The naiveFC function package for Gretl

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Version 0.6

Changelog

- Version 0.6 (May, 2019)
 - Fully revamped framework heavily exploiting the idea of bundles
 - Fix a bug related to some seasonal frequencies
 - Add the seasonal median, seasonal naive with and without drift forecasting methods
 - Add computation of (asymptotic) forecast intervals
 - Add further sample datasets of different frequencies to the sample script
 - Make use of the user-contributed gretl package CvDataSplitter for computing rolling and recursive forecasts
 - Eventual missing values of the series passed to the naiveFC() function will be handled internally now
 - Improved plotting
 - Further minor changes
- Version 0.4 (Jan, 2019)
 - correct bug in smeanf() which caused referencing the forecast to the wrong minor period (quarter, month, day) under some circumstances
 - add option to compute median value for both meanf() and smeanf()
 - speed-up: loop in stack fc() replaced by matrix operation
 - speed-up: use aggregate() in get mean obsminor() and avoid a loop
 - use --contiguous instead of --missing option to ensure correct time-series pattern in case of missing values
- Version 0.3 (Oct, 2018)
 - add NaiveThroughTime() for computing rolling/ recursive forecasts
 - add nttplot() for computing plotting rolling/ recursive forecasts
- Version 0.11 (Oct, 2018)
 - initial public version
 - add AR(1)-based forecasts
 - minor changes and corrections
 - set minimum gretl version to 2018a
- Version 0.1 (Oct, 2018)
 - initial non-public version

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1 Introduction

The naiveFC package is a collection of gretl scripts for computing forecasts using simple forecasting methods. These may yield surprisingly good (in terms of forecast accuracy) results, and may serve as benchmarks for more sophisticated approaches. For details on the methods read Rob J Hyndman and George Athanasopoulos' book "Forecasting: Principles and Practice" and especially chapter 3.1. there (URL: https://otexts.org/fpp2/simple-methods.html). The functions implemented in naiveFC are inspired by Hyndman's well-known forecast package for R.

The package currently comprises the following features:

- Point estimates for 10 simple forecasting methods, namely the 'Average' (mean & median), 'Seasonal Average' (seasonal mean & median), 'Naive' (Random-Walk), the "Naive plus drift', the 'Seasonal Naive' both with and without drift and the AR(1) model, are implemented.
- Asymptotic forecast intervals for all methods are available.
- Easy computation of an average of forecasts by taking the mean point forecasts of all available simple forecast methods (depending on whether the underlying time-series has seasonality, or not).

- Computation of moving-window based sequences of forecasts using either the rolling or recursive method.
- Simple plotting of the h-step ahead forecast results as well as moving-window based sequences of forecasts.
- Easy GUI access through the gret menu "Model -> Time series -> naive forecast(s)".

2 Install and load the package

The naiveFC package is publicly available on the gretl server. The package must be downloaded once, and loaded into memory each time gretl is started.

```
# turn extra output off
set verbose off
# Download package (only once need)
pkg install naiveFC
# Load the package into memory
include naiveFC.gfn
# Get the help file
help naiveFC
```

3 Example

For illustration we use the AWM-macroeconomic data set comprising various series observed at a quarterly frequency over 28 years. The data set ends in 1998Q4. The objective is to forecast the output gap (series named YGA). Note, the last valid observation for YGA is 1998Q2. Hence, the 1-step ahead forecast will be computed for period 1998Q3.

The sample script opens the data set, computes and plots some forecasts. Lastly, an average of forecasts is computed which is an average of the (currently) nine forecasting methods implemented (for details see below).

```
open AWM.gdt --quiet
series y = YGA
                         # output gap
                         # set max. forecast horizon
scalar h = 11
# Mean forecast
bundle b = null
                                 # initialize an empty bundle
b = naiveFC(y, "meanFC")
                                 # compute forecasts
naivePlot(&b)
                                 # plot forecast values
eval b.fc
                                 # print matrix hodling forecast values
# RW with drift
bundle b = naiveFC(y, "rwdFC")
naivePlot(&b)
eval b.fc
# Average of Forecasts
bundle b = null
b = naiveFC(y, "avgFC")
naivePlot(&b)
eval b.fc
                                 # 1st col: point forecast, 2nd col: std. deviation
```

The estimated h-step ahead average of forecasts, named 'Average-FC', and the cross-sectional standard deviation ('SD') as well as the point forecasts of the separate methods are reported in the output below for the first three horizons (only 2 digits are shown here):

```
Naive Forecasting Method
Forecasting method:
Start valid data set:
                               1971:4
End valid data set:
                               1998:2
Number of observations:
                               106
Forecast horizon:
First observation forecasted:
                               1998:3
**************
Average - FC SD Mean Median RW RW+Drift AR(1) AR(1)+Trend Seas-Mean Seas-Median Seas - Naive
1998:07 0.99
              0.002
                      0.99
                             0.99
                                    0.99
                                          0.99
                                                 0.99
                                                        0.99
                                                               0.99 0.99
                                                                          0.98
1998:10
        0.99
                      0.99
                             0.99
                                    0.99
                                                 0.99
                                                        0.98
                                                               0.99
                                                                     0.99
                                                                          0.98
              0.002
                                          0.99
1999:01 0.99
              0.001
                      0.99
                             0.99
                                    0.99
                                          0.99
                                                 0.99
                                                        0.98
                                                               0.99
                                                                    0.99
                                                                          0.99
```

The private NaiveThroughTime() function implements the easy computation of either (i) "rolling" (fixed window length) or (ii) "recursive" (expanding window length) forecasts for a specific naive forecast type. The user just needs to set the string variable type_roll which actually triggers the NaiveThroughTime() function. The following sample script computes the 1- to 10-steps ahead random-walk plus drift (rwdFC) forecasts based on a rolling window of length wsize=100.

Given the length of the current data set and the chosen window length, eight training sets (moving window samples) on which separate forecasts are made, are internally defined. For each of these eight sets, a 10-steps ahead forecast is computed resulting in a sequence of h-step ahead forecasts which are stored in matrix fc in bundle b. The first 1-step ahead forecast for series y is made conditional on information up to 1996Q3 for period 1996Q4 and is 0.982, and so on (see output below).

The public naivePlot() function grabs all relevant information from bundle b, and allows for an easy illustration of the moving forecast exercise, as depicted below in Plot 1. The plot nicely illustrates the 10-step ahead forecasts for each of the eight training sets.

```
Naive Forecasting Method
Forecasting method:
                                        rwdFC
Start valid data set:
                                        1971:4
End valid data set:
                                        1998:2
Number of observations:
                                        106
Forecast horizon:
                                        10
Moving window length:
                                        100
Number of rolling forecasts:
First observation forecasted (h=1): 1996:4
         h = 1
                h = 2
                         h=3
                               h = 4
                                        h=5
                                               h=6
                                                        h=7
                                                               h = 8
                                                                        h = 9
                                                                              h = 10
1996:3
       0.982 0.981
                       0.981
                              0.981
                                      0.981
                                              0.981
                                                      0.981
                                                              0.980
                                                                     0.980
                                                                             0.980
        0.980 0.980
                                                                             0.977
1996:4
                       0.979
                               0.979
                                      0.979
                                              0.978
                                                      0.971
                                                              0.978
                                                                     0.978
1997:1
        0.978 0.978
                       0.977
                               0.977
                                      0.977
                                              0.977
                                                      0.976
                                                              0.976
                                                                     0.976
                                                                             0.976
```

4 Forecasting methods

A brief description of the implemented forecasting methods follows in this section. The user calls the respective method, by passing a string variable with the respective name, e.g. string which="meanFC" to the main function naiveFC() as the 2nd function argument (see subsection 5.1 for details).

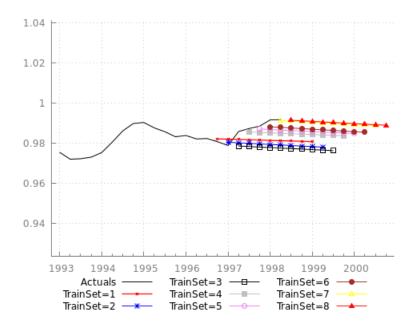


Figure 1: Rolling-window 10-steps ahead random-walk plus drift forecasts.

4.1 meanFC

Forecasts of all future values are equal to the "mean" of the historical data. The h-step ahead forecast conditional on using data up to period T is computed by the historical mean of the time-series:

$$\hat{y}_{T+h|T} = \frac{1}{T} \sum_{i=1}^{T} y_i$$

Estimation is done by regressing an intercept-only model using OLS.

4.2 medianFC

This method works similar as the meanFC approach, but instead forecasts of all future values are equal to the "median" of the historical data. Estimation is done by regressing an intercept-only model using gretl built-in quantreg command for quantile regression estimation.

4.3 smeanFC

Forecasts of all future values are equal to the "mean" of the historical data for each specific seasonality (e.g. daily, monthly, or quarterly). For example, with monthly data, the forecast for all future for February is equal to mean value of all past February values. With quarterly data, the forecast of all future 2nd quarter values is equal to mean of all past Q2 values. Similar rules apply for other months and quarters, and for other seasonal periods. For daily frequency data one can either have a 7d (standard week) or 5d (business week) season.

Estimation is done by adding dummy variables indicating the different seasons to a linear regression where coefficient are estimated by means of OLS.

4.4 smedianFC

Works as the "smeanFC" method but computes the seasonal median instead of the mean statistics. Estimation is done by adding dummy variables indicating the different seasons to a linear regression where coefficient are estimated by means the least absolute deviation estimator using the quantreg command.

4.5 ar1FC

Forecasts are based on an AR(1) model including an intercept where parameters are estimated by standard OLS. Out-of-sample forecasts are recursively (also known as the iterated forecasting method) constructed. The 1-step ahead forecast is based on realized values from the previous period. The h-step ahead (for h > 1) forecast is based on the forecast value from horizon h - 1, respectively. We rely on gretl's built-in ols and fcast commands for estimating the parameters of the model and computing the dynamic forecast, respectively, based on the following time-series model:

$$y_t = \beta_0 + \beta_1 y_{t-1} + u_t \quad u_t \sim iid(0, \sigma^2)$$

4.6 ar1trendFC

Works similar as the ar1FC forecasting method but adds a linear trend to the specification. We rely on gretl's built-in ols and fcast commands for estimating the parameters of the model and computing the dynamic forecast, respectively, based on the following time-series model:

$$y_t = \beta_0 + \beta_1 y_{t-1} + \beta_2 T + u_t \quad u_t \sim iid(0, \sigma^2)$$

4.7 rwFC

The random-walk forecast for period T + h equals the value of the last valid observation:

$$\hat{y}_{T+h|T} = y_T$$

Estimation is done by fitting an ARIMA(0,1,0) model without intercept using gretl's arima command.

4.8 rwdFC

A variation of the rwFC method is to allow the forecasts to increase or decrease over time, where the amount of change over time (called the drift) is set to be the average change seen in the historical data. Thus the forecast for period T + h is given by:

$$\hat{y}_{T+h|T} = y_T + h\left(\frac{y_T - y_1}{T - 1}\right)$$

Estimation is done by fitting an ARIMA(0,1,0) model including an intercept using gretl's arima command.

4.9 snaiveFC

This is a similar method as the random-walk forecast but especially useful for seasonal data. Forecasts are based on an ARIMA(0,0,0)(0,1,0)[m] model where m is the seasonal period. We rely on gretl's built-in arima and fcast commands for computation.

4.10 avgFC

This is meant to be a convenience function. This function computes the mean and cross-sectional (across forecast methods) standard deviation of the respective point forecasts at each forecast horizon using all k forecasting methods available. For annual data the (i) mean-forecast (meanFC), the (ii) median-forecast (medianFC), (iii) random-walk without drift (rwFC), (iv) random-walk with drift (rwdFC), (v) the AR(1)-forecast without linear trend (ar1FC) and (vi) with linear trend (ar1trendFC) will be computed. For data with seasonality (e.g., monthly, quarterly etc.) we also add the (vii) the seasonal-mean (smeanFC), (viii) the seasonal-median (smedianFC) and the (ix) seasonal-naive forecast without drift (snaiveFC) and (x) with drift (snaivedriftFC) to the collection of forecasts.

The resulting matrix fc stored in the bundle will be of dimension $h \times (2 + k)$ comprising the h-step ahead combined cross-sectional mean forecasts in the 1st column and the cross-sectional standard-deviations across all (k) separate forecasting methods.

Note, the avgFC method will not be computed when combined with either the rolling or recursive moving-window method.

5 Public functions and parameter values

The following public functions are intended to be used for scripting purposes only. Hence, calling these functions through the GUI will not return any printout. Instead, the user can access the function avgfc_gui() through the gretl GUI menu "Model -> Time series -> naive forecast(s)" which allows steering key functions by *point and click*.

5.1 The naiveFC() function

The naiveFC() function marks the main function. The function arguments are:

```
naiveFc(const series y, string which "Select forecasting method", bundle opts[null] "Bundle incl. optional parameters"))
```

Return type: bundle

The user must pass a time-series (potentially with missing values) and a string variable selecting one of the supported forecasting methods. Optionally, the user pass another bundle element including further parameters which are described below. In case the function is successfully called, a bundle including various items will be returned to the user.

The additional parameters which can be passed by means of the opts bundle to naiveFC() are: In case the user sets type_roll to either "rolling" or "recursive", the internal private function NaiveThroughTime() is called. This function computes point forecasts for some method either in (i)

Parameter	Data type	Description	Default value
h	int	Forecast horizon: Must be > 0	10
type_roll	str	Moving-window type: "static", "rolling", "recursive"	"static"
wsize	int	Length of the moving window in case type_roll	25% of the total sample
		takes either "rolling" or "recursive".	of series y
level	scalar	Probability level for forecast interval.	0.9
verbose	bool	Print details or not: either 0 or 1	1 (True)
preobs_fc	int	No. of pre-forecast observations to plot when	25% of the total sample
		calling the naivePlot() function	of series y
title	str	Title string for the plot when calling naivePlot()	empty
ylab	str	String of the y-label of the plot	empty
xlab	str	String of the x-label of the plot	empty
filename	str	String of the path+filename+file-extension	"display"
		(either png, pdf or eps) for storing the plot	

Table 1: Parameters which can be set through the optional bundle opts.

a rolling or (ii) a recursive manner. For details see the user-contributed package CvDataSplitter written by this author (URL: http://ricardo.ecn.wfu.edu/gretl/cgi-bin/current_fnfiles/CvDataSplitter.gfn). The bundle returned by naiveFC() includes the following items:

5.2 The naivePlot() function

The naivePlot() function is a convenience function for plotting the results initially compiled by having successfully called naiveFC(). This user function accepts a bundle argument in pointer form as returned by naiveFC():

naivePlot(bundle *self "F	'Bundle returned from naiveFC()")
---------------------------	-----------------------------------

Return type: void

Item	Data type	Description
T_all	int	No. of observation of series y originally
		passed to naiveFC() by the user.
T	T int No. of effective observations after omitting e	
		missing values in series y .
t1_label	str	Date string of the 1st valid obs. of the training set.
t2_label	str	Date string of the last valid obs. of the (last) training set.
fc	matrix	If type_roll="static": $h \times m$ matrix holding h -step
		ahead forecasts made by m methods.
		For type_roll="rolling/ recursive": $tr \times h$ matrix holding
		h-step ahead forecasts for tr training sets using a single method.
h	int	No. of maximum forecast horizon
level	scalar	Probability level for forecast interval.
wsize	int	Length of the moving-window scheme.
type_roll	str	String of the chosen moving-window scheme
verbose	bool	Flag for printing details or not
w_drift	bool	Flag whether a drift-term is incl. or not.
w_trend	bool	Flag whether a linear trend is incl. or nor
is_seas	bool	Flag whether the data set has seasonal frequency or not
which	str	String of the selected forecasting method
fcperiods	string array	Array of date strings referring the last training date on which
		each of the moving-window forecasts is based on.

Table 2: Parameters which are returned by the function naiveFC().