Analyzing the time-frequency content of EEG data

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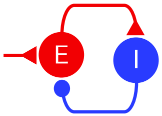
Today

1. Why study neural oscillations?
    - Evoked vs. induced activity
2. Frequency analysis
    - Sine waves, Fourier transform
3. Time-frequency analysis
    - Morlet wavelets
4. Example workflow
    - MNE-Python style, hu-neuro-pipeline style

Why study neural oscillations?

Empirical data

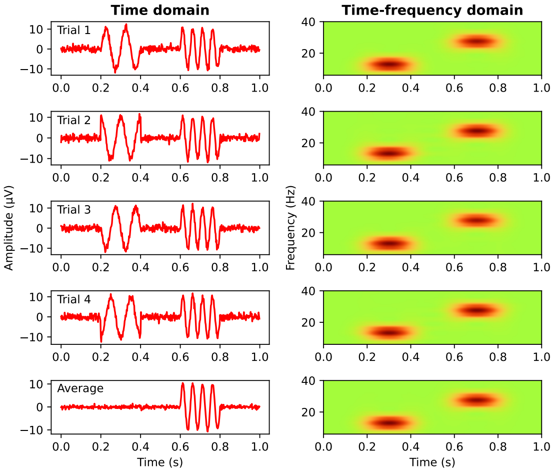
Algorithm



Computation

- Working memory
- Language
- Consciousness

Evoked vs. induced activity

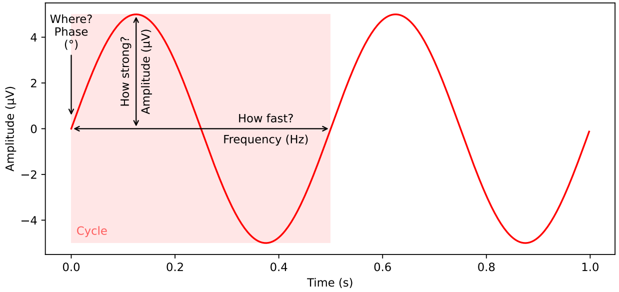


Frequency analysis

Goal: Examine which frequencies (oscillations) contribute to a stretch of continuous EEG

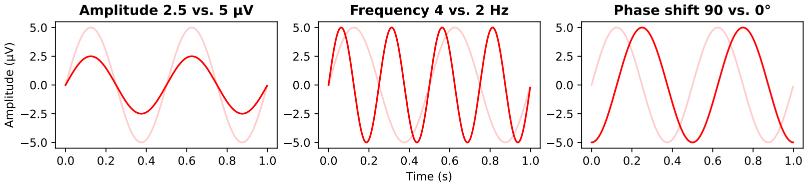
Approach: Decompose the continuous EEG into a set of sine waves $\rightarrow$ Fourier transform

Sine waves



Where?
Phase
(°)
How strong?
Amplitude (µV)
How fast?
Frequency (Hz)
Cycle
Amplitude (µV)
Time (s)
4
2
0
−2
−4
0.0
0.2
0.4
0.6
0.8
1.0

Sine waves


Amplitude 2.5 vs. 5 µV
Frequency 4 vs. 2 Hz
Phase shift 90 vs. 0°
Amplitude (µV)
Time (s)
5.0
2.5
0.0
−2.5
−5.0
0.0
0.2
0.4
0.6
0.8
1.0

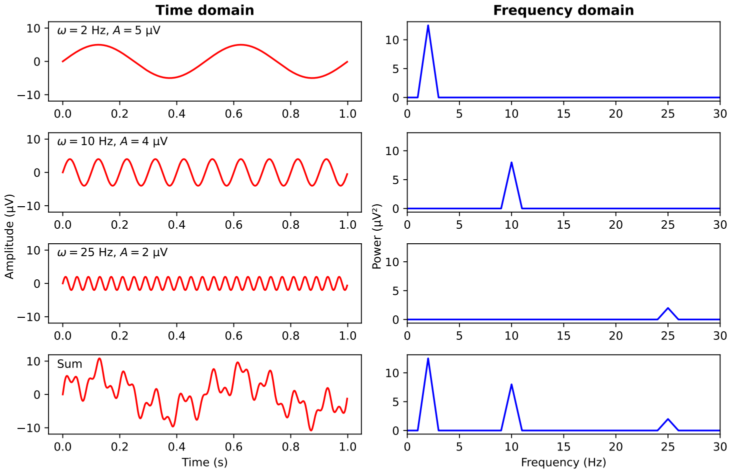
Fourier transform

Joseph Fourier (1768–1830):

Any signal can be expressed as sum of weighted sine waves, each with its own frequency, amplitude, and phase

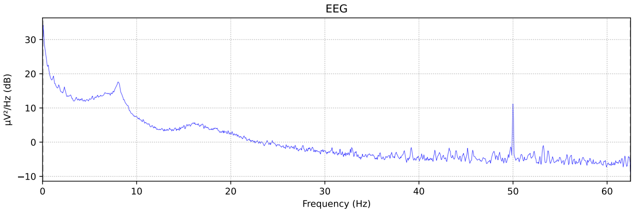
$$
\begin{aligned}
f(t) &= A_0 + A_1 \cos(\omega t + \varphi_1) + A_2 \cos(\omega t + \varphi_2) + \ldots + A_N \cos(\omega t + \varphi_N) \\
&= \sum_{n=0}^{N} A_n \cos(\omega t + \varphi_n) \quad \text{where } A = \text{amplitude}, \ \omega = \text{frequency}, \ \varphi = \text{phase}
\end{aligned}
$$

Fourier transform



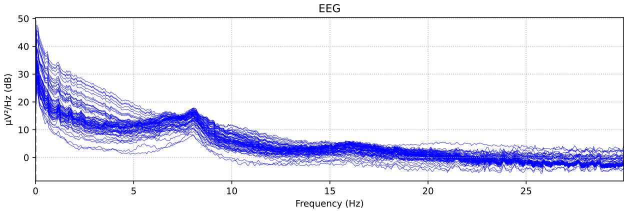
Frequency analysis in MNE-Python

```
# Read raw data
from mne.io import read_raw_brainvision
raw = read_raw_brainvision('data/raw/05.vhdr')

# Downsample to make subsequent computations faster
raw = raw.resample(125.)

# Plot spectrum for a single channel
_ = raw.plot_psd(picks='Cz', color='b', spatial_colors=False)
```

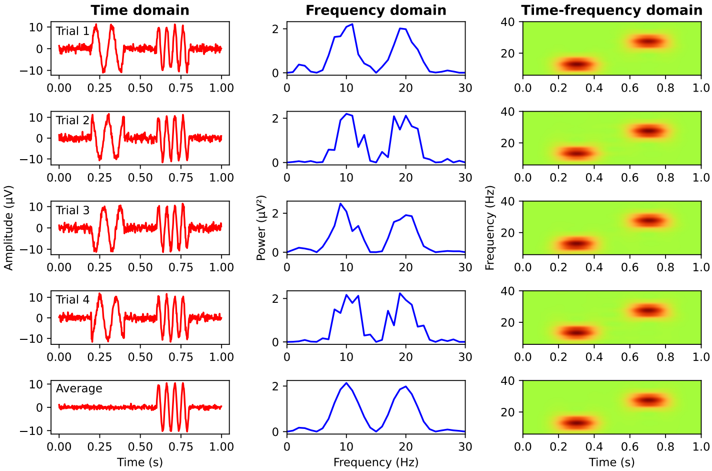


Frequency analysis in MNE-Python

```python
# Plot spectrum for all channels, restricted to 0-30 Hz
_ = raw.plot_psd(fmax=30, color='b', spatial_colors=False)
```



Frequency analysis

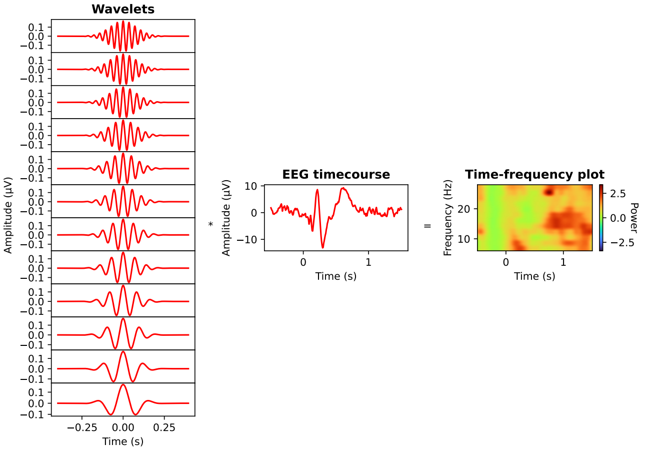


Time-frequency analysis

Goal: Estimate how power (or phase) at each frequency changes over time, e.g., in response to a stimulus

Approach: Apply the Fourier transform to a short time window and move this window over time points in the epoch $\rightarrow$ Short-term Fourier transform (STFT), Morlet wavelet convolution

Morlet wavelets



Basline correction

- Should fit at least one full cycle at the lowest frequency
  - E.g., 5 Hz $\rightarrow$ min. 200 ms baseline
- Should account for the $1/f$ scaling $\rightarrow$ Divisive baseline
  - Subtract + divide by mean baseline: Percent signal change
  - Divide by mean baseline + take logarithm: Decibel
- Baseline should end *before* rather than *at* stimulus onset
  - Prevents post-stimulus activity “smearing” into the baseline

Time-frequency analysis in MNE-Python

```python
# Load functions
import numpy as np
from mne import events_from_annotations, Epochs
from mne.time_frequency import tfr_morlet

# Segment continuous signal to epochs
events, _ = events_from_annotations(raw, regexp='Stimulus')
triggers = [201, 205]
epochs = Epochs(raw, events, triggers, tmin=-0.5, tmax=1.5, baseline=(-0.2, 0.))
print(epochs.get_data().shape) # Dimensions: (trials, channels, time points)
```

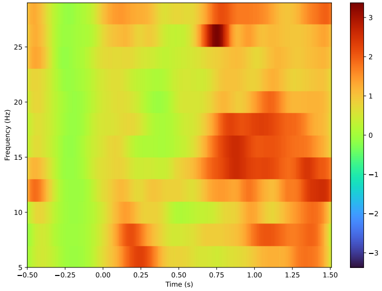
```
## (240, 64, 251)
```

```python
# Apply Morlet wavelet decomposition
freqs = np.arange(6., 30., step=2.)
n_cycles = np.arange(3., 15., step=1.)
tfr = tfr_morlet(epochs, freqs, n_cycles, return_itc=False, average=False)
print(tfr.data.shape) # Dimensions: (trials, channels, frequencies, time points)
```

```
## (240, 64, 12, 251)
```

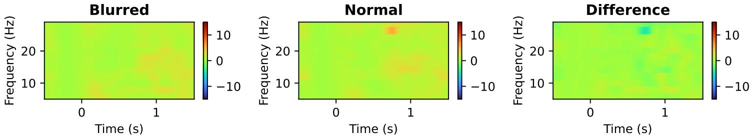
Time-frequency analysis in MNE-Python

```
# Divisive baseline correction to get percent signal change
tfr = tfr.apply_baseline((-0.3, -0.1), mode='percent')

# Plot power at one channel, averaged across epochs
tfr_ave = tfr.average()
tfr_ave.plot(picks='Cz', cmap='turbo')
```



Time-frequency analysis in MNE-Python

```python
# Compute power per condition and the difference between conditions
tfr_aves = {'Blurred': tfr['201'].average(),
            'Normal': tfr['205'].average(),
            'Difference': tfr['201'].average() - tfr['205'].average()}

# Create multi-panel plot
import matplotlib.pyplot as plt
fig, axs = plt.subplots(nrows=1, ncols=len(tfr_aves), figsize=(9, 2))
for ix, (label, tfr_ave) in enumerate(tfr_aves.items()):
    axs[ix].set_title(label, weight='bold')
    tfr_ave.plot(picks='Cz', cmap='turbo', vmin=-15, vmax=15,
                 axes=axs[ix], show=False)
```



Time-frequency analysis with the pipeline

General settings:

```r
# Import the Python package from R
pipeline <- reticulate::import("pipeline")

# Run the pipeline with the `tfr` (time-frequency) options
res <- pipeline$group_pipeline(
  vhdr_files = "data/raw",
  log_files = "data/log",
  output_dir = "output",
  ocular_correction = "data/cali",
  triggers = c(201:208, 211:218),
  average_by = c("n_b", "DeviantPosRL", "n_b/DeviantPosRL"),
  perform_tfr = TRUE,
  tfr_freqs = seq(6, 30, by = 2),
  tfr_cycles = seq(3, 15, by = 1),
  tfr_baseline_tmin = -0.3,
  tfr_baseline_tmax = -0.1,
  ... # See next 2 slides
)
```

Time-frequency analysis with the pipeline

For effects with *a priori* knowledge about their distribution:

```r
# Define time-frequency "components" of interest
res <- pipeline$group_pipeline(
  ...,
  tfr_components = list(
    "name" = list("alpha"),
    "tmin" = list(0.0),
    "tmax" = list(0.2),
    "fmin" = list(8),
    "fmax" = list(14),
    "roi" = list(
      c("PO9", "PO7", "PO3", "POz", "PO4", "PO8", "PO10", "O1", "Oz", "O2")
    )
  )
)
```

→ Then use the single trial data frame to run mixed models

Time-frequency analysis with the pipeline

For exploratory analyses → Cluster-based permutation tests:

```r
# Run 3D cluster-based permutation tests for contrasts of interest
res <- pipeline$group_pipeline(
  ...,
  perm_contrasts = list(
    c("blurr", "normal"),
    c("blurr/re", "blurr/li"),
    c("normal/re", "normal/li")
  )
)
```

→ Creates a new data frame with cluster-level *p*-values across time, space (channels), and frequencies

General remarks

- Richer view of the EEG signal (evoked + induced activity)
- Many new parameters to think carefully about:
  - Design $\rightarrow$ Longer inter-trial interval; jittering
  - Wavelet frequencies + number of cycles $\rightarrow$ T/f tradeoff
  - Baseline correction window and method
  - Interpretation:
    - Narrow-band vs. broad-band
    - Oscillation vs. rate of change
- Everything matters

Thanks