




PAOS: a fast, modern, and reliable Python package for Physical Optics studies

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DOI: [N/A](#)

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Submitted: 01 January 1970

Published: 01 January 1970

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Summary

PAOS is an open-source code implementing physical optics propagation (POP) in Fresnel approximation and paraxial ray-tracing to analyze complex waveform propagation through both generic and off-axes optical systems, enabling the generation of realistic Point Spread Functions across various wavelengths and focal planes. It improves upon other POP codes offering extensive customization options and the liberty to access, utilize, and adapt the software library to the user's application. With a generic input system and a built-in Graphical User Interface, PAOS ensures seamless user interaction and facilitates simulations. The versatility of PAOS enables its application to a wide array of optical systems, extending beyond its initial use case. PAOS presents a fast, modern, and reliable POP simulation tool, enhancing the assessment of optical performance for a wide range of scientific and engineering applications and making advanced simulations more accessible and user-friendly.

Developed using a Python 3 stack, PAOS is released under the BSD 3-Clause license and is available on [GitHub](#). The plugin can be installed from the source code or from [PyPI](#), so it can be installed as `pip install paos`. The documentation is available on [readthedocs](#), including a quick-start guide, documented examples, a comprehensive description of the software functionalities, and guidelines for developers. The documentation is continuously updated and is versioned to match the software releases.

Benchmark

We benchmarked PAOS against PROPER ([Krist, 2007](#)) on the HST optical system, because PROPER is not designed to handle Ariel's, which i) is off-axis and ii) involves more complex elements than simple thin lenses, such as dichroics. The description of the HST system used is the one provided in the `Hubble_simple.py` file in the PROPER package¹. This description was translated into an input file² for PAOS for reproducibility. All simulation inputs have been matched (e.g., wavelength, grid size, zoom³). We added a line in the PROPER HST routine to set the pixel subsampling factor used to antialias the edges of shapes. We set this value to 101 from the default 11 to more closely match the exact treatment given in PAOS.

We compared the resulting PSFs at the focal plane of the telescope, both in the central region and in the outer wings. The first benchmark is reported below, showing the results for the PSFs at 1 μm . [Figure 1](#) shows the central region of the HST PSFs as computed with PAOS and PROPER, and their difference. No significant residuals were found, with sporadic outlier

¹The PROPER source code and documentation can be downloaded at <https://proper-library.sourceforge.net/>.

²`Hubble_simple.ini`, included in the package under the `lens_data` directory.

³The ratio between the grid's linear dimension and the beam size at the initial surface.

pixels showing deviations by < 0.1 dB in regions corresponding to the PSF zeros due to small numerical errors.

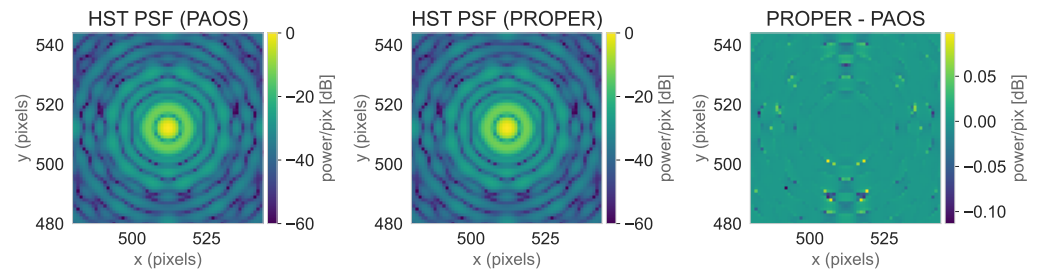


Figure 1: The central region of the HST PSF at $1 \mu\text{m}$ as estimated with PAOS (left) and PROPER (center) and normalized to the maximum value in the array. The axes are in oversampled pixels. The color scale represents the power per pixel in decibels (dB), with a lower cut-off at -60 dB for better visualization. The right panel reports the difference between the PSF computed with PROPER and PAOS in the same physical units.

Figure 2 shows a detailed view of the slices of the PSFs along the horizontal and vertical axes, and their differences. The signal curves show an almost perfect overlap, with negligible residuals, all corresponding to values < -50 dB from the PSF maximum in the far wings.

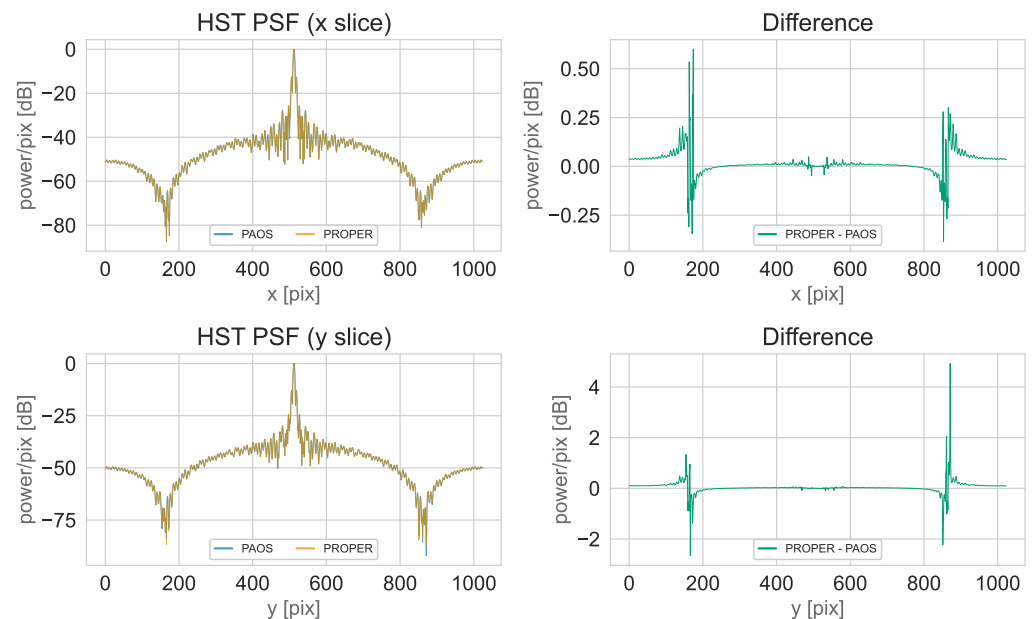


Figure 2: Comparison between PSF slices along the x and y axis, respectively. The left column reports the slice values for both codes, whilst the right column reports their difference. The units are the same (power per pixel in dB) to highlight even the smallest discrepancies. As can be observed, these differences are negligible for powers $\gtrsim -50$ dB for the HST application.

Figure 3 and 4 report the second benchmark; in this case, we simulate an aberrated PSF by HST described by a superposition of Zernike polynomials. At M2, we added 100 nm RMS (WFE) each for defocus, vertical astigmatism, and oblique astigmatism, totaling $\sigma \approx 173.2$ nm WFE. The simulation is performed at $\lambda = 1.0 \mu\text{m}$; therefore, using the Ruze formula (Ross, 2009), the Strehl ratio is $S = \exp(-2\pi\sigma/\lambda) \approx 0.3$. Consequently, the PSF is highly aberrated and the main lobe is spread over more pixels. Thus, we can validate the PAOS implementation of optical aberrations, and we have a larger region of high signal. The latter is

especially useful for investigating aliasing errors, which tend to occur more severely where the distribution has the highest amplitude because the amplitudes of the signal and the error add rather than the intensities (Lawrence et al., 1992).

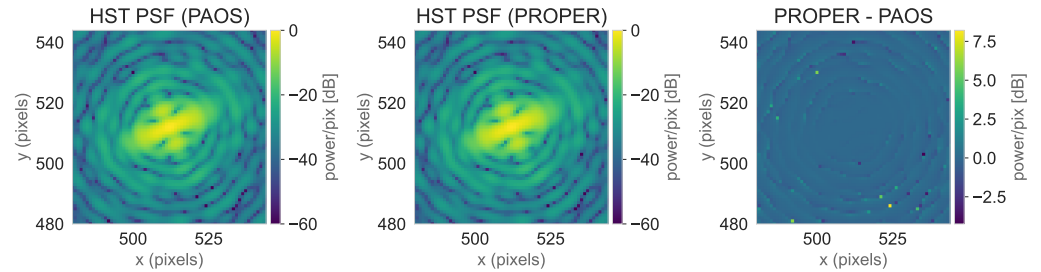


Figure 3: Same as Figure 1, but adding an optical aberration using Zernike polynomials: 100 nm RMS (WFE) for each of three low-order coefficients in the Zernike expansion: defocus and primary astigmatism (vertical and oblique), corresponding to the coefficients 4, 5, and 6 in the Noll ordering, respectively. The difference between the large-scale features of the PSFs is negligible.

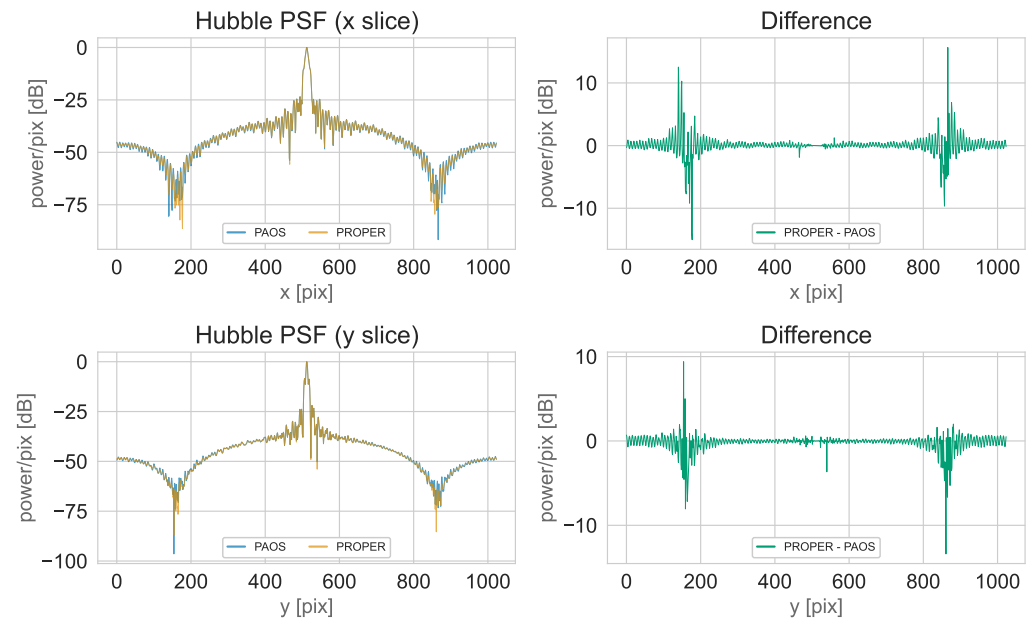


Figure 4: Comparison between PSF slices along the x and y axis, respectively. Locally, slightly hotter and colder pixels can be identified in the PSF wings, although, for powers $\gtrsim -50$ dB, this happens only sporadically. These minute numerical differences may be caused by the different treatment of aperture edges (exact for PAOS, sub-pixelled for PROPER), causing tiny aliasing errors.

We find that the differences between the aberrated PSFs are negligible and reach peaks of a few dB only in the far wings. However, even in the central region, there is an increase in hot and cold pixels compared to the unaberrated case. These discrepancies are probably due to the different treatment of the edges of apertures and vanes in the optical system, causing small aliasing errors when not exact. However, they are so tiny that they can be safely neglected for the HST application.

In summary, we find that PAOS is a robust and reliable tool for simulating the propagation of optical wavefronts through complex optical systems, as shown by the excellent agreement with the results obtained with PROPER for HST in our benchmark tests.

Statement of need

Accurate assessment of the optical performance of advanced telescopes and imaging systems is essential to achieve an optimal balance between optical quality, system complexity, costs, and risks. Optical system design has witnessed significant advancements in recent years, necessitating efficient and reliable tools to simulate and optimize complex systems (Smith, 2000). Ray-tracing and Physical Optics Propagation (POP) are the two primary methods for modelling the propagation of electromagnetic fields through optical systems. Ray-tracing is often employed during the design phase due to its speed, flexibility, and efficiency in determining basic properties such as optical magnification, aberrations, and vignetting. POP provides a comprehensive understanding of beam propagation by directly calculating changes in the electromagnetic wavefront (Goodman, 2005). POP is particularly useful for predicting diffraction effects and modelling the propagation of coherently interfering optical wavefronts. Yet, it may require supplementary input from direct measurements or a ray-tracing model for comprehensive analysis including aberration variations, especially in the Fresnel approximation. Commercial tools like Zemax and Code V enable POP calculations, offering advanced capabilities in aberration reduction and optical system optimization. However, these programs often come with substantial costs and steep learning curves, which may not be justifiable for every application. Furthermore, accessibility to their source code is often limited or not available.

To address these limitations, we developed PAOS, a reliable, user-friendly, and open-source POP code that integrates an implementation of Fourier optics. PAOS employs the Fresnel approximation for efficient and accurate optical system simulations. By including a flexible configuration file and paraxial ray-tracing, PAOS seamlessly facilitates the study of various optical systems, including non-axial symmetric ones, as long as the Fresnel approximation remains valid. Initially developed to evaluate the optical performance of the Ariel Space Mission (Tinetti et al., 2021, 2018), PAOS has proven its value in assessing the impact of diffraction, aberrations, and related systematics on Ariel's optical performance. By offering a general-purpose tool capable of simulating the optical performance of diverse optical systems, PAOS fills a crucial gap in the field and makes advanced physical optics research more accessible.

Acknowledgements

This work was supported by the Italian Space Agency (ASI) with Ariel grant n. 2021.5.HH.0.

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