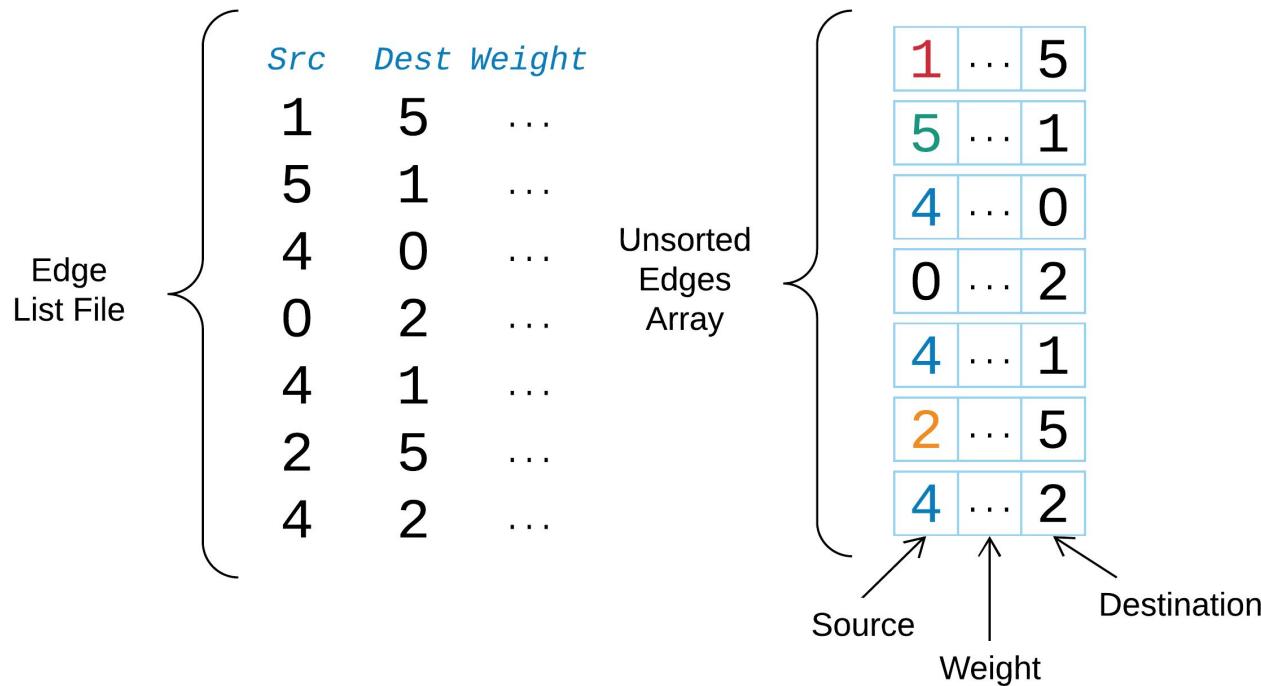

End-to-End Graph Processing

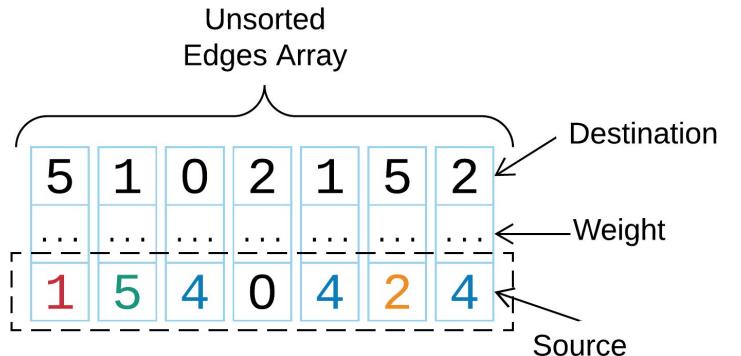
Algorithms

Presented by : Abdullah Mughrabi

Recap

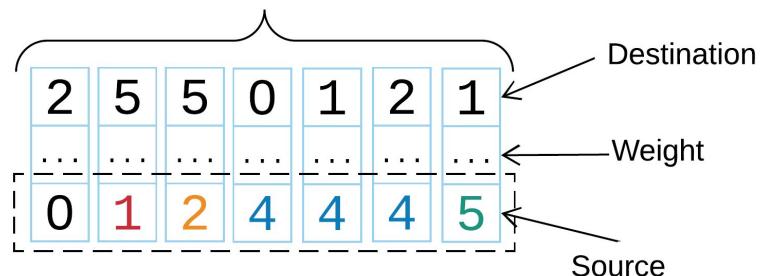


Recap



Radix/Count Sort

Sorted Edges Array



Sorting in linear time

Counting-sort : No comparison between elements.

- ***Input***: $A[1..n]$, where $A[j] \in \{1, 2, \dots, k\}$.
- ***Output***: $B[1..n]$, sorted.
- ***Auxiliary storage***: $C[1..k]$, counting array.

Counting-sort (Serial)

```
for i ← 0 to (k-1)
    do C[i] ← 0

for j ← 0 to (n-1)
    do C[A[j]] ← C[A[j]]+1

for i ← 1 to (k-1)
    do C[i] ← C[i]+C[i-1]

for j ← (n-1) downto 0
    do B[C[A[j]]-1] ← A[j]
        C[A[j]] ← C[A[j]]-1
```

Counting-sort (Serial) - Example

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

--	--	--	--	--	--

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

--	--	--	--	--	--	--

Counting-sort (Serial) - Loop 1

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

0	0	0	0	0	0
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

--	--	--	--	--	--	--

Counting-sort (Serial) - Loop 2

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

0	0	0	0	0	0	0
---	---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

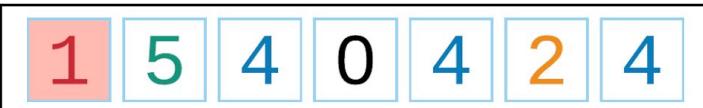
B

--	--	--	--	--	--	--

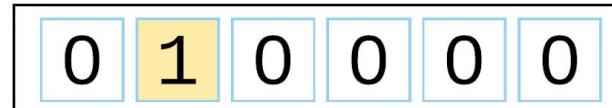
Counting-sort (Serial) - Loop 2



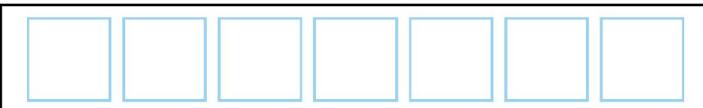
A



C



B



Counting-sort (Serial) - Loop 2

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

0	1	0	0	0	1
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

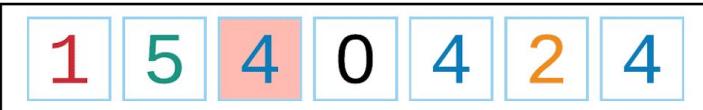
B

--	--	--	--	--	--	--

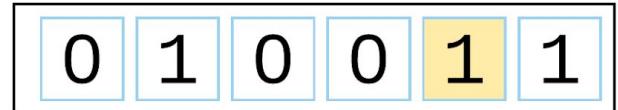
Counting-sort (Serial) - Loop 2



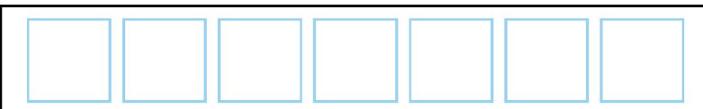
A



C



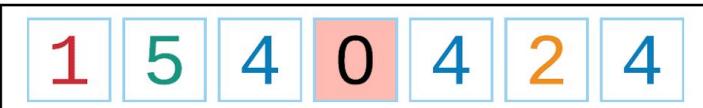
B



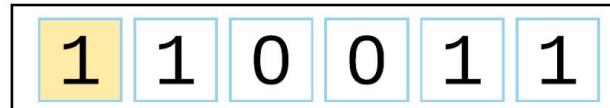
Counting-sort (Serial) - Loop 2



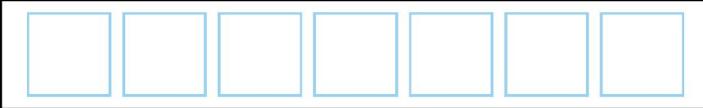
A



C



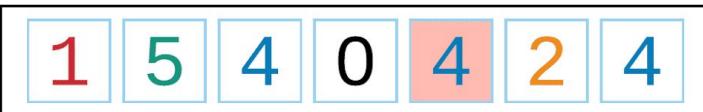
B



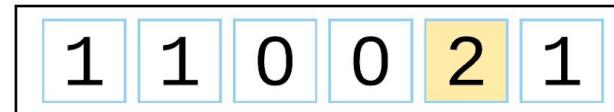
Counting-sort (Serial) - Loop 2



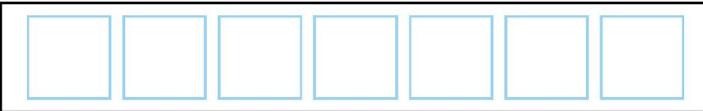
A



C



B



Counting-sort (Serial) - Loop 2

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

1	1	1	0	2	1
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

--	--	--	--	--	--	--

Counting-sort (Serial) - Loop 2

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

1	1	1	0	3	1
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

--	--	--	--	--	--	--

Counting-sort (Serial) - Loop 3

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

1	1	1	0	3	1
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

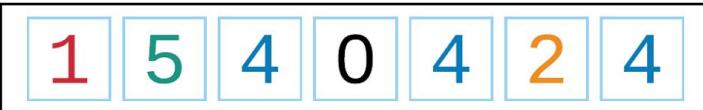
B

--	--	--	--	--	--	--

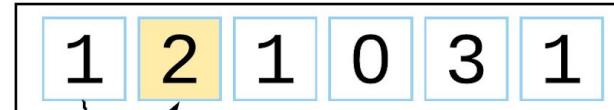
Counting-sort (Serial) - Loop 3



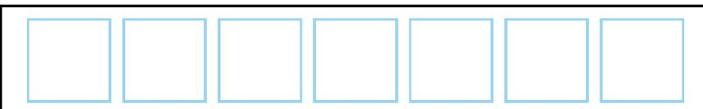
A



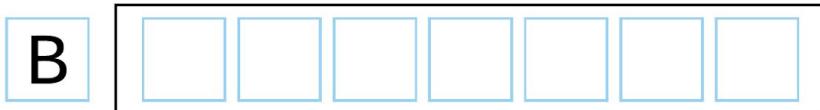
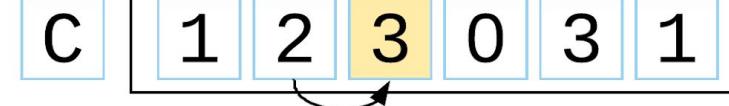
C



B



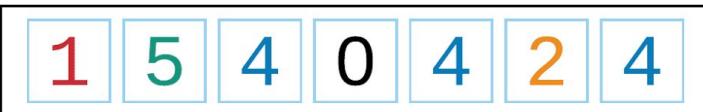
Counting-sort (Serial) - Loop 3



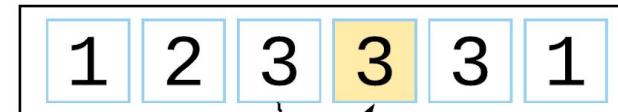
Counting-sort (Serial) - Loop 3



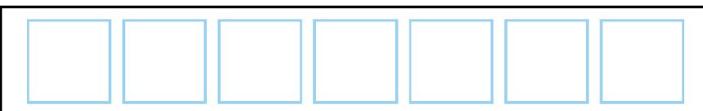
A



C



B



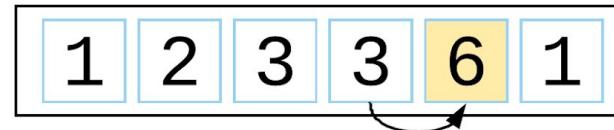
Counting-sort (Serial) - Loop 3



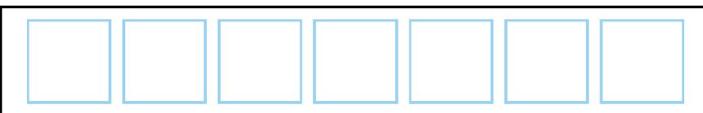
A



C



B



Counting-sort (Serial) - Loop 3



Counting-sort (Serial) - Loop 4

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

C

1	2	3	3	6	7
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

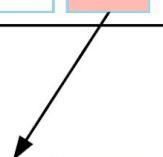
--	--	--	--	--	--	--

Counting-sort (Serial) - Loop 4

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---



0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

					4	
--	--	--	--	--	---	--

0	1	2	3	4	5
---	---	---	---	---	---

C

1	2	3	3	5	7
---	---	---	---	---	---

Counting-sort (Serial) - Loop 4

0	1	2	3	4	5	6
---	---	---	---	---	---	---

A

1	5	4	0	4	2	4
---	---	---	---	---	---	---

0	1	2	3	4	5
---	---	---	---	---	---

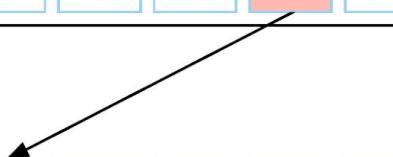
C

1	2	2	3	5	7
---	---	---	---	---	---

0	1	2	3	4	5	6
---	---	---	---	---	---	---

B

		2			4	
--	--	---	--	--	---	--



Counting-sort (Serial) - Loop 4



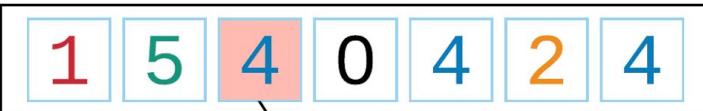
Counting-sort (Serial) - Loop 4



Counting-sort (Serial) - Loop 4



A



B



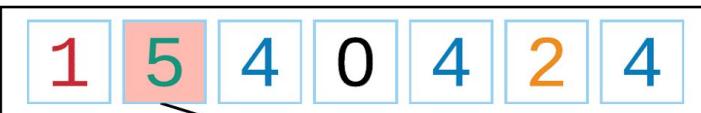
C



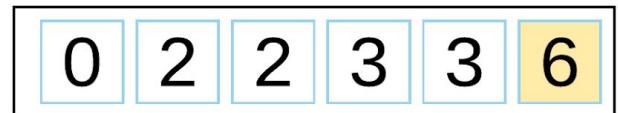
Counting-sort (Serial) - Loop 4



A



C



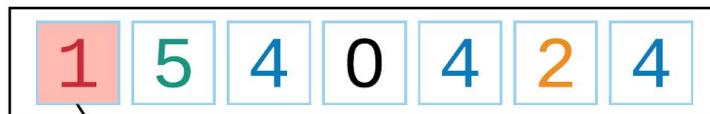
B



Counting-sort (Serial) - Loop 4



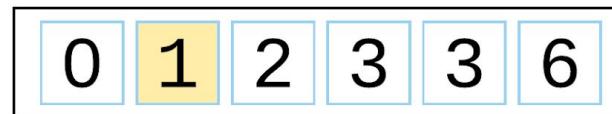
A



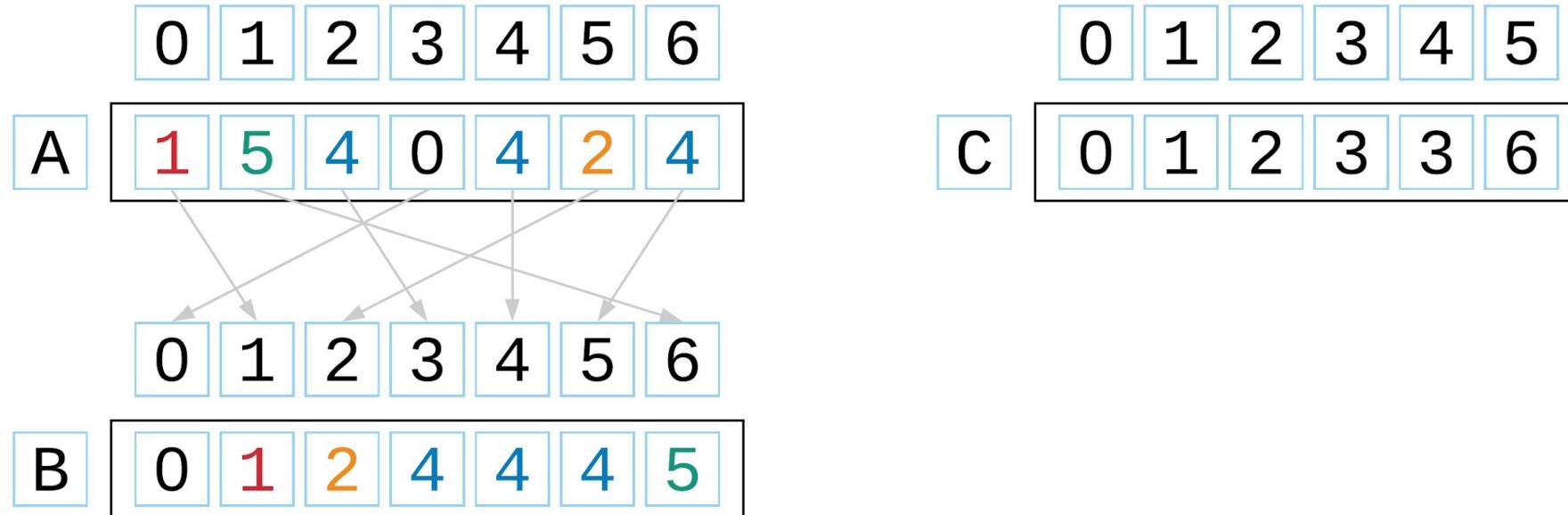
B



C



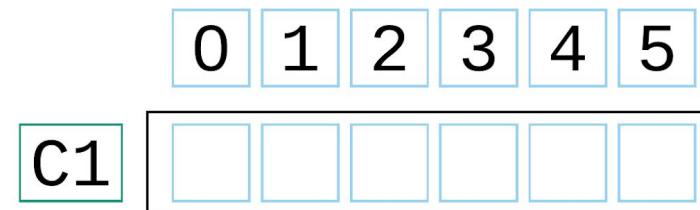
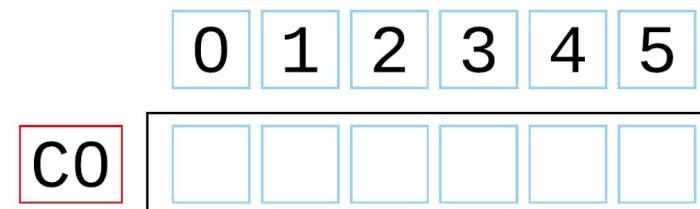
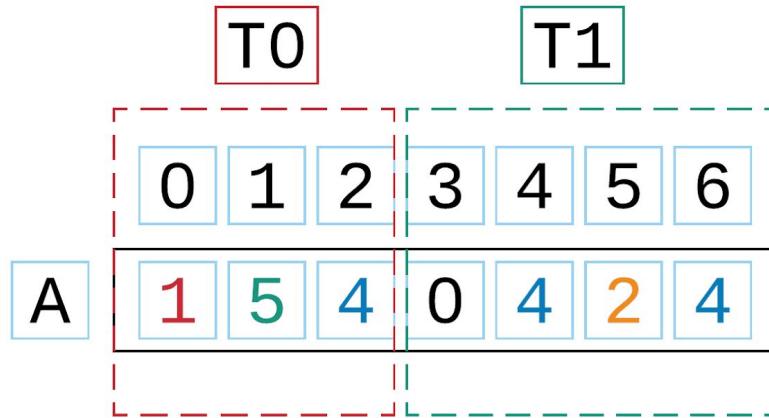
Counting-sort (Serial) - Loop 4



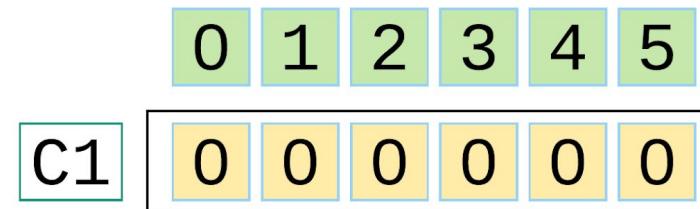
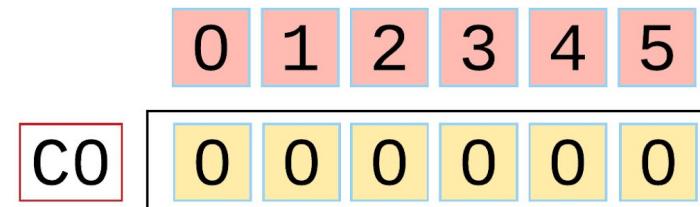
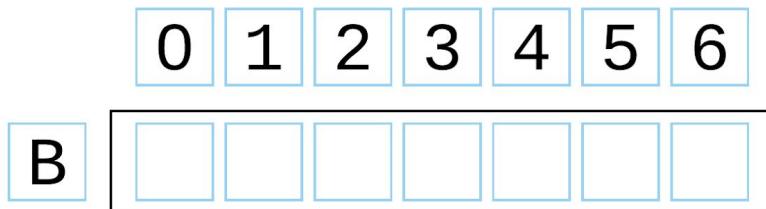
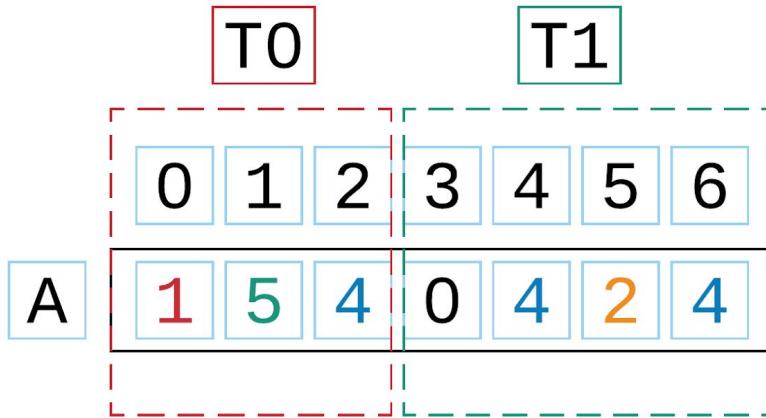
Counting-sort (Parallel)

```
base←0
Parallel for i←0 to (k-1)
  do C[tid][i]←0
Parallel for j←tid_start to tid_end
  do C[tid][A[j]]←C[tid][A[j]]+1
Parallel barrier
for i←0 to (k-1)
  for tid←0 to (t-1)
    do base←base + C[tid][i]
    C[tid][i]←base
Parallel barrier
Parallel for j←(tid_end-1) downto tid_start
  do B[C[tid][A[j]]-1] ←A[j]
  C[tid][A[j]]←C[tid][A[j]]-1
```

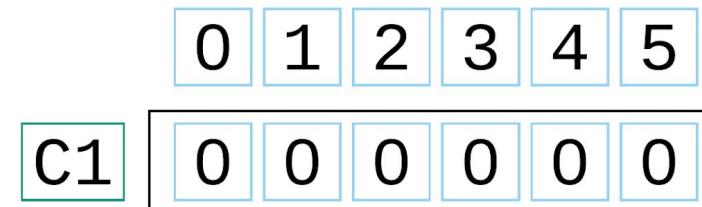
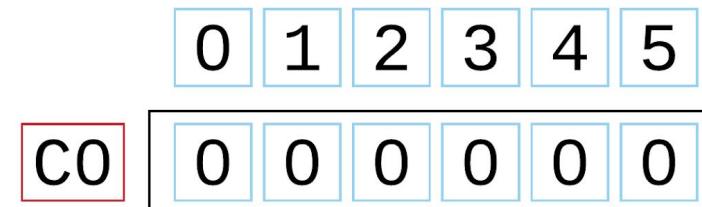
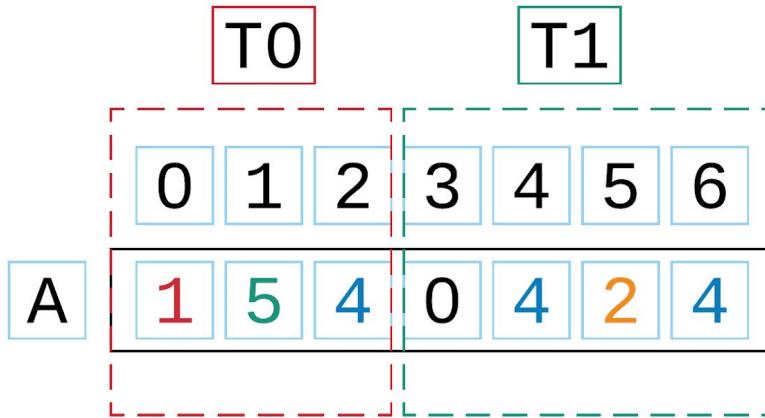
Counting-sort (Parallel)



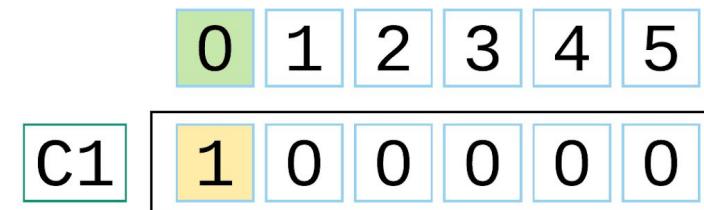
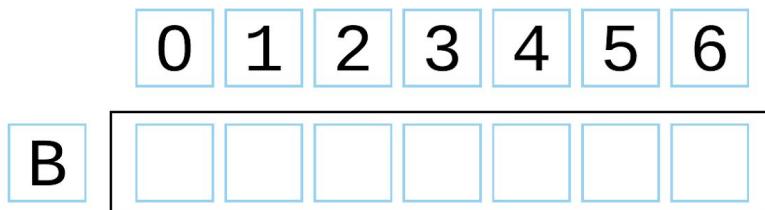
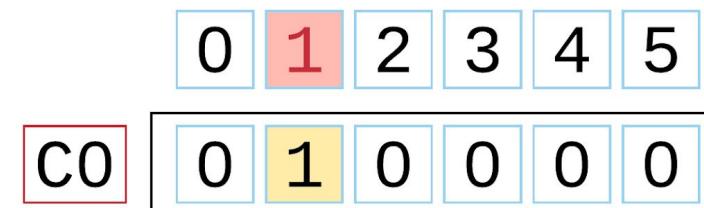
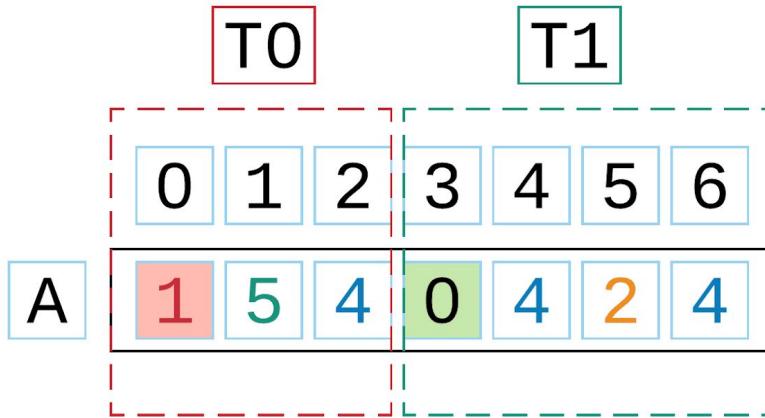
Counting-sort (Parallel) - Loop 1



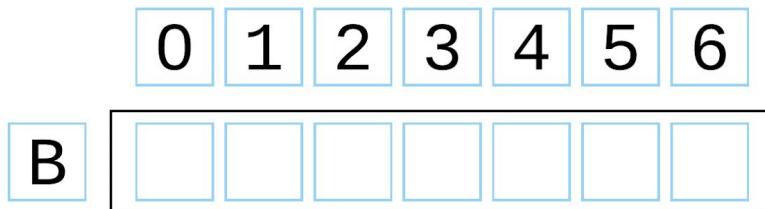
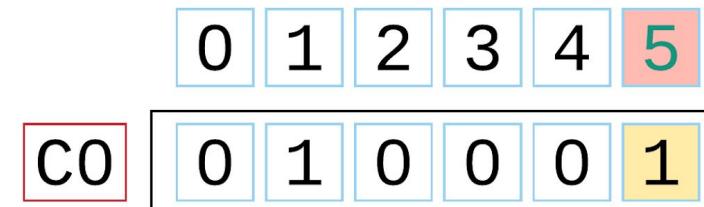
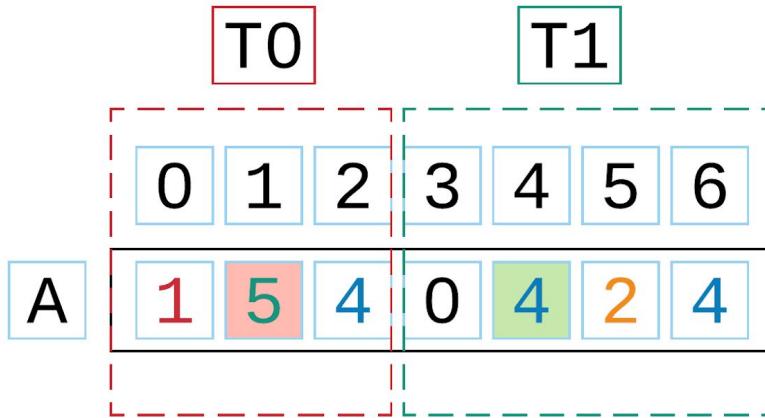
Counting-sort (Parallel) - Loop 2



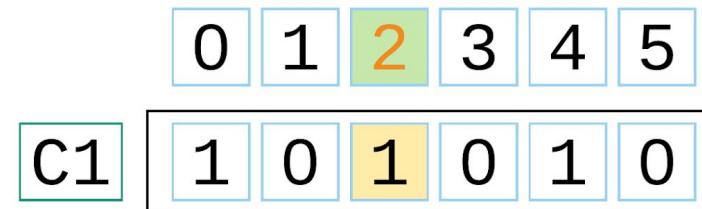
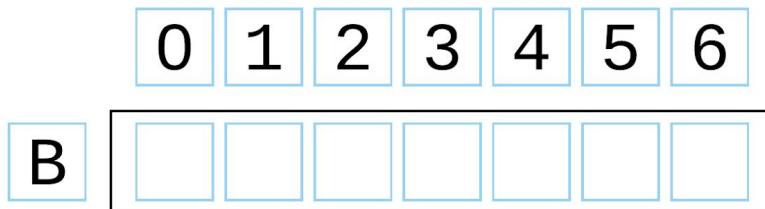
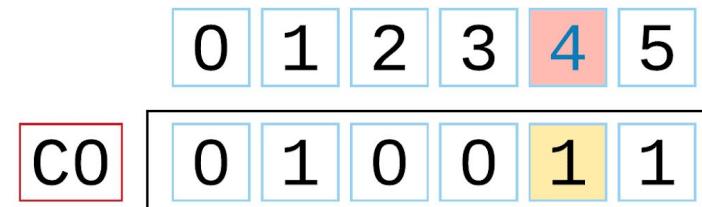
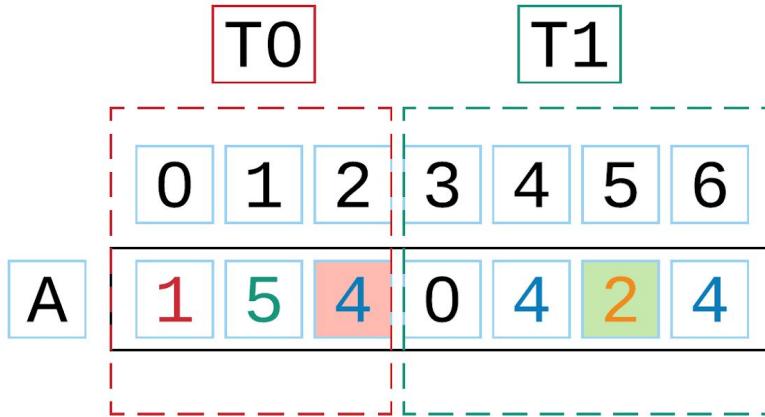
Counting-sort (Parallel) - Loop 2



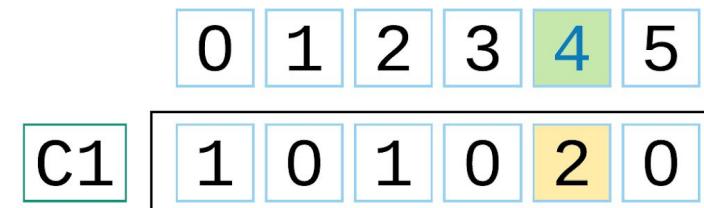
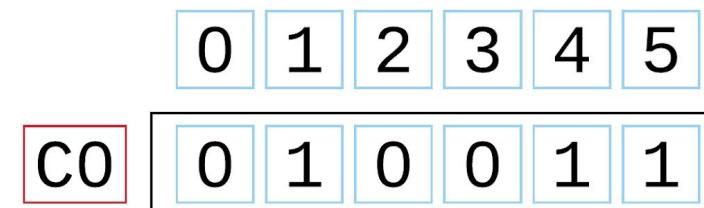
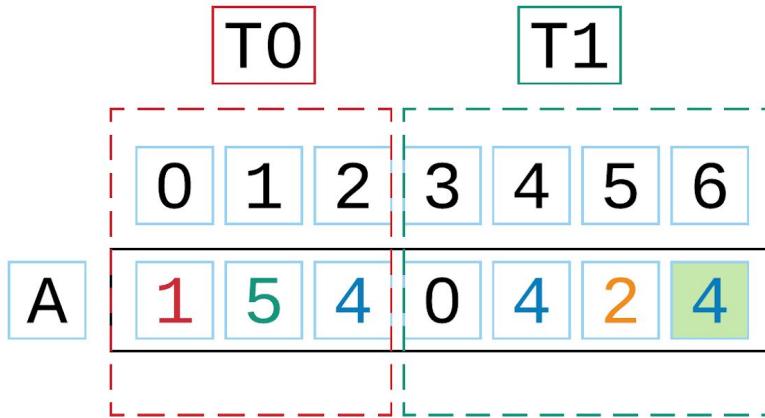
Counting-sort (Parallel) - Loop 2



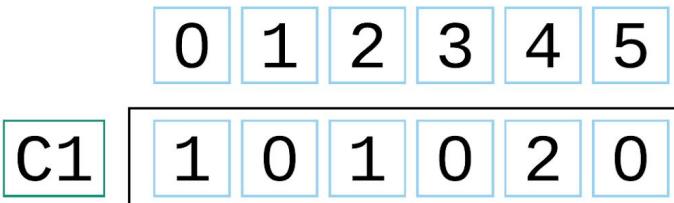
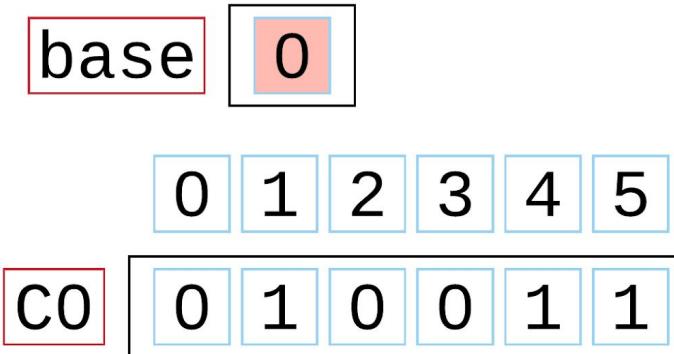
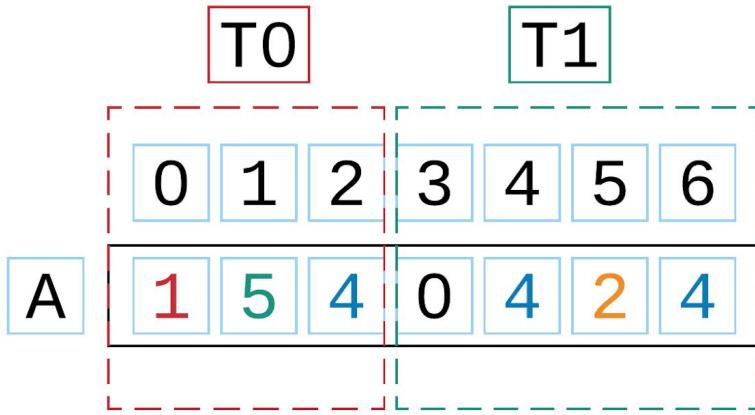
Counting-sort (Parallel) - Loop 2



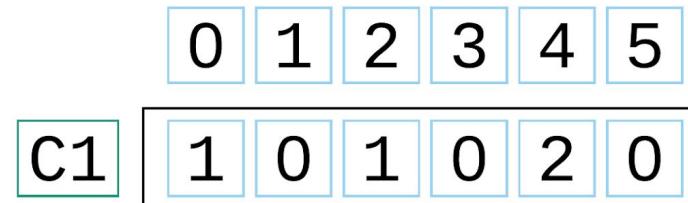
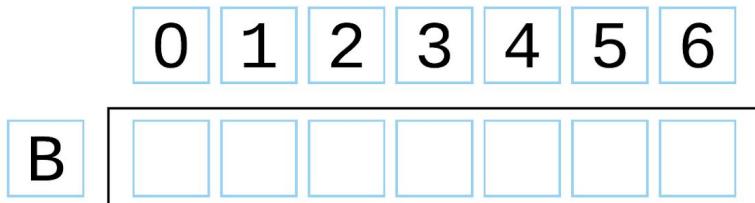
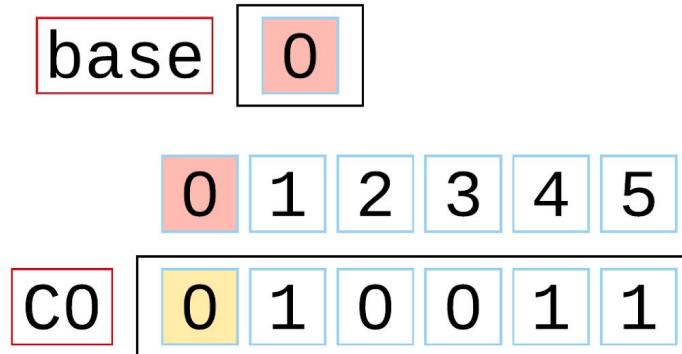
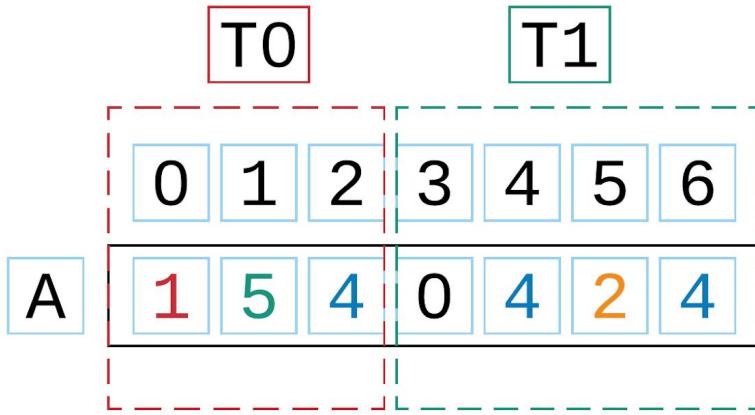
Counting-sort (Parallel) - Loop 2



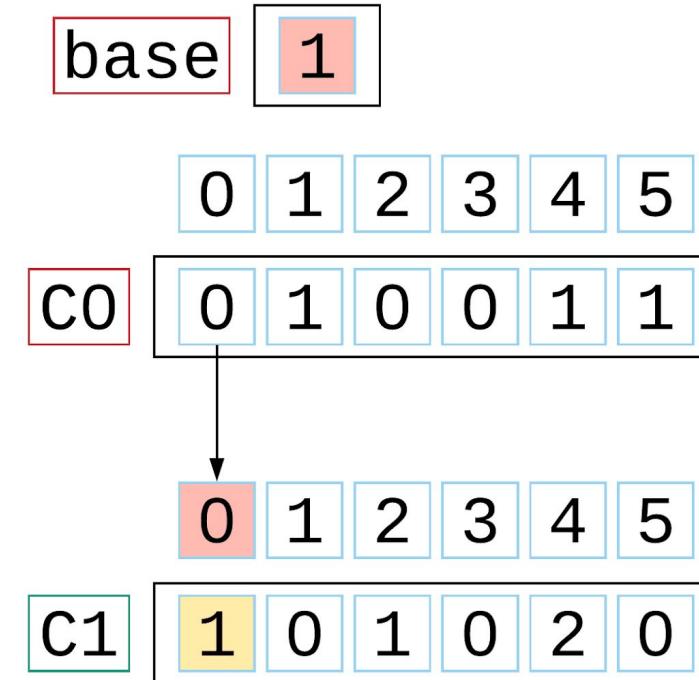
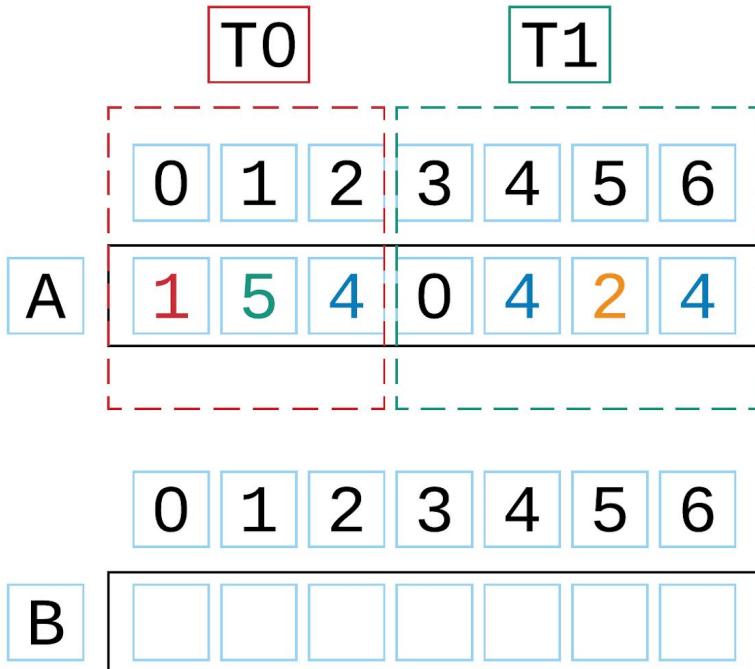
Counting-sort (Parallel) - Loop 3



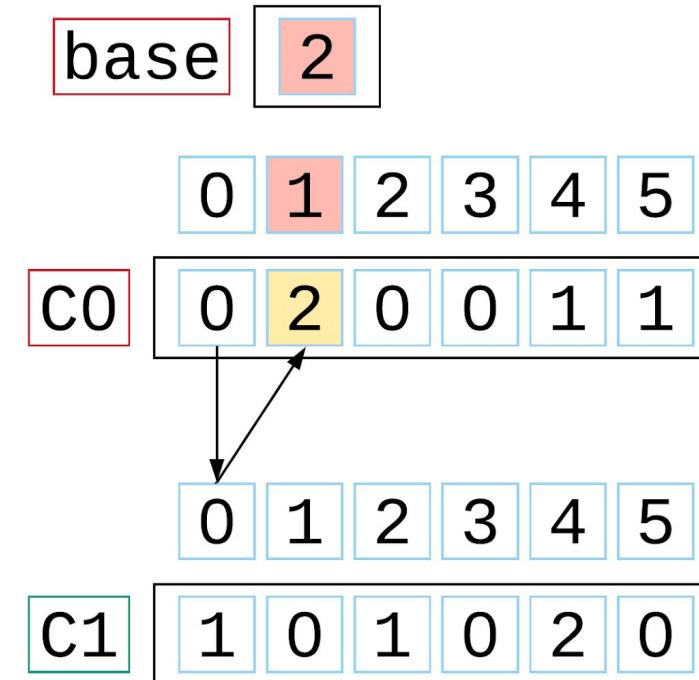
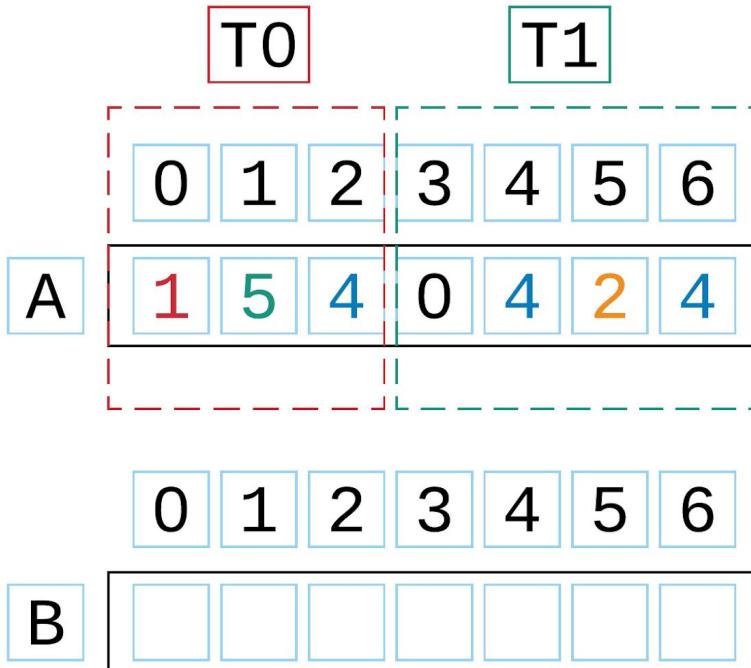
Counting-sort (Parallel) - Loop 3



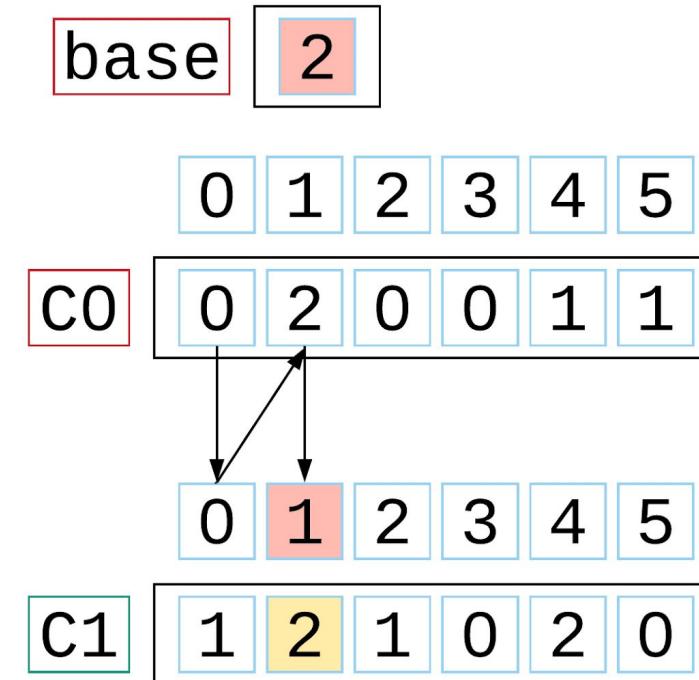
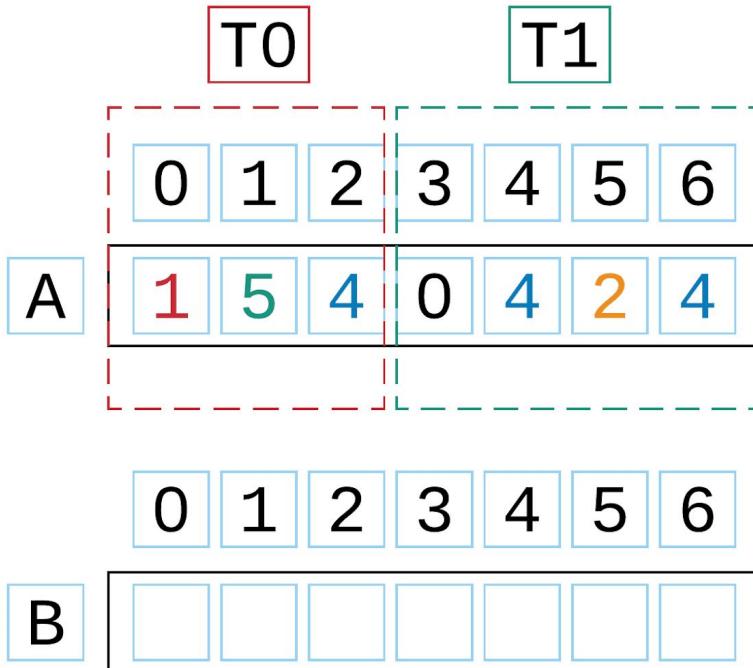
Counting-sort (Parallel) - Loop 3



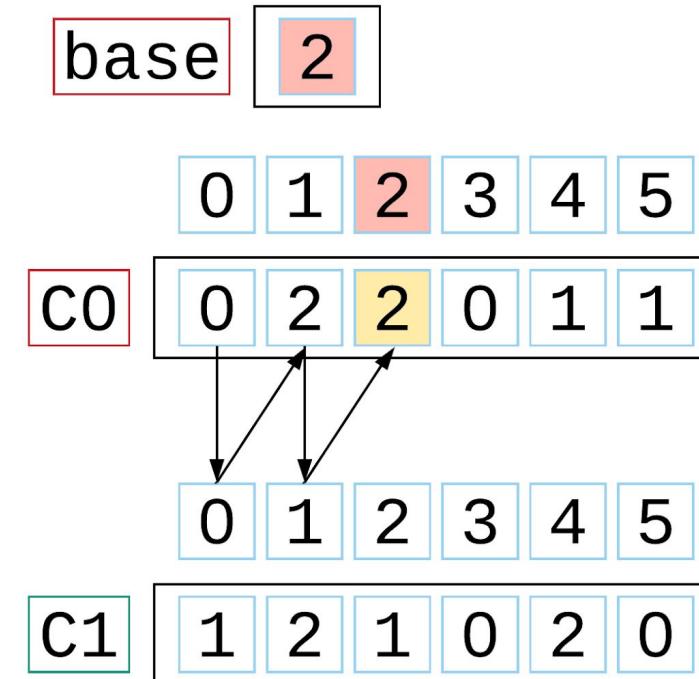
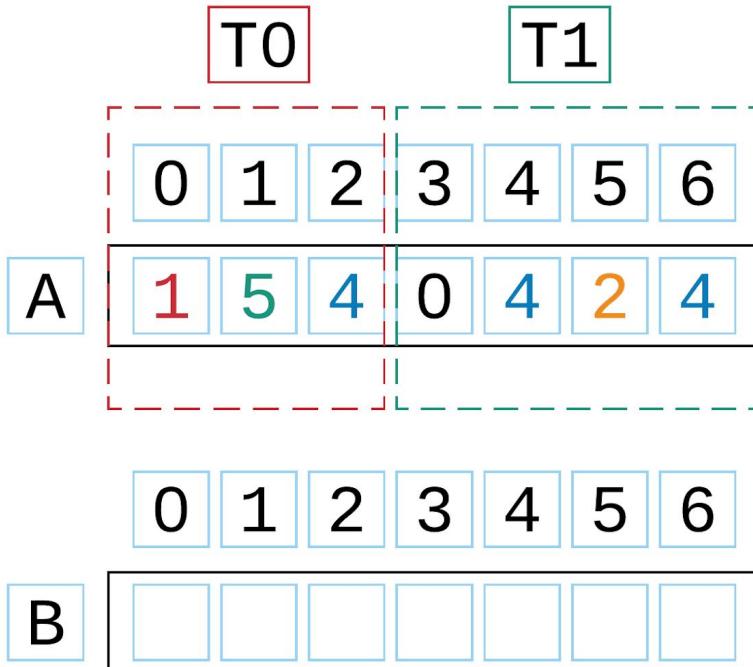
Counting-sort (Parallel) - Loop 3



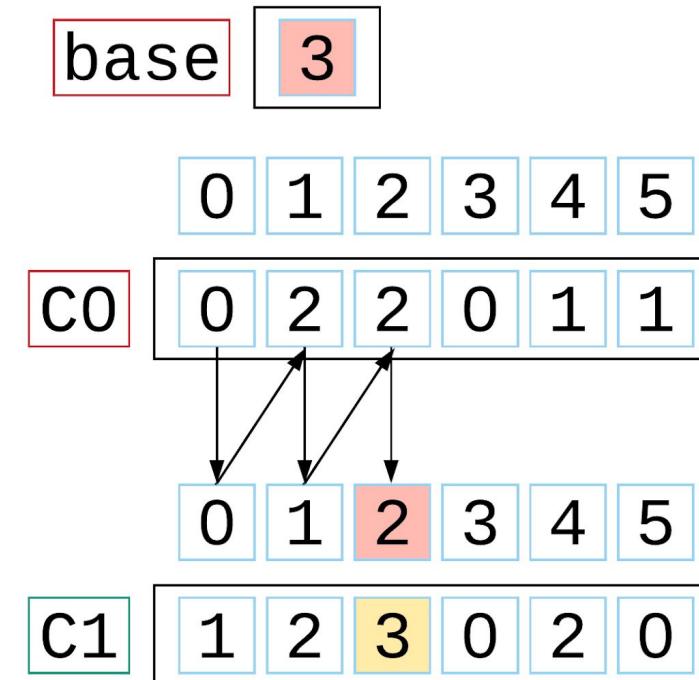
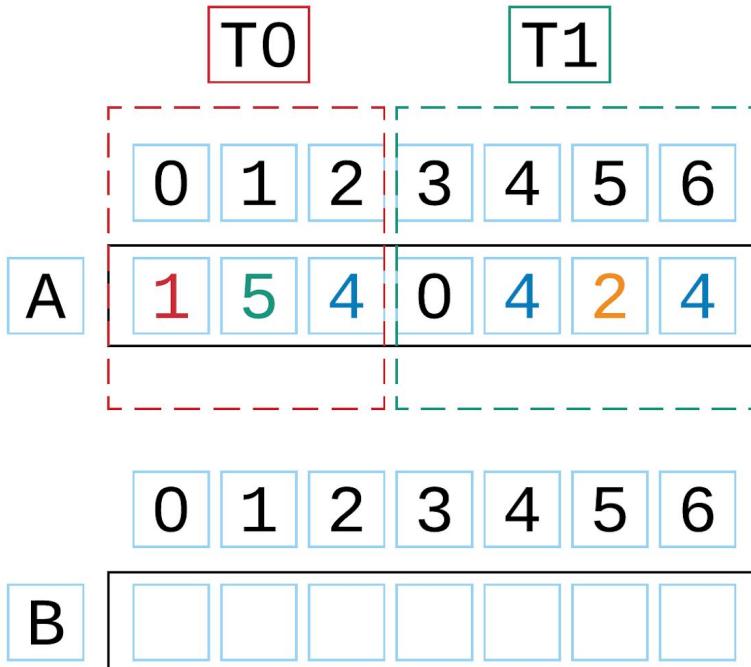
Counting-sort (Parallel) - Loop 3



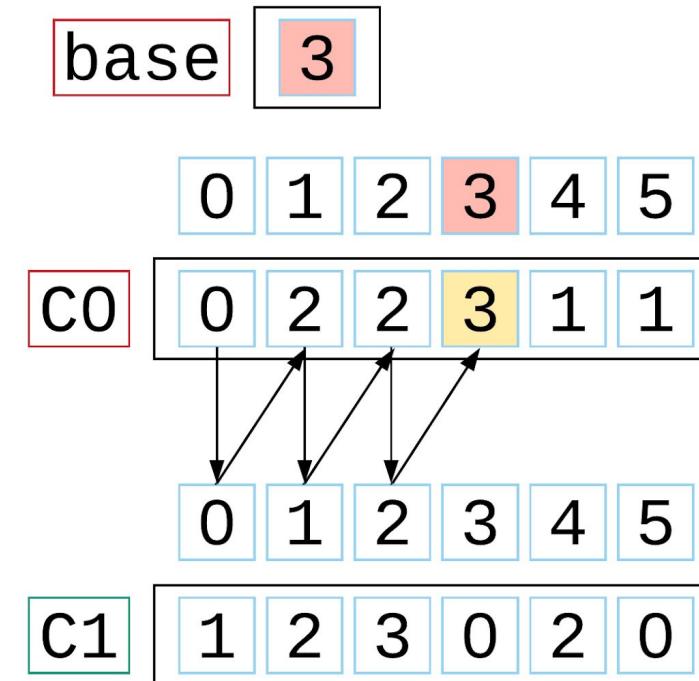
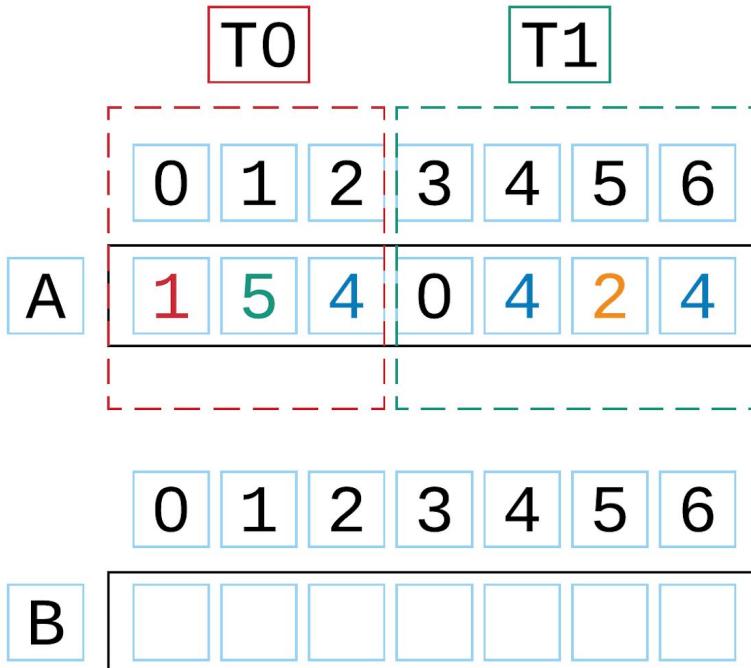
Counting-sort (Parallel) - Loop 3



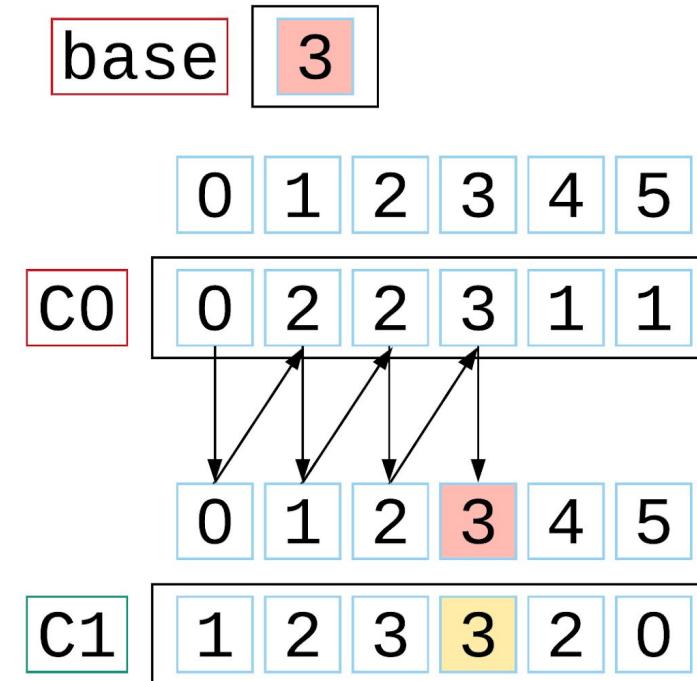
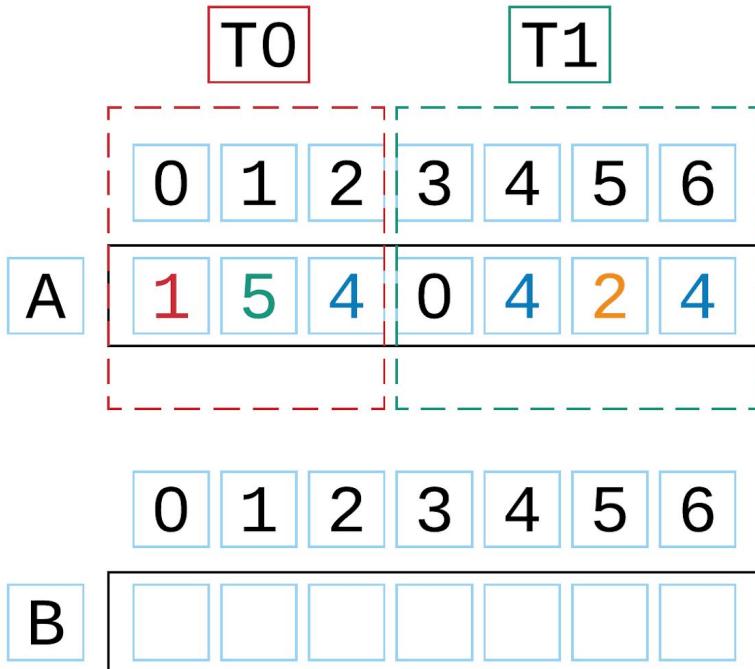
Counting-sort (Parallel) - Loop 3



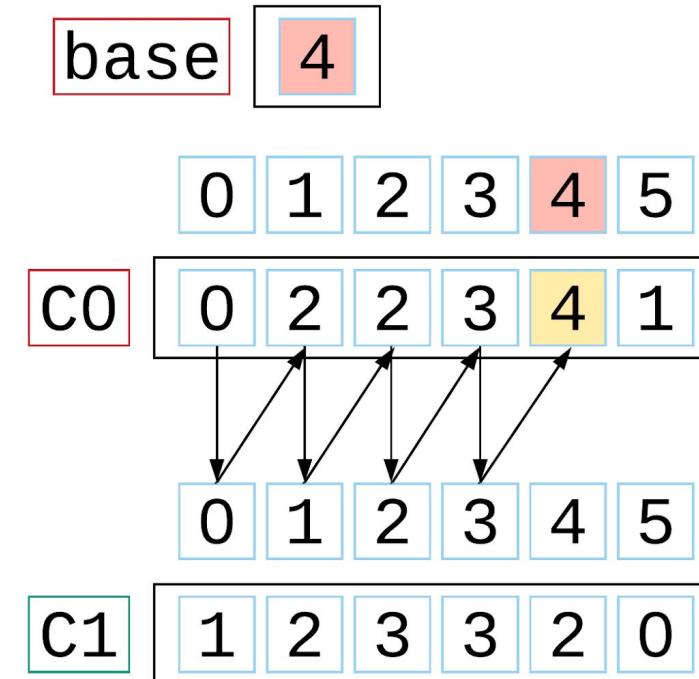
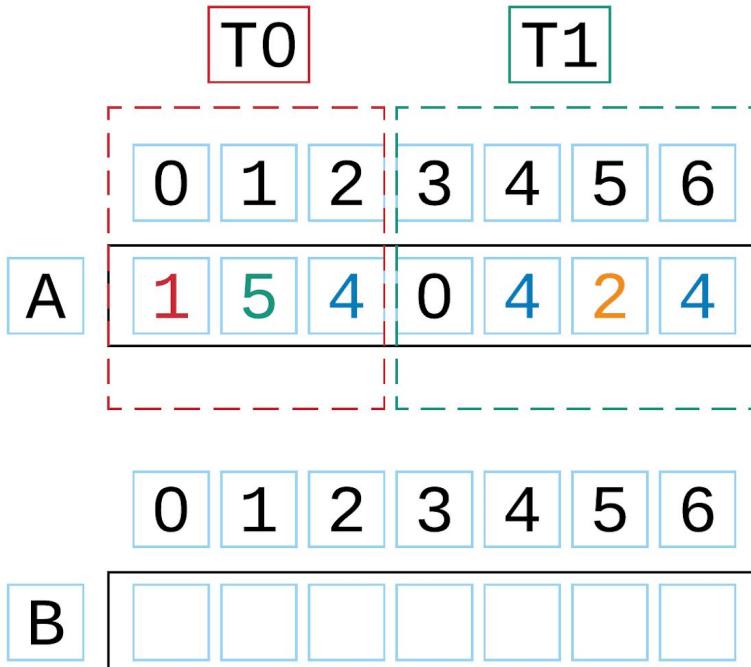
Counting-sort (Parallel) - Loop 3



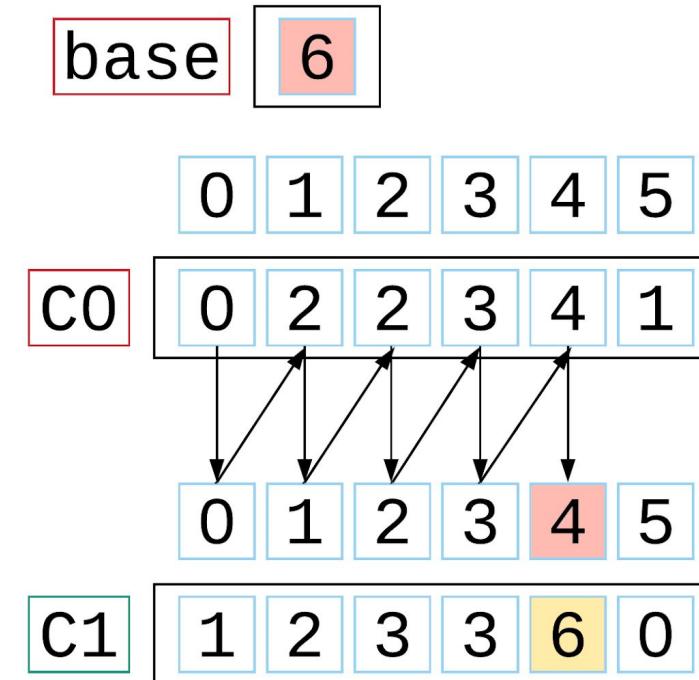
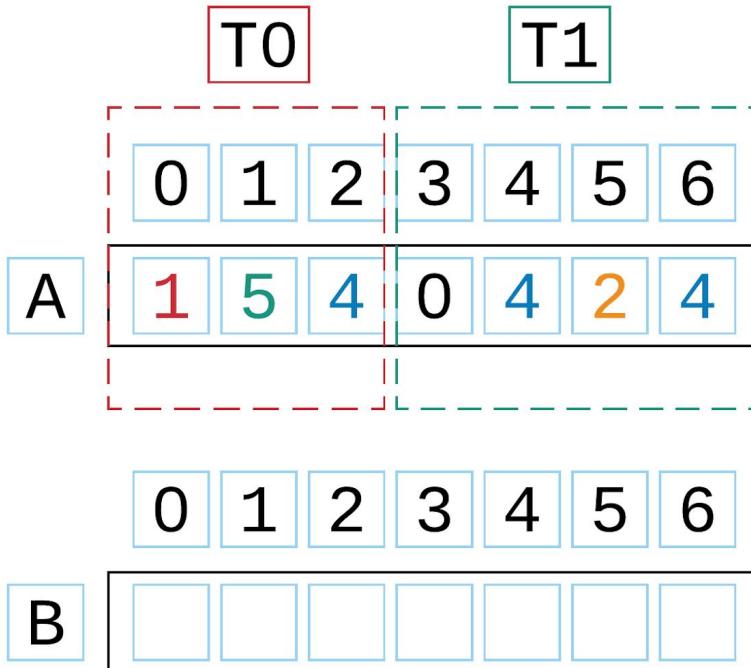
Counting-sort (Parallel) - Loop 3



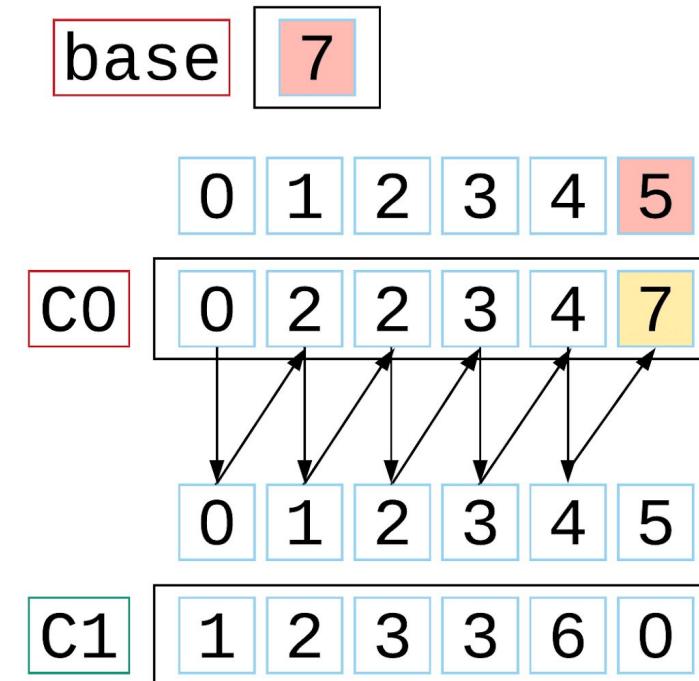
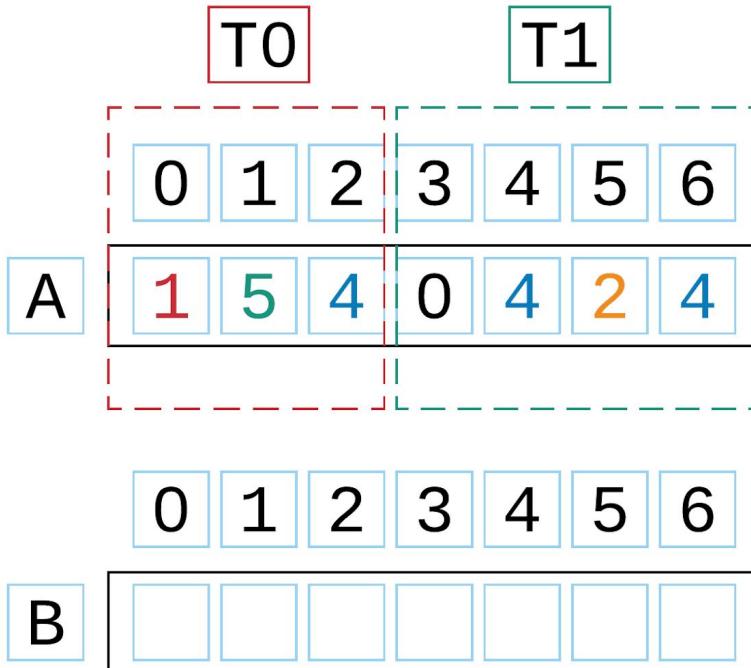
Counting-sort (Parallel) - Loop 3



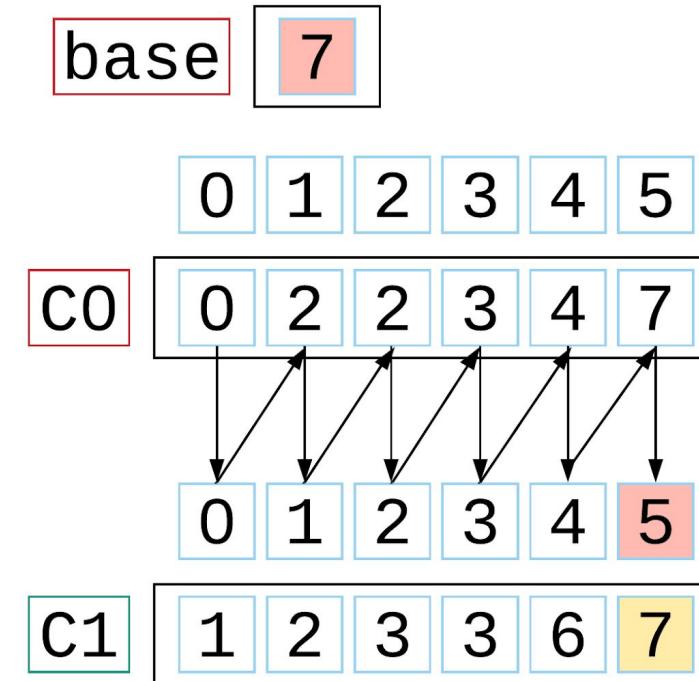
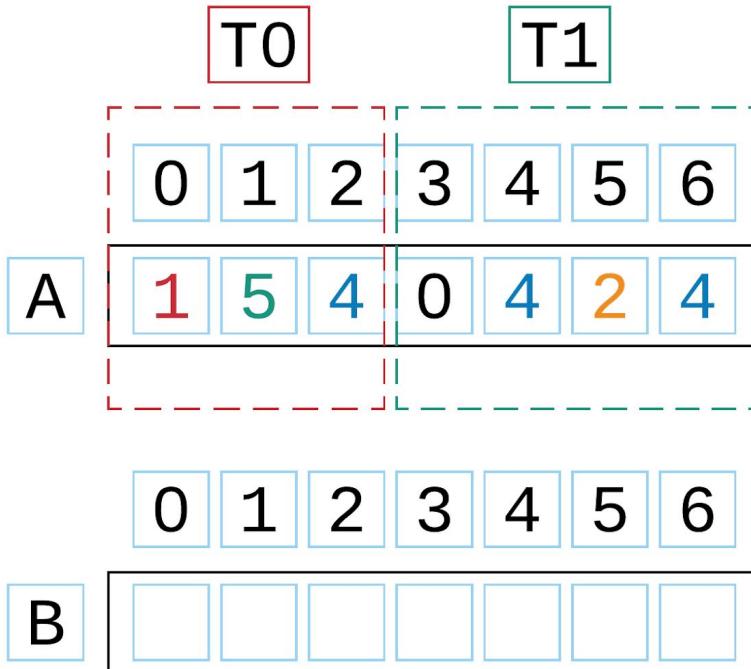
Counting-sort (Parallel) - Loop 3



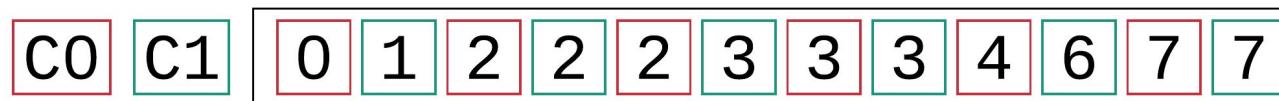
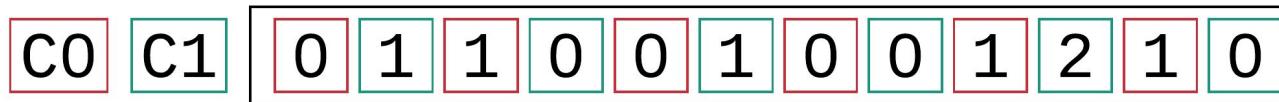
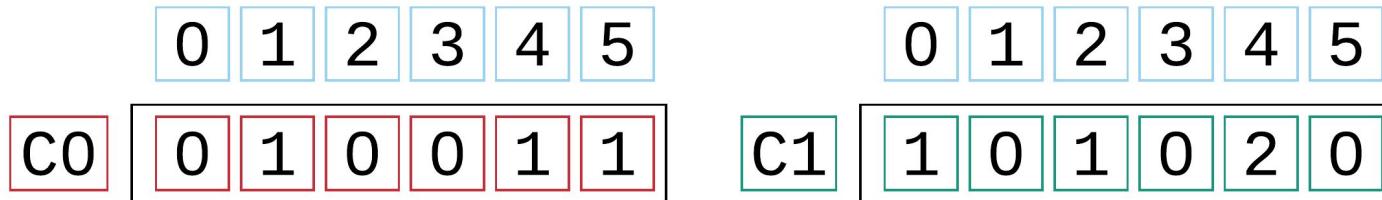
Counting-sort (Parallel) - Loop 3



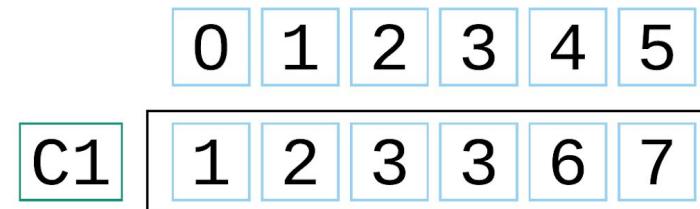
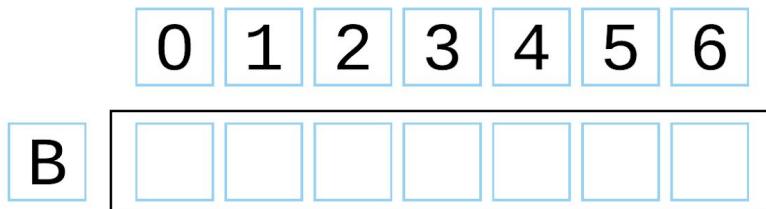
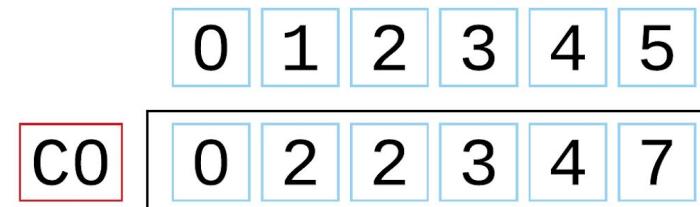
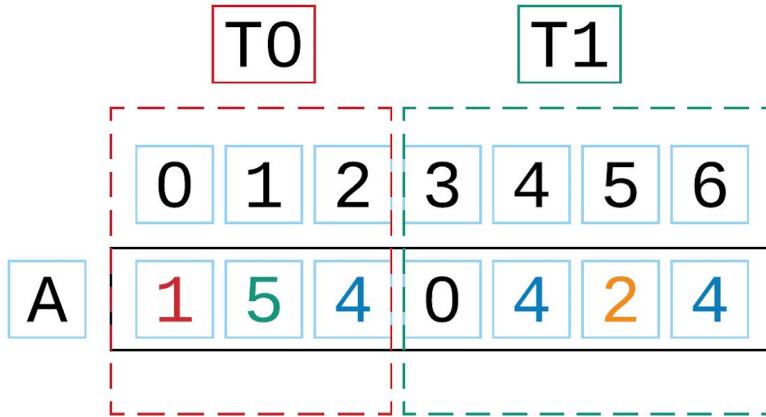
Counting-sort (Parallel) - Loop 3



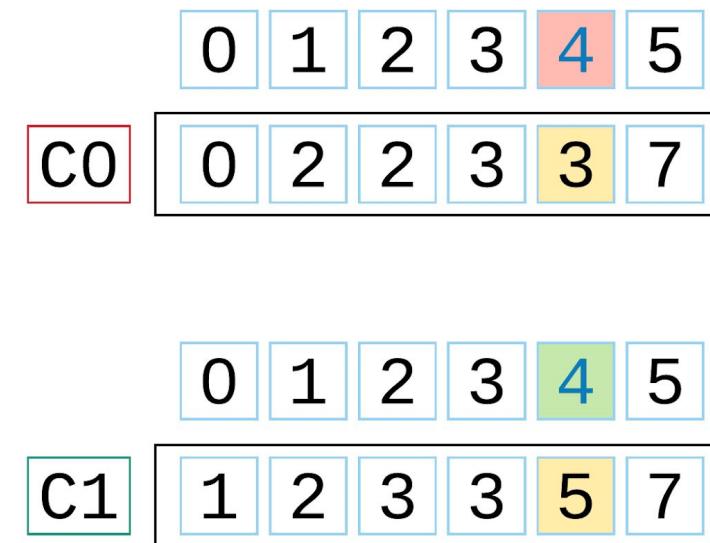
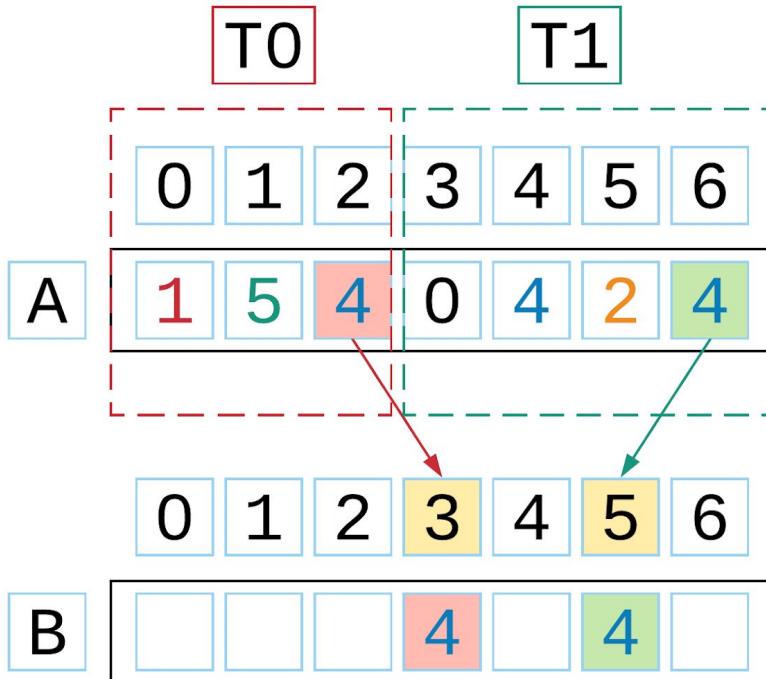
Counting-sort (Parallel) - Loop 3



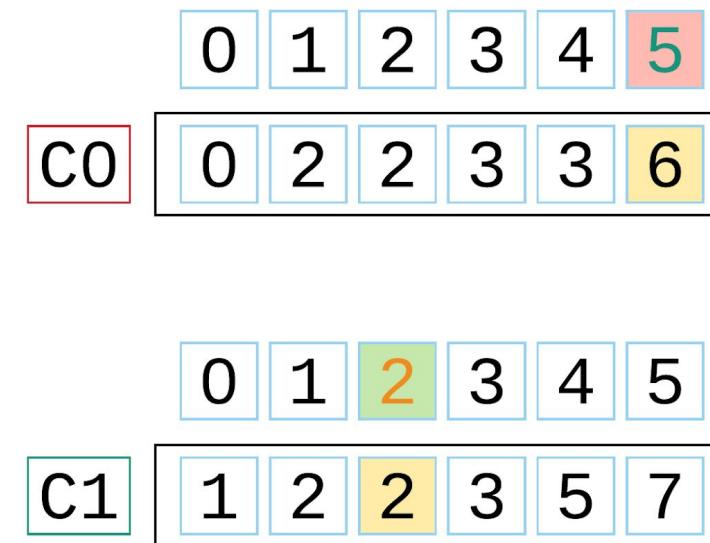
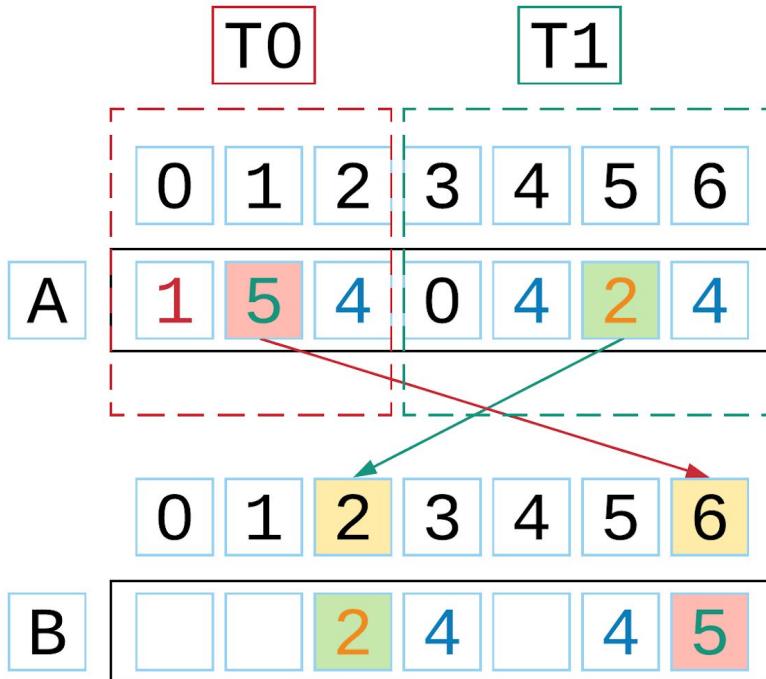
Counting-sort (Parallel) - Loop 4



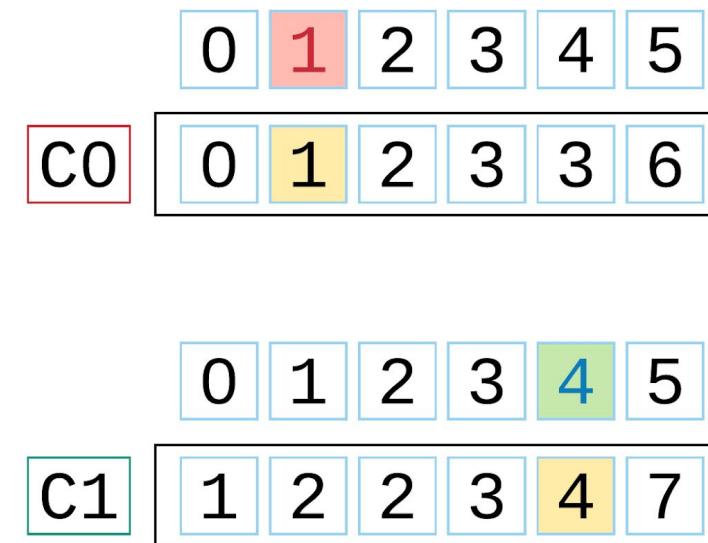
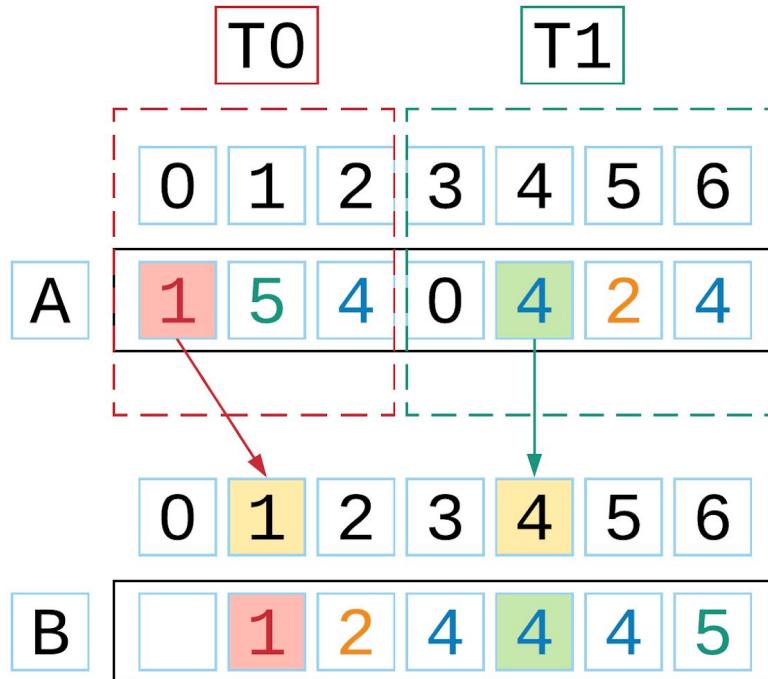
Counting-sort (Parallel) - Loop 4



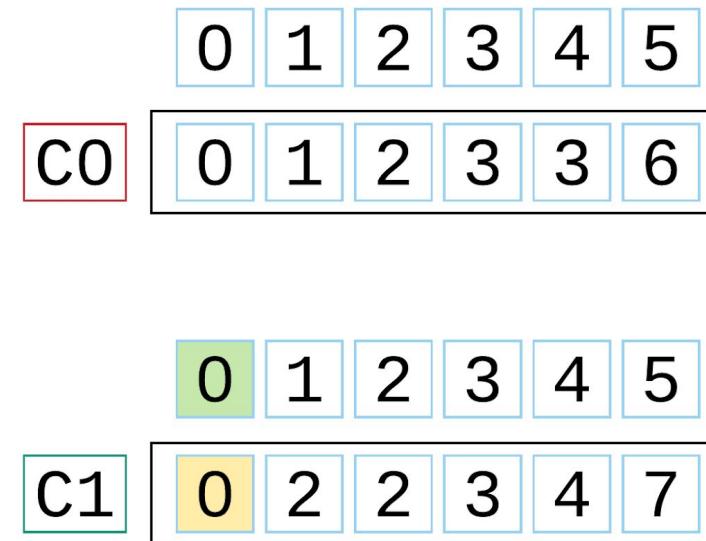
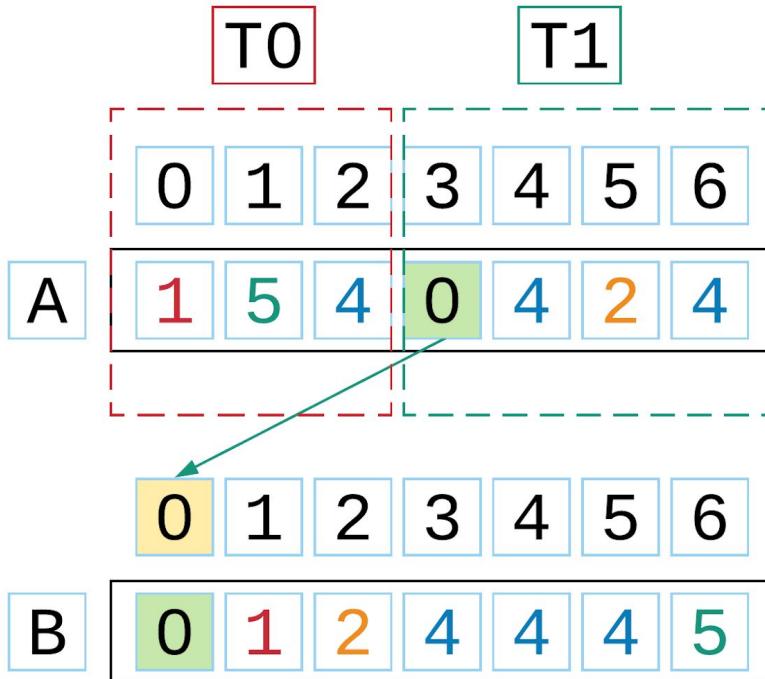
Counting-sort (Parallel) - Loop 4



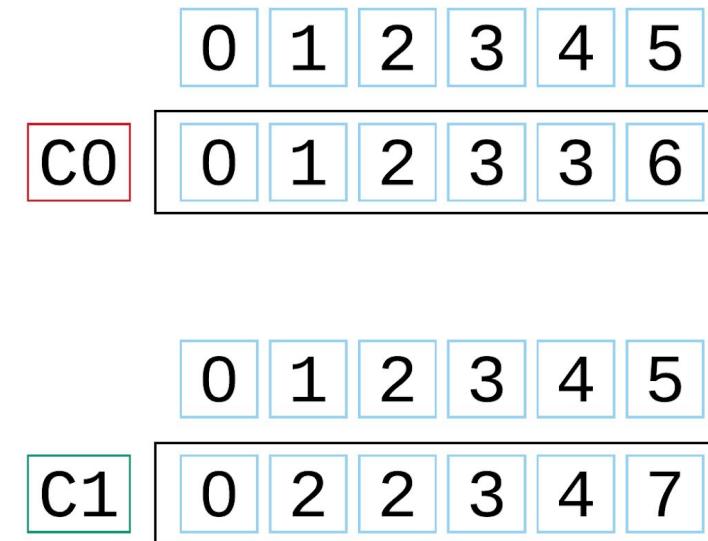
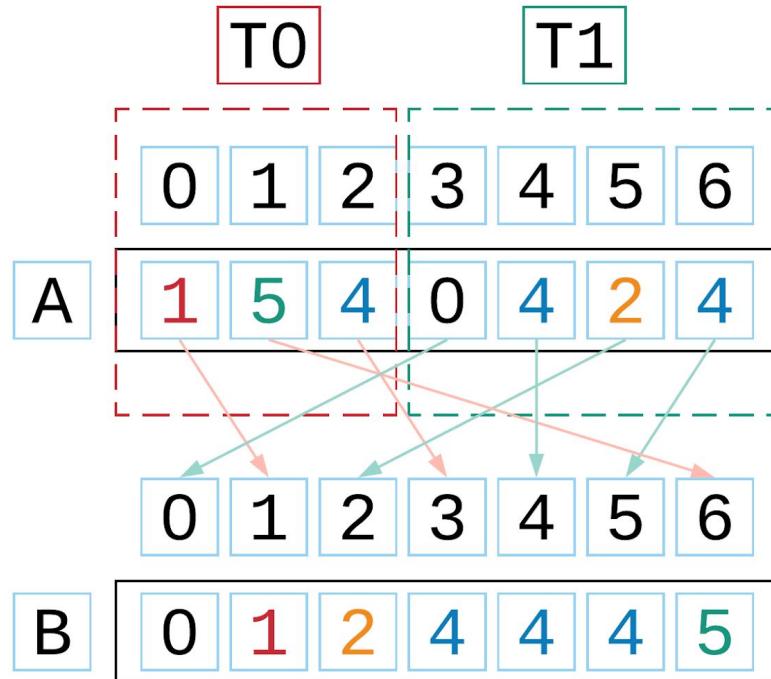
Counting-sort (Parallel) - Loop 4



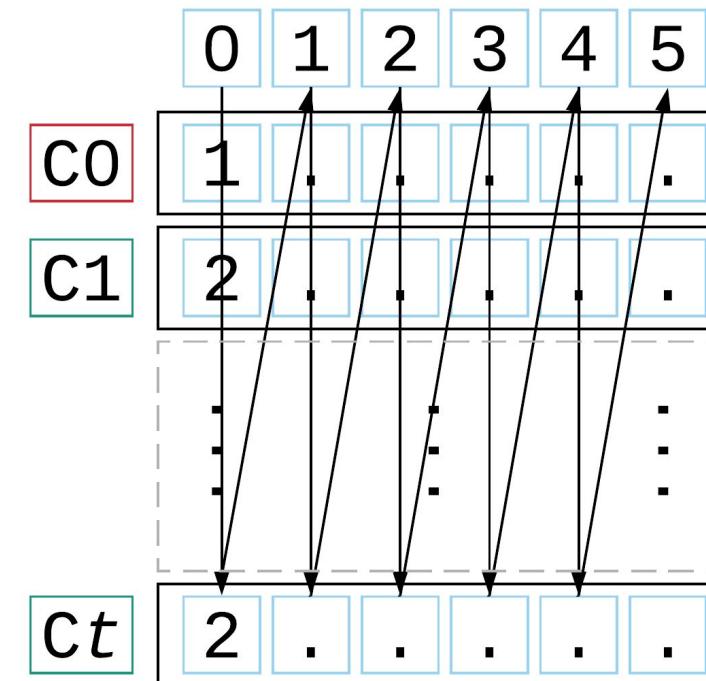
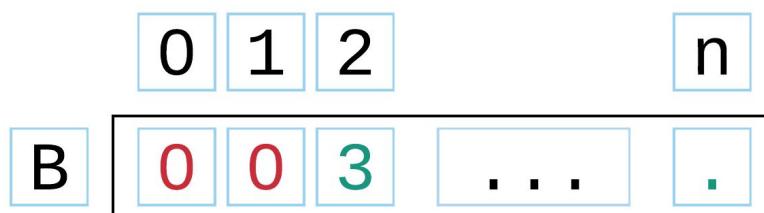
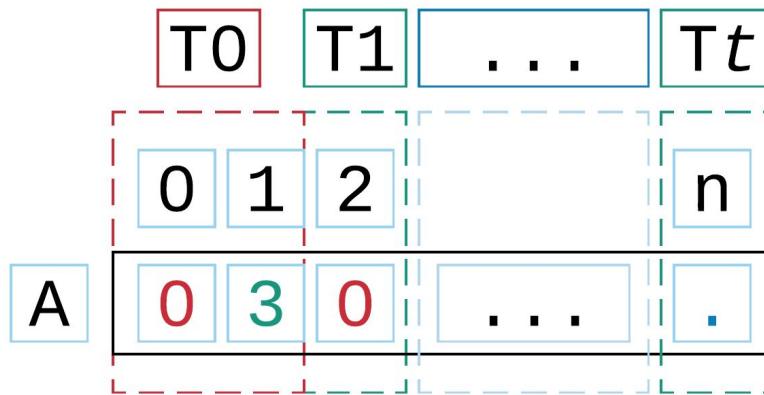
Counting-sort (Parallel) - Loop 4



Counting-sort (Parallel) - 2 Threads



Counting-sort (Parallel) - (t) Threads



Breadth First Search (BFS)

Breadth First Search (BFS) : Traversing or searching tree or graph data structures.

- ***Input***: vertices[1..n], Source.
- ***Output***: parent[1..v].
- ***Auxiliary storage***: frontier, next.

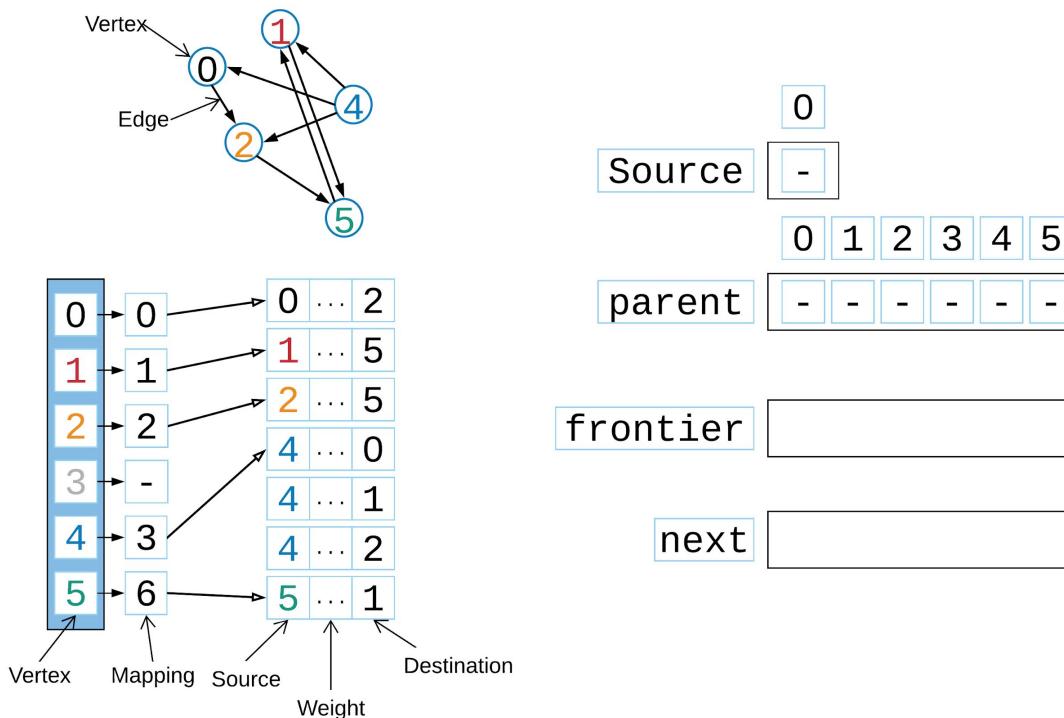
Breadth First Search (BFS)

```
function breadth-first-search(vertices, source)
    frontier ← {source}
    next ← {}
    parents ← [-1, -1, ..., -1]
    while frontier ≠ {} do
        top-down-step(vertices, frontier, next, parents)
        frontier ← next
        next ← {}
    end while
    return tree
```

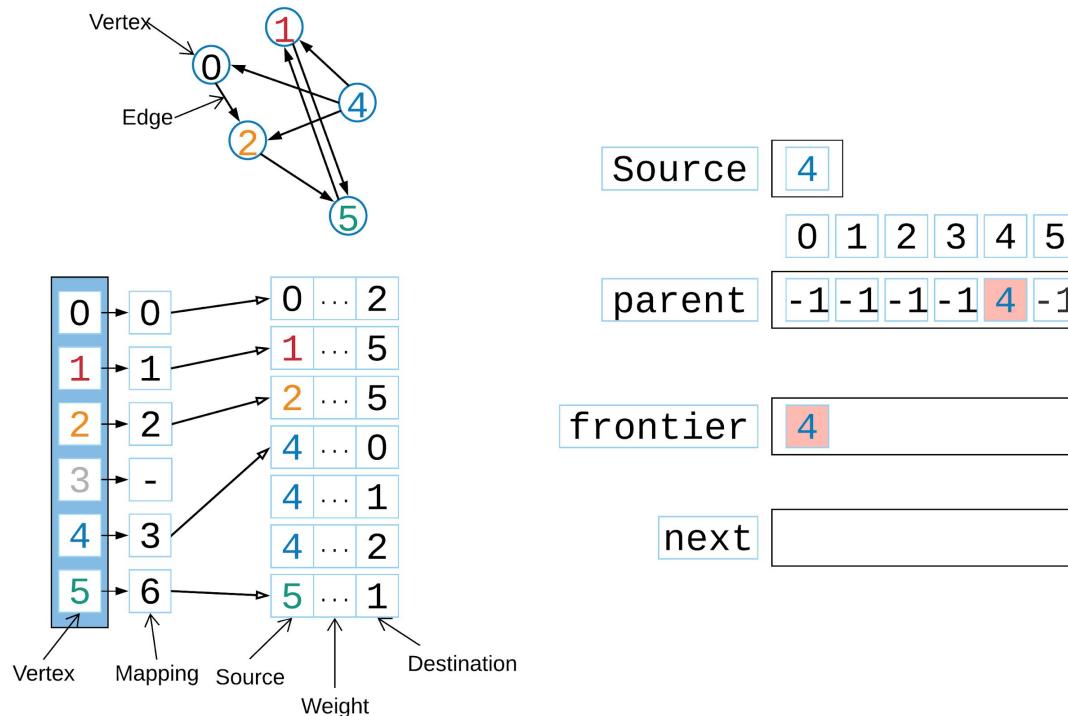
Top Down Step (Push)

```
function top-down-step(vertices, frontier, next, parents)
    for v ∈ frontier do
        for n ∈ neighbors[v] do
            if parents[n] = -1 then
                parents[n] ← v
                next ← next ∪ {n}
            end if
        end for
    end for
```

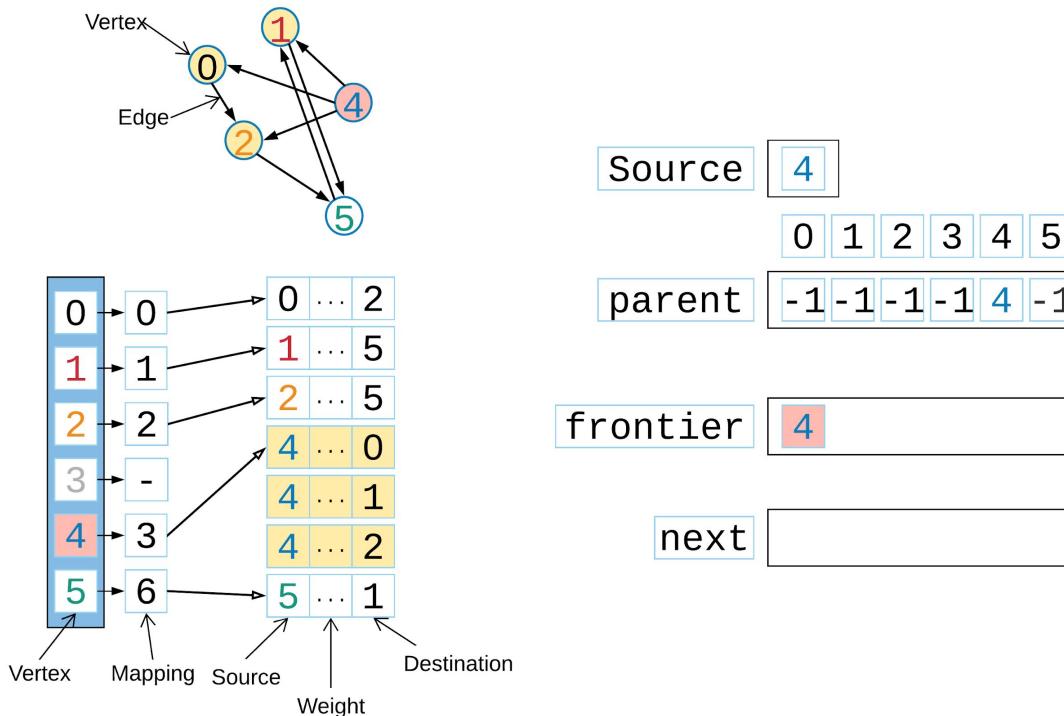
Breadth First Search (BFS)



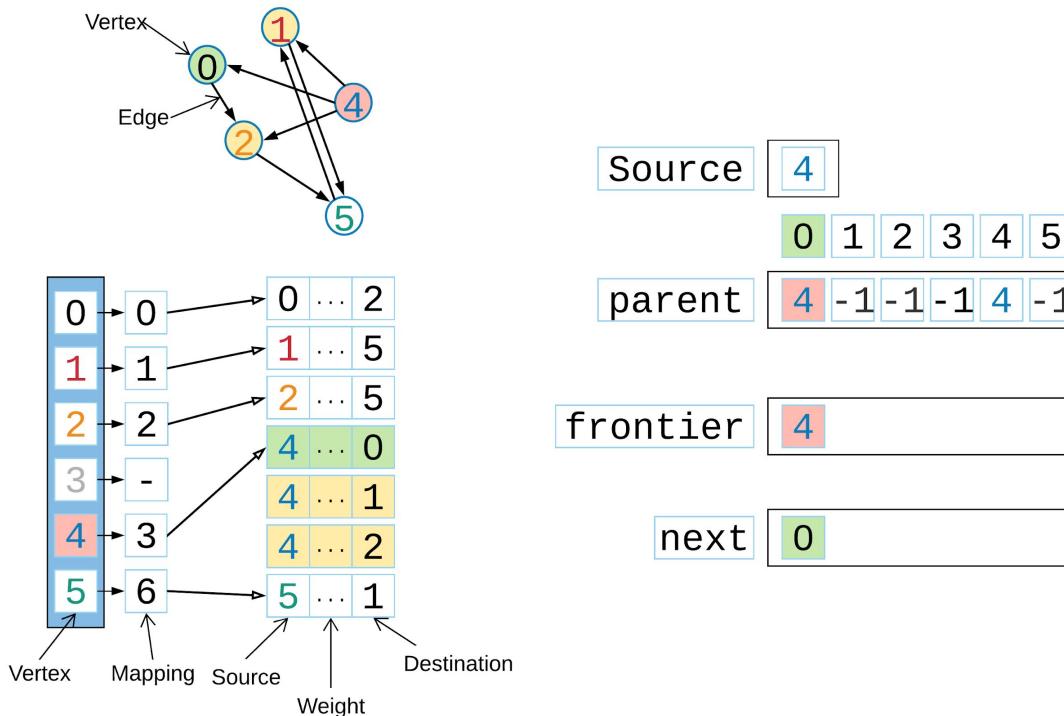
Breadth First Search (BFS) Initialize



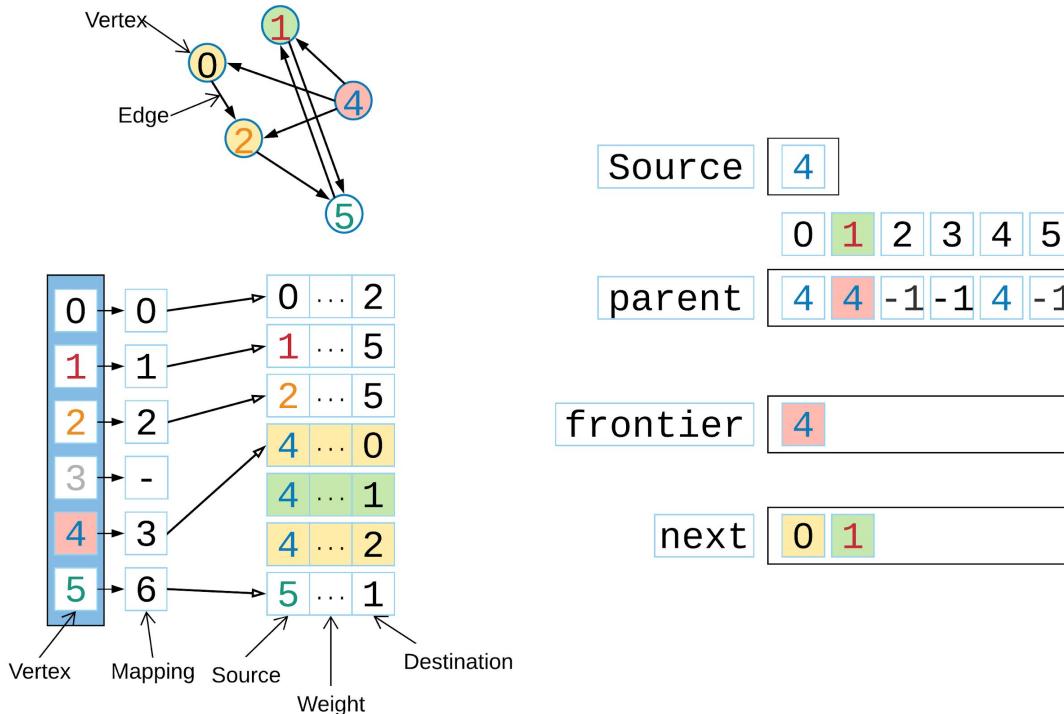
Breadth First Search (BFS) Iteration-1



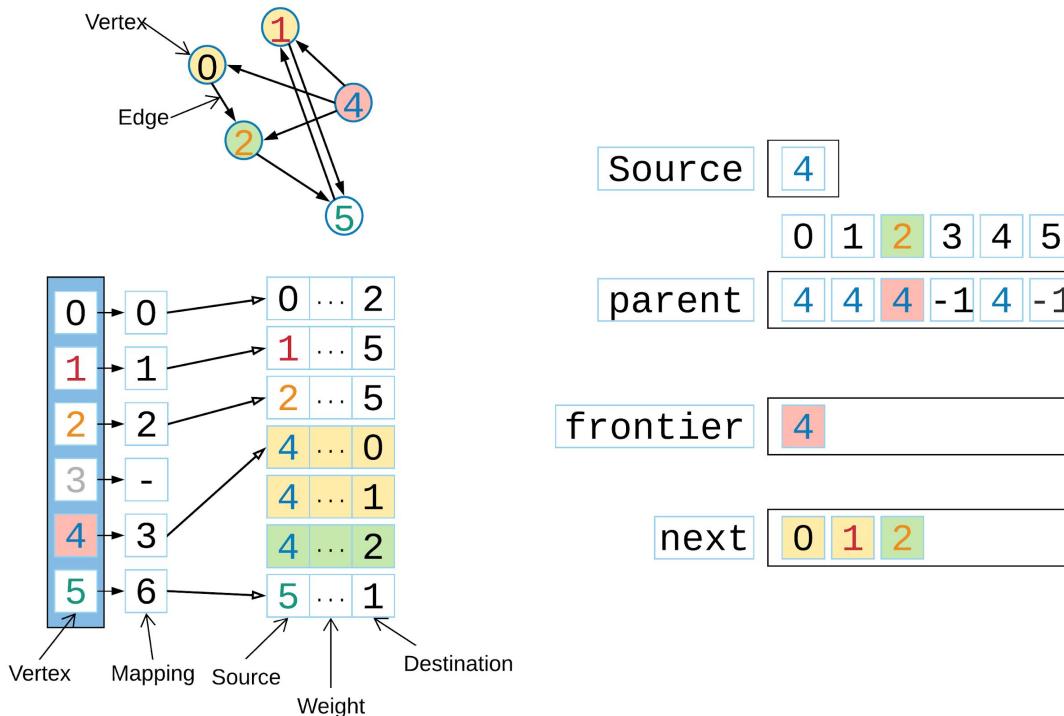
Breadth First Search (BFS) Iteration-1



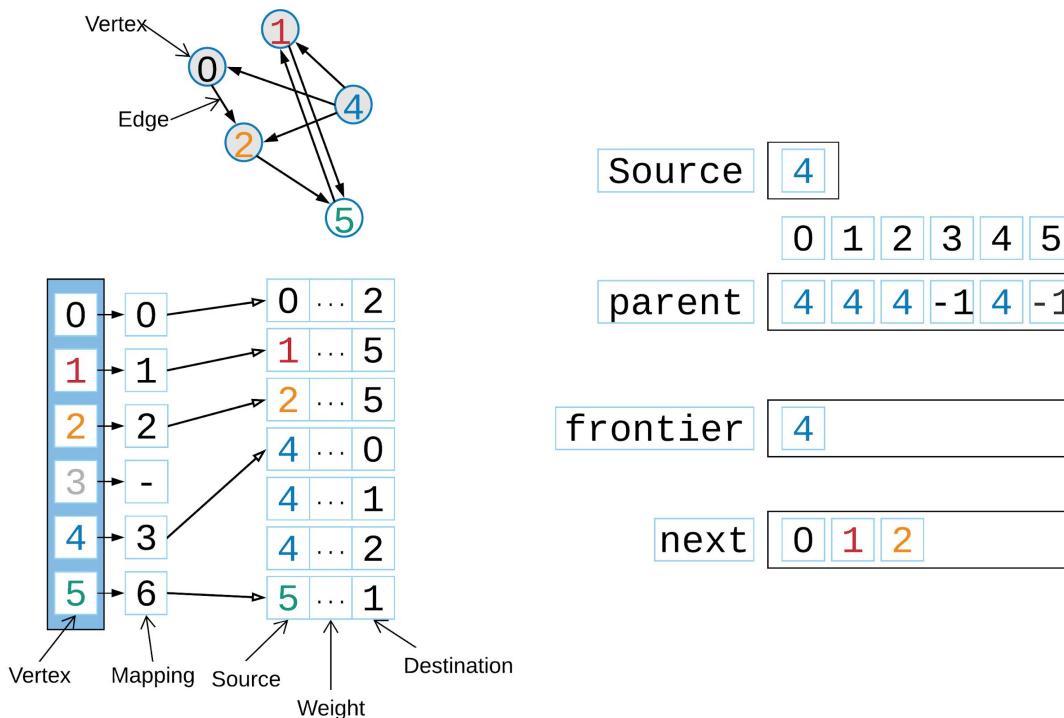
Breadth First Search (BFS) Iteration-1



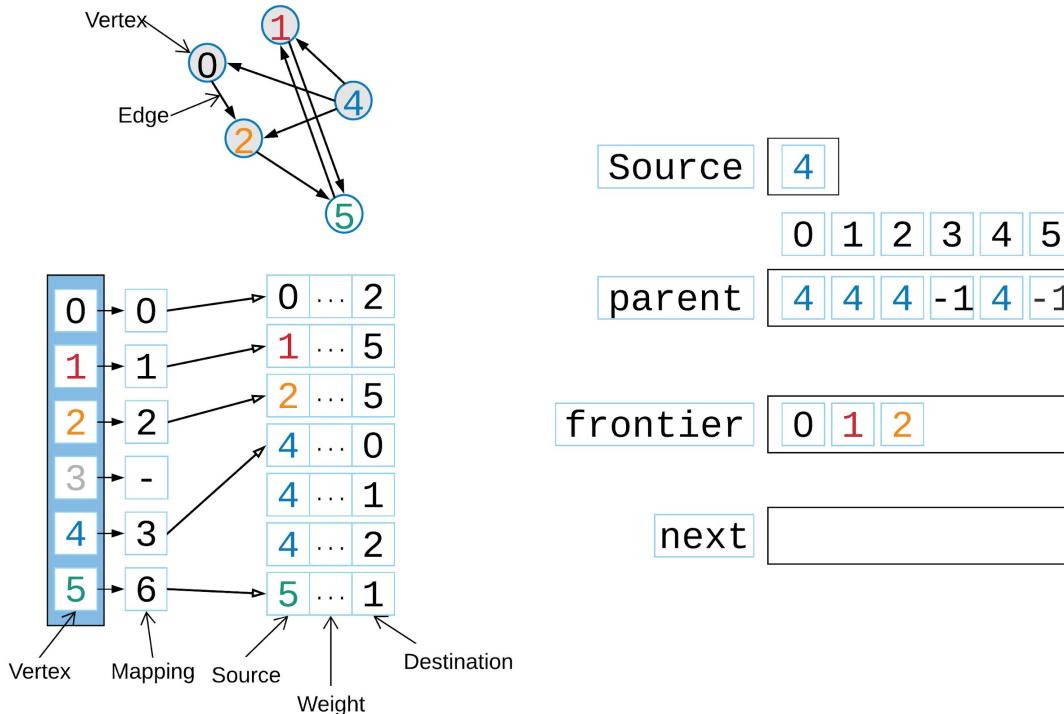
Breadth First Search (BFS) Iteration-1



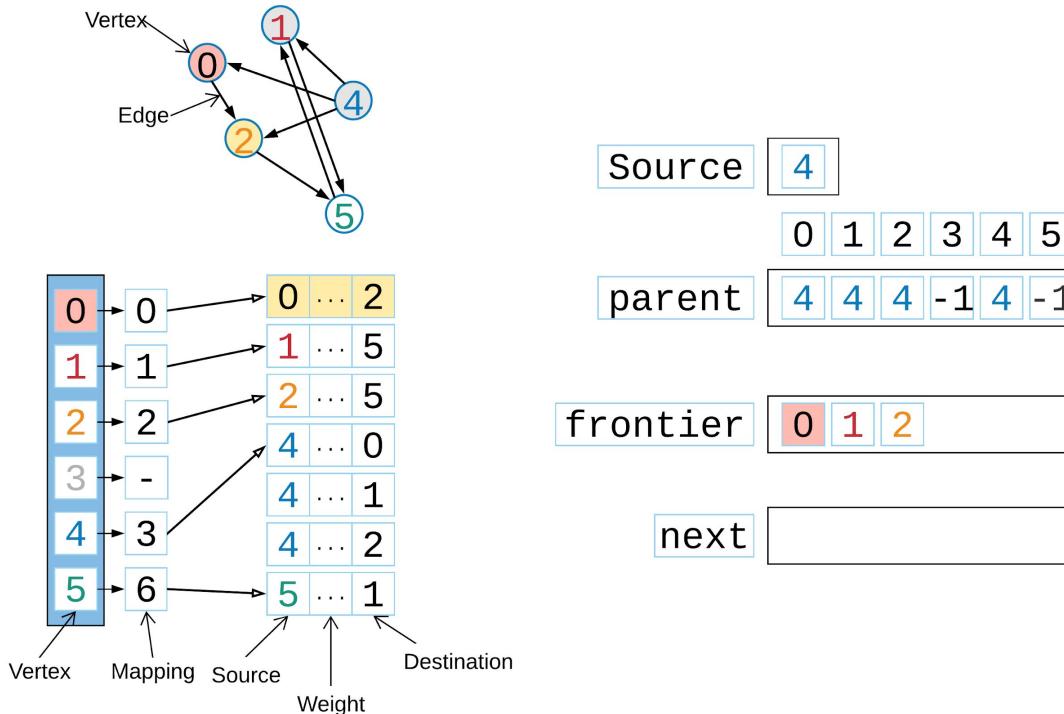
Breadth First Search (BFS) Iteration-1-end



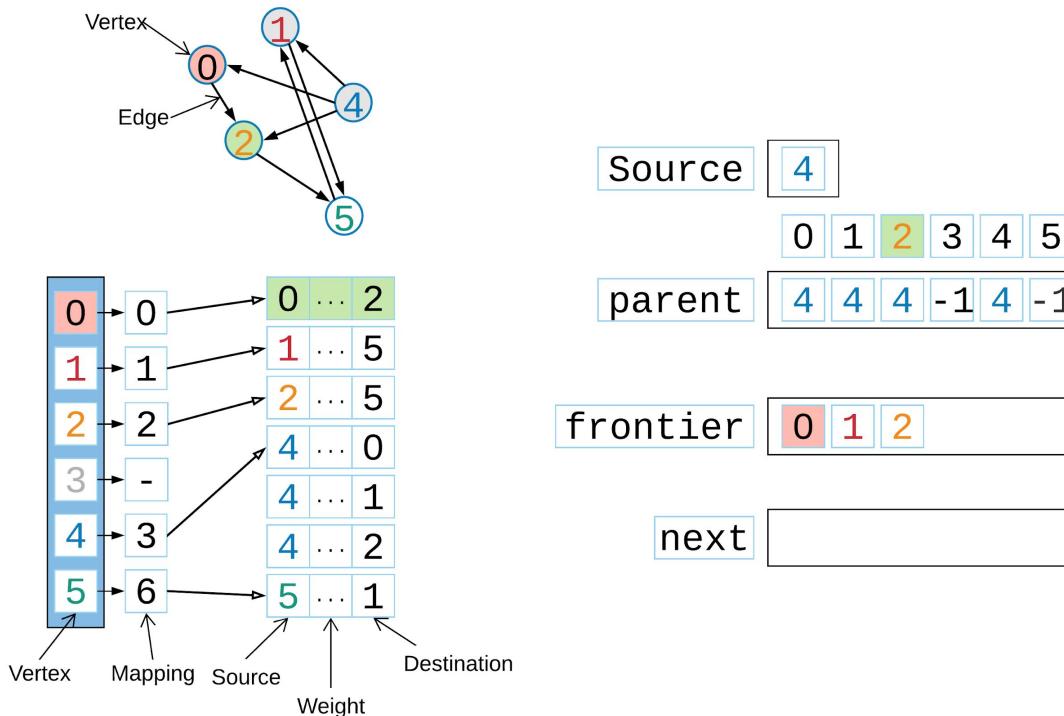
Breadth First Search (BFS) Iteration-2



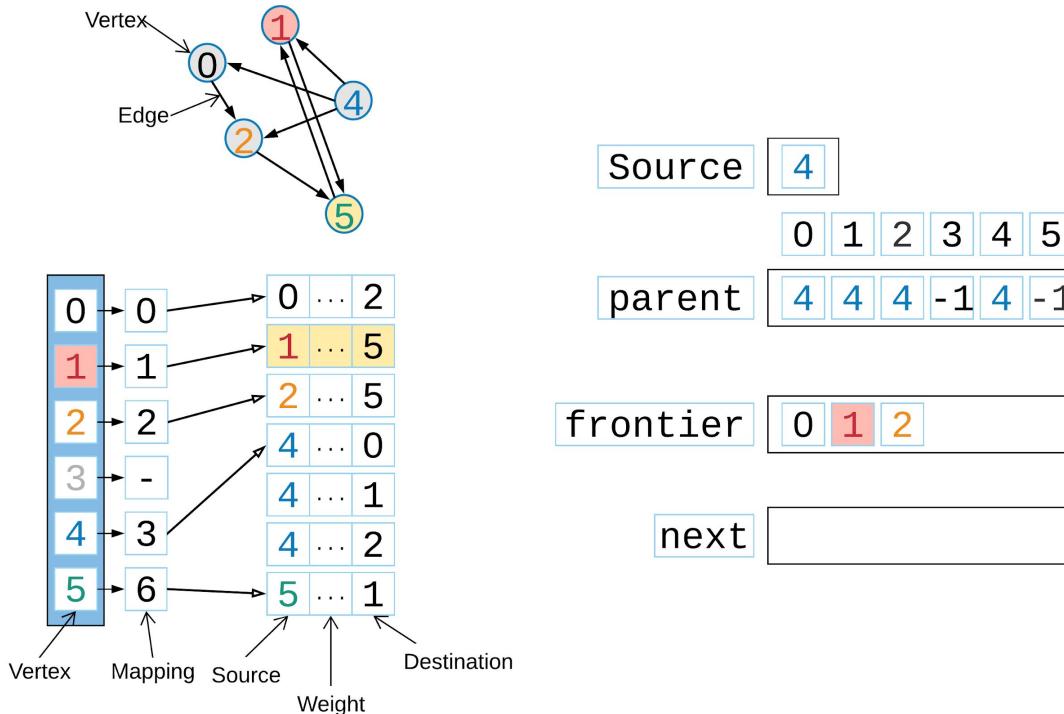
Breadth First Search (BFS) Iteration-2



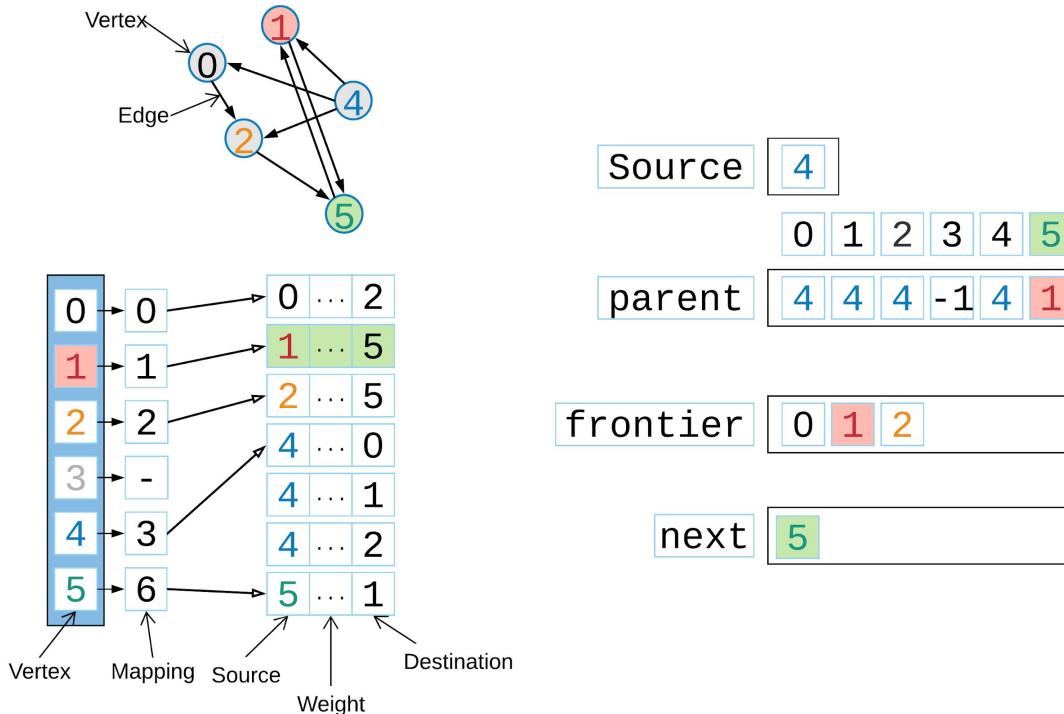
Breadth First Search (BFS) Iteration-2



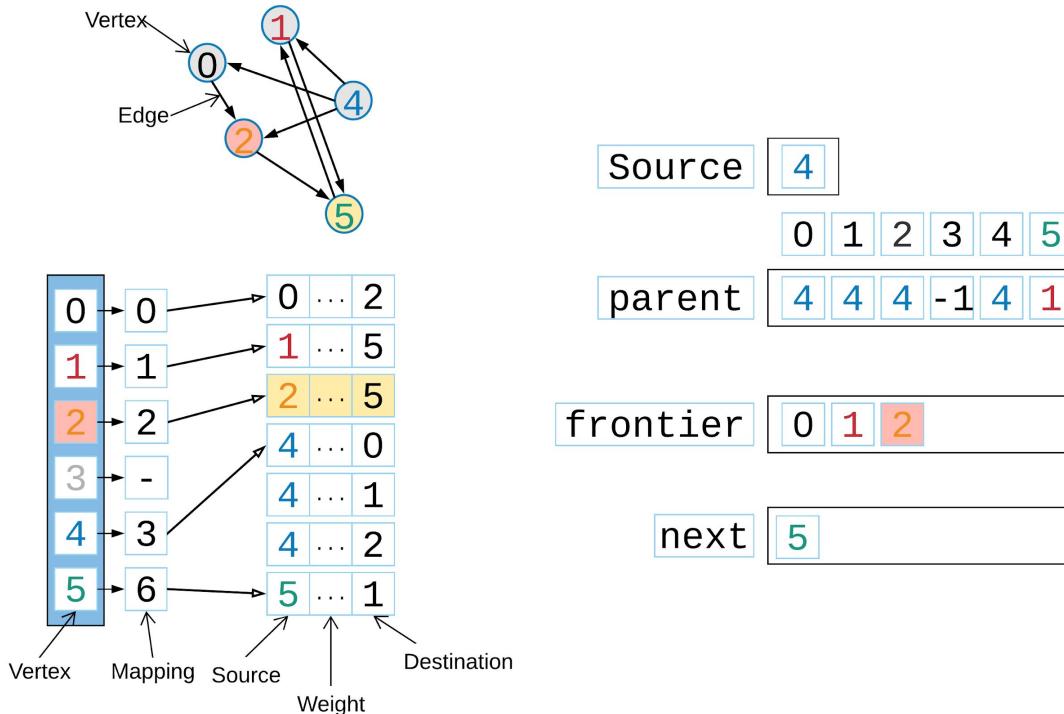
Breadth First Search (BFS) Iteration-2



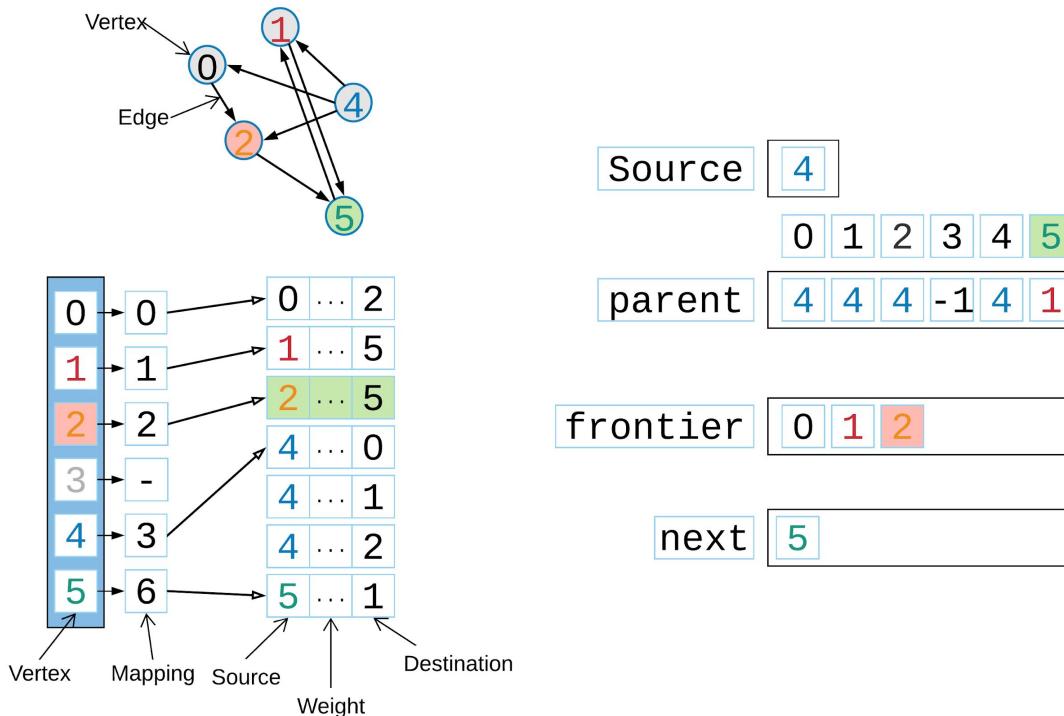
Breadth First Search (BFS) Iteration-2



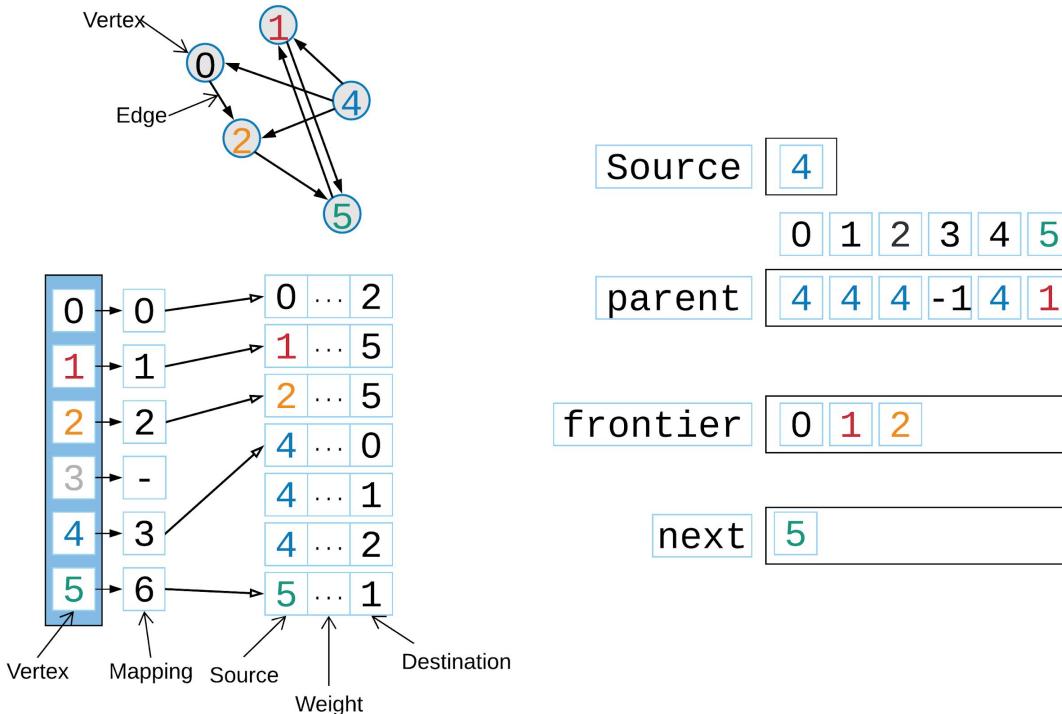
Breadth First Search (BFS) Iteration-2



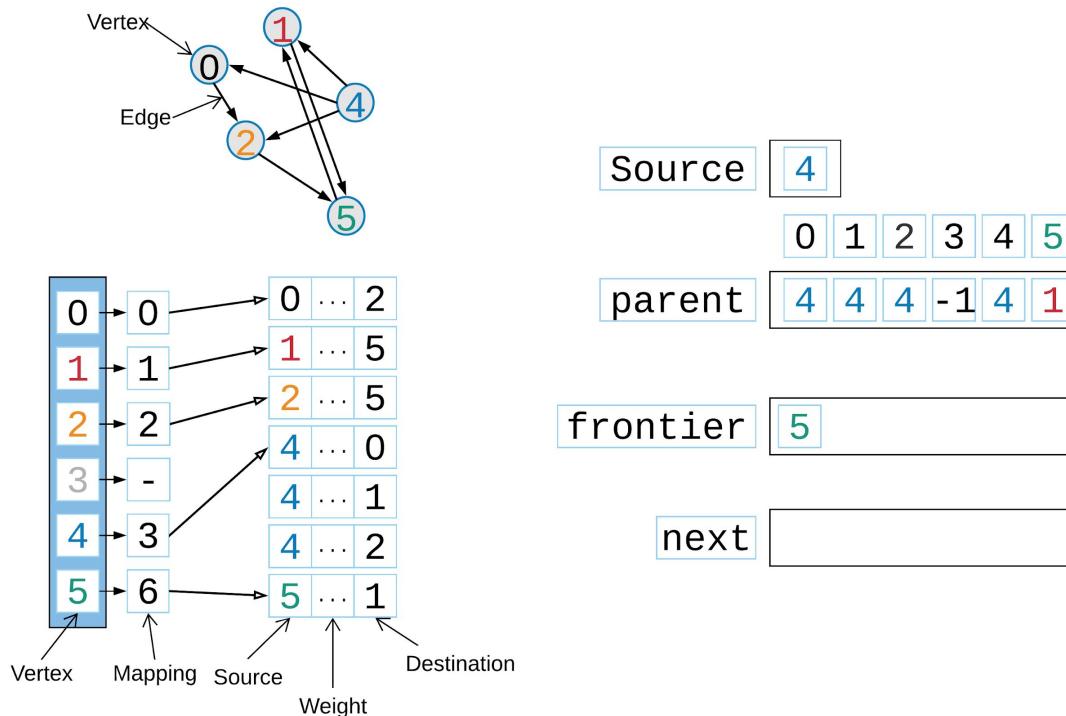
Breadth First Search (BFS) Iteration-2



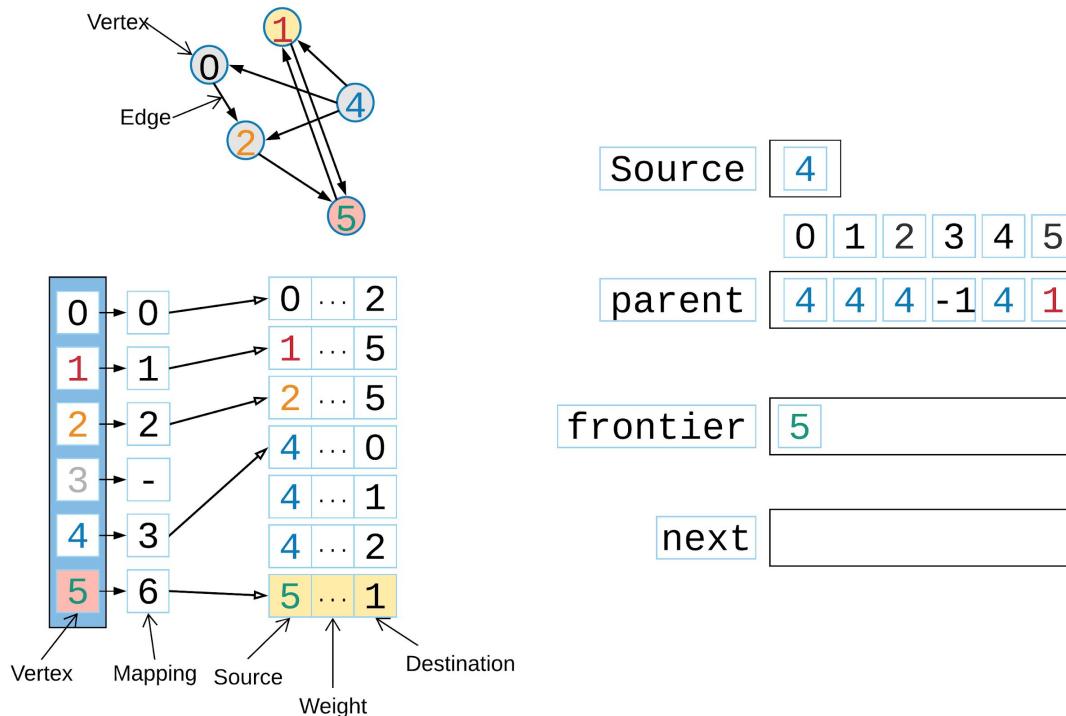
Breadth First Search (BFS) Iteration-2-end



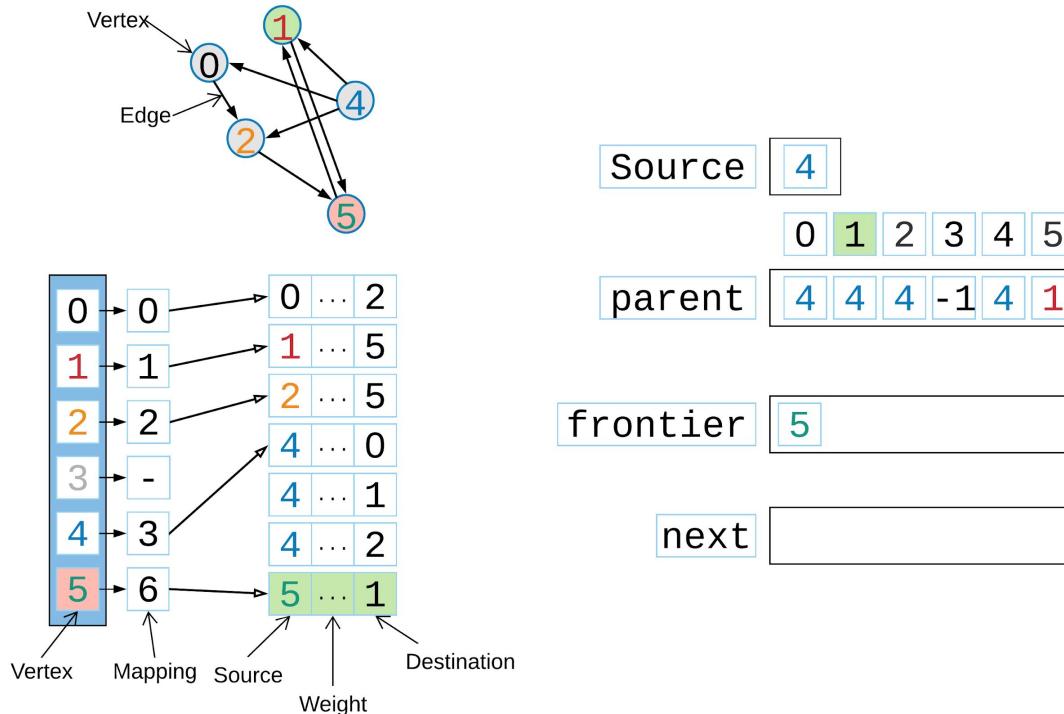
Breadth First Search (BFS) Iteration-3



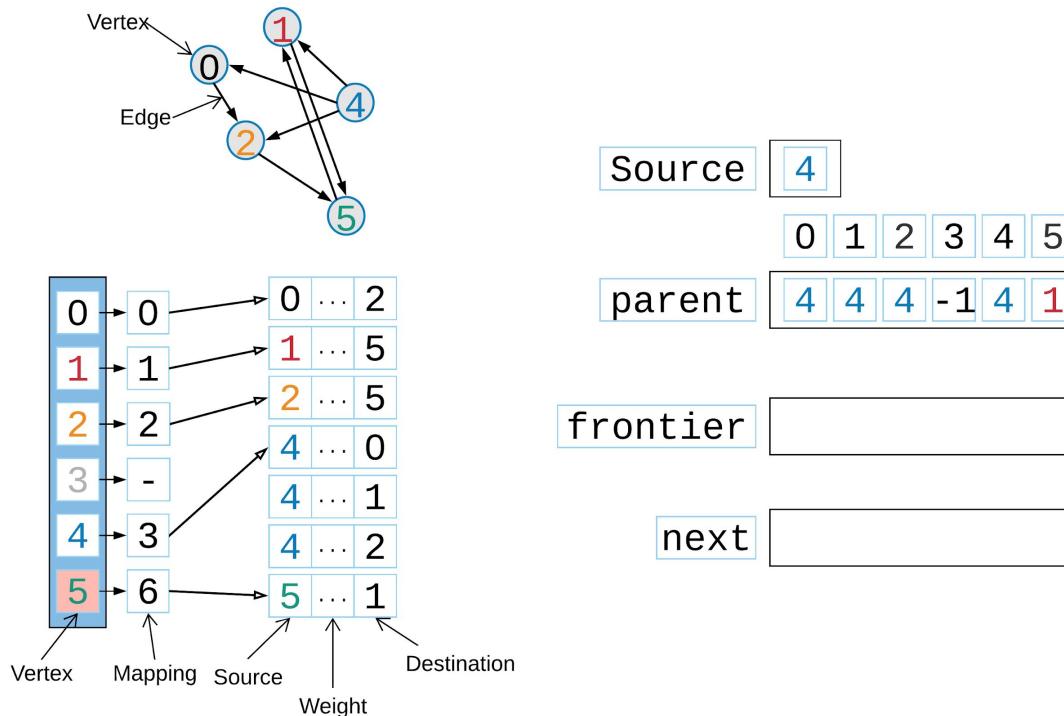
Breadth First Search (BFS) Iteration-3



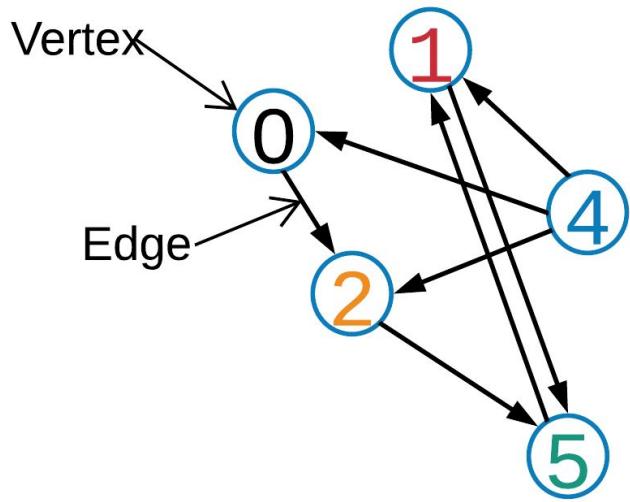
Breadth First Search (BFS) Iteration-3



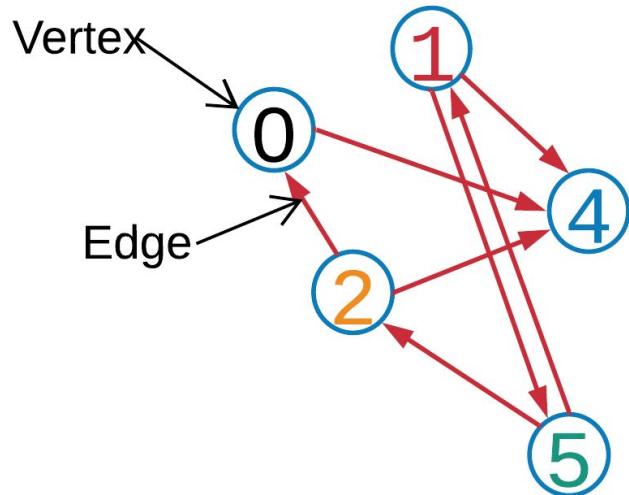
Breadth First Search (BFS) Iteration-3



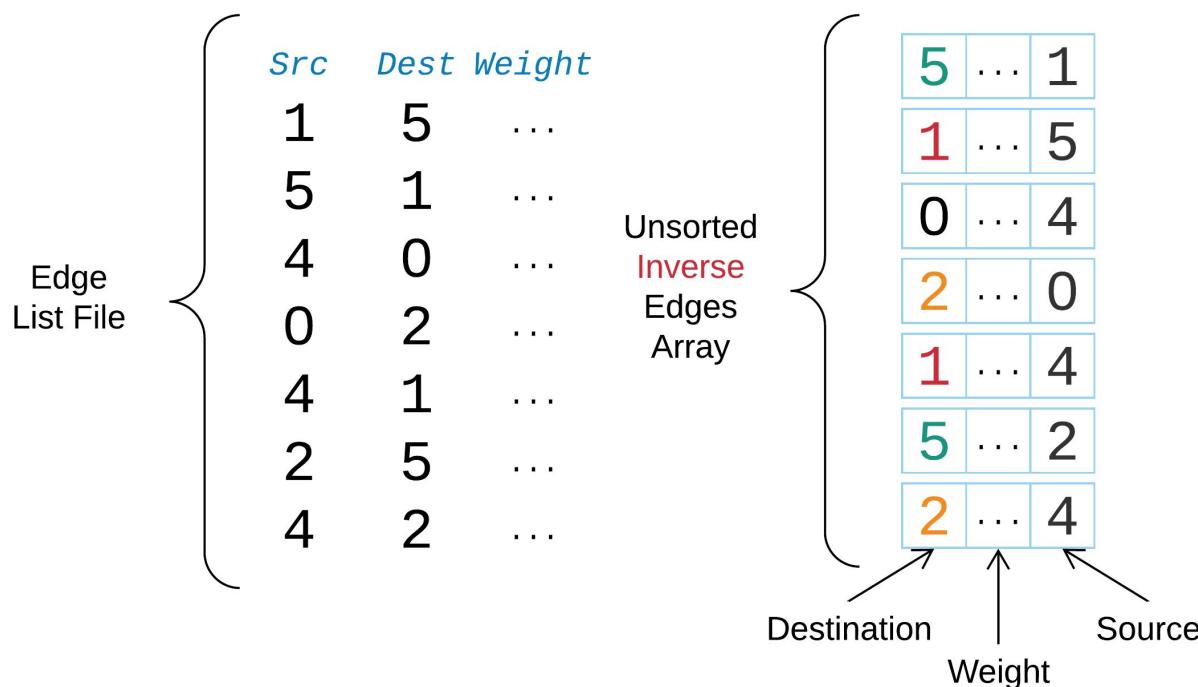
Inverse Graph



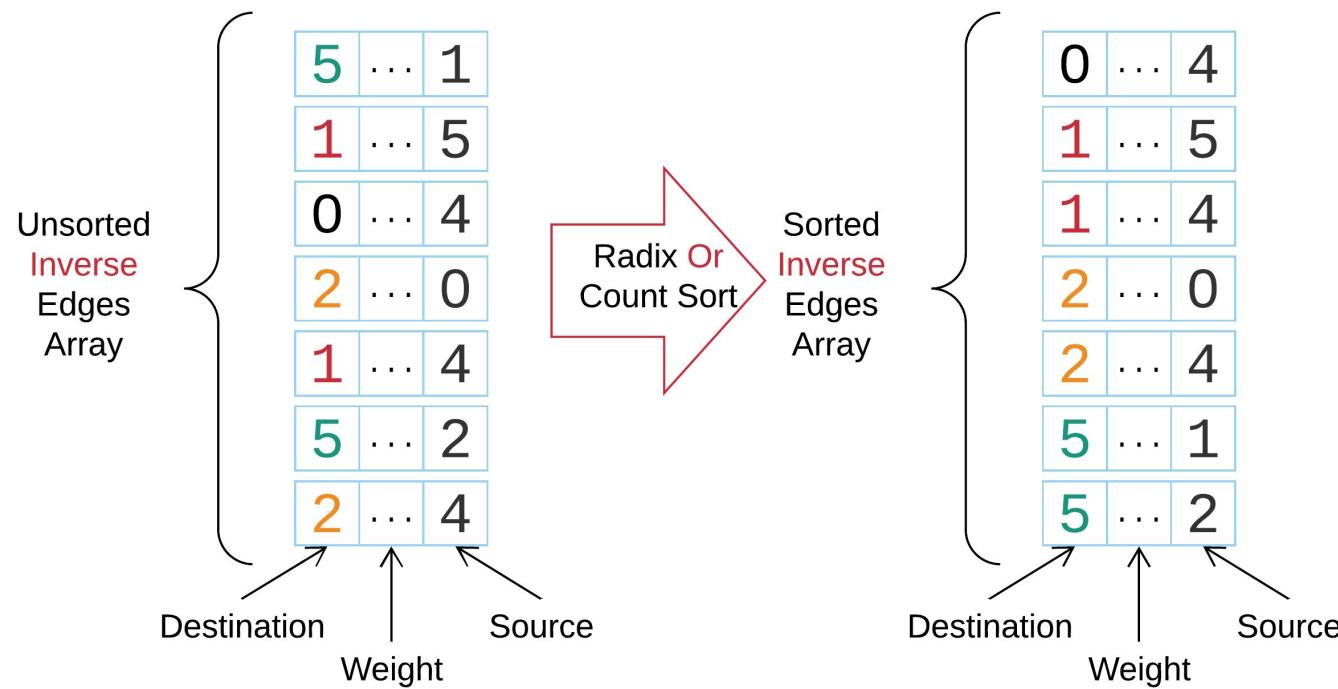
Inverse
Graph



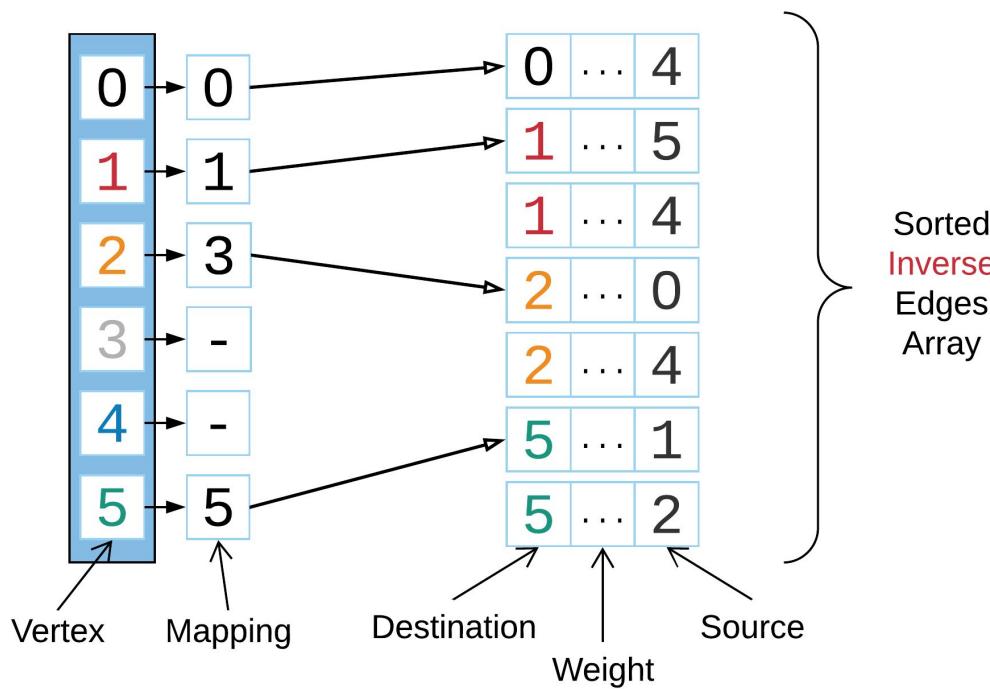
Inverse Graph (load)



Inverse Graph (sort)



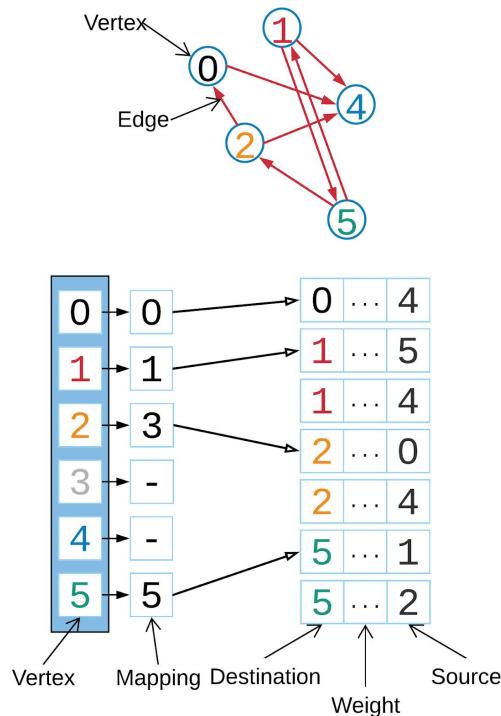
Inverse Graph (map)



Bottom Up Step (Pull)

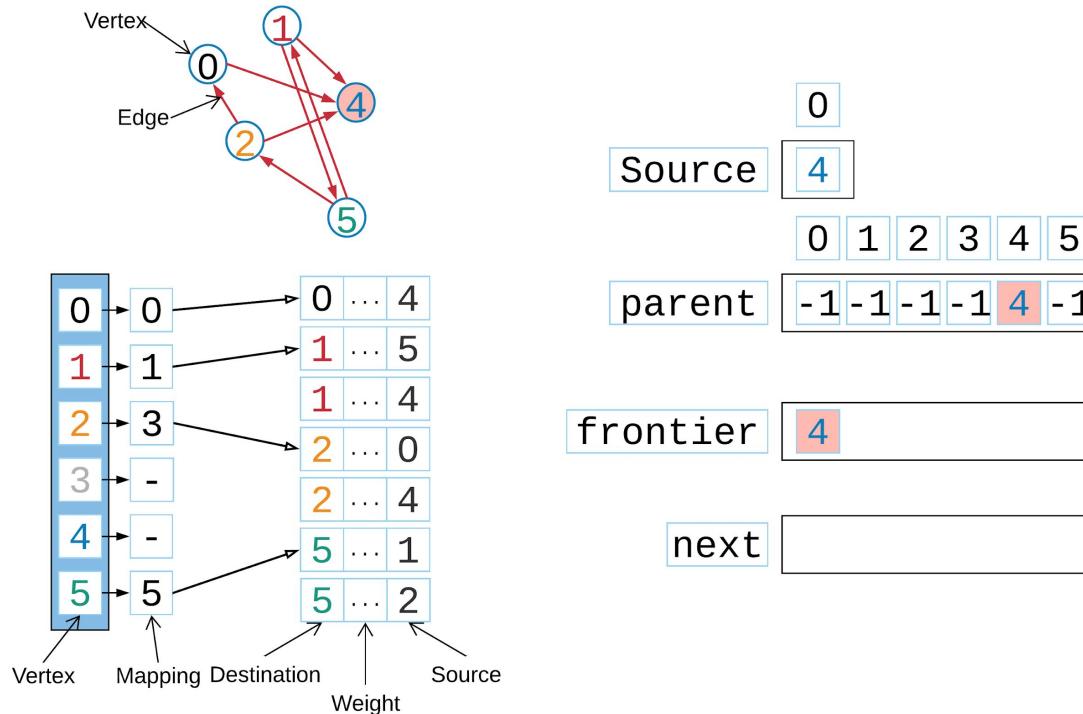
```
function bottom-up-step(vertices, frontier, next, parents)
    for v ∈ vertices do
        if parents[v] = -1 then
            for n ∈ neighbors[v] do
                if n ∈ frontier do
                    parents[v] ← n
                    next ← next ∪ {v}
                    break
                end if
            end for
        end if
    end for
```

Bottom Up Step (Pull)

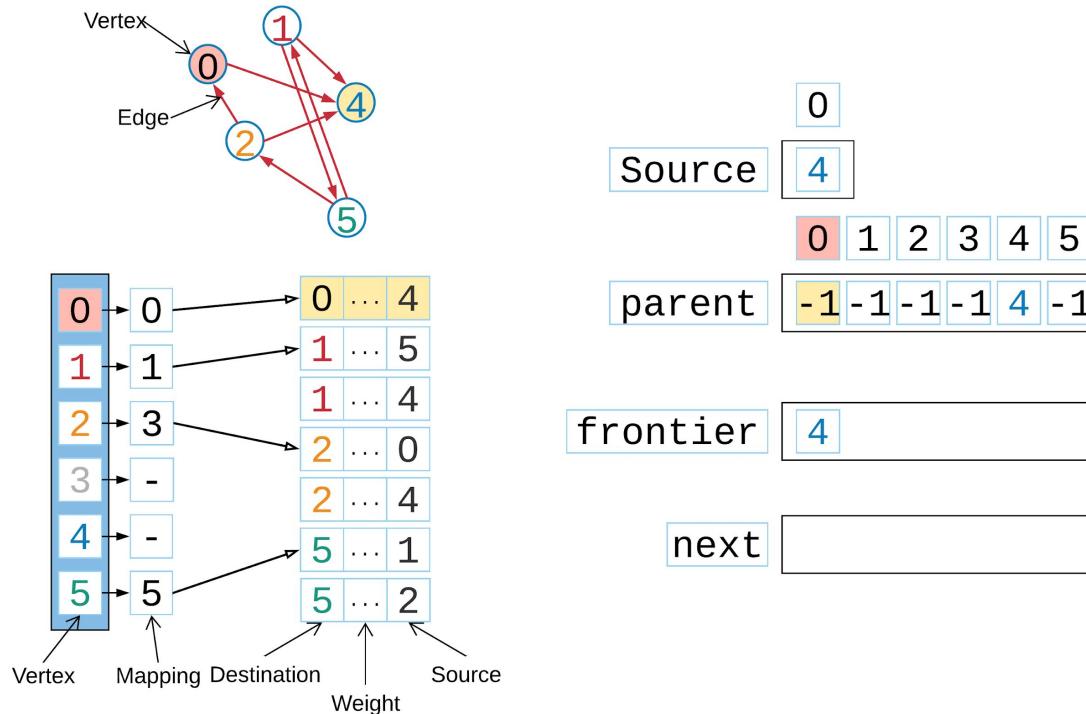


Source	0	-	0 1 2 3 4 5
parent	-	-	- - - - - -
frontier			
next			

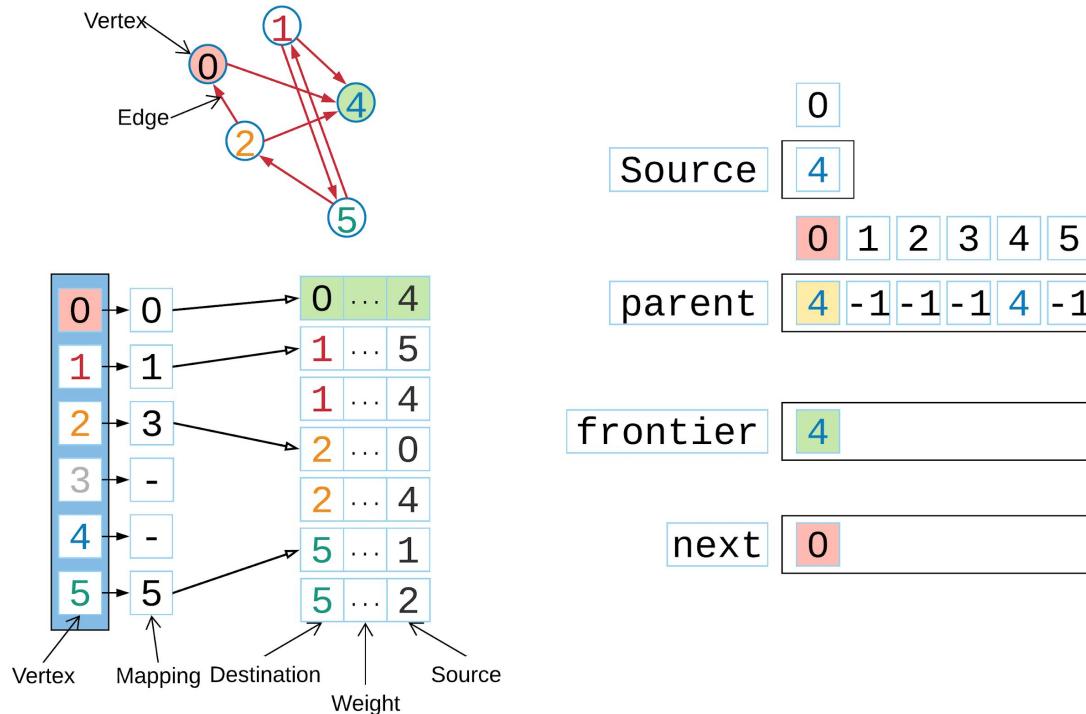
Breadth First Search (BFS) Initialize



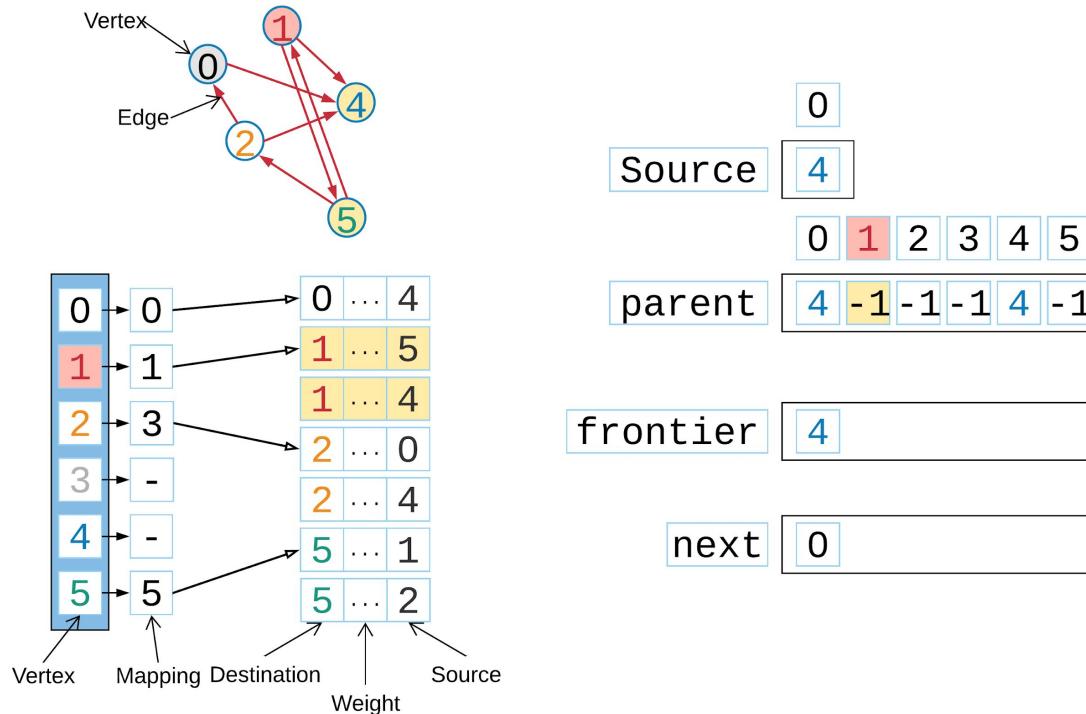
Breadth First Search (BFS) Iteration-1



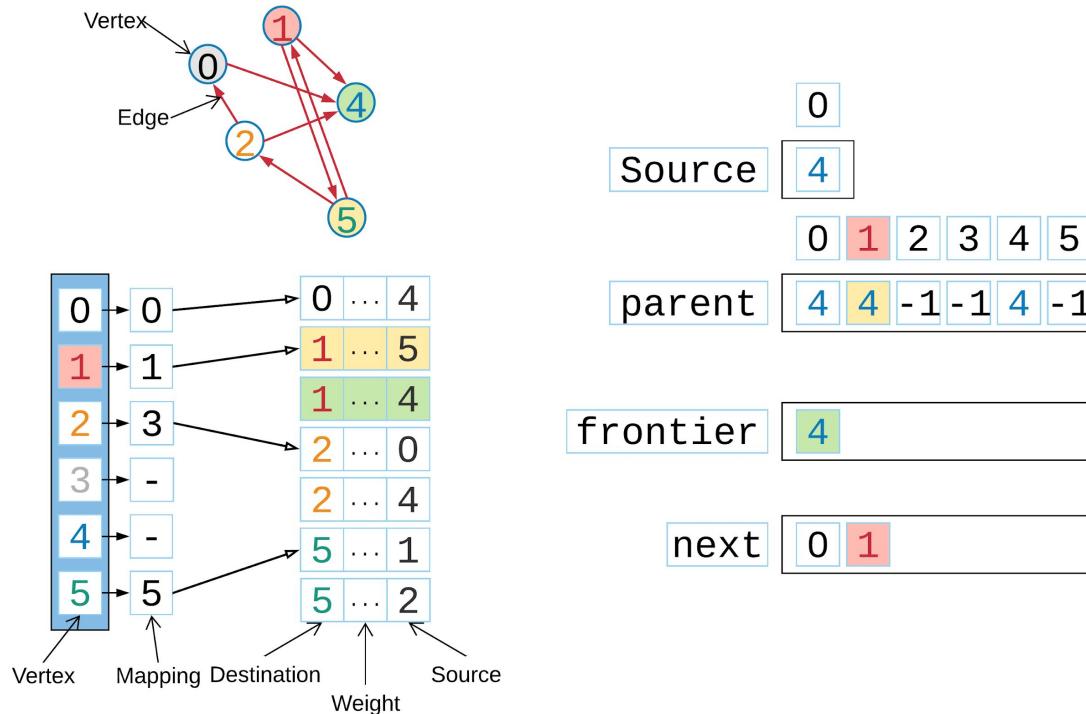
Breadth First Search (BFS) Iteration-1



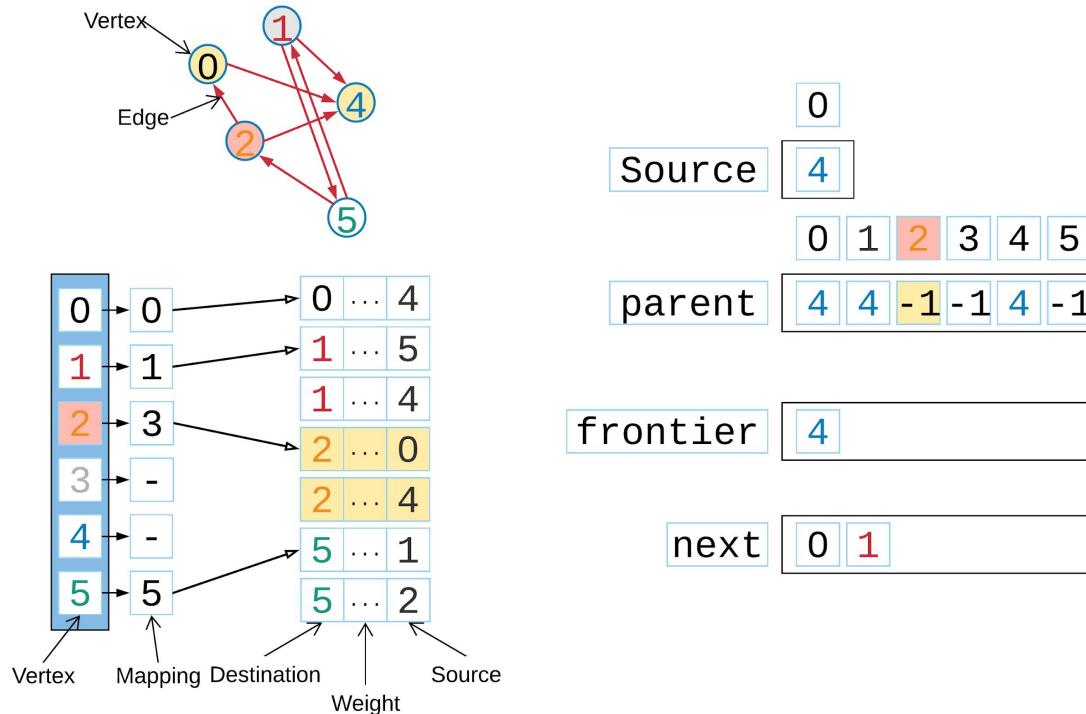
Breadth First Search (BFS) Iteration-1



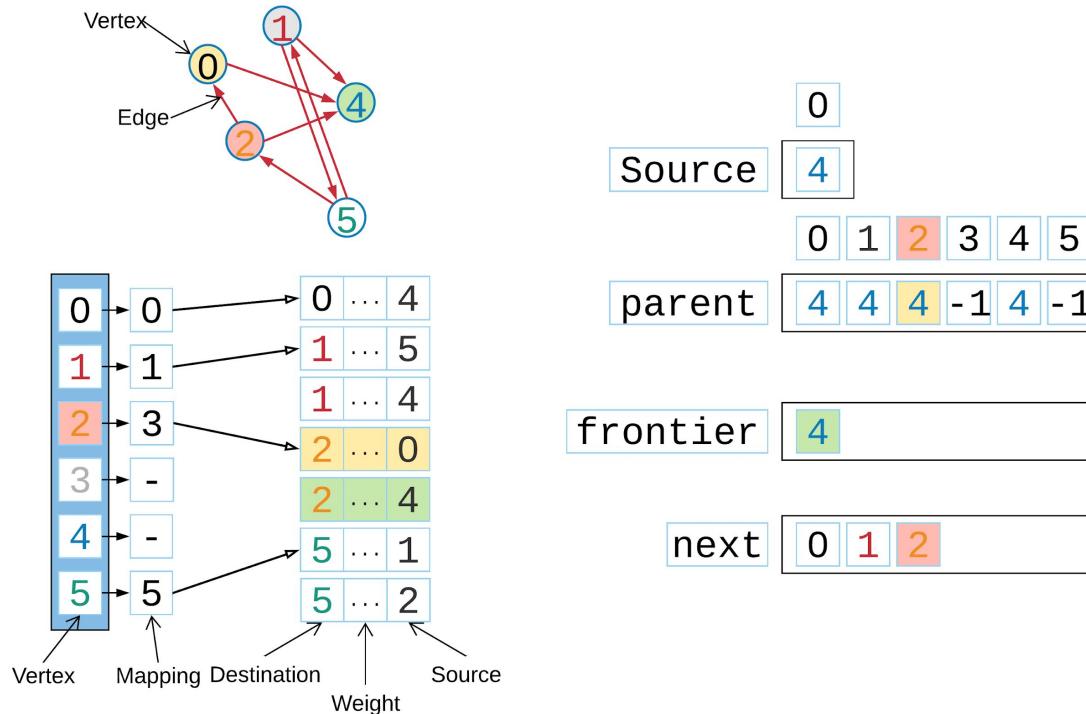
Breadth First Search (BFS) Iteration-1



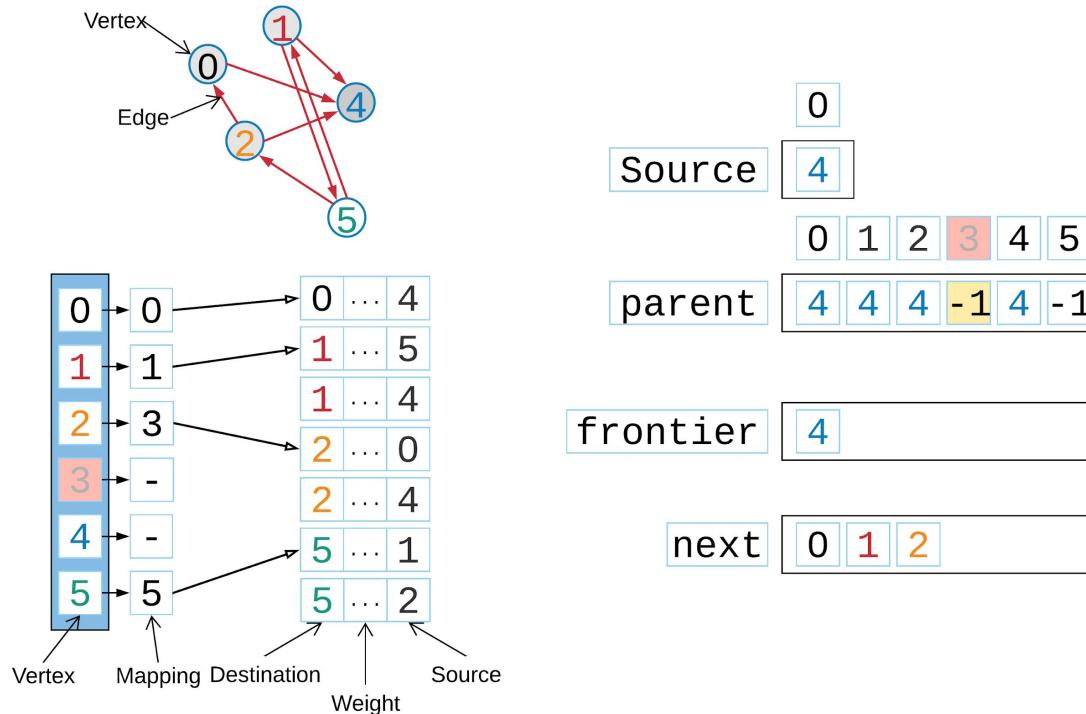
Breadth First Search (BFS) Iteration-1



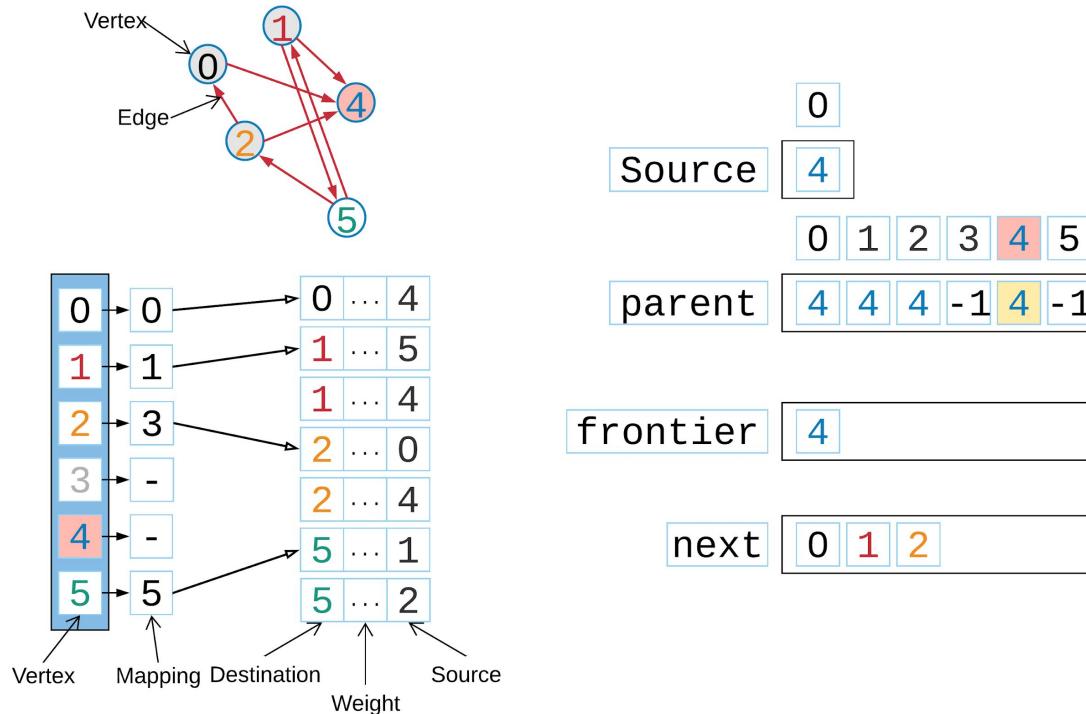
Breadth First Search (BFS) Iteration-1



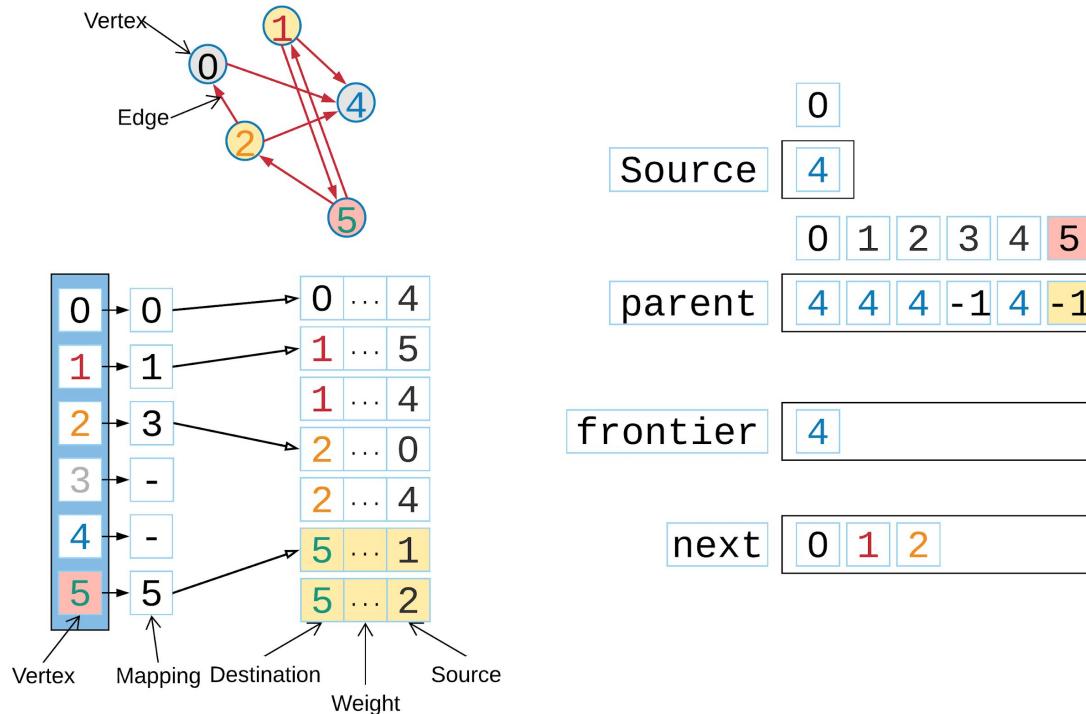
Breadth First Search (BFS) Iteration-1



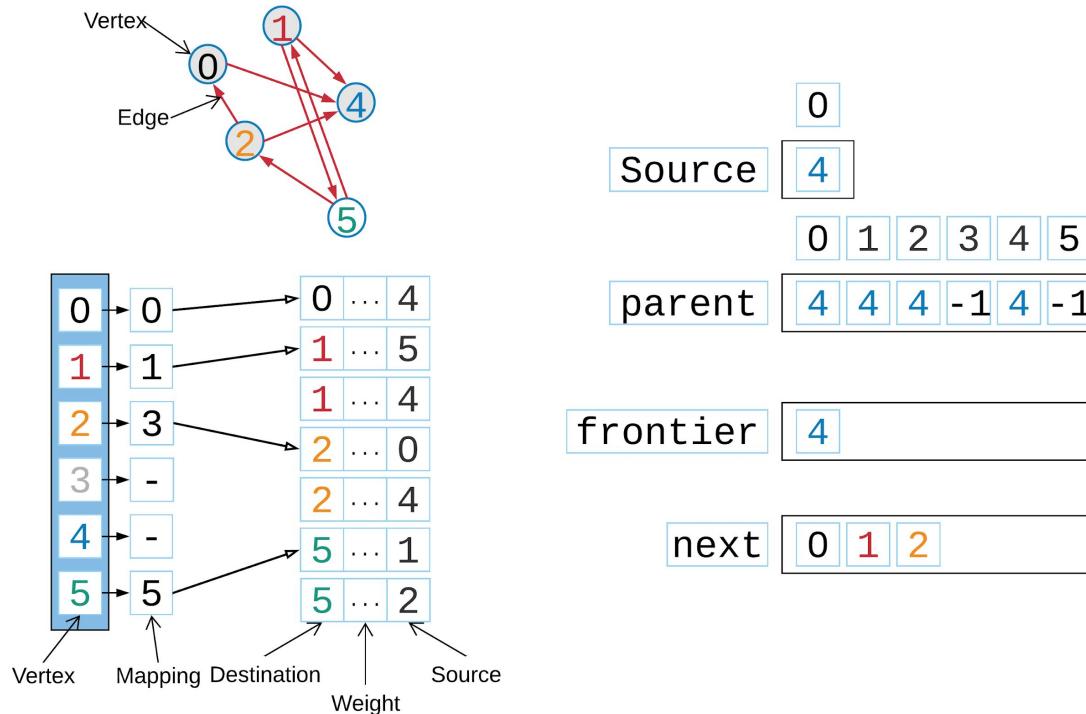
Breadth First Search (BFS) Iteration-1



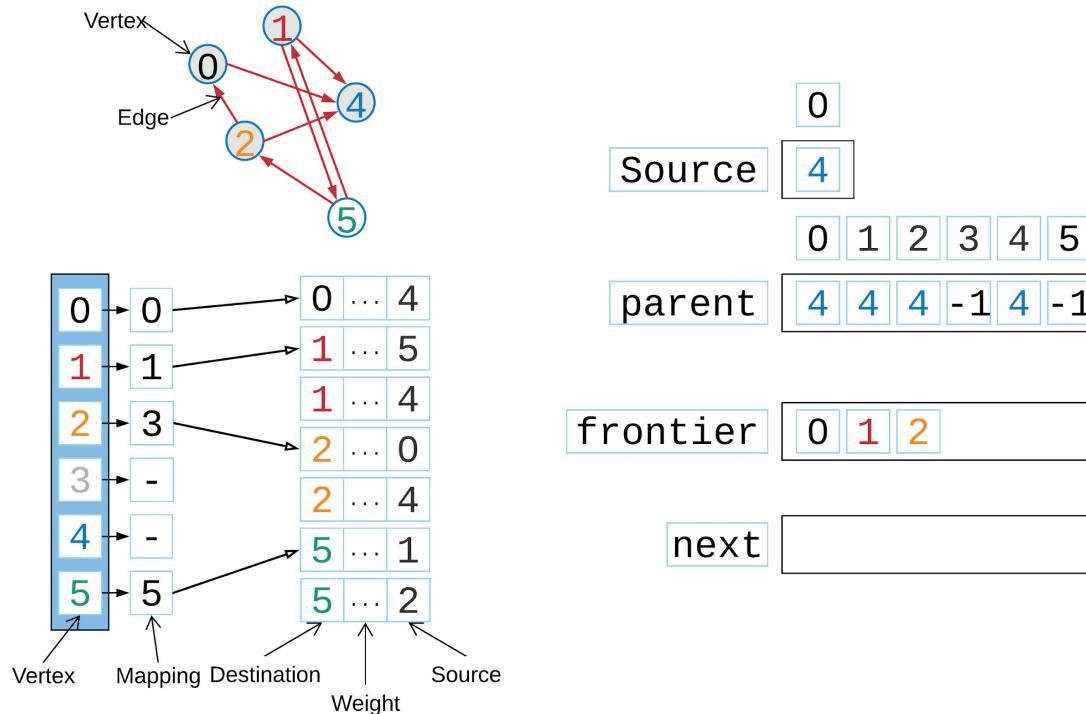
Breadth First Search (BFS) Iteration-1



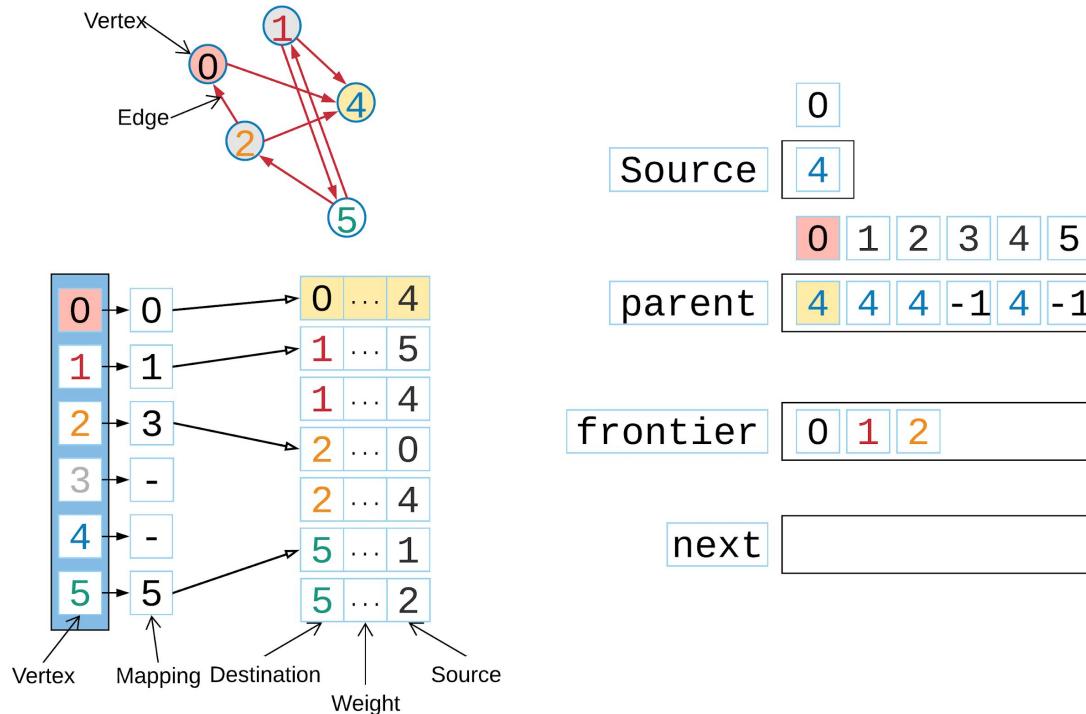
Breadth First Search (BFS) Iteration-1-end



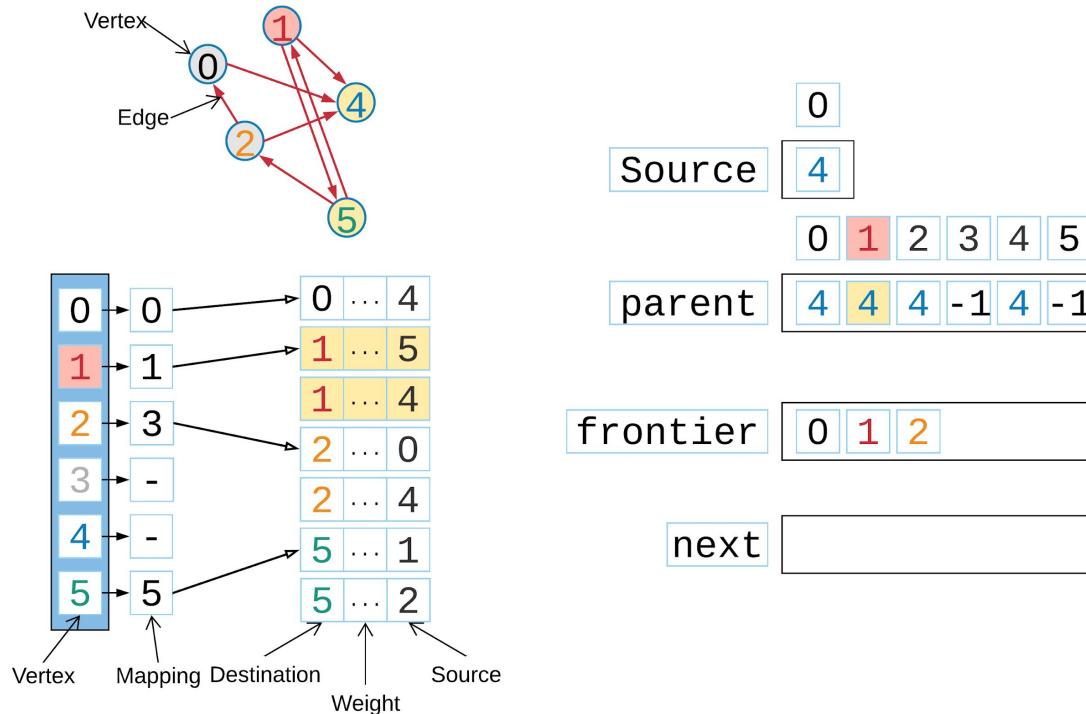
Breadth First Search (BFS) Iteration-2



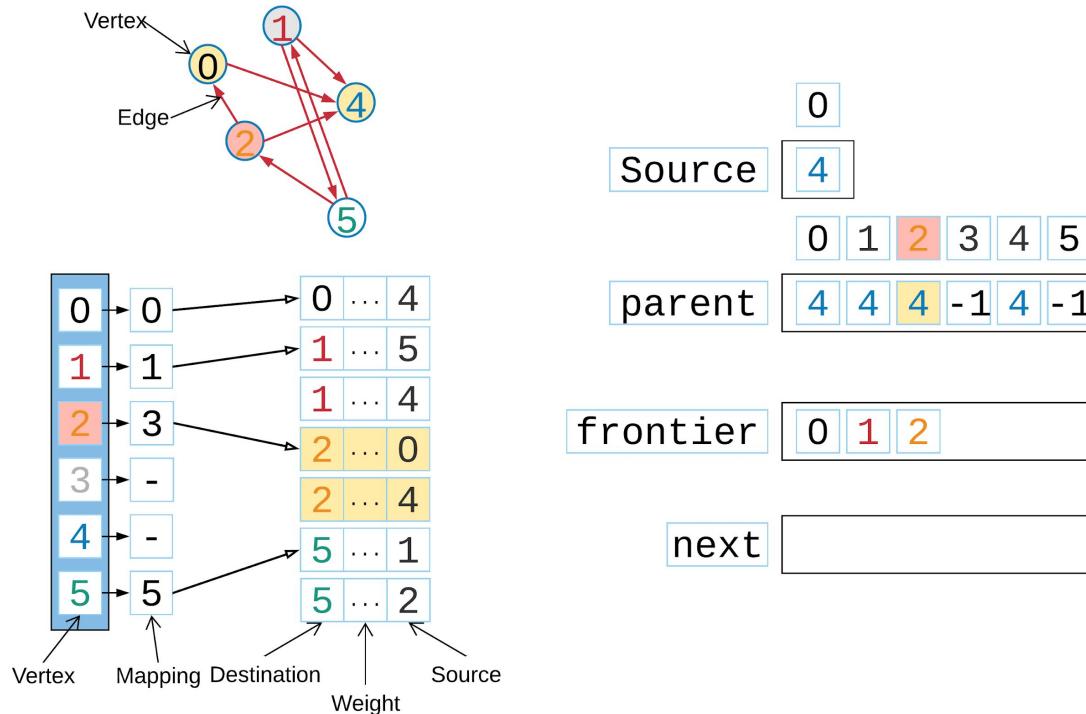
Breadth First Search (BFS) Iteration-2



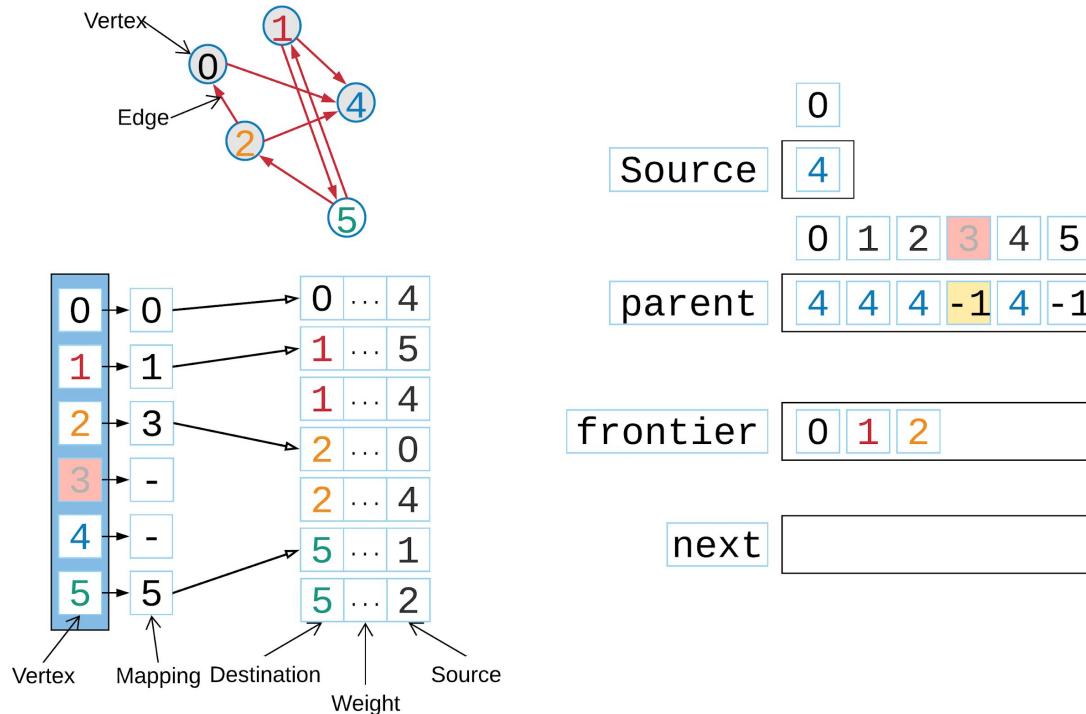
Breadth First Search (BFS) Iteration-2



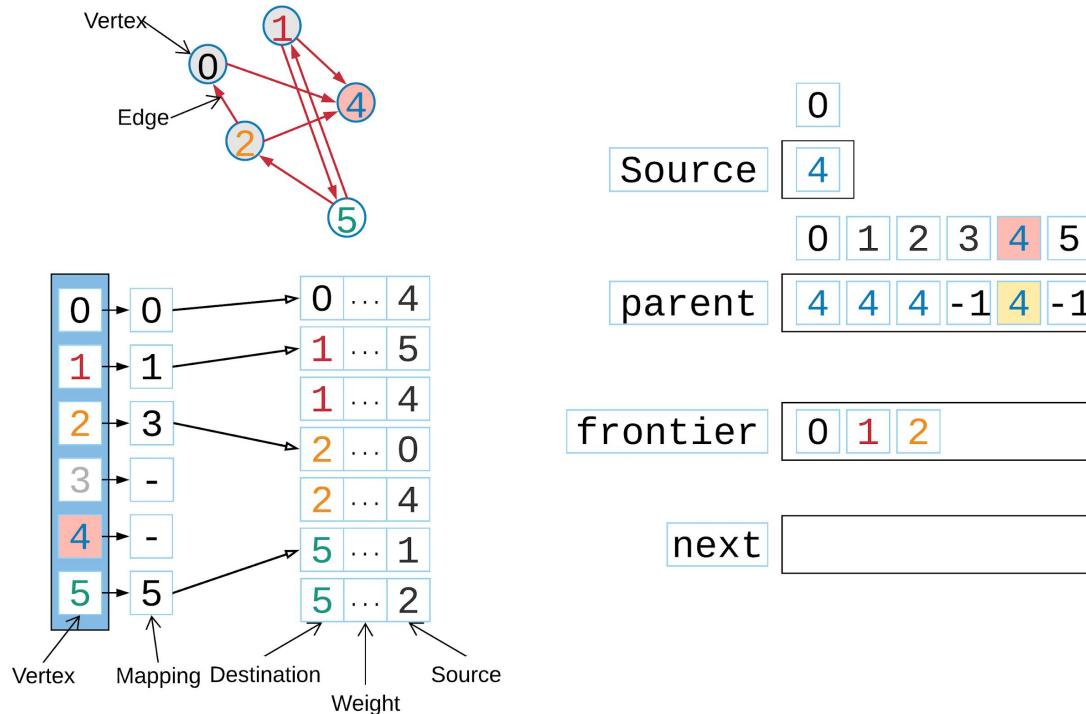
Breadth First Search (BFS) Iteration-2



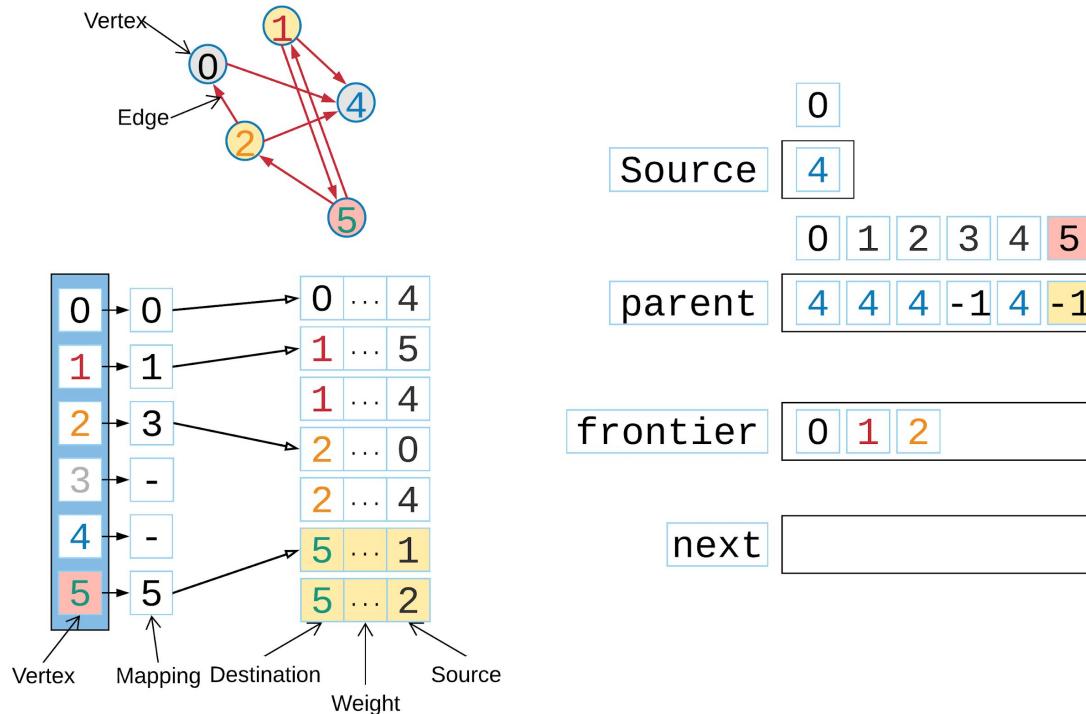
Breadth First Search (BFS) Iteration-2



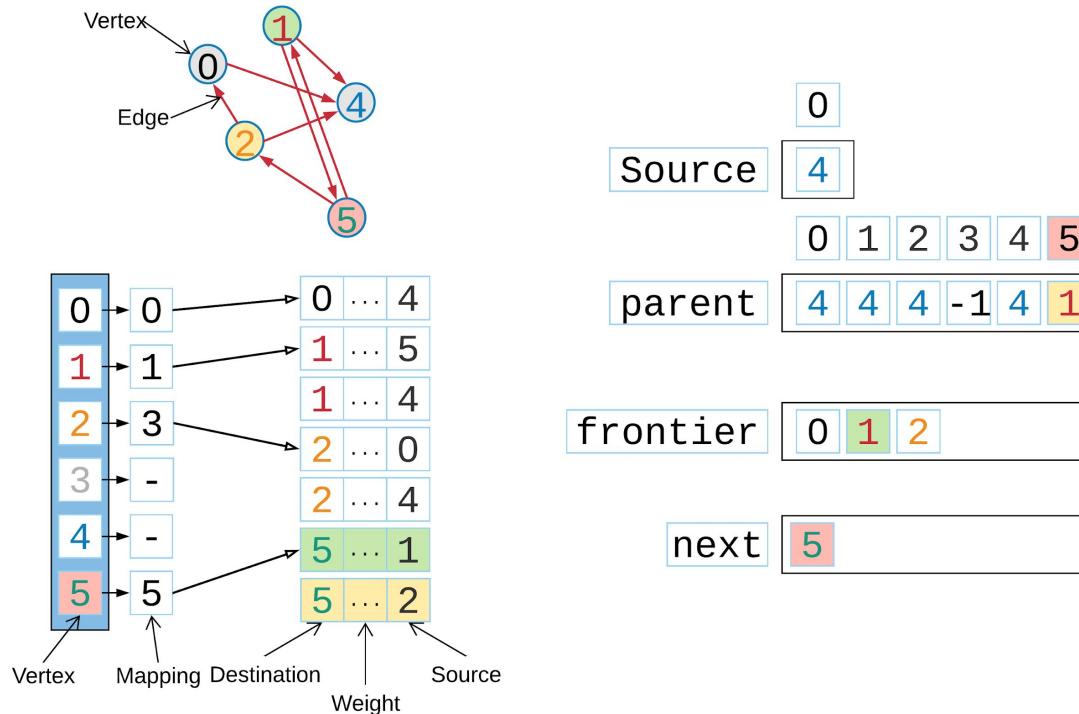
Breadth First Search (BFS) Iteration-2



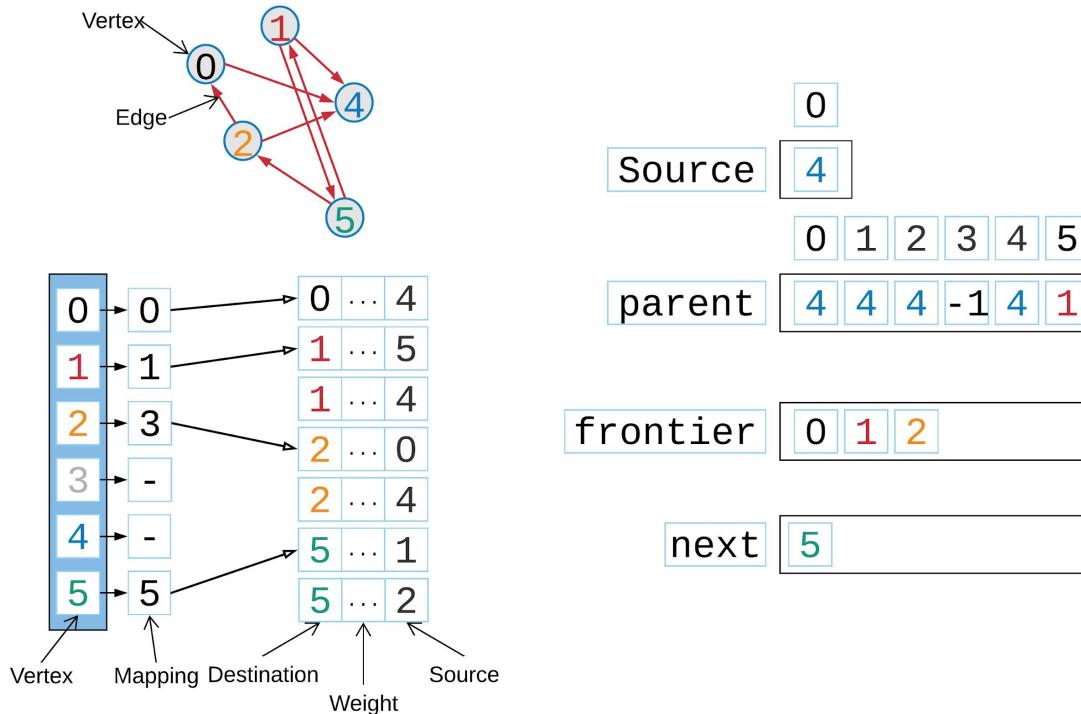
Breadth First Search (BFS) Iteration-2



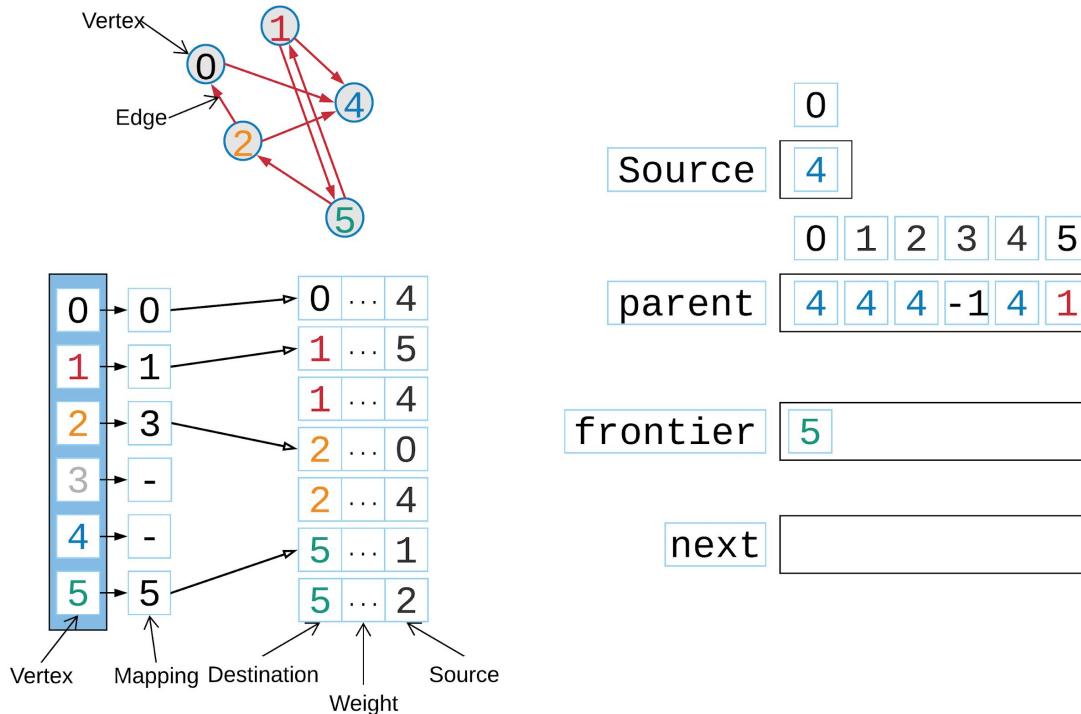
Breadth First Search (BFS) Iteration-2



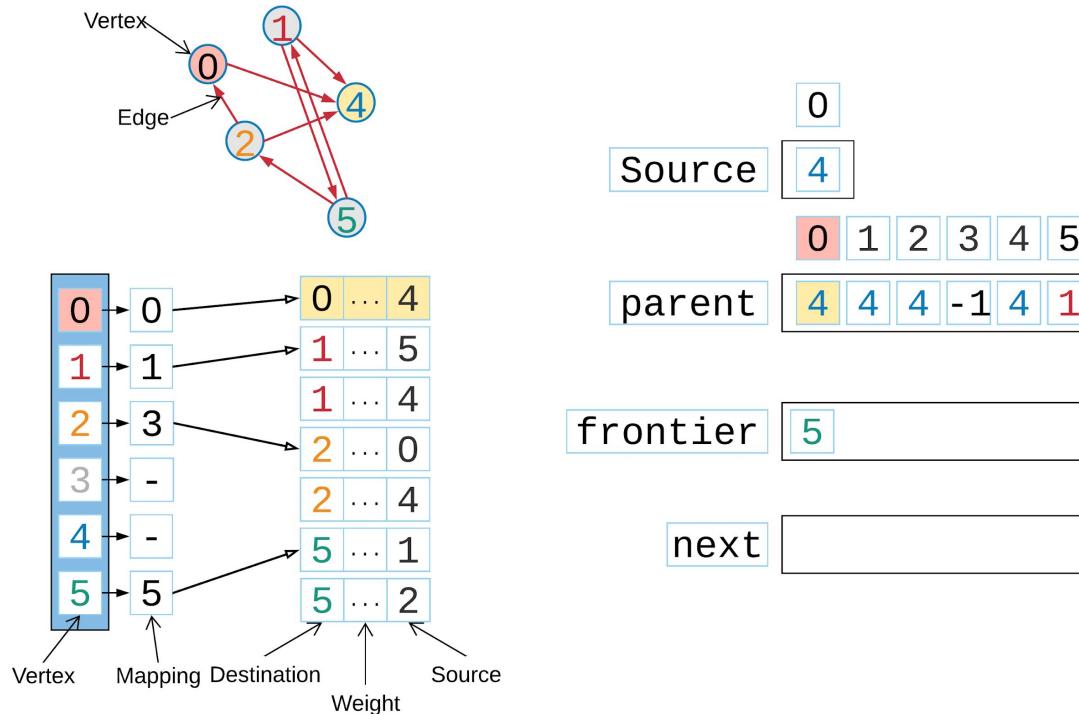
Breadth First Search (BFS) Iteration-2-end



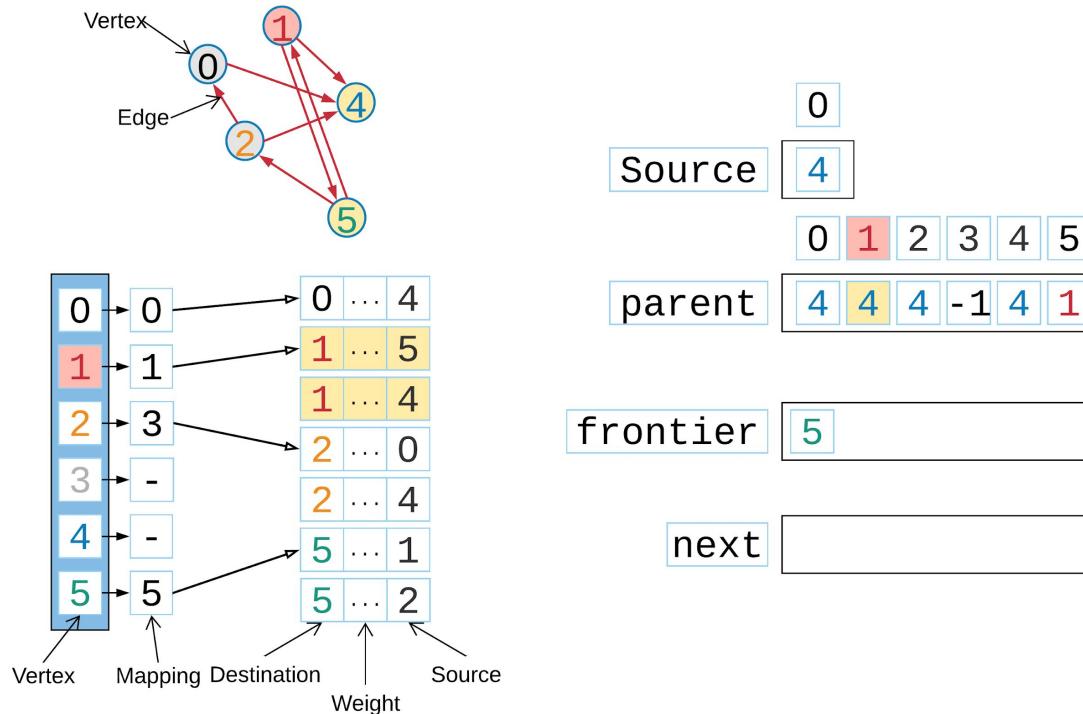
Breadth First Search (BFS) Iteration-3



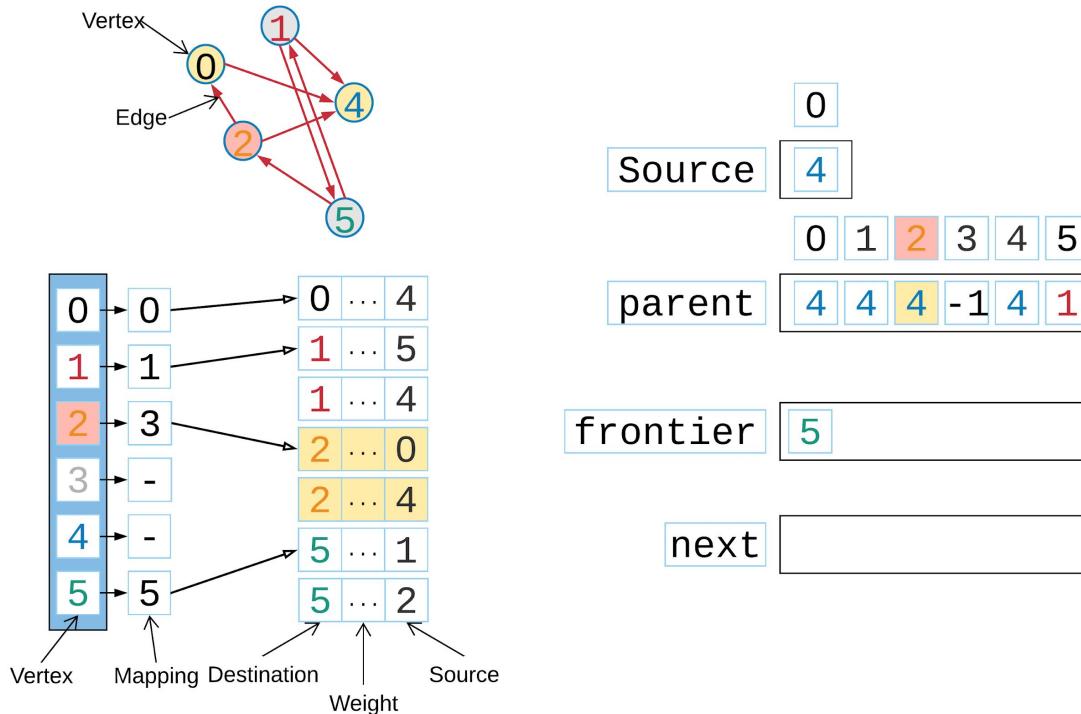
Breadth First Search (BFS) Iteration-3



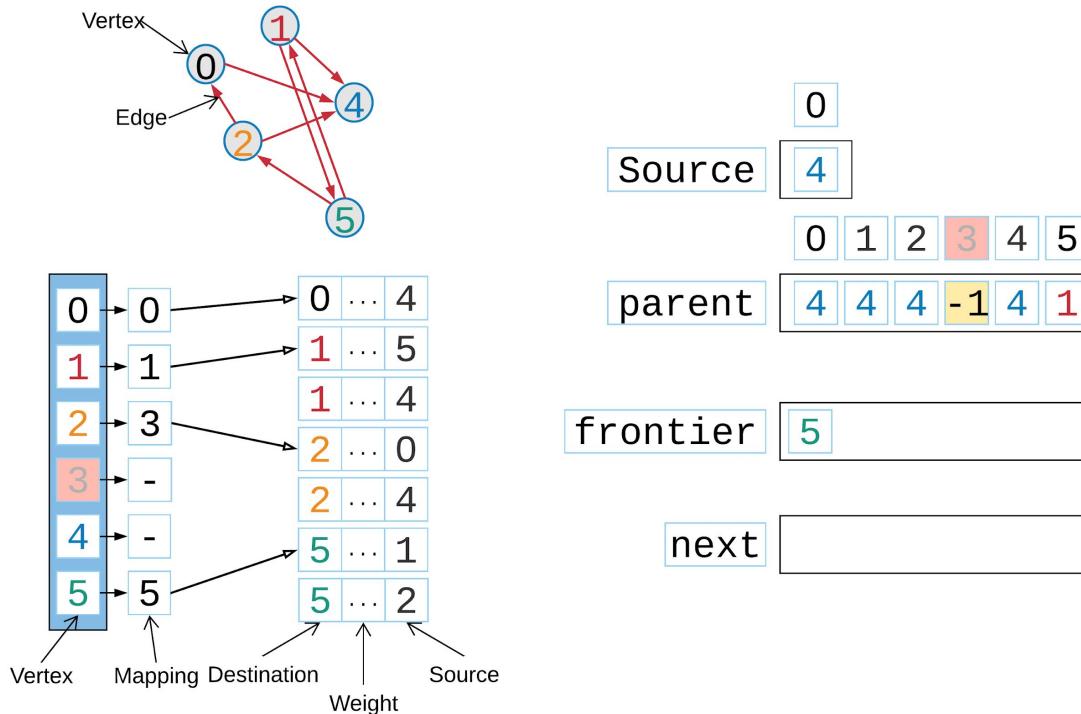
Breadth First Search (BFS) Iteration-3



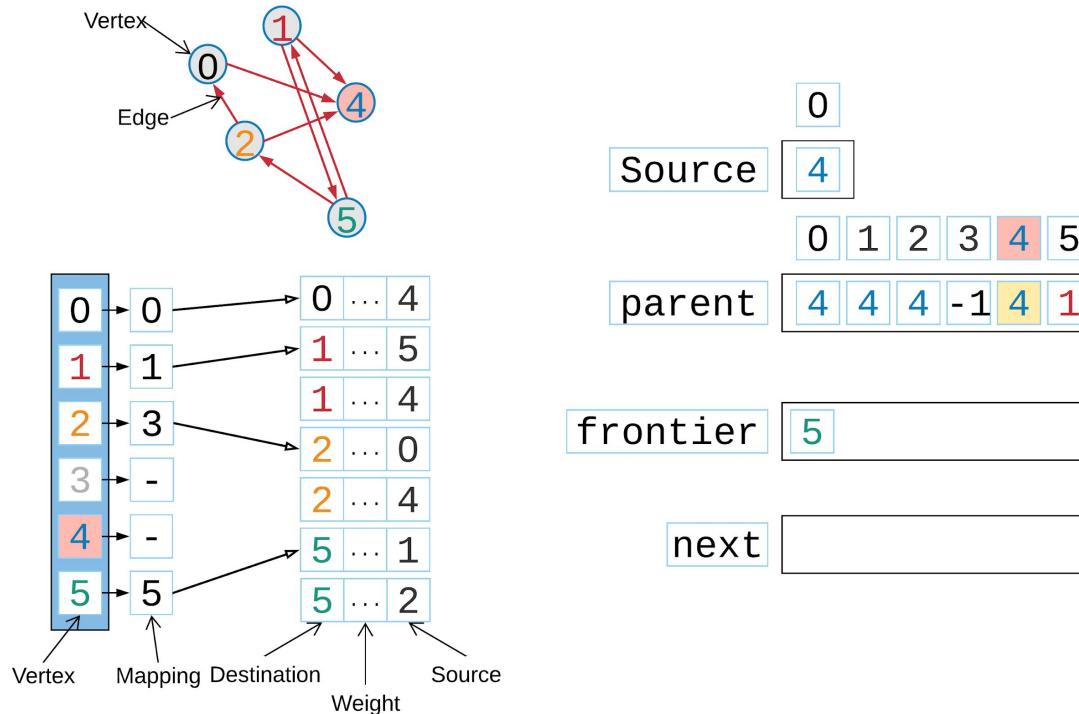
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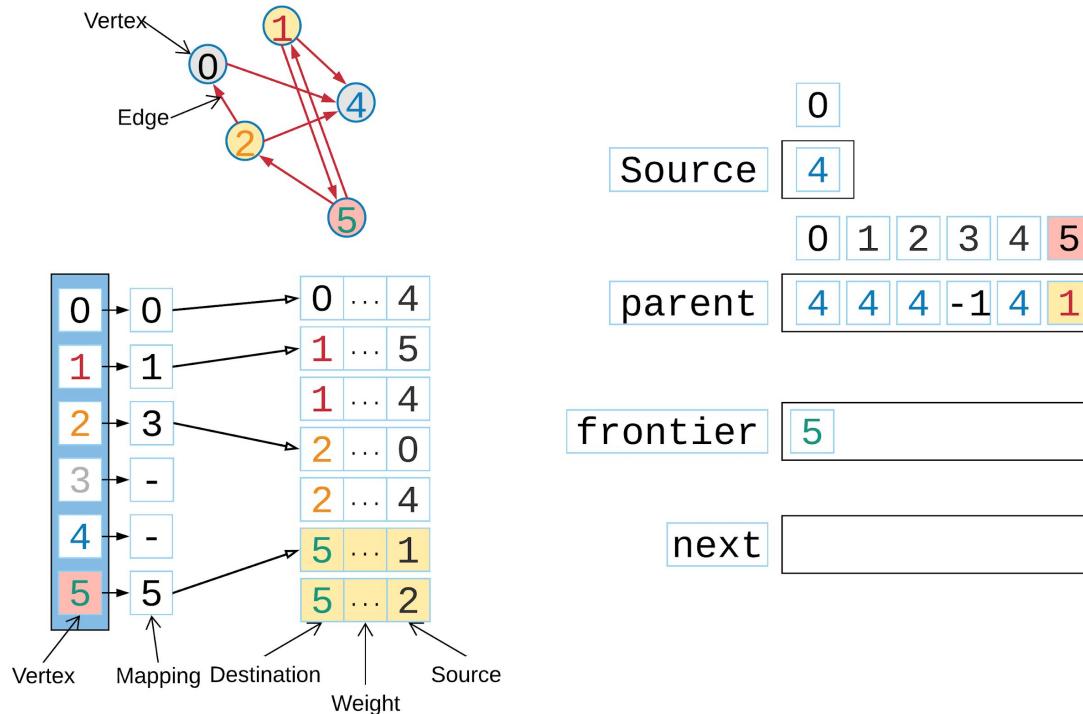
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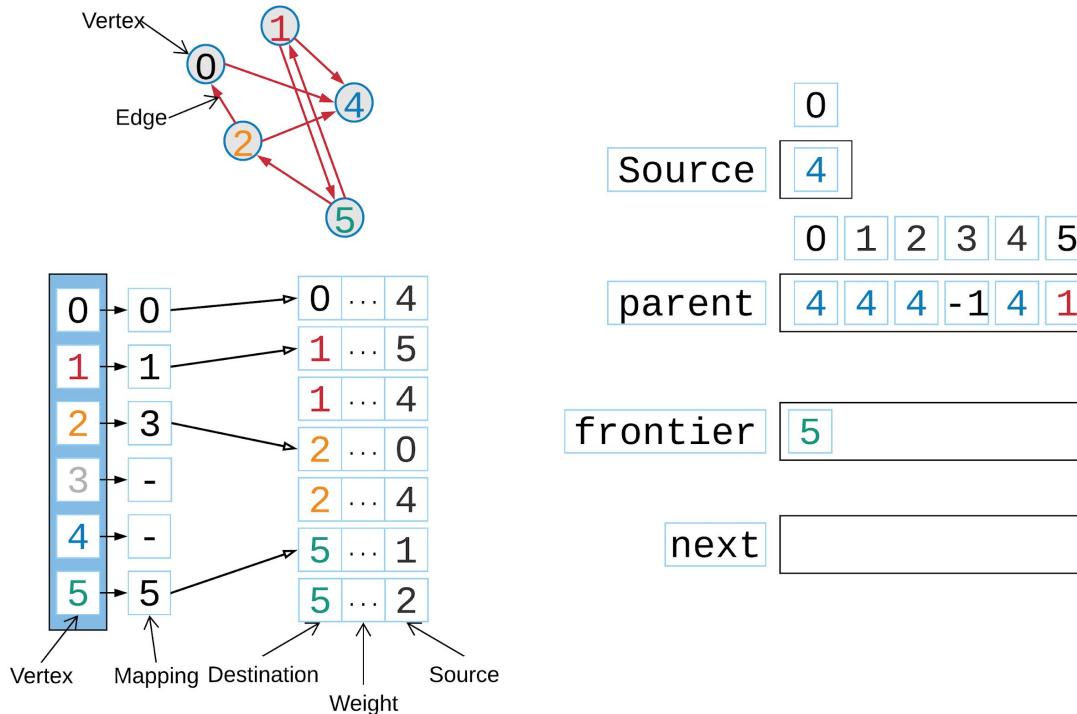
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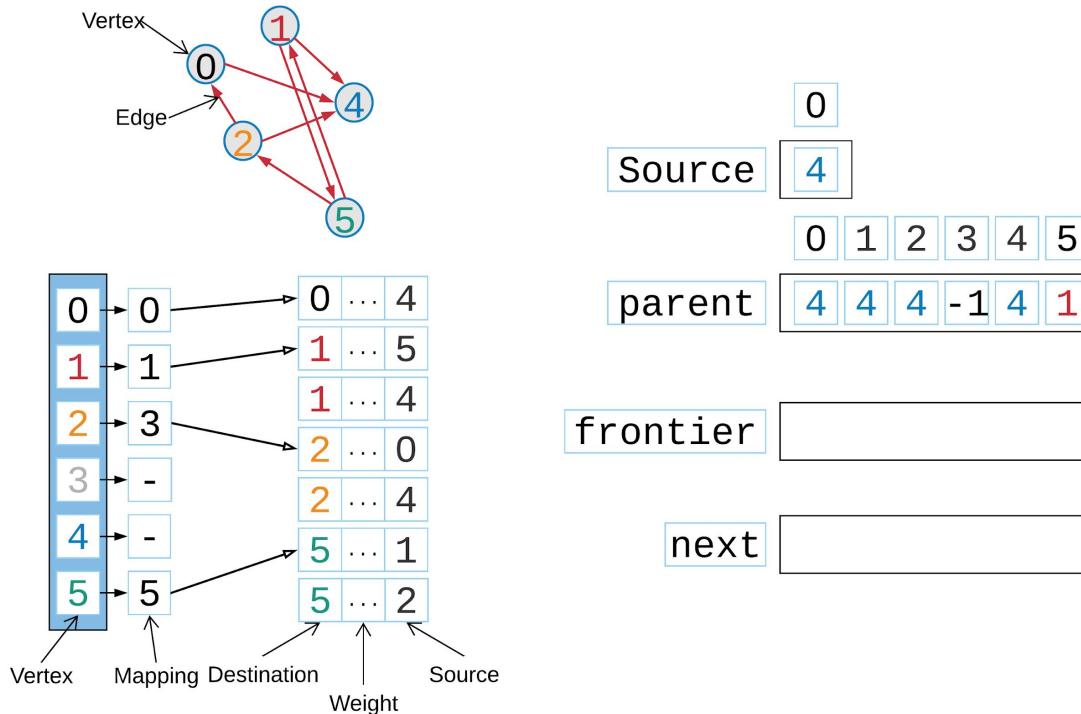
Breadth First Search (BFS) Iteration-3



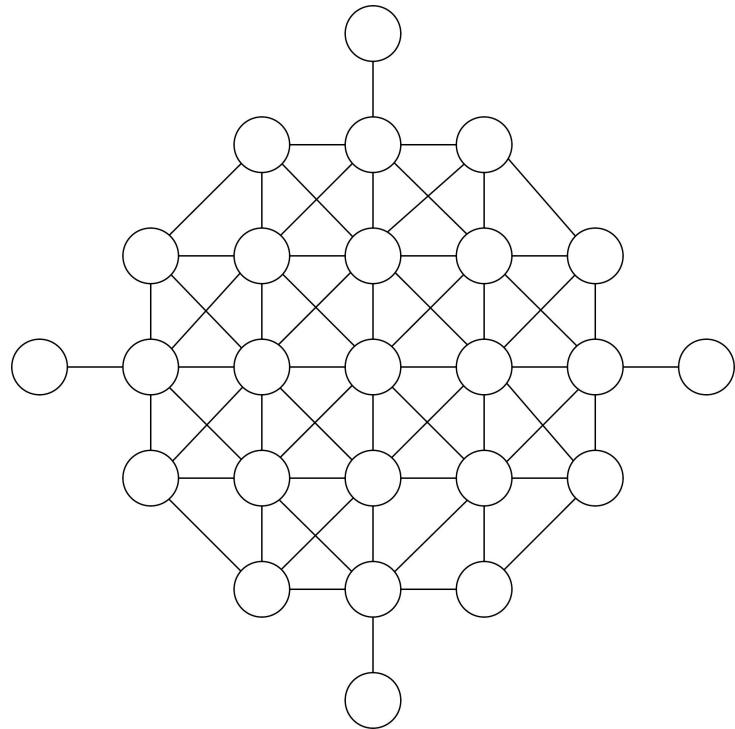
Breadth First Search (BFS) Iteration-end



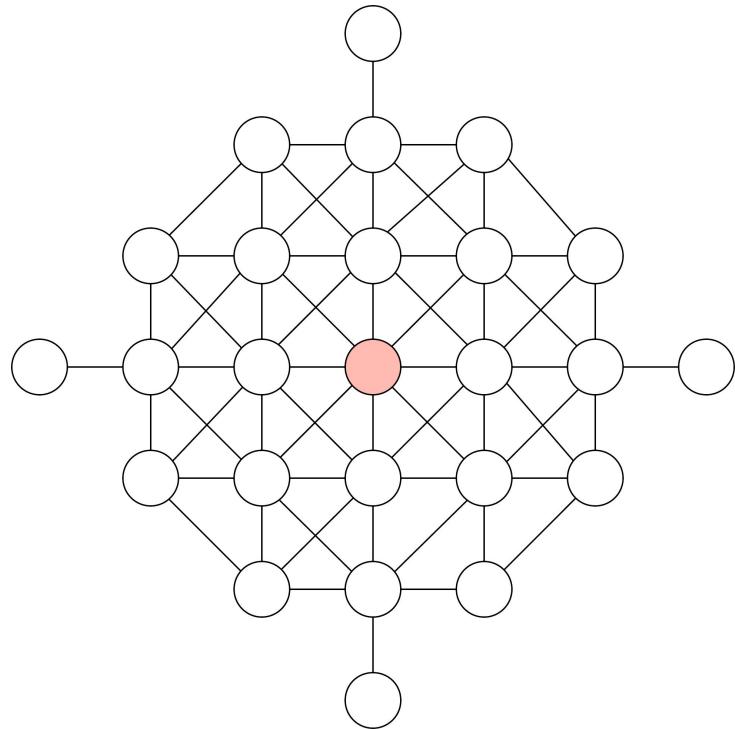
Breadth First Search (BFS) Done



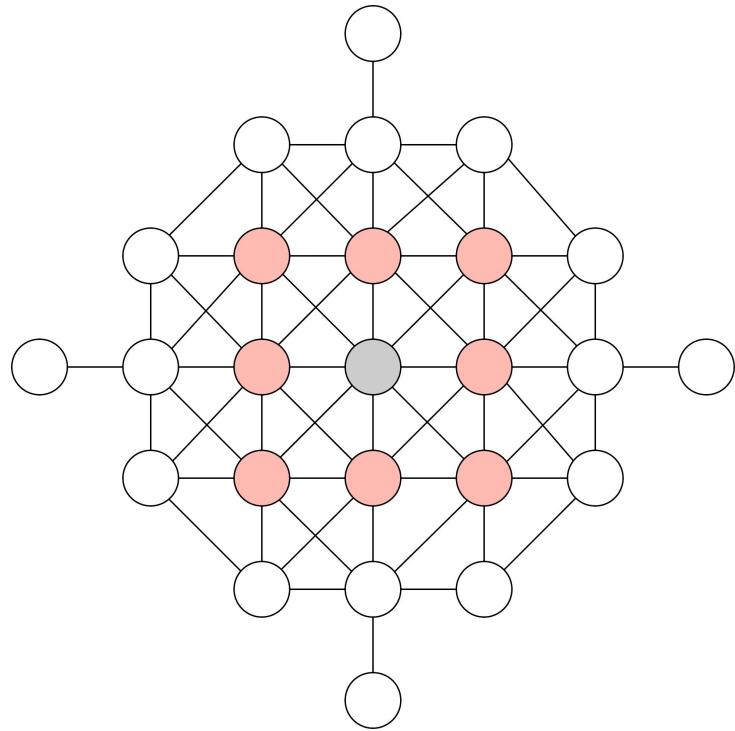
Breadth First Search (BFS)



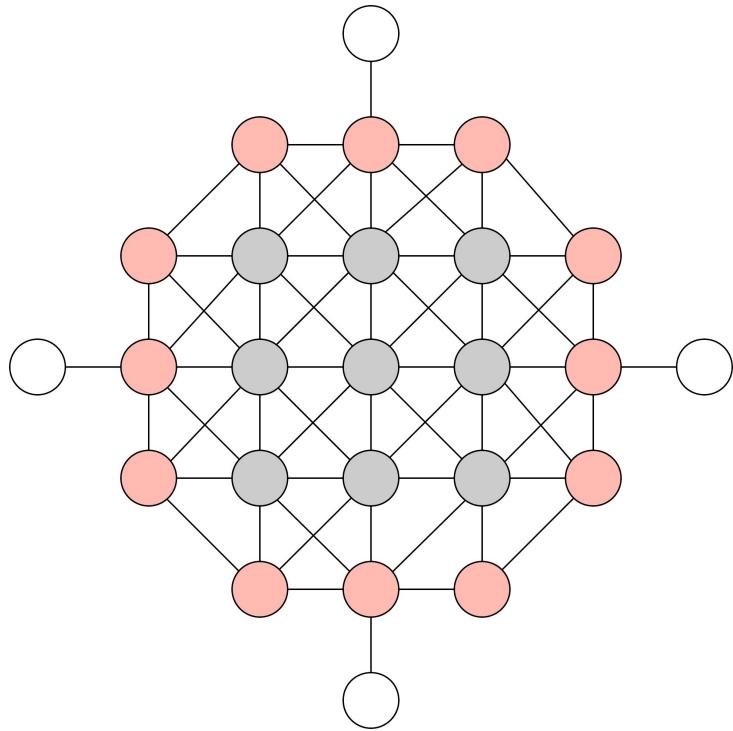
Breadth First Search (BFS)



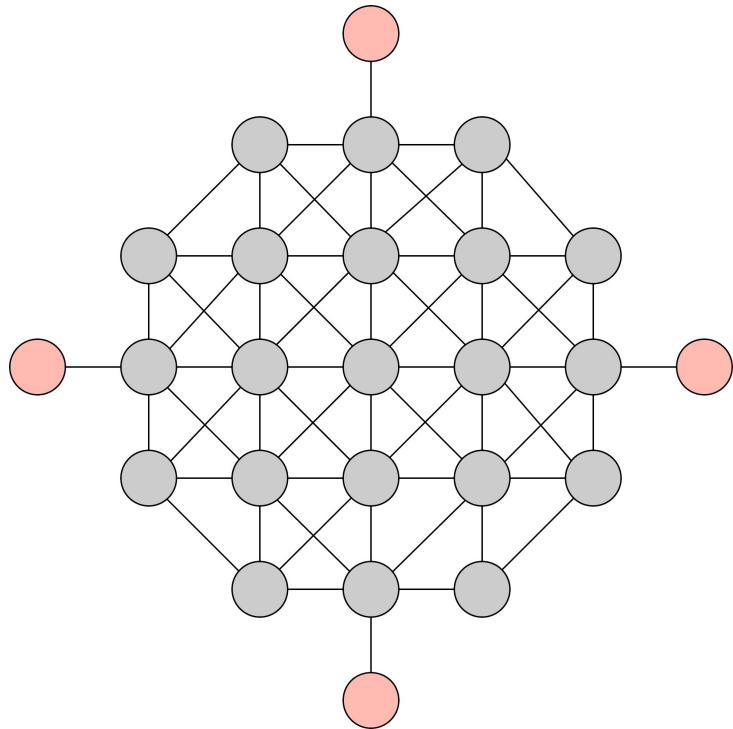
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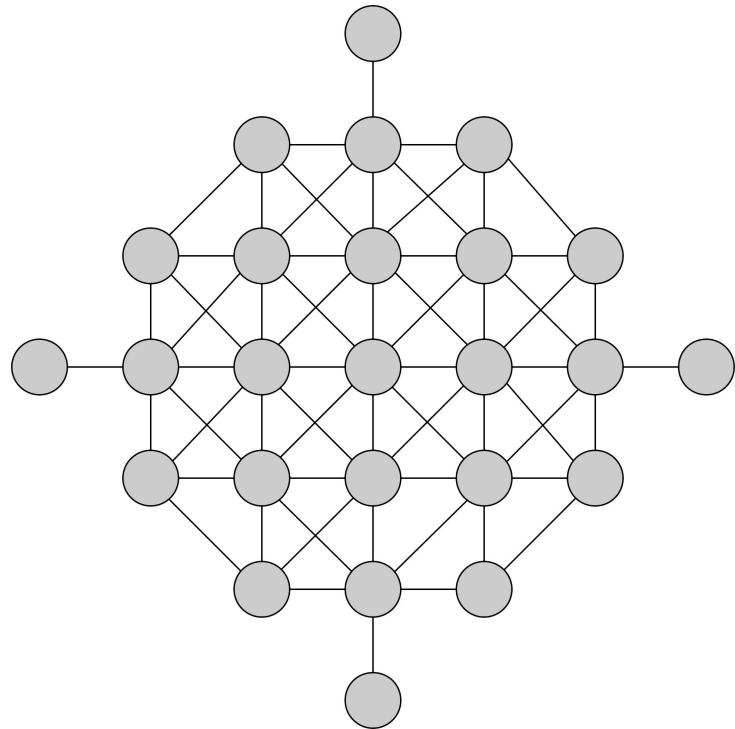
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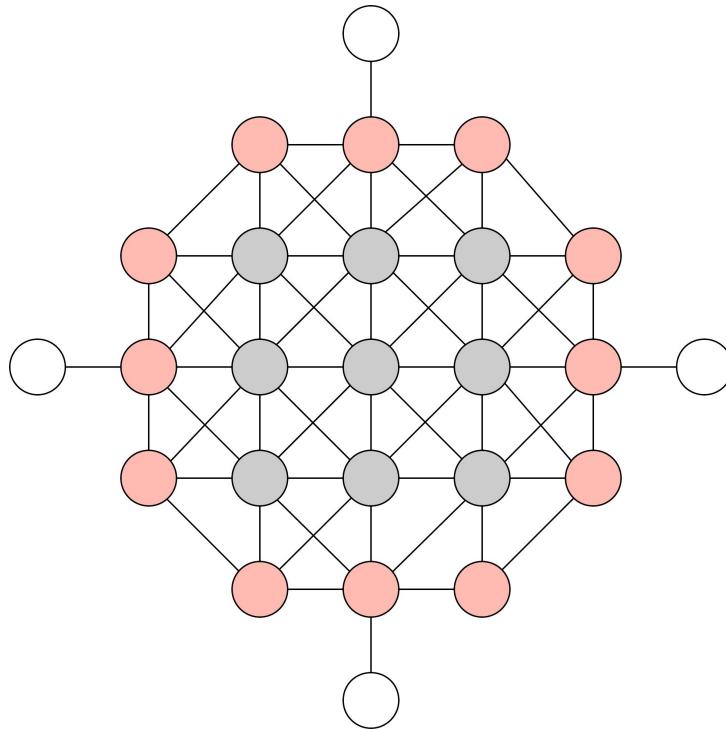
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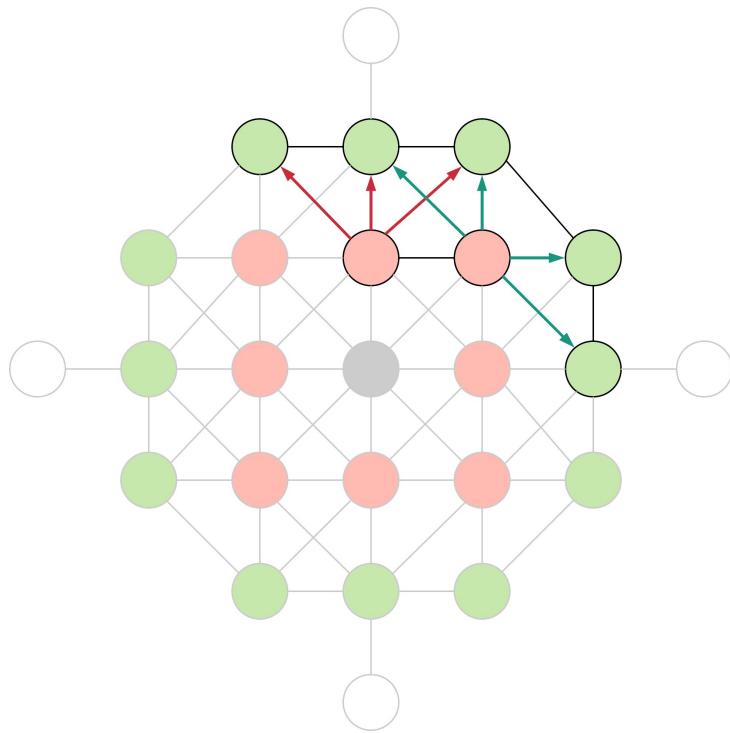
Breadth First Search (BFS)



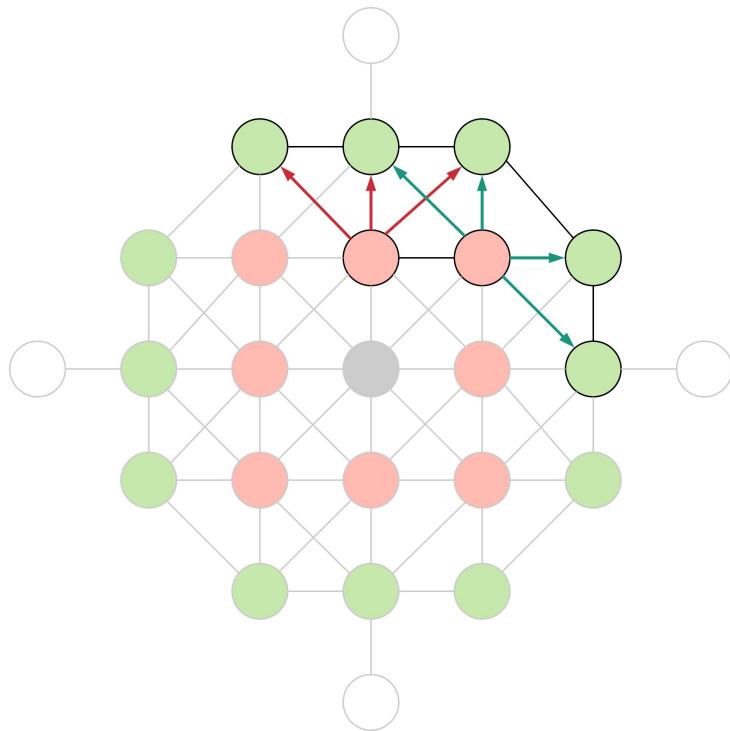
Breadth First Search (BFS) (push)



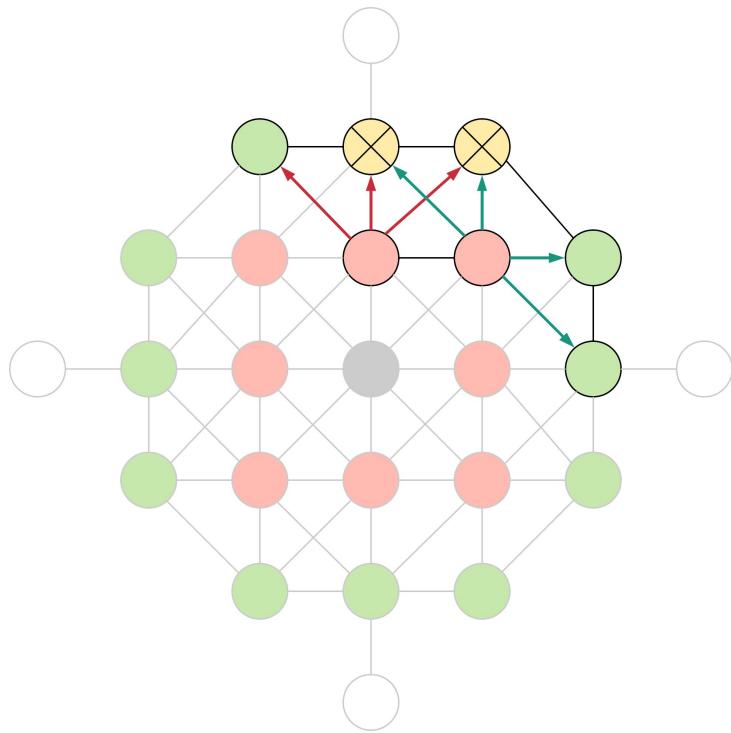
Breadth First Search (BFS) (push)



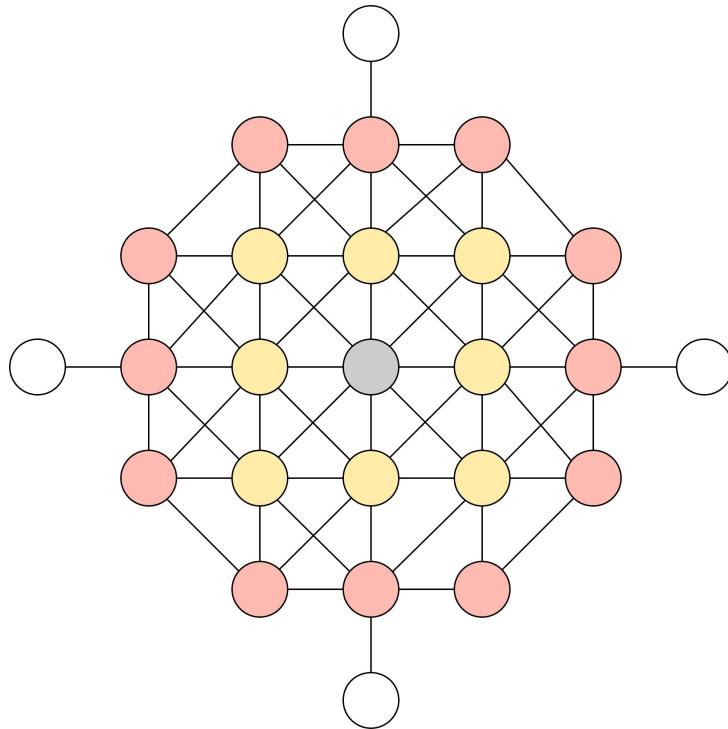
Breadth First Search (BFS) (push)



Breadth First Search (BFS) (push)



Breadth First Search (BFS) (pull)



Breadth First Search (BFS) (pull)

