

1) Verify that $|+\rangle$ and $|-\rangle$ are eigenstates of X

Ans. All Pauli matrices eigenvalues are +1 and -1. Eigenvalues are $[1/\sqrt{2}, 1/\sqrt{2}]$ and $[1/\sqrt{2}, -1/\sqrt{2}]$

2) What eigenvalues do they have?

Ans. All Pauli Matrices have eigenvalues +1 and -1.

3) Why would we not see these eigenvalues appear on the Bloch sphere?

Ans. The eigenvalues act as a global phase, hence they are not visualized on the Bloch Sphere

4) Find the eigenstates of the Y-gate, and their co-ordinates on the Bloch sphere.

Ans. Eigenvector are $[1/\sqrt{2}, i/\sqrt{2}]$ and $[1/\sqrt{2}, -i/\sqrt{2}]$

Coordinate on Bloch sphere = $[0, 1, 0]$ and $[0, -1, 0]$

5) Write H gate as the outer products of $|0\rangle$, $|1\rangle$, $|+\rangle$, $|-\rangle$

Ans. $H = |+\rangle\langle 0| + |-\rangle\langle 1|$

6) Write Y as a combination of H, X and Z gate(ignoring global phase)

Ans. $Y = HZXH$

7) If we initialise our qubit in the state $|+\rangle$, what is the probability of measuring it in state $|-\rangle$?

Ans. 0. Since $|+\rangle = 1/\sqrt{2} (|0\rangle + |1\rangle)$ whereas $|-\rangle = 1/\sqrt{2} (|0\rangle - |1\rangle)$, hence it results in zero.

8) Use Qiskit to display the probability of measuring a $|0\rangle$ qubit in the states $|+\rangle$ and $|-\rangle$

(Refer code file attached)

9) Try to create a function that measures in the Y-basis

(Refer code file attached)

10) What are the eigenstates of I gate?

Ans. Eigenvalue is 1, and since I gate leaves all states unchanged, all states are eigenstates.