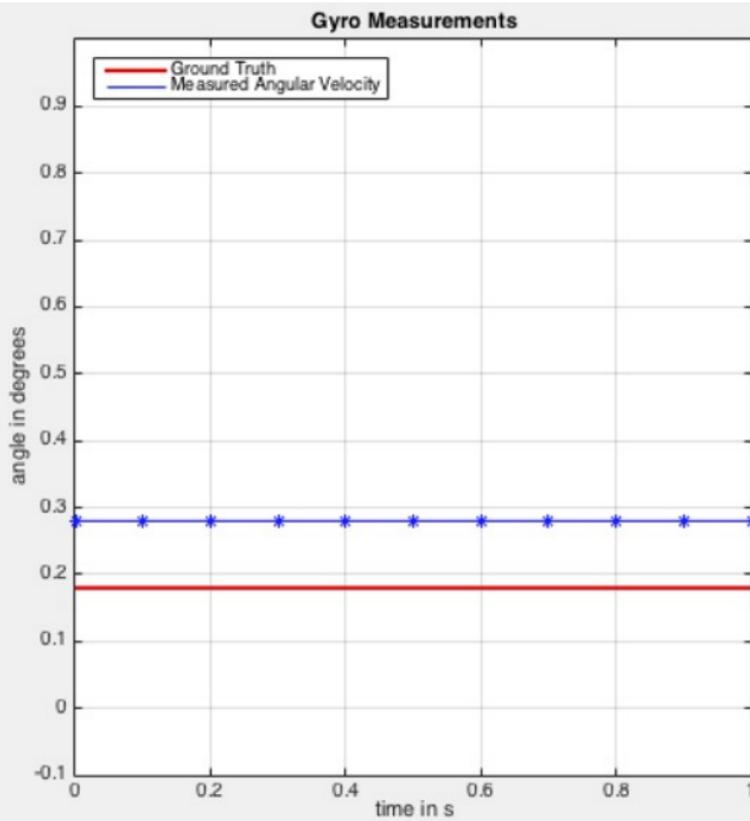
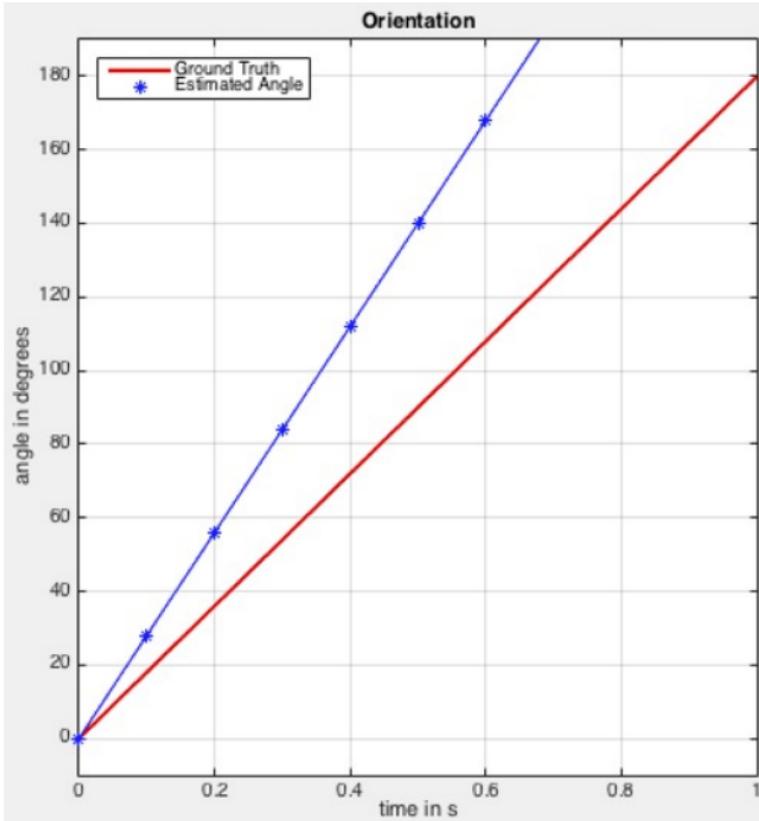
Gyro Integration: linear motion, no noise, no bias



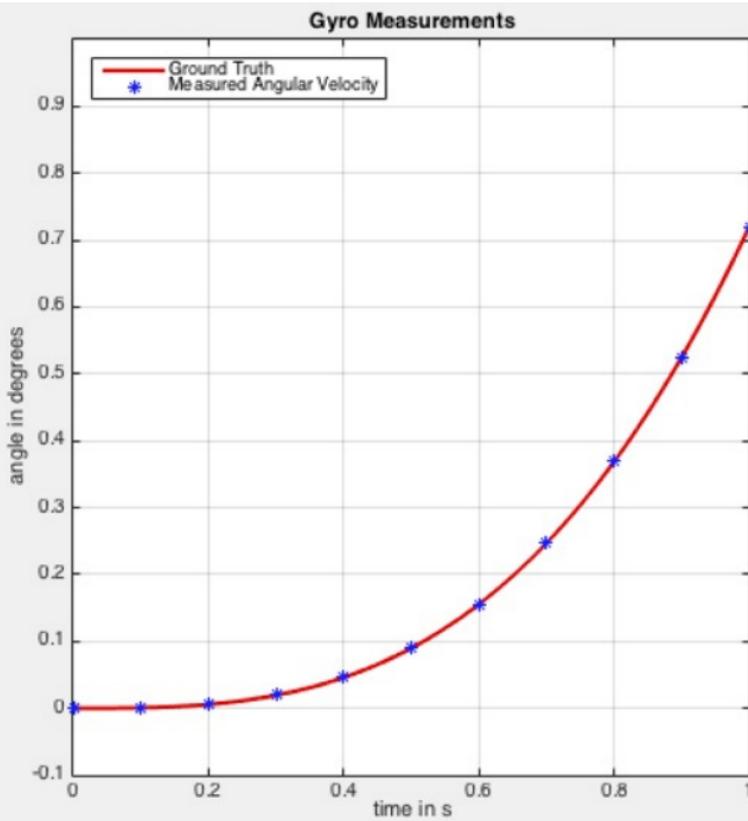
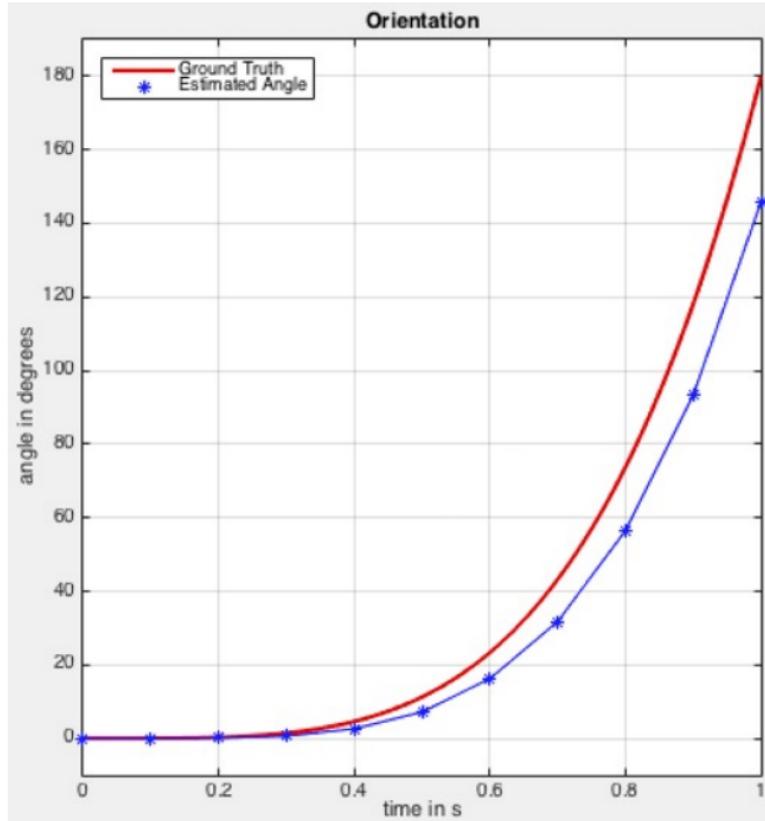
Gyro Integration: linear motion, noise, no bias



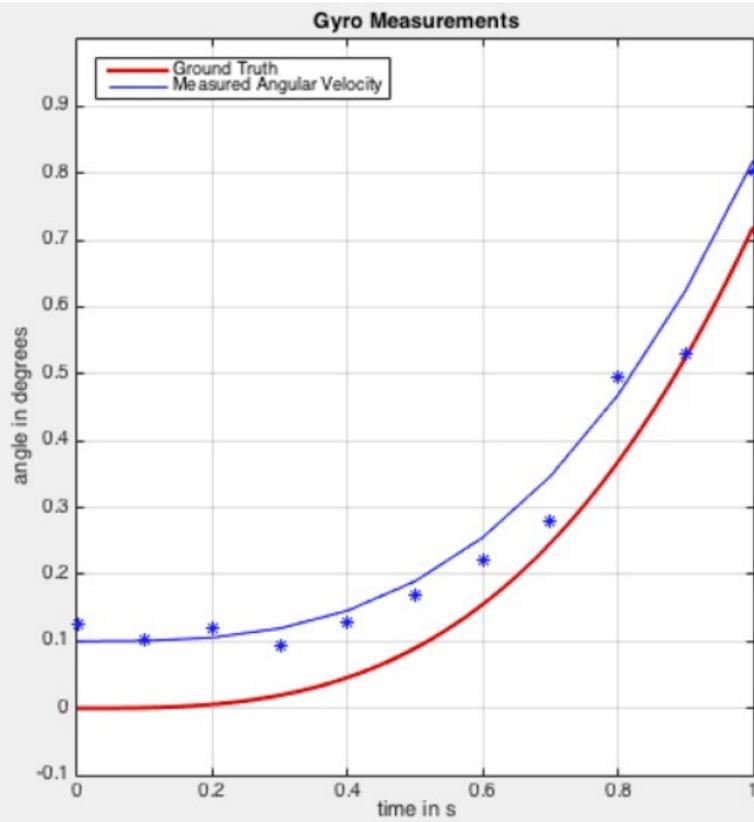
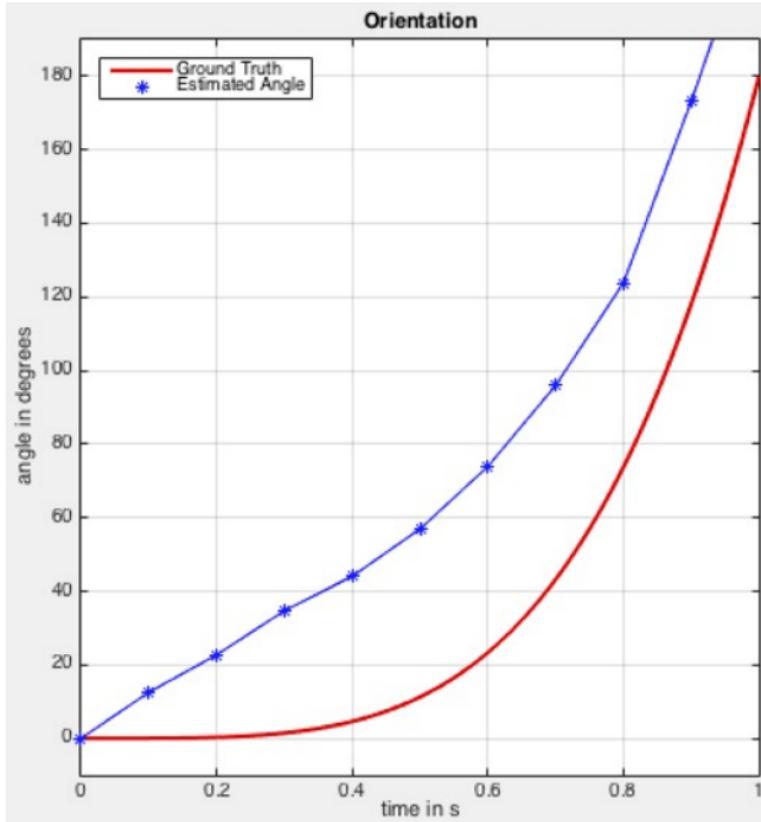
Gyro Integration: linear motion, no noise, bias



Gyro Integration: nonlinear motion, no noise, no bias



Gyro Integration: nonlinear motion, noise, bias



Gyro Integration aka *Dead Reckoning*

- works well for linear motion, no noise, no bias = unrealistic
- even if bias is known and noise is zero → drift (from integration)
- bias & noise variance can be estimated, other sensor measurements used to correct for drift (sensor fusion)
- accurate in short term, but not reliable in long term due to drift

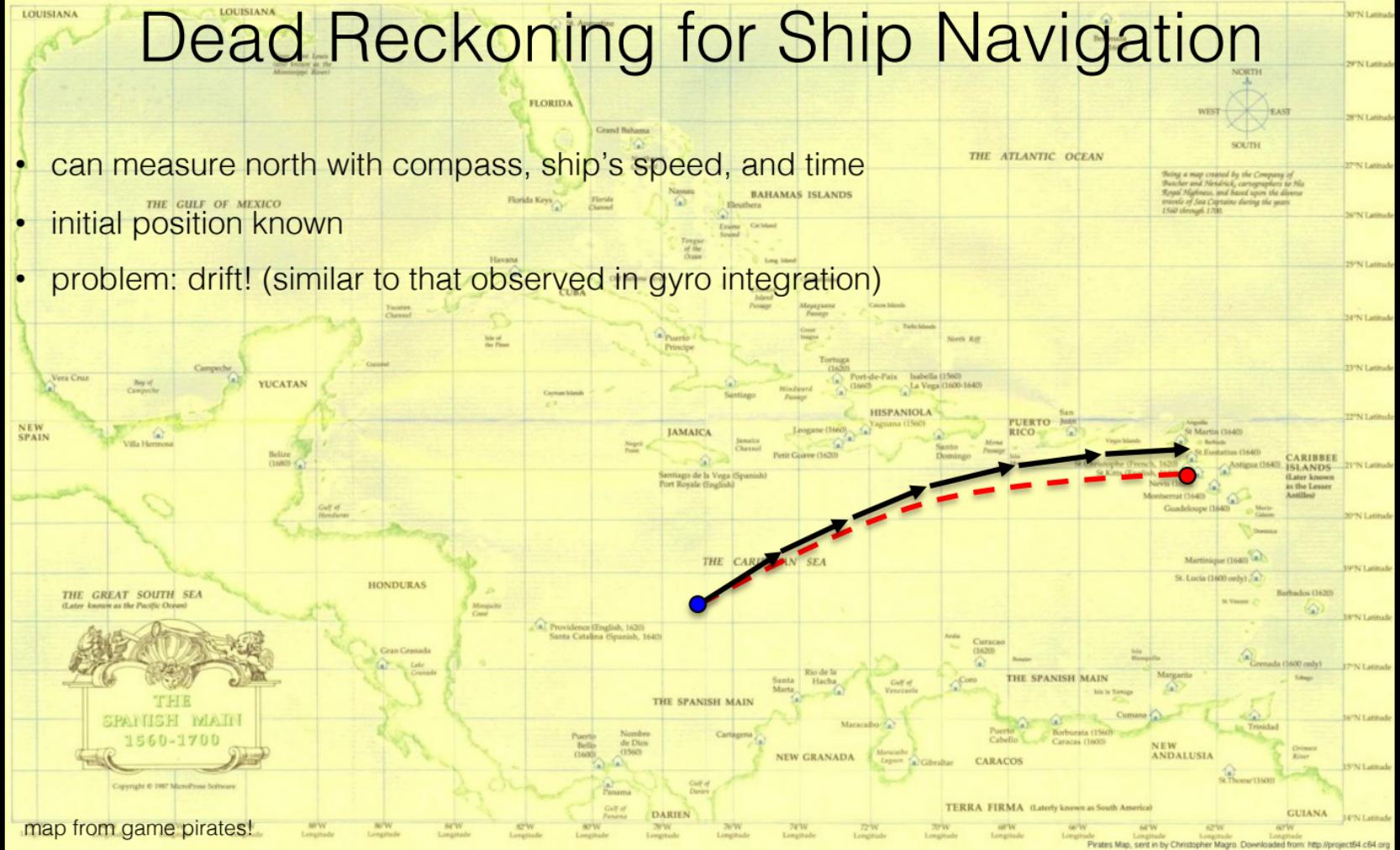
Dead Reckoning for Ship Navigation

- can measure north with compass, ship's speed, and time
- initial position known



Dead Reckoning for Ship Navigation

- can measure north with compass, ship's speed, and time
- initial position known
- problem: drift! (similar to that observed in gyro integration)



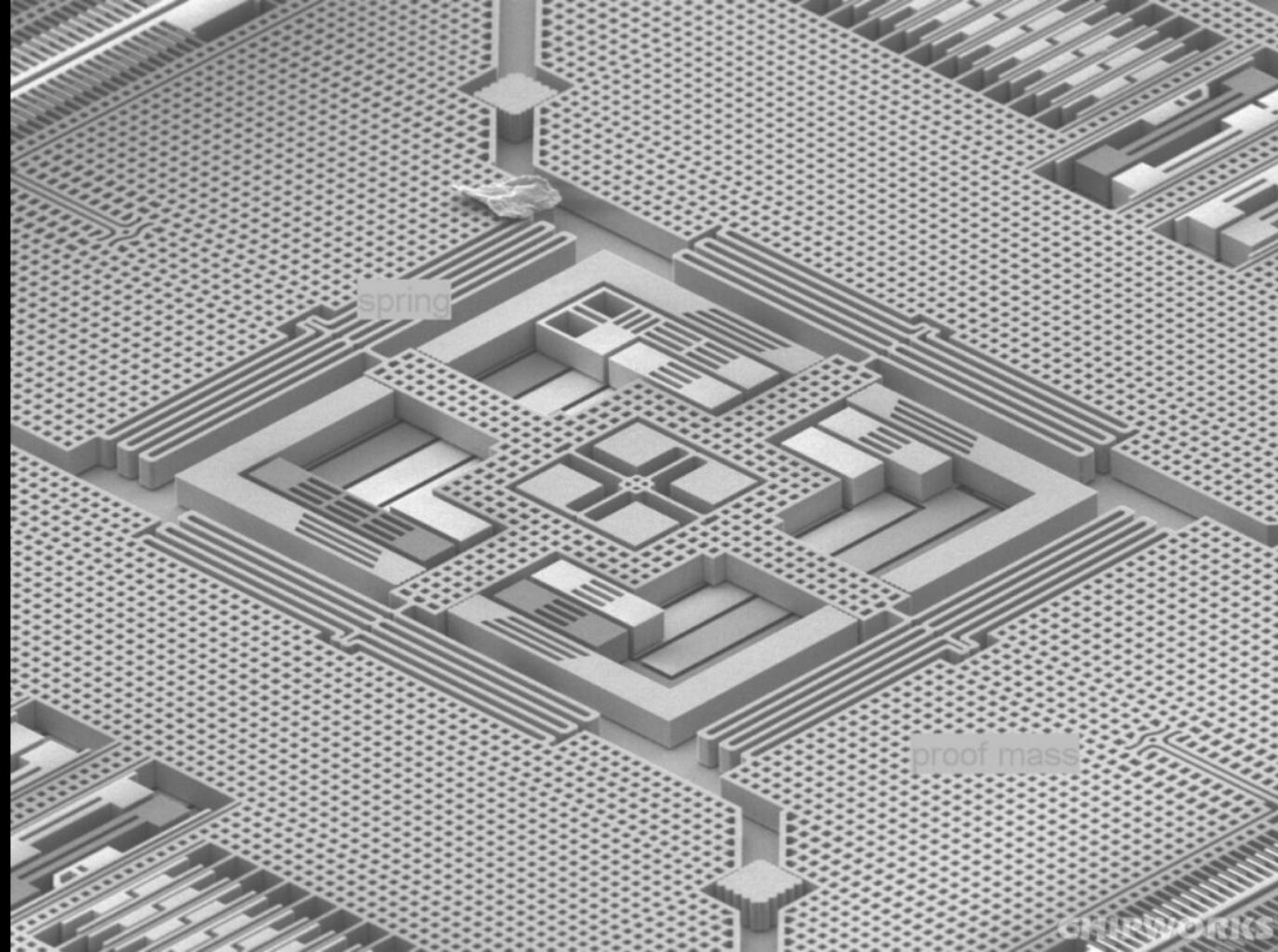
map from game pirates!

Gyro Advice

Always be aware of what units you are working with, degrees per second vs. radians per second!

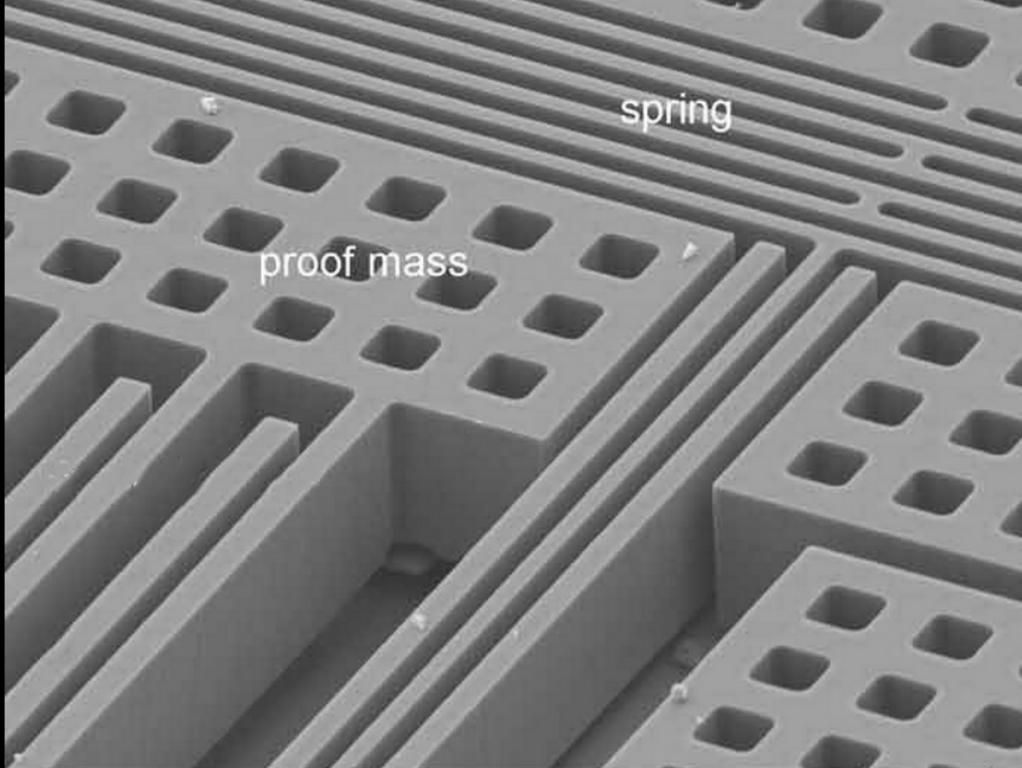
Accelerometers

- measure linear acceleration $\tilde{a} = a^{(g)} + a^{(l)} + \eta$, $\eta \sim N(0, \sigma_{acc}^2)$
- without motion: read noisy gravity vector $a^{(g)} + \eta$ pointing UP! with magnitude $9.81 \text{ m/s}^2 = 1\text{g}$
- with motion: combined gravity vector and external forces $a^{(l)}$

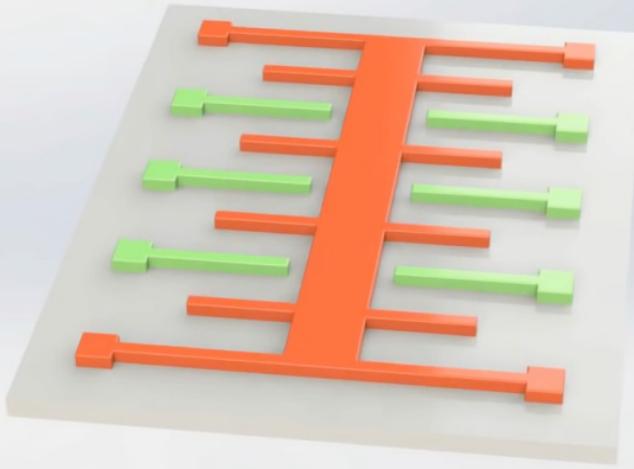


<https://stevecurd.wordpress.com/2015/08/25/mems-and-me-how-does-my-fitbit-know-im-walking/>

capacitive
plates



MEMS Accelerometer



Accelerometers

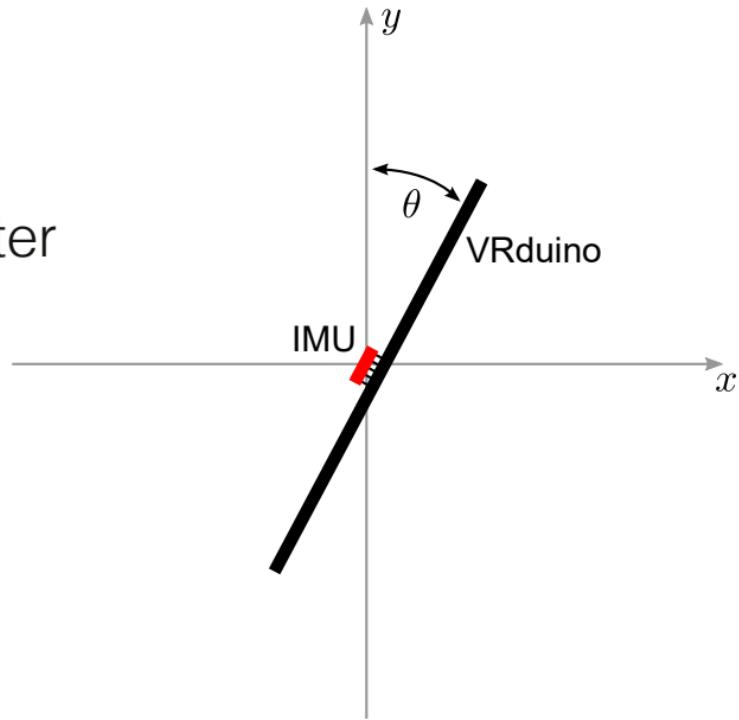
- advantages:
 - points up on average with magnitude of 1g
 - accurate in long term because no drift and the earth's center of gravity (usually) doesn't move
- problem:
 - noisy measurements
 - unreliable in short run due to motion (and noise)
- complementary to gyro measurements!

Accelerometers

- fusing gyro and accelerometer data = 6 DOF sensor fusion
- can correct tilt (i.e., pitch & roll) only – no information about yaw

Orientation Tracking in *Flatland*

- problem: track angle θ in 2D space
- sensors: 1 gyro, 2-axis accelerometer
- goal: understand sensor fusion

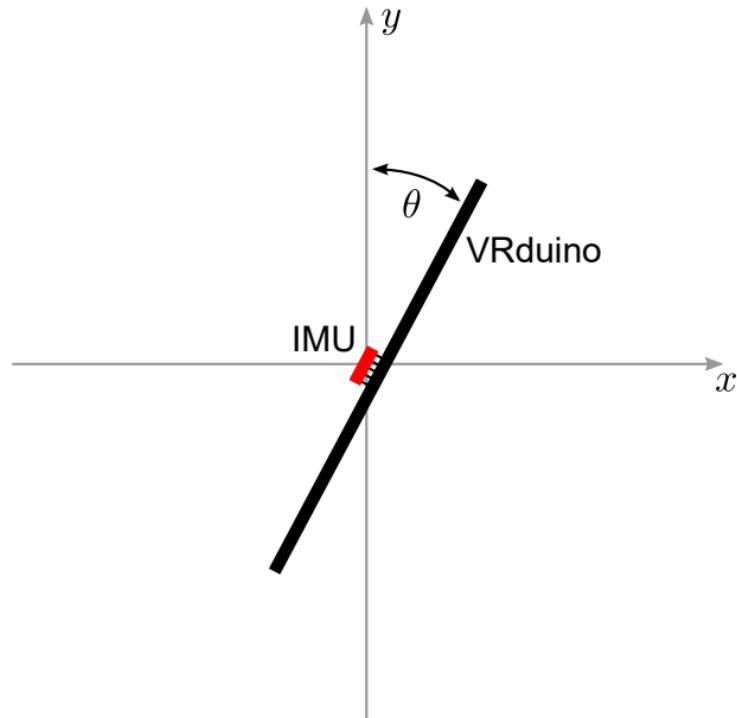


Orientation Tracking in *Flatland*

- gyro integration via Taylor series as

$$\theta_{gyro}^{(t)} = \theta_{gyro}^{(t-1)} + \tilde{\omega} \Delta t$$

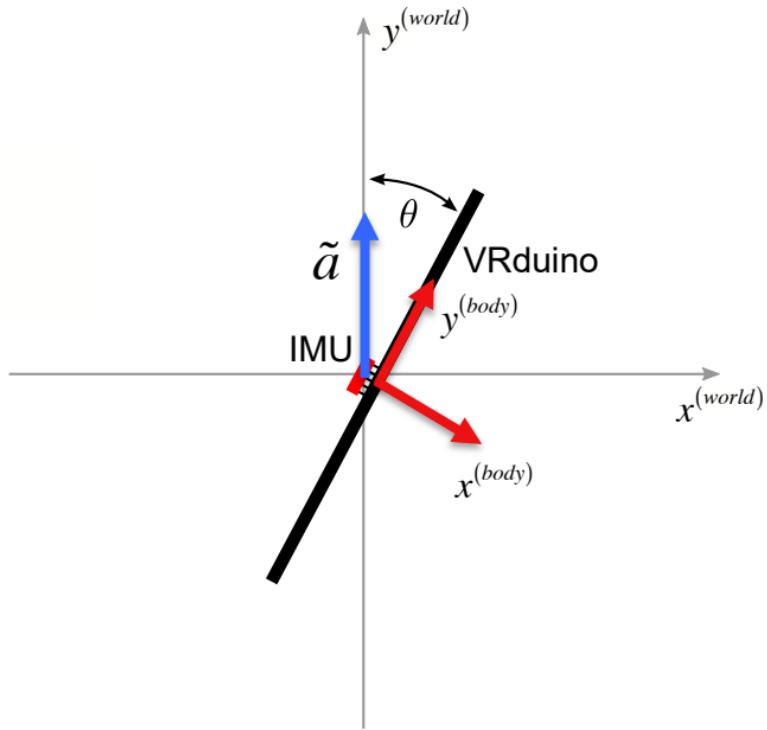
- get Δt from microcontroller
- set $\theta_{gyro}^{(0)} = 0$
- biggest problem: drift!



Orientation Tracking in *Flatland*

- angle from accelerometer

$$\theta_{acc} = \tan^{-1} \left(\frac{\tilde{a}_x}{\tilde{a}_y} \right)$$



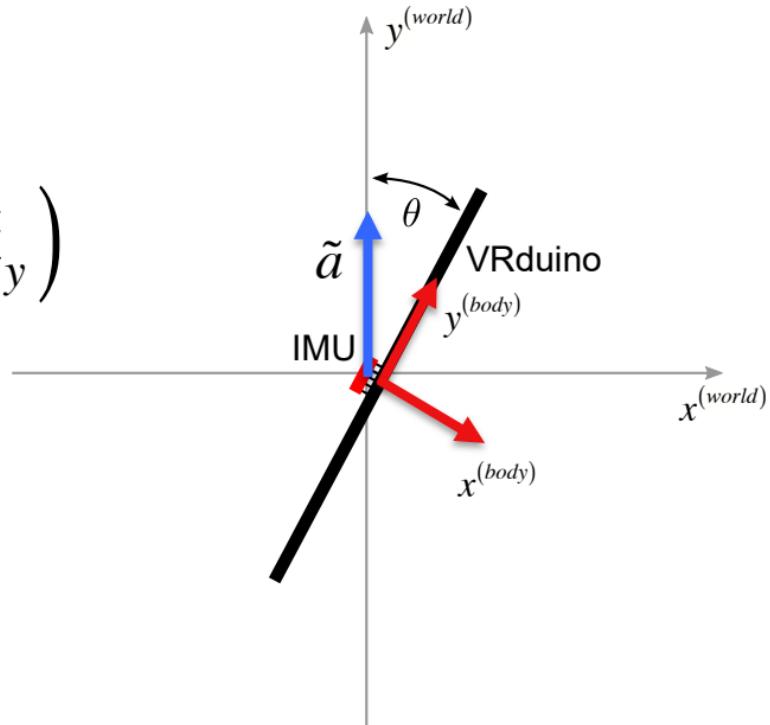
Orientation Tracking in *Flatland*

- angle from accelerometer

$$\theta_{acc} = \tan^{-1}\left(\frac{\tilde{a}_x}{\tilde{a}_y}\right) = \text{atan2}\left(\tilde{a}_x, \tilde{a}_y\right)$$

↑

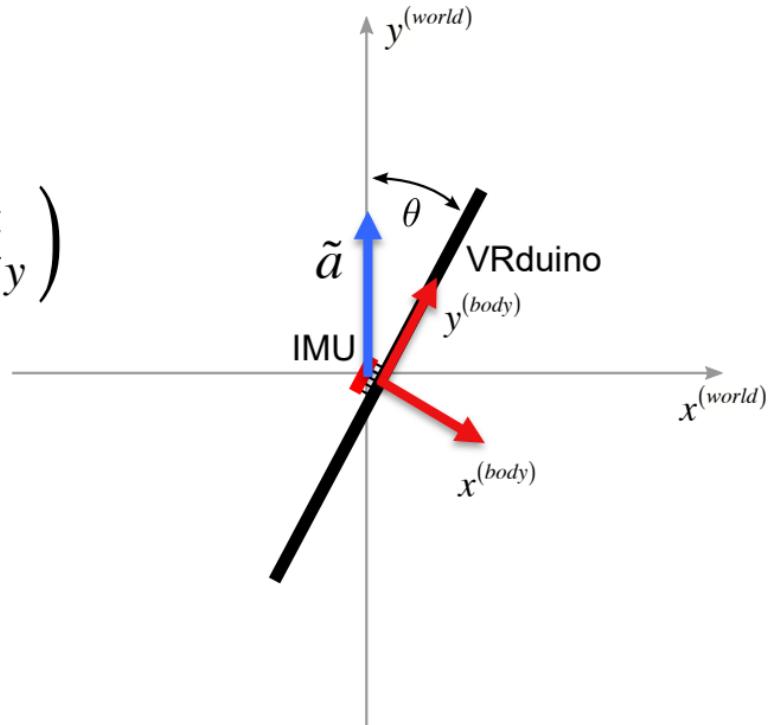
handles division by 0 and
proper signs, provided by most
programming languages



Orientation Tracking in *Flatland*

- angle from accelerometer

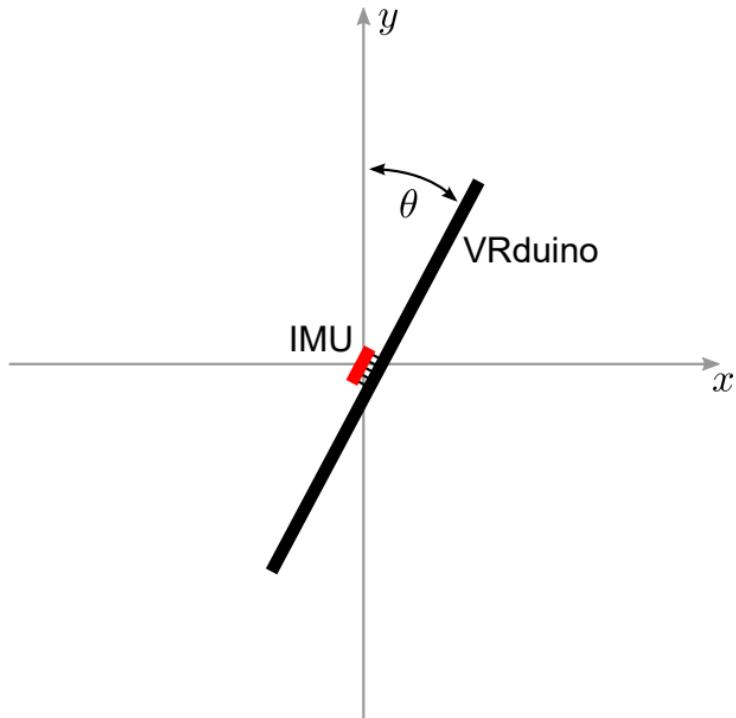
$$\theta_{acc} = \tan^{-1}\left(\frac{\tilde{a}_x}{\tilde{a}_y}\right) = \text{atan2}\left(\tilde{a}_x, \tilde{a}_y\right)$$



- biggest problem: noise

Orientation Tracking in *Flatland*

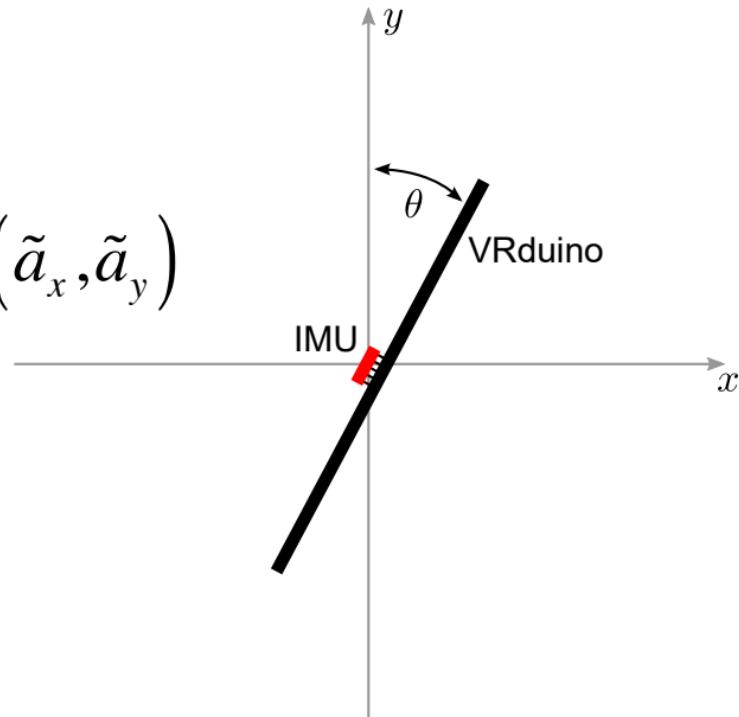
- sensor fusion: combine gyro and accelerometer measurements
- intuition:
 - remove drift from gyro via high-pass filter
 - remove noise from accelerometer via low-pass filter



Orientation Tracking in *Flatland*

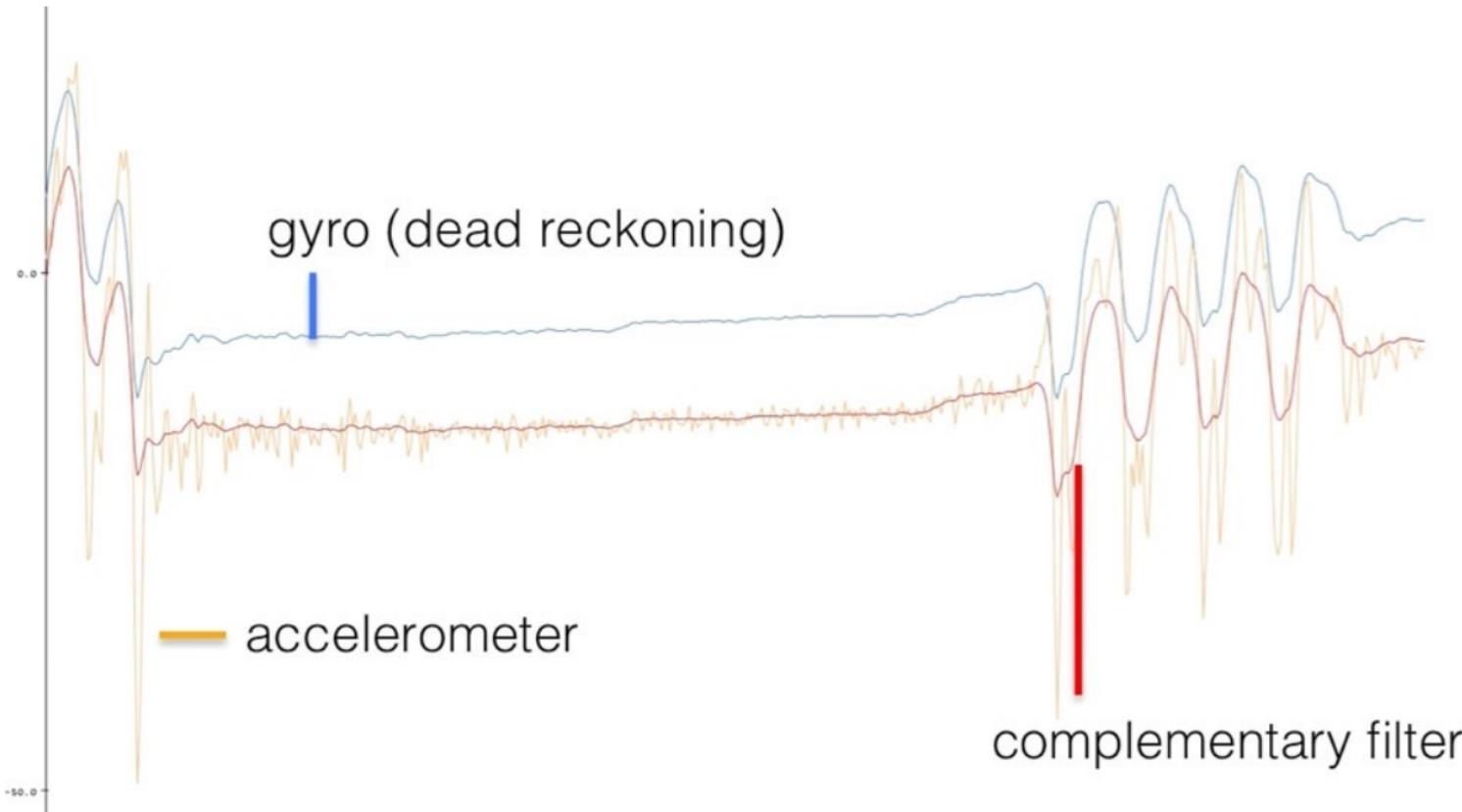
- sensor fusion with complementary filter, i.e. linear interpolation

$$\theta^{(t)} = \alpha(\theta^{(t-1)} + \tilde{\omega} \Delta t) + (1 - \alpha) \text{atan2}(\tilde{a}_x, \tilde{a}_y)$$



- no drift, no noise!

Orientation Tracking in *Flatland*



Pitch and Roll from 3-axis Accelerometer

- problem: estimate pitch and roll angles in 3D, from 3-axis accelerometer
- together, pitch & roll angles are known as *tilt*
- goal: understand tilt estimation in 3D

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

normalize gravity vector in
inertial coordinates

$$\hat{a} = \frac{\tilde{a}}{\|\tilde{a}\|} = R \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = R_z(-\theta_z) \cdot R_x(-\theta_x) \cdot R_y(-\theta_y) \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$$



normalize gravity vector rotated into
sensor coordinates

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

$$\begin{aligned}\hat{a} &= \frac{\tilde{a}}{\|\tilde{a}\|} = R \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = R_z(-\theta_z) \cdot R_x(-\theta_x) \cdot R_y(-\theta_y) \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \\ &= \begin{pmatrix} \cos(-\theta_z) & -\sin(-\theta_z) & 0 \\ \sin(-\theta_z) & \cos(-\theta_z) & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(-\theta_x) & -\sin(-\theta_x) \\ 0 & \sin(-\theta_x) & \cos(-\theta_x) \end{pmatrix} \begin{pmatrix} \cos(-\theta_y) & 0 & \sin(-\theta_y) \\ 0 & 1 & 0 \\ -\sin(-\theta_y) & 0 & \cos(-\theta_y) \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}\end{aligned}$$

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
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$$\hat{a} = \frac{\tilde{a}}{\|\tilde{a}\|} = \begin{pmatrix} -\cos(-\theta_x)\sin(-\theta_z) \\ \cos(-\theta_x)\cos(-\theta_z) \\ \sin(-\theta_x) \end{pmatrix}$$

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

$$\hat{a} = \frac{\tilde{a}}{\|\tilde{a}\|} = \begin{pmatrix} -\cos(-\theta_x)\sin(-\theta_z) \\ \cos(-\theta_x)\cos(-\theta_z) \\ \sin(-\theta_x) \end{pmatrix} \quad \text{roll} \quad \hat{a}_x = \frac{-\sin(-\theta_z)}{\cos(-\theta_z)} = -\tan(-\theta_z)$$

$$\theta_z = -\text{atan2}(-\hat{a}_x, \hat{a}_y) \text{ in rad } \in [-\pi, \pi]$$

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

$$\hat{a} = \frac{\tilde{a}}{\|\tilde{a}\|} = \begin{pmatrix} -\cos(-\theta_x)\sin(-\theta_z) \\ \cos(-\theta_x)\cos(-\theta_z) \\ \sin(-\theta_x) \end{pmatrix} \quad \text{pitch}$$

 $\frac{\hat{a}_z}{\sqrt{\hat{a}_x^2 + \hat{a}_y^2}} = \frac{\sin(-\theta_x)}{\sqrt{\cos^2(-\theta_x)(\sin^2(-\theta_z) + \cos^2(-\theta_z))}} = 1$

$$= \frac{\sin(-\theta_x)}{\cos(-\theta_x)} = \tan(-\theta_x)$$

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

$$\hat{a} = \frac{\tilde{a}}{\|\tilde{a}\|} = \begin{pmatrix} -\cos(-\theta_x)\sin(-\theta_z) \\ \cos(-\theta_x)\cos(-\theta_z) \\ \sin(-\theta_x) \end{pmatrix} \quad \text{pitch}$$

 $\frac{\hat{a}_z}{\sqrt{\hat{a}_x^2 + \hat{a}_y^2}} = \frac{\sin(-\theta_x)}{\sqrt{\cos^2(-\theta_x)(\sin^2(-\theta_z) + \cos^2(-\theta_z))}} = 1$

$$\theta_x = -\text{atan2}\left(\hat{a}_z, \sqrt{\hat{a}_x^2 + \hat{a}_y^2}\right) \text{ in rad } \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

Pitch and Roll from 3-axis Accelerometer

- use only accelerometer data – can estimate pitch & roll, not yaw
- assume no external forces (only gravity) – acc is pointing UP!

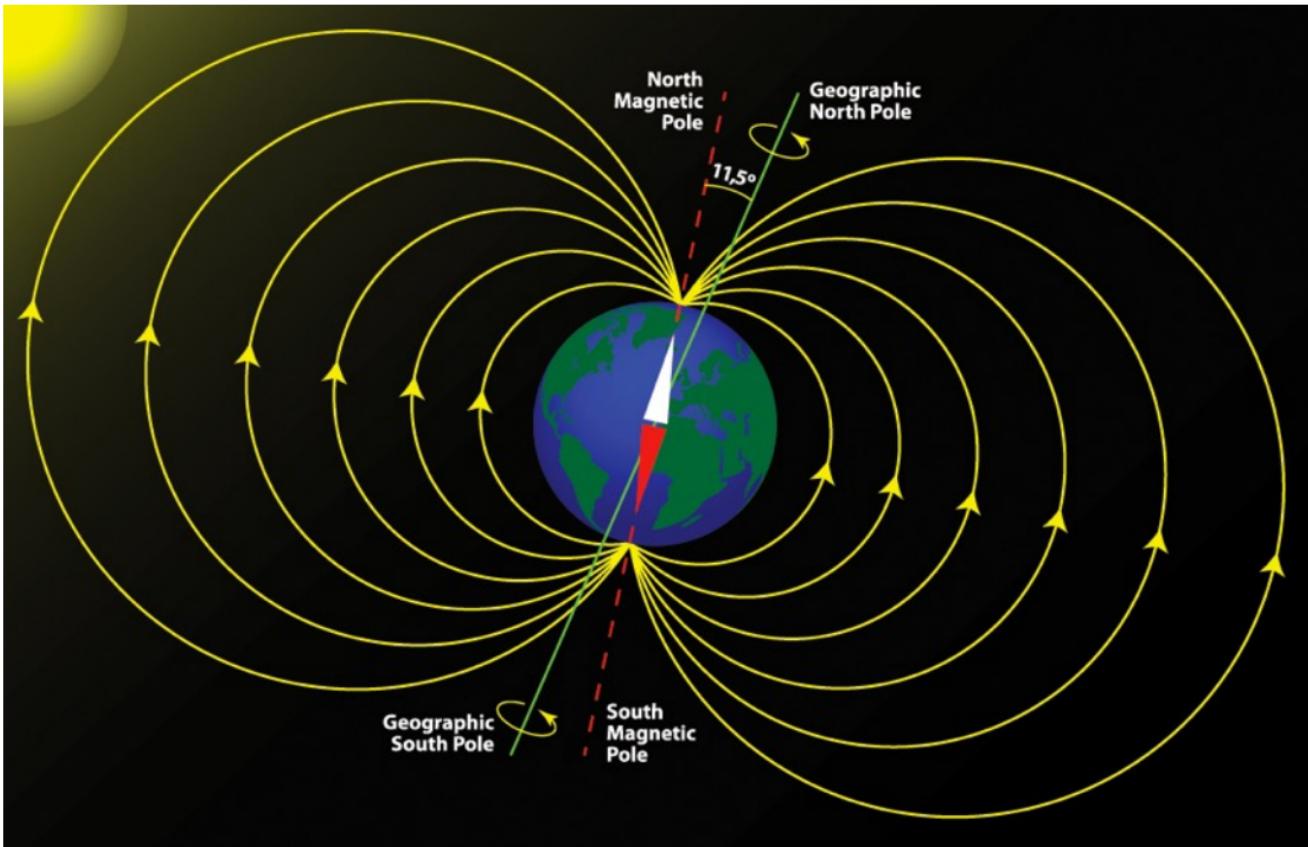
pitch

$$\frac{\hat{a}_z}{\sqrt{\hat{a}_x^2 + \hat{a}_y^2}} = \frac{\sin(-\theta_x)}{\sqrt{\cos^2(-\theta_x)(\sin^2(-\theta_z) + \cos^2(-\theta_z))}}$$
$$= 1$$

$$\theta_x = -\text{atan2}(\hat{a}_z, \text{sign}(\hat{a}_y) \cdot \sqrt{\hat{a}_x^2 + \hat{a}_y^2}) \text{ in rad } \in [-\pi, \pi]$$



Magnetometers



MEMS Magnetometer

Hall Effect

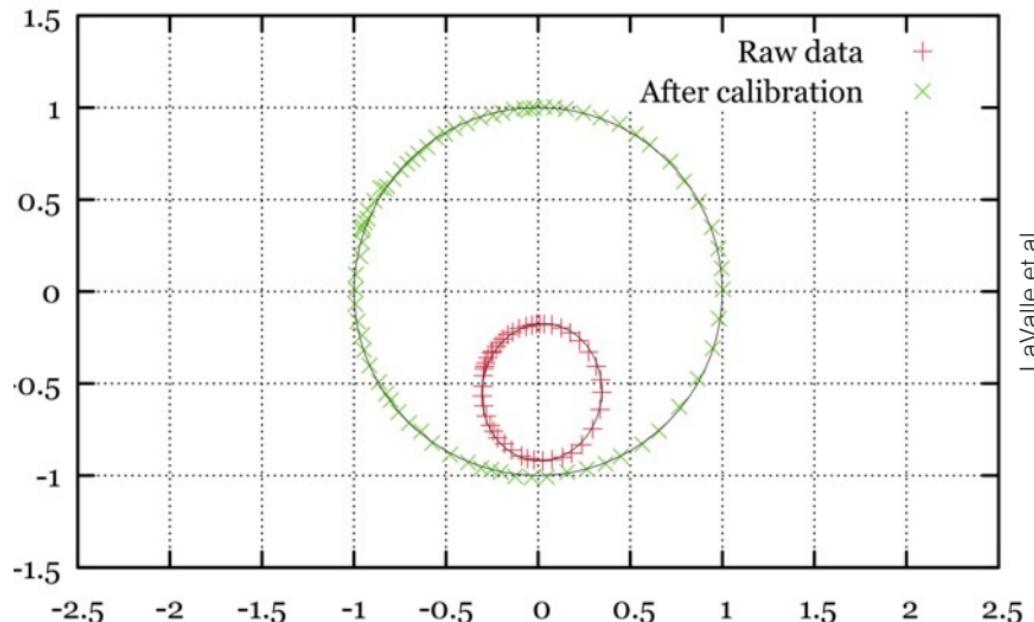
Magneto-resistive effect

Magnetometers

- measure earth's magnetic field in Gauss or uT
- 3 orthogonal axes = vector pointing along the magnetic field
- actual direction depends on latitude and longitude!
- distortions due to metal / electronics objects in the room or in HMD

Magnetometers

difficult to work with magnetometers without proper calibration →
we will not use the magnetometer in the HW!



LaValle et al.

Magnetometers

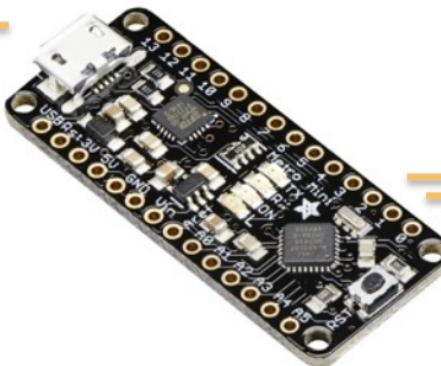
- advantages:
 - complementary to accelerometer – gives yaw (heading)
- problems:
 - affected by metal, distortions of magnetic field
 - need to know location, even when calibrated (e.g. GPS)
- together with gyro + accelerometer = 9 DOF sensor fusion

Prototype IMU

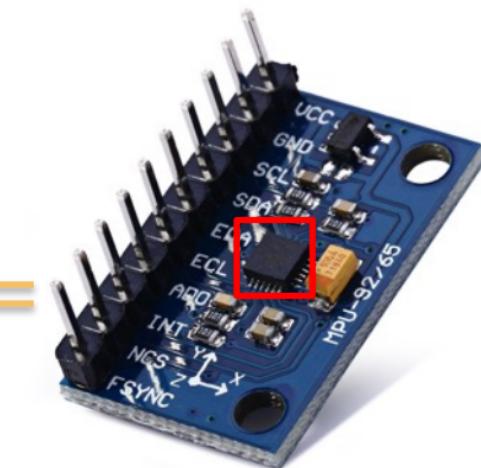
- 9 DOF IMU: InvenSense MPU-9250 = updated model of what was in the Oculus DK2
- 3-axis gyro, 3-axis accelerometer, 3-axis magnetometer all on 1 chip (we'll only use gyro and acc, but we'll give you code to read mag if you want to use it in your project)
- interface with I2C (serial bus) from Arduino

Prototype IMU

to host:
serial via USB



I2C



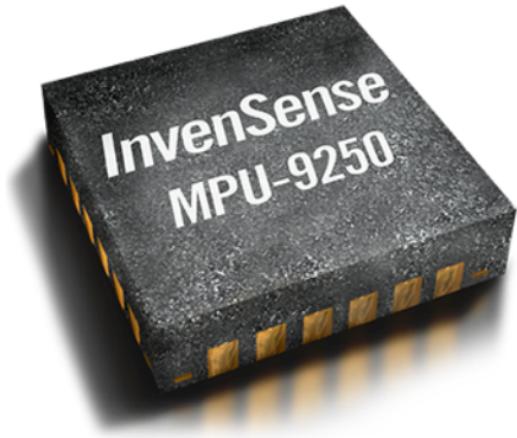
e.g. Arduino

InvenSense MPU-9250



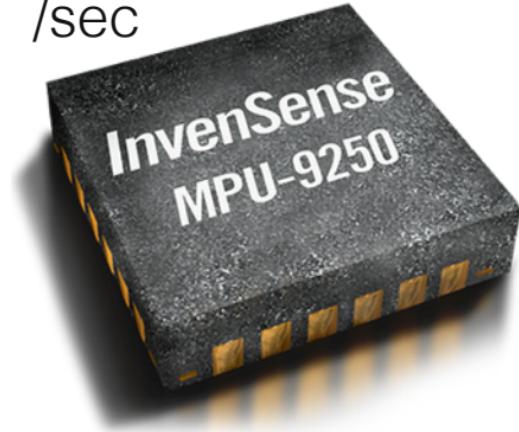
MPU-9250 Specs

- multi-chip module: 1 die houses gyro & accelerometer, the other the magnetometer
- magnetometer: Asahi Kasei Microdevices AK8963 (“3rd party device”)
- 9x 16 bit ADCs for digitizing 9DOF data



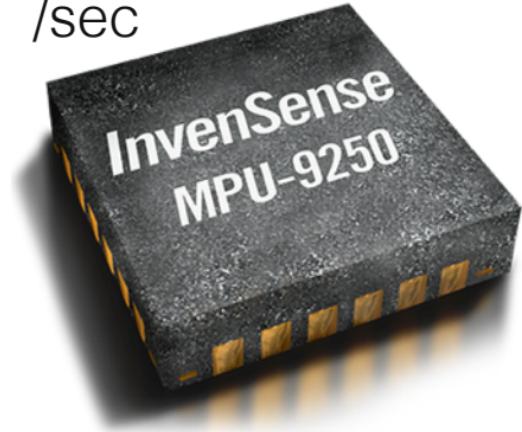
MPU-9250 Specs

- gyro modes: ± 250 , ± 500 , ± 1000 , ± 2000 ° /sec
- accelerometer: ± 2 , ± 4 , ± 8 , ± 16 g
- magnetometer: ± 4800 uT
- configure using registers (see specs) via I2C
- also supports on-board Digital Motion Processing™ (DMP™) sorry, we don't have access
- we'll provide starter code for Arduino in lab (easy to use for beginners, not consumer product grade!)



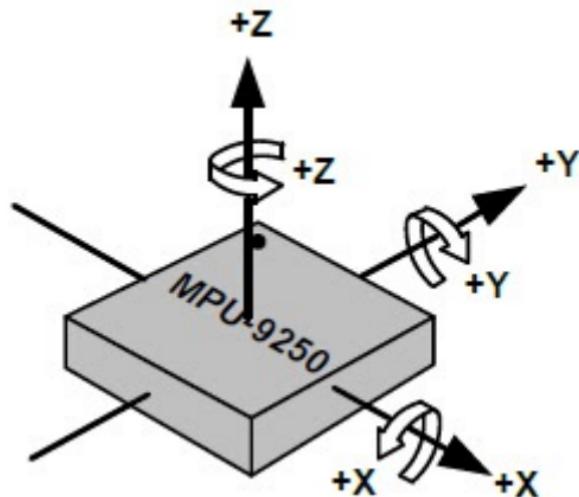
MPU-9250 Specs

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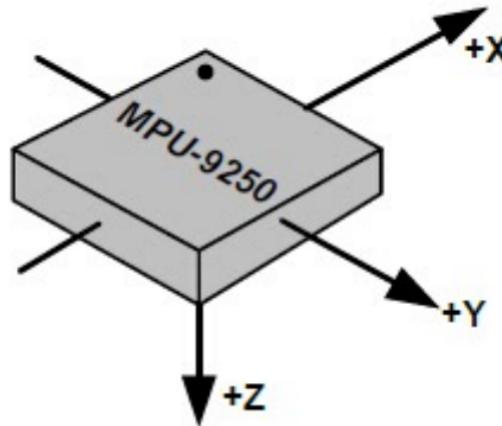


$$metric_value = \frac{raw_sensor_value}{2^{15} - 1} \cdot max_range$$

MPU-9250 Coordinate Systems



gyro & accelerometer



magnetometer

How to read data from IMU

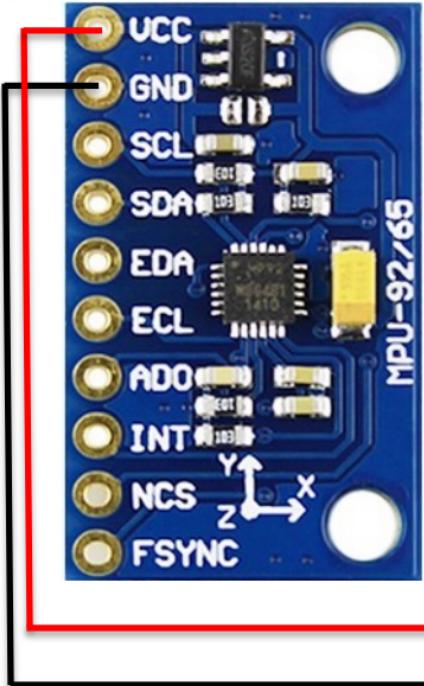
- I2C = serial interface with 2 wires (also see next lab)
- microcontroller to read, we'll use Teensy 3.2, but any Arduino can be used, e.g. past offerings used Metro Mini
- schematics - which pins to connect where
- quick intro to Arduino
- Wire library to stream out data via serial
- serial client using node server

How to read data from IMU



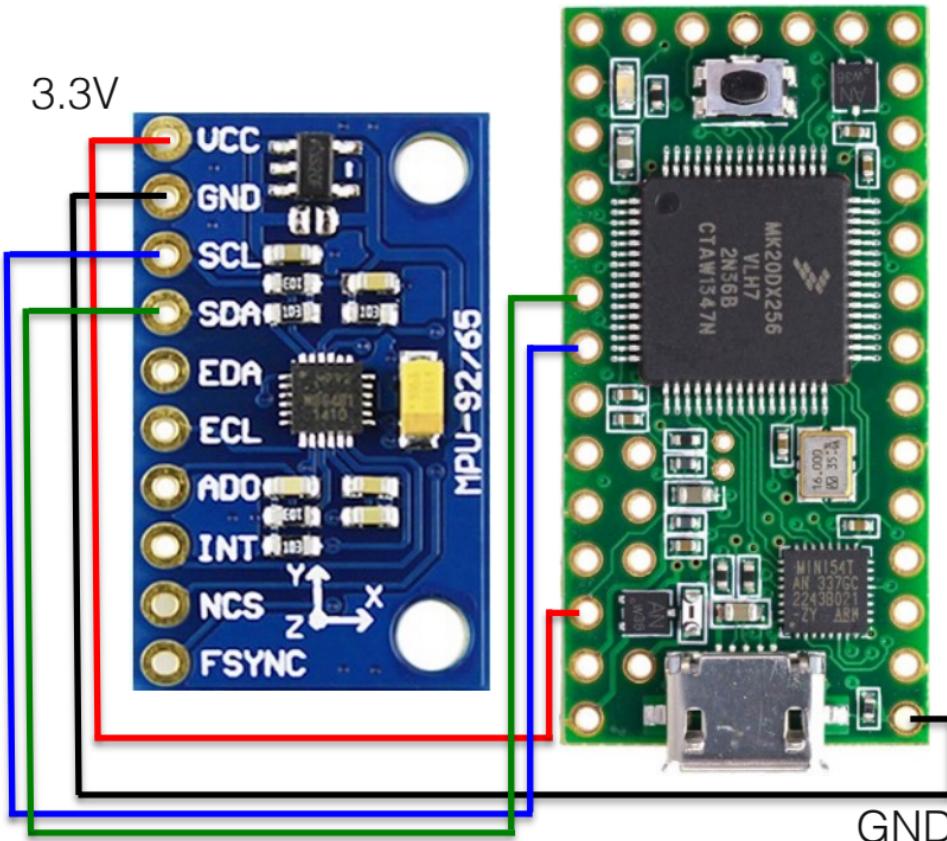
How to read data from IMU

3.3V



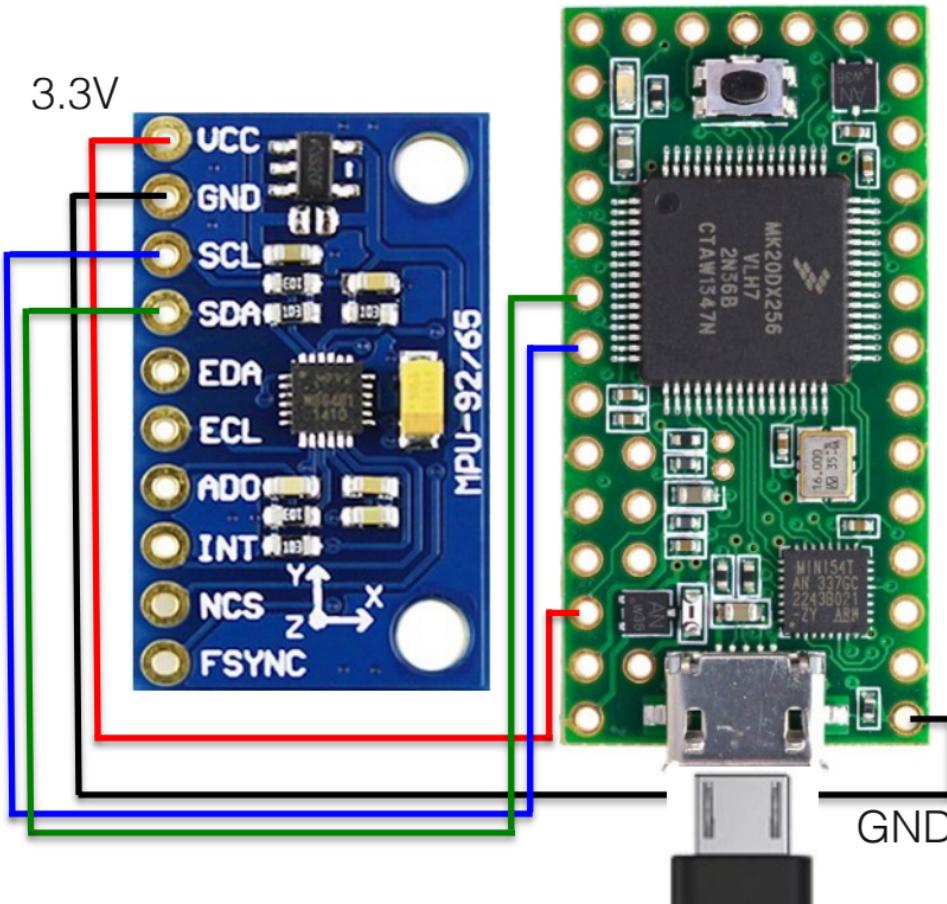
- connect power & ground

How to read data from IMU



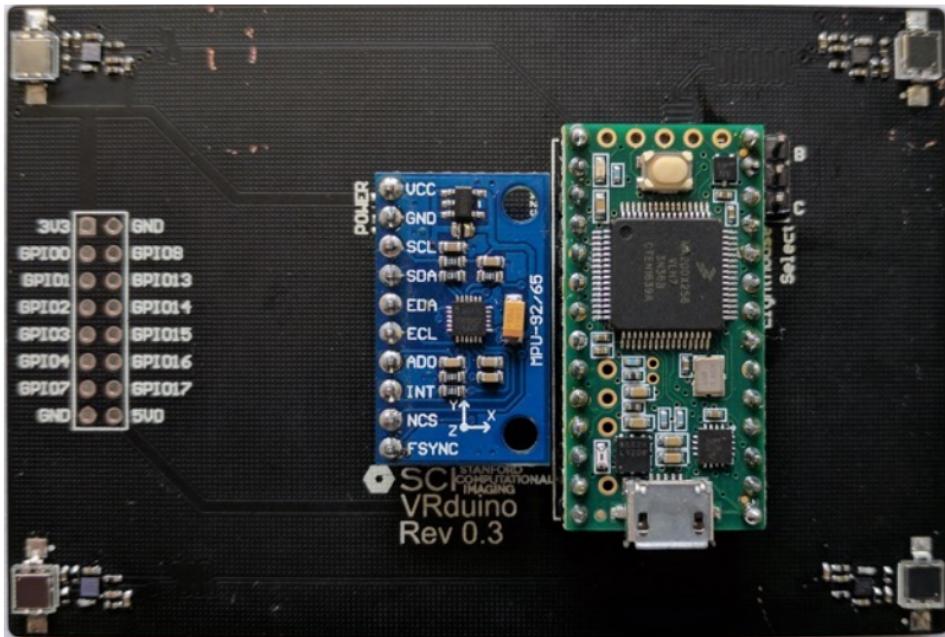
- connect power & ground
- connect I²C clock (SCL, pin19/A5) and data (SDA, pin18/A4) lines

How to read data from IMU



- connect power & ground
- connect I2C clock (SCL, pin19/A5) and data (SDA, pin18/A4) lines
- connect micro USB for power and data transfer

VRduino

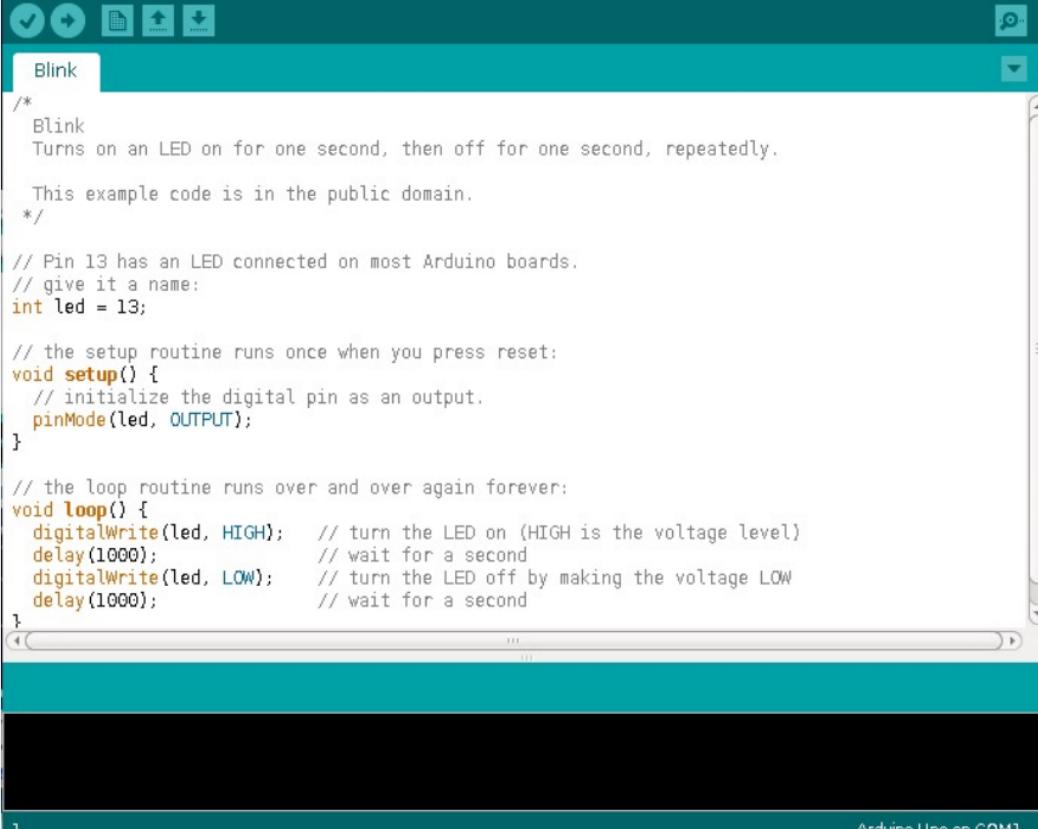


- Teensy 3.2 & IMU already connected through PCB
- also has 4 photodiodes (more details next week)
- GPIO pins for additional sensors or other add-ons

Introduction to Arduino

- open source microcontroller hardware & software
- directly interface with sensors (i.e. IMU) and process raw data
- we will be working with Teensy 3.2 (Arduino compatible)
- use Arduino IDE for all software development, installed on all lab machines
- if you want to install it on your laptop, make sure to get:
 - IDE: <https://www.arduino.cc/en/Main/Software>
 - Teensyduino: <https://www.pjrc.com/teensy/teensyduino.html>
 - Wire library (for serial & I2C): <http://www.arduino.cc/en/Reference/Wire>
 - FTDI drivers: <http://www.ftdichip.com/Drivers/VCP.htm>

Introduction to Arduino (Random Test Program)



The screenshot shows the Arduino IDE interface with the 'Blink' example sketch open. The code is as follows:

```
/*
Blink
Turns on an LED on for one second, then off for one second, repeatedly.

This example code is in the public domain.
*/

// Pin 13 has an LED connected on most Arduino boards.
// give it a name:
int led = 13;

// the setup routine runs once when you press reset:
void setup() {
  // initialize the digital pin as an output.
  pinMode(led, OUTPUT);
}

// the loop routine runs over and over again forever:
void loop() {
  digitalWrite(led, HIGH);    // turn the LED on (HIGH is the voltage level)
  delay(1000);               // wait for a second
  digitalWrite(led, LOW);     // turn the LED off by making the voltage LOW
  delay(1000);               // wait for a second
}
```

The status bar at the bottom right indicates "Arduino Uno on COM1".

- ← variable definition
- ← setup function = initialization
- ← loop function = runtime callback
- ← connected to COM1 serial port

Introduction to Arduino

- need to stream data from Arduino to host PC
- use Wire library for all serial & I2C communication
- use node server to read from host PC and connect to JavaScript (see lab)

Introduction to Arduino

The screenshot shows the Arduino IDE interface with the sketch titled "imu_test_9dof_corrected". The code is as follows:

```
imu_test_9dof_corrected | Arduino 1.6.5

// Put read bytes starting at register Register in the Data array.
void I2Cread(uint8_t Address, uint8_t Register, uint8_t Nbytes, uint8_t* Data)
{
  // Set register address
  Wire.beginTransmission(Address);
  Wire.write(Register);
  Wire.endTransmission();
}

// Read Nbytes
Wire.requestFrom(Address, Nbytes);
uint8_t Index=0;
while (Wire.available())
  Data[Index++]=Wire.read();
}

///////////////////////////////
// Write a byte (Data) in device (Address) at register (Register)
void I2CwriteByte(uint8_t Address, uint8_t Register, uint8_t Data)
{
  // Set register address
  Wire.beginTransmission(Address);
  Wire.write(Register);
  Wire.write(Data);
  Wire.endTransmission();
}

// Initializations
void setup()
{
  // Arduino initializations
  Wire.begin();
  Serial.begin(115200);

  // Configure gyroscope range
  I2CwriteByte(MPU9250_ADDRESS, 27, GYRO_FULL_SCALE_2000_DPS);
  I2CwriteByte(MPU9250_ADDRESS, 27, GYRO_FULL_SCALE_500_DPS);

  // Configure accelerometers range
  I2CwriteByte(MPU9250_ADDRESS, 28, ACC_FULL_SCALE_16_G);
  I2CwriteByte(MPU9250_ADDRESS, 28, ACC_FULL_SCALE_2_G);

  // Set by pass mode for the magnetometers
  I2CwriteByte(MPU9250_ADDRESS, 0x37, 0xB2);

  // Request First magnetometer single measurement
  I2CwriteByte(MAG_ADDRESS, 0x0A, 0x01);
}

///////////////////////////////
// Main loop, read and display data
void loop()
{
  // Read Gyro data
  I2Cread(MPU9250_ADDRESS, 0x43, 6, gyroData);

  // Read Accelerometer data
  I2Cread(MPU9250_ADDRESS, 0x3B, 6, accData);

  // Read Magnetometer data
  I2Cread(MAG_ADDRESS, 0x0A, 3, magData);

  // Convert data to degrees and print it to the serial port
  Serial.print("Gyro X: ");
  Serial.print(gyroData[0]);
  Serial.print(" Gyro Y: ");
  Serial.print(gyroData[1]);
  Serial.print(" Gyro Z: ");
  Serial.print(gyroData[2]);
  Serial.print(" Accelerometer X: ");
  Serial.print(accData[0]);
  Serial.print(" Accelerometer Y: ");
  Serial.print(accData[1]);
  Serial.print(" Accelerometer Z: ");
  Serial.print(accData[2]);
  Serial.print(" Magnetometer X: ");
  Serial.print(magData[0]);
  Serial.print(" Magnetometer Y: ");
  Serial.print(magData[1]);
  Serial.print(" Magnetometer Z: ");
  Serial.println(magData[2]);
}

Sketch uses 6,894 bytes (21%) of program storage space. Maximum is 32,256 bytes.
Global variables use 410 bytes (20%) of dynamic memory, leaving 1,638 bytes for local variables. Maximum is 2,048 bytes.
```

← read from I2C (connected to IMU)

← write to I2C (connected to IMU)

← setup function = one time initialization

← open serial connection to
communicate with host PC

← set registers to configure IMU

Read Serial Data in Windows

- serial ports called COMx (USB serial usually COM3-COM7)
 1. establish connection to correct COM port (choose appropriate baud rate)
 2. read incoming data (in a thread)

Summary

- coordinate systems (world, body/sensor, inertial, transforms)
- overview of inertial sensors: gyroscopes, accelerometers, and magnetometers
- gyro integration aka *dead reckoning*
- orientation tracking in *flatland*
- pitch & roll from accelerometer
- overview of VRduino

Next Lecture

- quaternions and rotations with quaternions
- 6 DOF sensor fusion with quaternions & complementary filtering

Must read: course notes on IMUs!

Additional Information

- D. Sachs “Sensor Fusion on Android Devices: A Revolution in Motion Processing”, Google Tech Talks 2010, Video on youtube.com (<https://www.youtube.com/watch?v=C7JQ7Rpwn2k>)
- S. LaValle, A. Yershova, M. Katsev, M. Antonov “Head Tracking for the Oculus Rift”, Proc. ICRA 2014
- <http://www.chrobotics.com/library>