Case Study 6.1: Mazda price vs age

Tou Ohone Andate - staff number 1234567

Problem

The ages and prices of 123 Mazda cars were collected from the Melbourne Age newspaper in 1991. We want to learn about Mazda prices, and how they decrease with age.

The variables measured are:

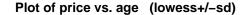
price: Price in Australian \$.
year: Year of manufacture (note that 1990 = 90).

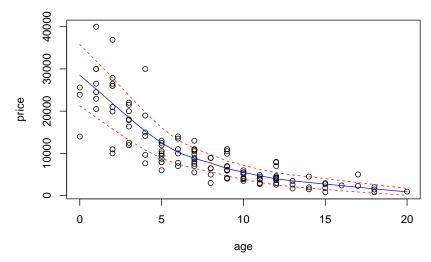
Question of Interest

We want to see how Mazda car prices decrease with age.

Read in and Inspect the Data

```
Mazda.df = read.table("mazda.txt", header = T)
head(Mazda.df)
     year price
## 1
      79 2950
## 2
       82 5900
## 3
       83 2999
## 4
       88 11950
## 5
      82 6100
      90 26500
# We need to creates a new variable called age ourselves
Mazda.df$age = 91 - Mazda.df$year
head(Mazda.df)
     year price age
##
## 1
      79 2950 12
       82 5900
           2999
## 3
       83
                  8
       88 11950
                  3
## 5
       82 6100
                  9
## 6
       90 26500
# Plot these data
trendscatter(price ~ age, data = Mazda.df)
```





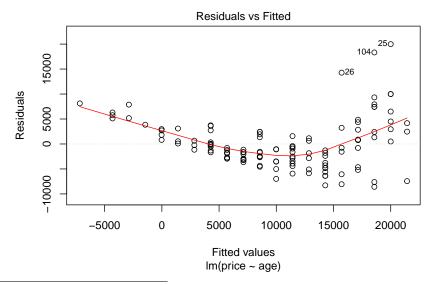
The scatter plot shows a decreasing non-linear relationship. As the age increases, the price decreases - but the rate of decrease is rapid at first, then declines, so also decrease. This suggests an exponentially decreasing relationship.

We also see that the scatter around the trend is not constant: it is higher when the price is higher and lower when the price is lower, so higher centre is associated with higher spread.

Let's fit a naive simple linear model using age for now.¹

Model Building and Check Assumptions

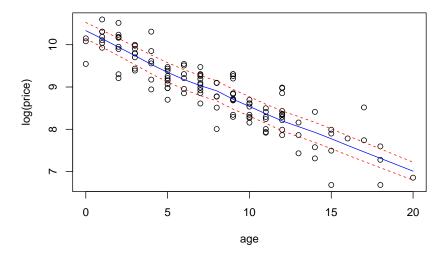
```
PriceAge.fit = lm(price ~ age, data = Mazda.df)
plot(PriceAge.fit, which = 1)
```



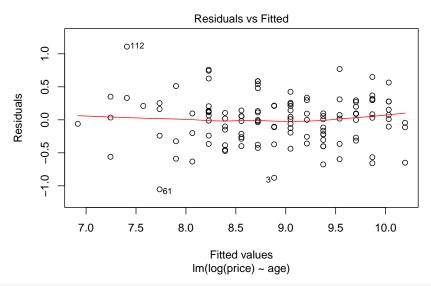
 $^{^{1}}$ In practice, one could omit this step since our assumptions are obviously not valid.

```
trendscatter(log(price) ~ age, data = Mazda.df)
```

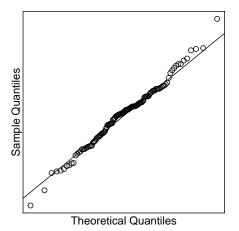
Plot of log(price) vs. age (lowess+/-sd)

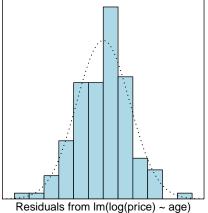


PriceAge.fit2 = lm(log(price) ~ age, data = Mazda.df)
plot(PriceAge.fit2, which = 1)

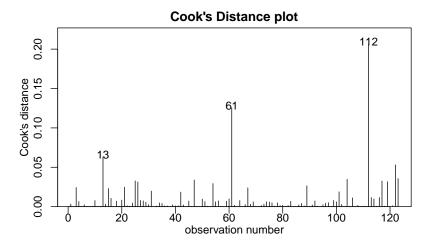


normcheck(PriceAge.fit2)





cooks20x(PriceAge.fit2)



summary(PriceAge.fit2)

```
-0.163915
                           0.007034
                                      -23.3
                                              <2e-16 ***
## age
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3615 on 121 degrees of freedom
## Multiple R-squared: 0.8178, Adjusted R-squared: 0.8163
## F-statistic: 543.1 on 1 and 121 DF, p-value: < 2.2e-16
# Backtransform
exp(confint(PriceAge.fit2))
##
                      2.5 %
                                  97.5 %
## (Intercept) 2.360688e+04 3.036744e+04
## age
               8.370758e-01 8.607164e-01
# Backtransform to % difference
100 * (exp(confint(PriceAge.fit2)) - 1)
##
                       2.5 %
                                    97.5 %
## (Intercept) 2360588.14537 3036644.20481
## age
                   -16.29242
                                 -13.92836
```

Method and Assumption Checks

The scatter plot of age vs price showed clear nonlinearity and an increase in variability with price.

Residuals from a simple linear model showed failed the equality of variance and no-trend assumptions, and so the prices were log transformed. A simple linear model fitted to logged price satisfied all assumptions.

Our final model is

$$log(Price_i) = \beta_0 + \beta_1 \times Age_i + \epsilon_i,$$

where $\epsilon_i \sim iid \ N(0, \sigma^2)$.

Our model explained 82% of the variability in the logged Mazda prices.

Executive Summary

We wanted to see how Mazda car prices decrease with age.

There was clear evidence the price of the cars was exponentially decreasing as the cars got older (P-value \approx 0).

We estimate that the median price for new Mazda cars (in 1991) was between A\$23,600 to A\$30,400 (to the nearest A\$100).

We estimate that each additional year in age results in depreciation of between 13.9% to 16.3%.