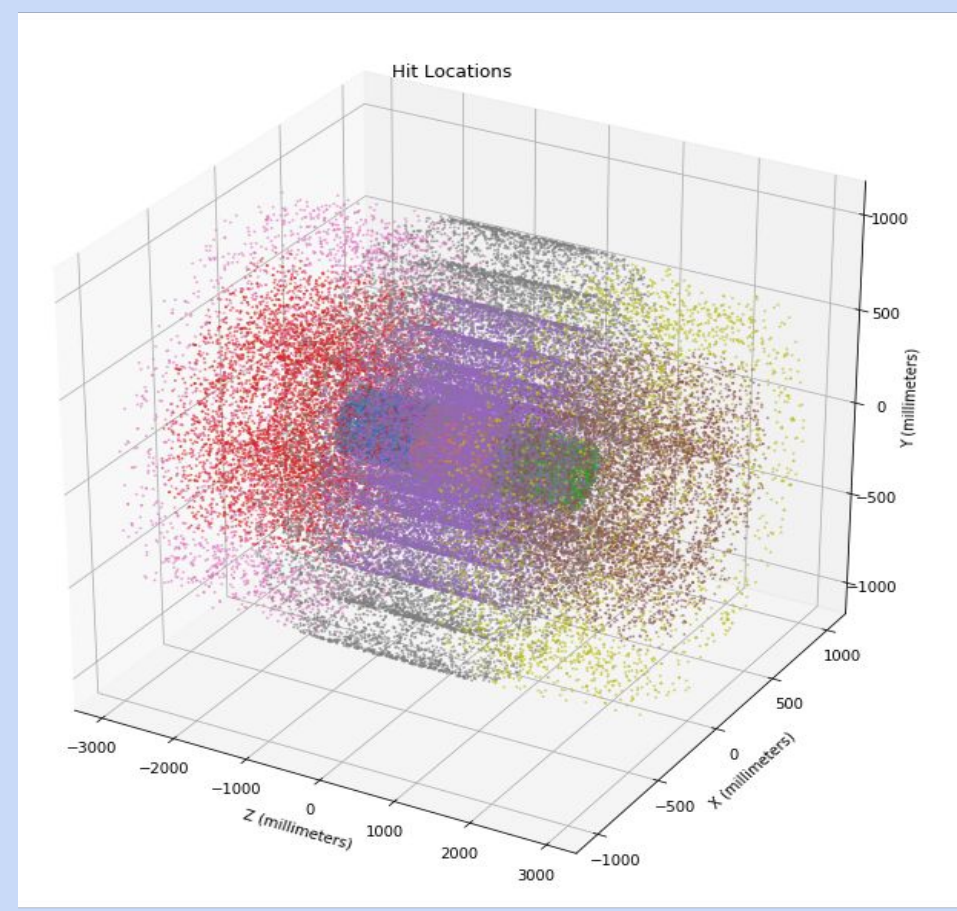
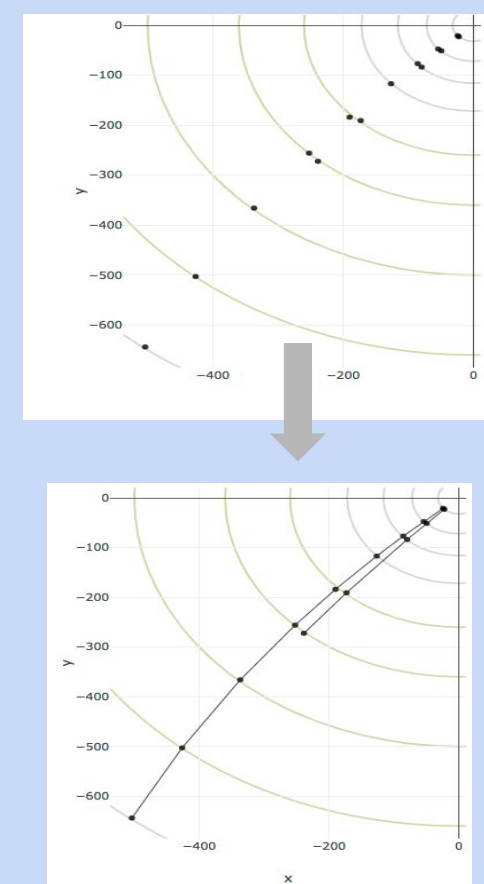


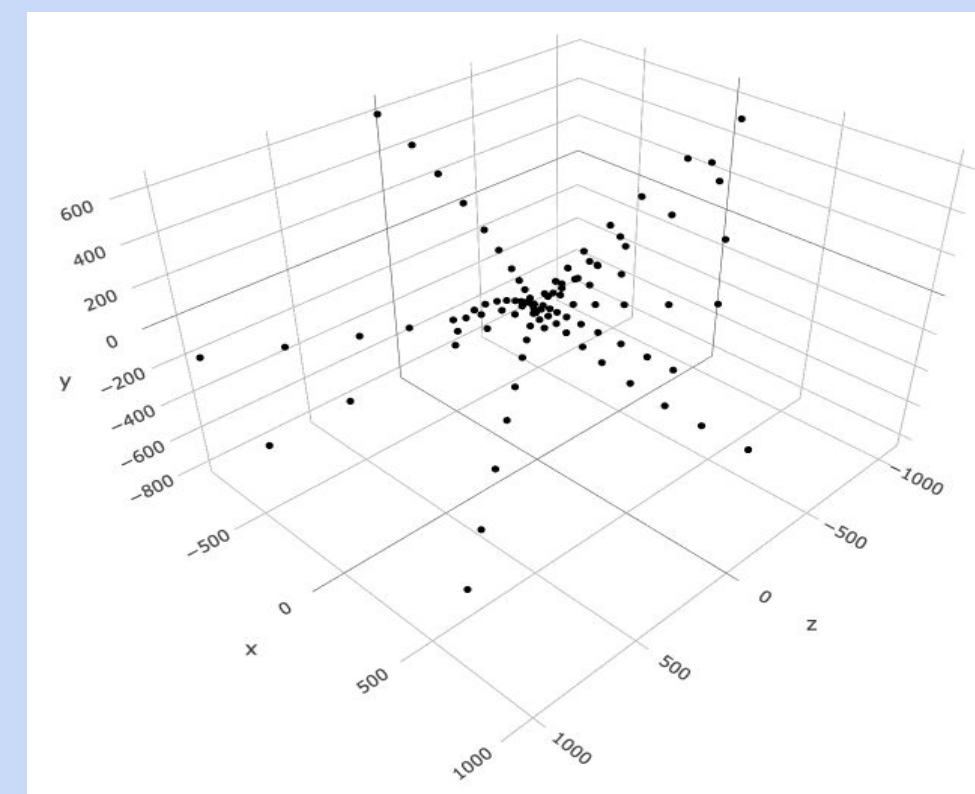
# LHC Pattern Recognition Challenge



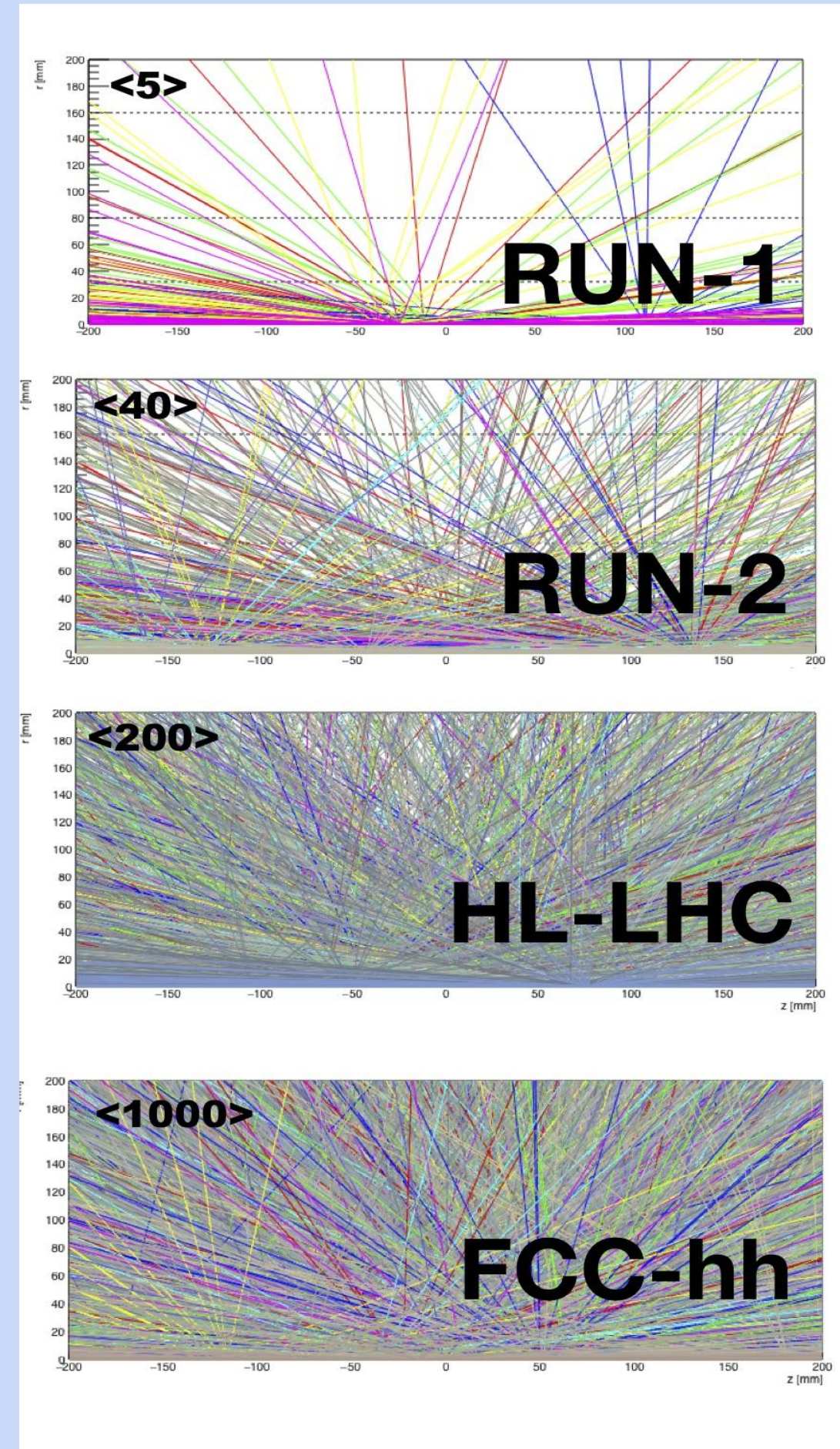
From Detector Measurements...



...to Particle Tracks...



...to Particle Properties



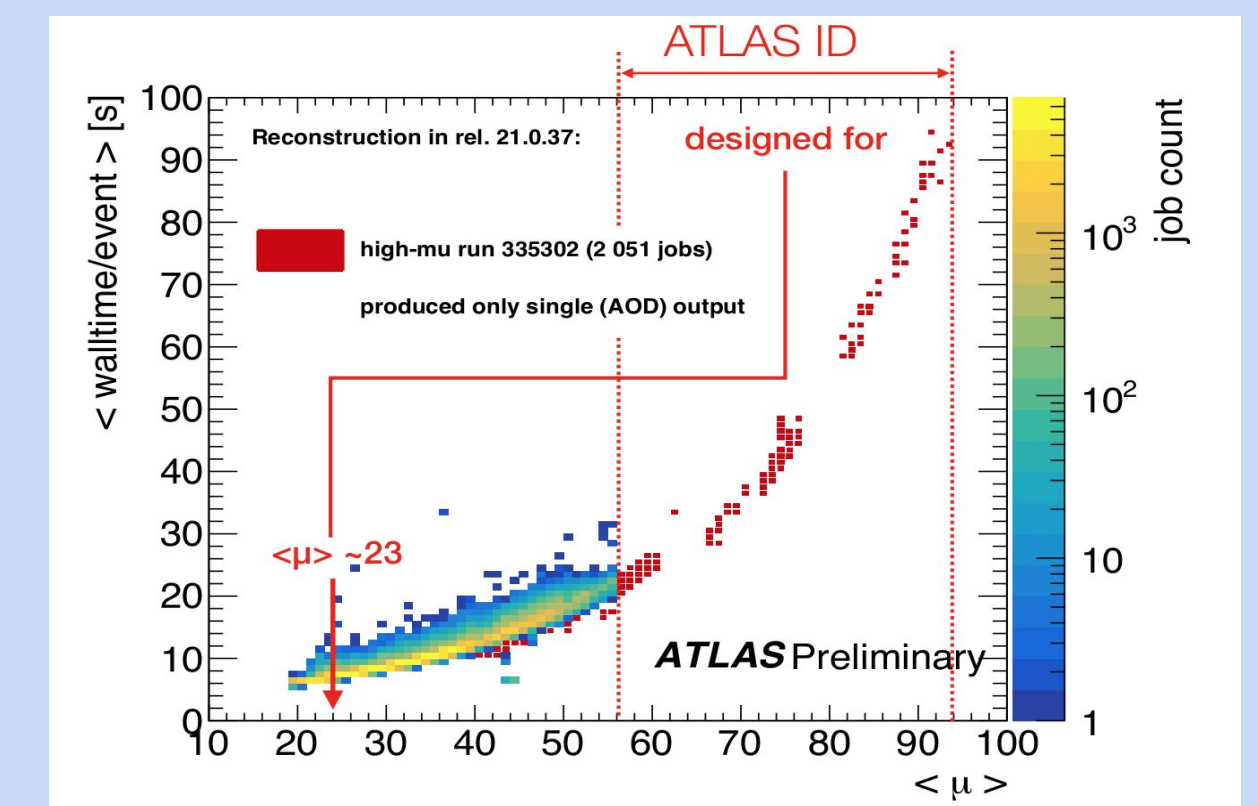
2008

2016

2028

~2040

Combinatorially hard optimization.  
Current algorithms show polynomial scaling.



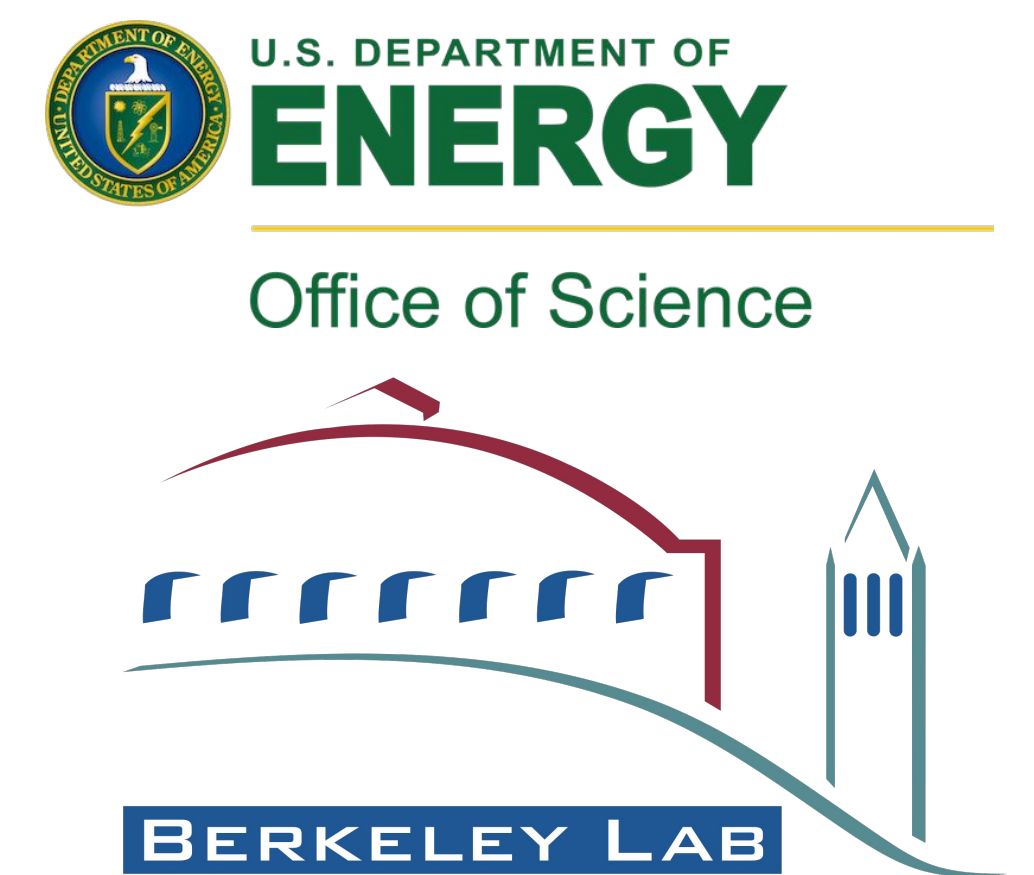
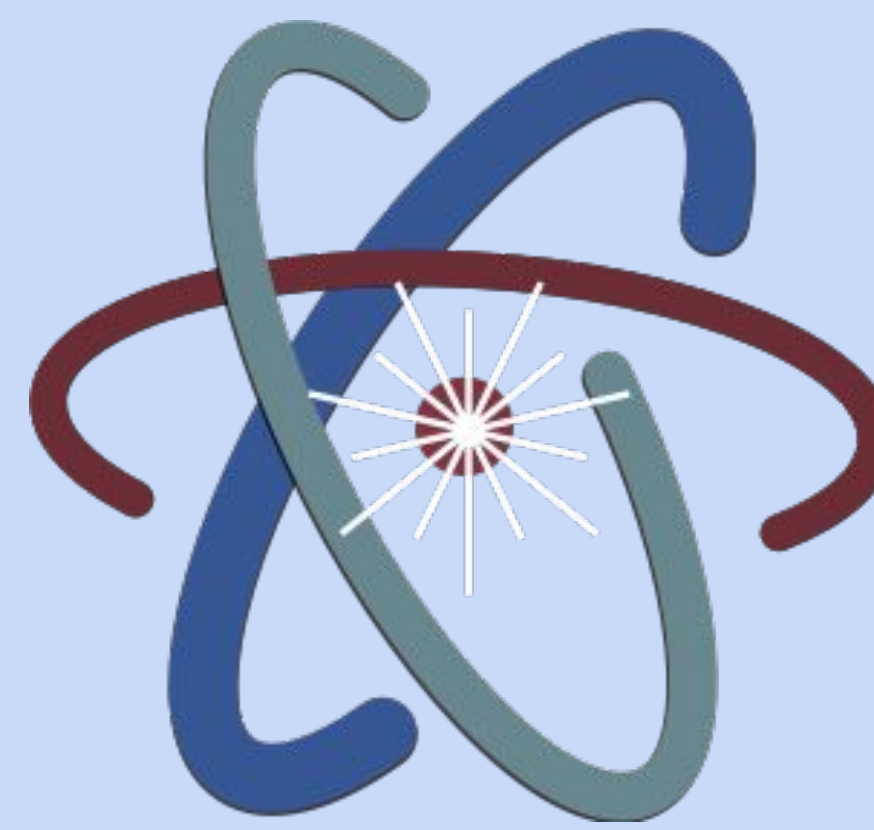
Can quantum pattern recognition provide a solution for FCC-hh?

Wahid Bhimji, Paolo Calafiura, Heather Gray (PI), Wim Lavrijsen, Eric Rohm, Amitabh Yadav



<https://hep-qpr.lbl.gov>

## HEP.QPR A QuantISED Project



## QAOA Global Pattern Recognition

Rationale

Tracking as a global optimization problem

• QAOA for QUBO (Eric Rohm)



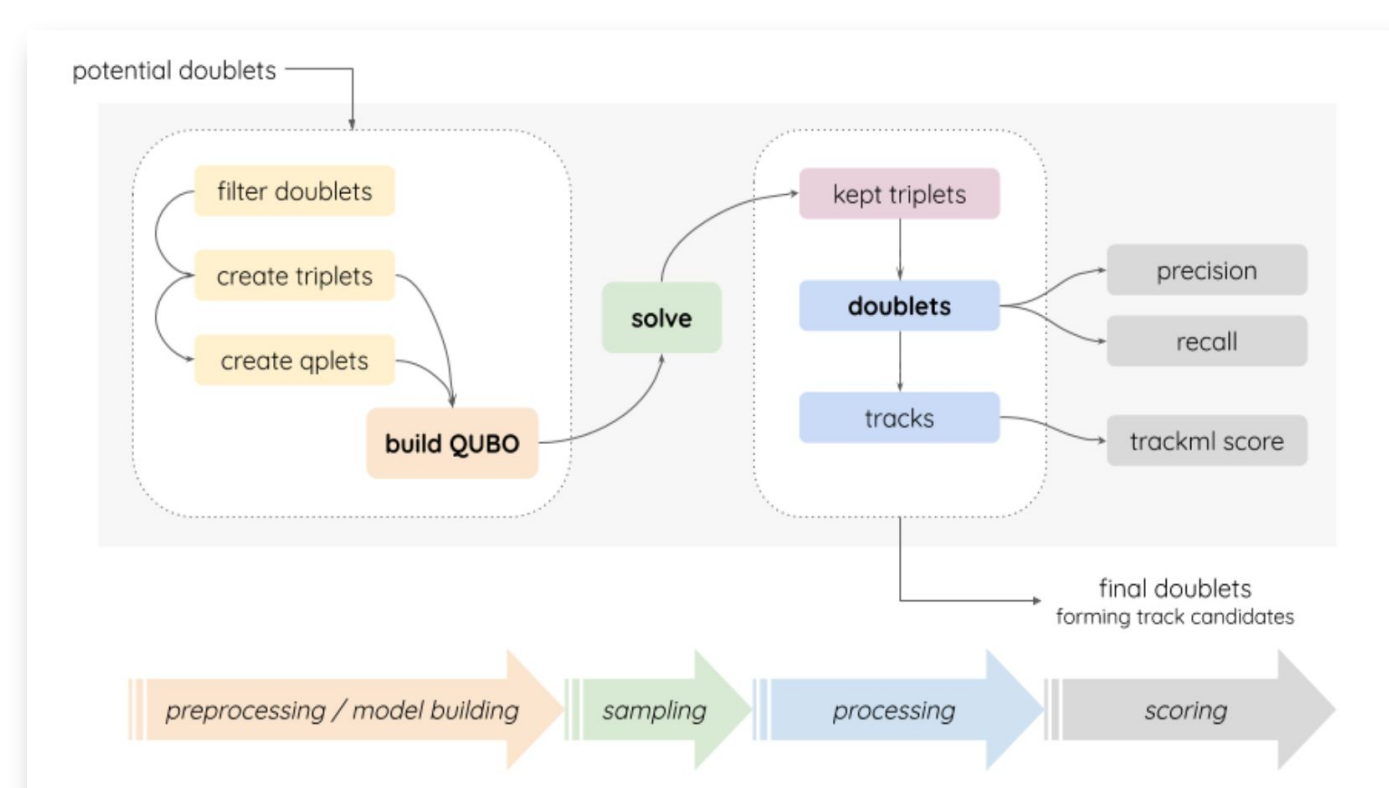
QUBO Minimization

Building on our previous study, we express tracking as a QUBO

$$O(a; b; q) = \sum_{i=1}^N a_i q_i + \sum_{i=1}^N \sum_{j=1}^N b_{ij} q_i q_j \quad q_i \in \{0, 1\}$$

Where  $q_i$  are **doublets**, segments composed by two hits.

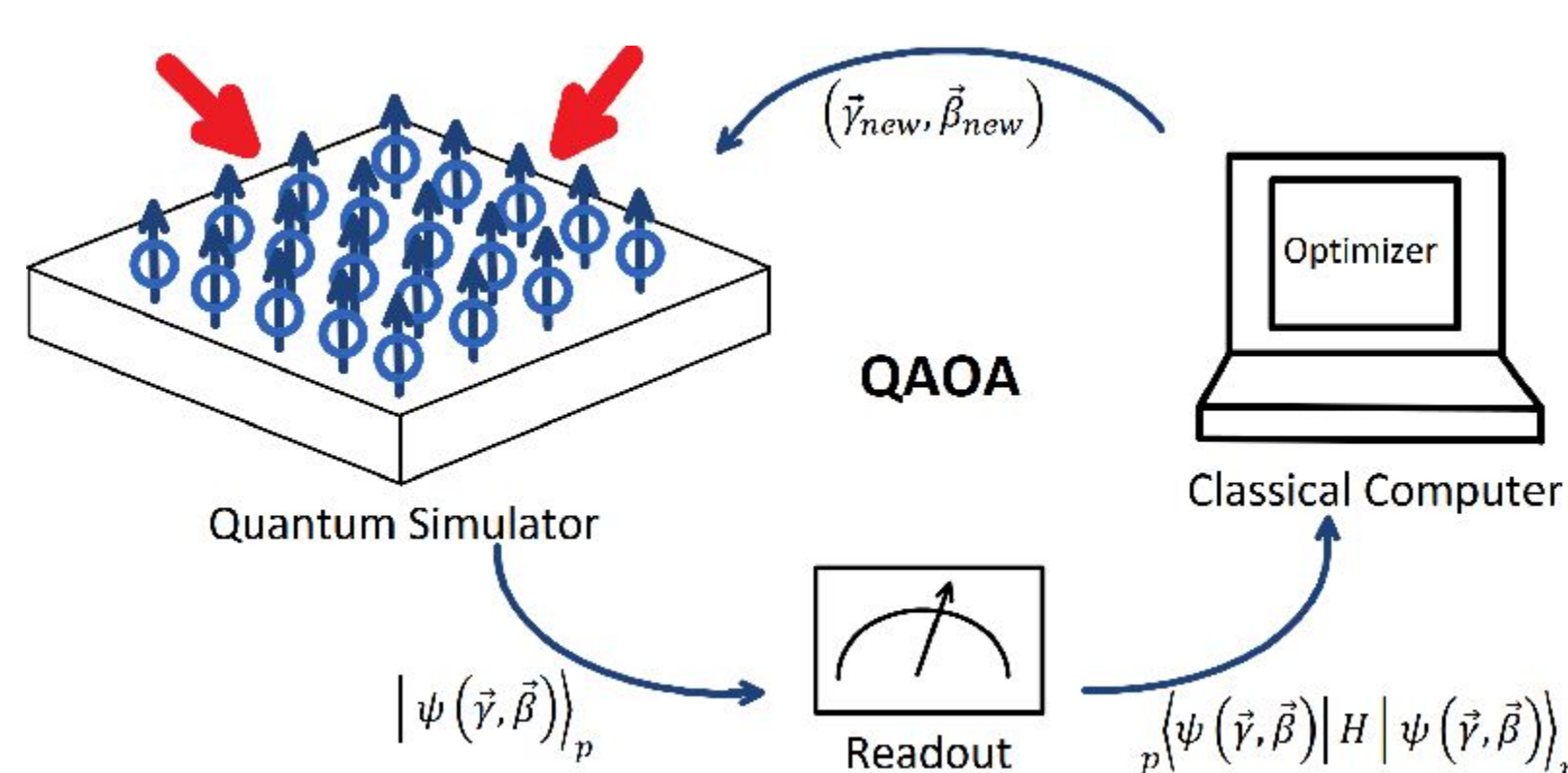
Minimizing  $O$  means selecting the best **triplets** to form track candidates.



QAOA

### Quantum Approximate Optimization Algorithm (QAOA)

Hybrid classical-quantum algorithm that combines quantum circuits and classical optimization of those circuits

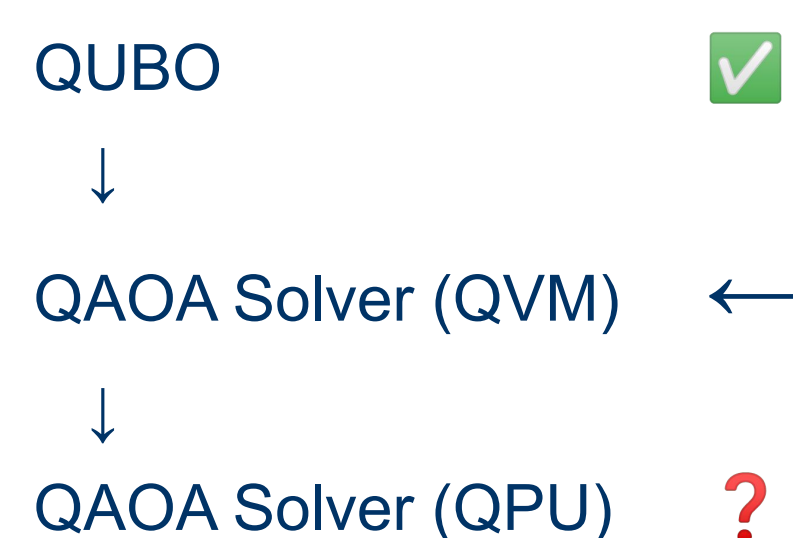


A superposition of input states is prepared on a quantum circuit, while each successive iteration of parameters is optimized classically then returned to the quantum machine (Ho, Hsieh 2018).

### EntropicaQAOA

Implementation on Rigetti QVM and QPU  
Apply QAOA directly to QUBOs (and Ising models)

Status:



Implementation

## Quantum Hough Transform

Rationale

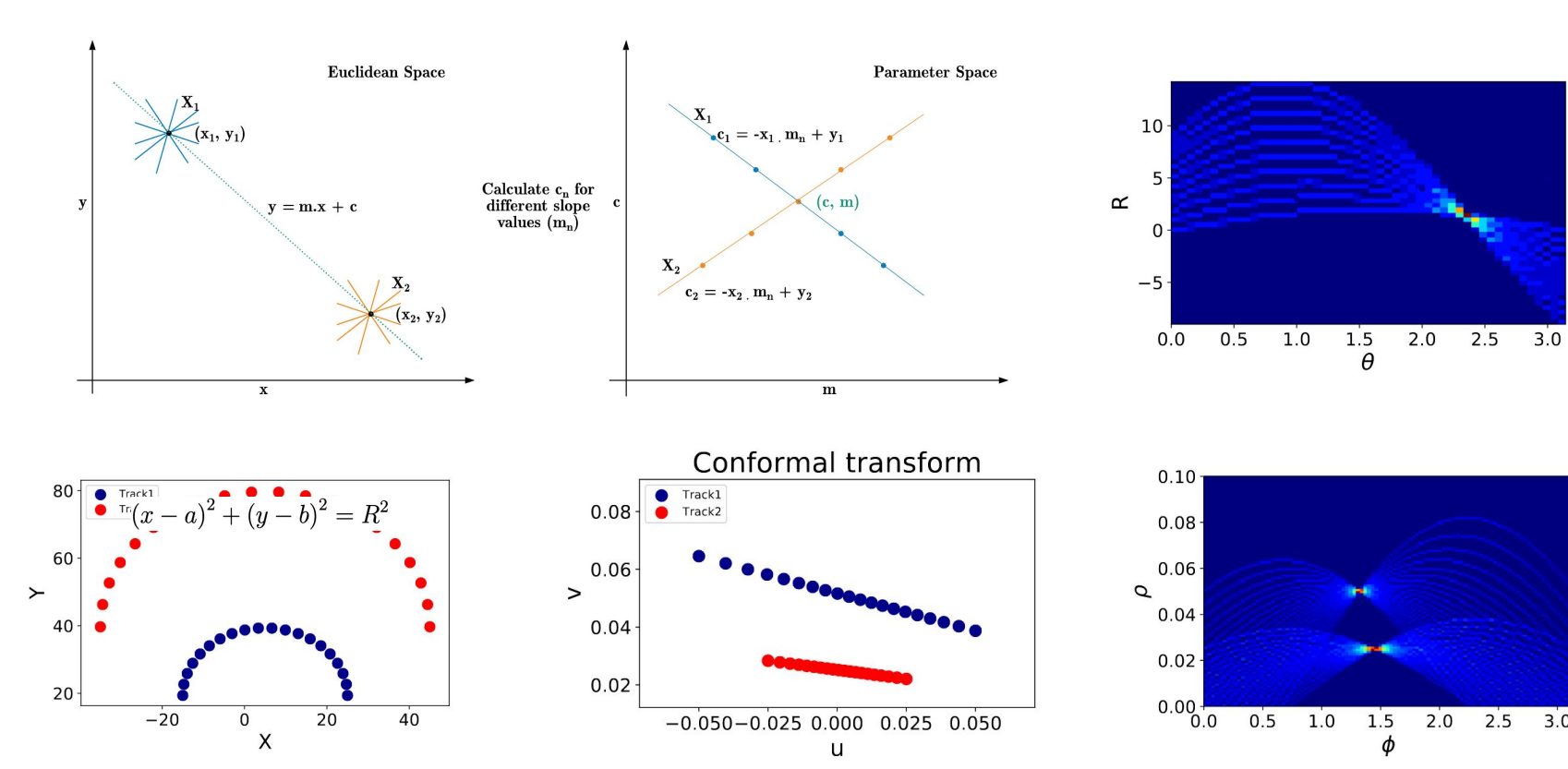
Tracking as a geometrical transformation

• QLSA  
• Quantum Counting (Amitabh Yadav)

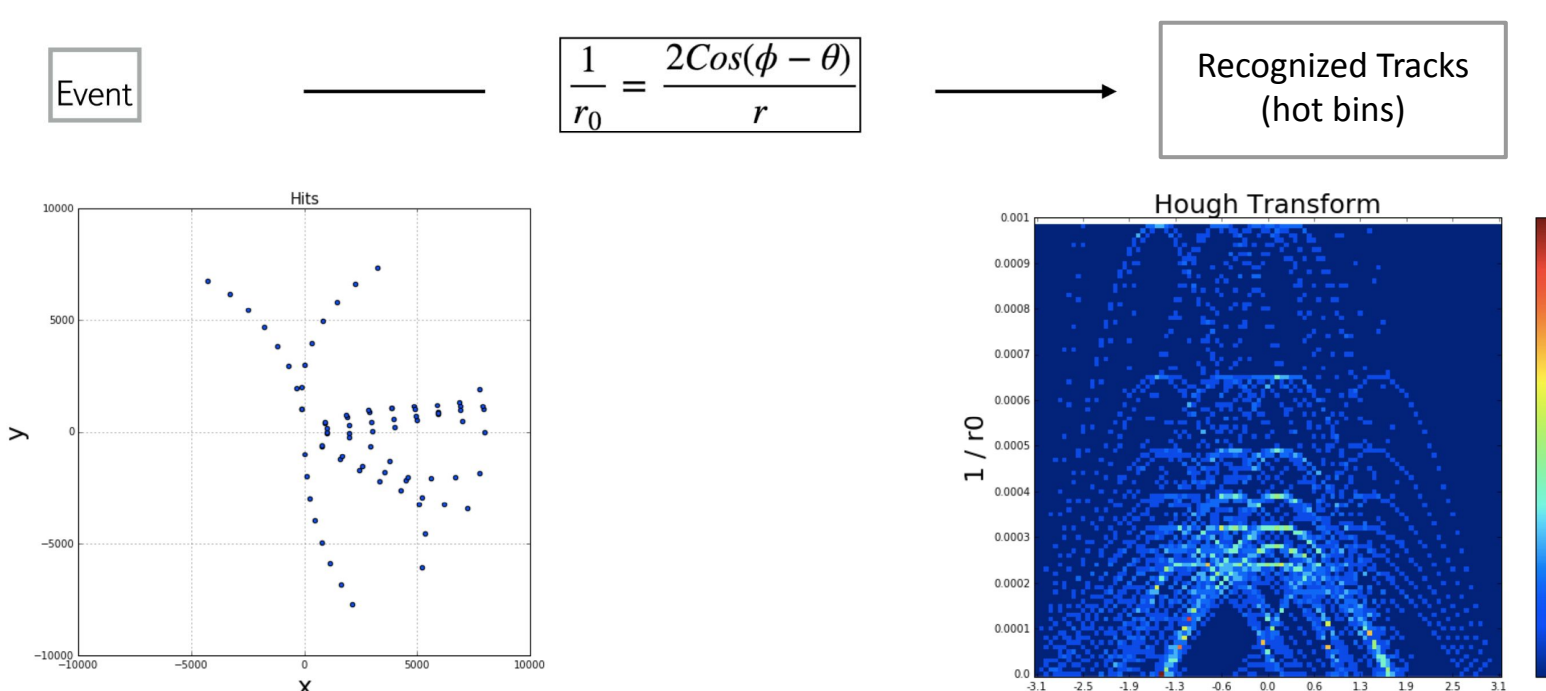


Hough Transform

Classic feature extraction algorithm, used for HEP tracking from the '70s  
Accumulate points belonging to a line or circle to bins in **Hough Space**

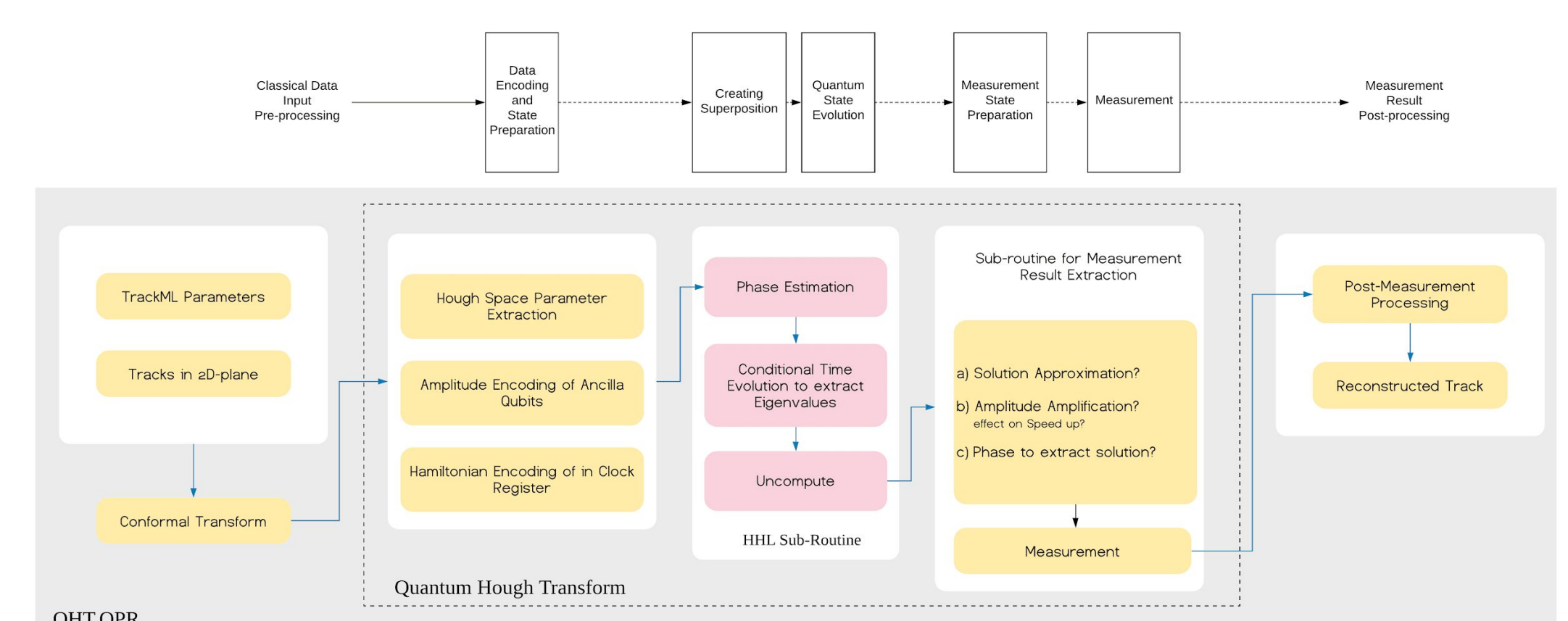


Ref.: Alpouf Tehrani, Niloufar "Simulation and tracking studies for a drift chamber at the FCC-ee experiment" (2019), cds.cern.ch



Implementation

### QHT.QPR as a Quantum Linear System Algorithm (using HHL)



Current Work

- Algorithmic pipeline design with idealized tracks
- QISKIT Aqua for HHL subroutine
  - HHL offers exponential speed-up for solving linear equations
- Accumulator space formed by superposition of qubits
- Post HHL measurement result extraction subroutine [\[10.1103/PhysRevLett.110.250504\]](https://arxiv.org/abs/10.1103/PhysRevLett.110.250504)

Key Challenges:

- $|b\rangle$  State encoding
- Measurement result interpretation (i.e. sampling exact solutions from  $|x\rangle$  measurement)

Alternative Approaches:

- Max/Min finding  $O(\sqrt{N})$  [\[arXiv:1908.07943v1\]](https://arxiv.org/abs/1908.07943v1)
- Quantum counting
- Grover search