Musical Dice Game Waltzes I

based on

Der allezeit fertige Polonoisen- und Menuettencomponist (1757)

by Johann Philipp Kirnberger

compiled by I. T. Author



Musical Dice Game Waltzes I

based on

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Wonders of the Musical World Series 3



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1 Introduction¹

"Der allezeit fertige Polonoisenund Menuetten-componist" "The
Ever-Ready
Polonaise
and
Minuet Composer"

Thus is the German title (and its English translation) of the earliest of Musical Dice Games (MDG). Rightly and interestingly so, as the Instructions provided in the published work allow a non-professional musician to generate ("compose") up to $6^{32} = 7,958,661,109,946,400,884,391,936$ or nearly eight (8) septillion minuet-trios of which $6^{27} = 1,023,490,369,077,469,249,536$ or about one (1) sextillion are unique (see Subsection 2.2 for more details).

A Musikalisches Würfelspiel (German for "musical dice game" or MDG) is a system for randomly "generating" (e.g., by using a die or two dice) musical compositions from precomposed options and was quite popular throughout Western Europe in the 18th century. Aside from Kirnberger's Der allezeit fertige Polonoisen- und Menuettencomponist (1st ed. 1757; rev. 2nd ed. 1783), other well-known composers that are to known to have composed (or have been attributed the composition of) a MDG are Wolfgang Amadeus Mozart (Anleitung zum Componieren von Walzern so viele man will vermittelst zweier Würfel, ohne etwas von der Musik oder Composition zu verstehen—German for "Instructions for the composition of as many waltzes as one desires with two dice, without understanding anything about music or composition"), C.P.E. Bach (Einfall, einen doppelten Contrapunct in der Octave von sechs Tacten zu machen, ohne die Regeln davon zu wissen (1758); translated from German as "A method for making six bars of double counterpoint at the octave without knowing the rules") and Abbé Maximillian Stadler (Table pour composer des minuets et des Trios à la infinie; avec deux dez à jouer (1780); translated from French as "A table for composing minuets and trios to infinity, by playing with two dice").

Musikalisches Würfelspiel K. 516f (1787), another title for the MDG attributed to Mozart and is the most famous of MDGs, was first published by J.J. Hummel in 1793 in Berlin, and was republished in 1796 by Nikolaus Simrock in Bonn (as K. 294d or K. Anh. C 30.01). Simrock attributed this work to Mozart and it may have been based on Mozart's manuscript K. 516f, written in 1787, consisting of numerous two-bar fragments of music, that appear to be some kind of game or system for constructing music out of two-bar fragments, but contains no instructions nor hints as to the use of dice. Antt about online article by Hideo Noguchi offers a possible explanation for this attribution.

This book is a collection of 28 MDG minuet-trios generated according to the rules given in *Der allezeit fertige* (we will refer to this MDG in this manner from here onward). The scores of the generated minuettrios, that were initially written in using theidi abc environment of Chris Walshaw, were converted to Scalar Vector Graphics (SVG) images (with corresponding MIDIs) by using abcm2ps and abcmidi, and were then pre-processed with Inkscape to be included in IATEX to produce this book.

2 Der allezeit fertige

2.1 Rules

The Rules provided in *Der allezeit fertige* generate MDG minuets-trios consisting of 32 bars (or measures), 16 bars each for the minuet and trio sections. For each of these two sections, the first eight (8) bars are played then repeated. The last eight bars are then similarly played. Finally, the 16 bars of the minuet are again played but without repeats for each set of 8 bars.

The following Rules are followed for generating each minuet:

1. For each bar from the first to the 16th, a regular six-sided die is tossed and the face that comes up is obtained. Hence, 16 one-die tosses (with possible outcomes from the set {1, 2, 3, 4, 5, 6, }), a toss of a die for each bar, are needed to generate a minuet section.

¹The information contained in the introduction were culled from the following online resources: Wikipedia: *Musikalisches Würferspiel* (2017), https://opus-infinity.org/, and Mozart's Melody Machine (Peterson, 2001)

- 2. Table 1(a) is then used to determine which bar number from the Table of Measures for Minuets (Figures 1 to 2) is to be used for obtaining the notes—based on the outcome of each one-die toss—for the particular bar of the minuet-to-be-generated. The possible outcomes of a die toss (1 to 6) are given on the left-hand side (stub items) of Table 1, while the bar numbers of the minuet-to-be-generated are given on the top of that table (captions or column headings).
- 3. For example, suppose for bar 1, the outcome of the two-dice toss is 5. If we now look for bar number 1 at the top of Table 1 and for the outcome 5 on the left-hand side of that table, we obtain 43 as the measure number of the Table of Measures for Minuets (see Figure 1) to be used for obtaining the notes to be played for the first bar of the minuet-to-be-generated. Similarly, an outcome of 4 for the one-die toss for bar 9 of the minuet-to-be-generated leads us to obtain the notes from bar 95 of the Table of Measures for Minuets (see Figure 2).

The following Rules are followed for generating each trio:

- 1. For each bar of the trio, from the first bar to the 16th, a die is tossed. Hence, 16 one-die tosses with possible outcomes from the set {1, 2, 3, 4, 5, 6}, a toss of a die for each bar, are needed to generate a trio.
- 2. Table 1(b) is then used to determine which bar number from the Table of Measures for Trios (Figures 3 to 4) is to be used for obtaining the notes, based on the outcome of each die toss, for the bar of the trio corresponding to that one-die toss. The possible outcomes of a toss of a die (1 to 6) are given on the left-hand side (stub items) of Table 1(b), while the measure numbers of the minuet-to-be-generated are given on the top of that table (captions or column headings).
- 3. For example, suppose for bar 1, the outcome of the one-die toss is 3. If we now look for measure number 1 at the top of Table 1 and for the outcome 3 on the left-hand side of that table, we obtain 8 as the bar number of the Table of Measures for Trios (see Figure 3) to be used for obtaining the notes to be played for the first measure of the trio-to-be-generated. Similarly, an outcome of 1 on the one-die toss for bar 9 of the trio-to-be-generated leads us to obtain the notes from bar 94 of the Table of Measures for Trios (see Figure 5).

2.2 Table for finding Measure Number from Table of Measures

The table given here (Table 1) combines the two tables given on pages 9 and 10 of *Der fertige allezeit* but the contents are exactly as given there with the roles of the rows and columns switched. The leftmost column contains the possible one-die outcomes while the topmost row contains the bar number for the MDG minuet/trio to be generated.

	(a) Measure Number of Minuet																
		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
	1	23	77	62	70	29	83	59	36	33	60	21	14	45	68	26	40
D	2	63	54	2	53	41	37	71	90	55	46	88	39	65	6	91	81
i	3	79	75	42	5	50	69	52	8	4	12	94	9	25	35	66	24
е	4	13	57	64	74	11	3	67	73	95	78	80	30	1	51	82	16
1	5	43	7	86	31	18	89	87	58	38	93	15	92	28	61	72	85
	6	32	47	84	20	22	49	56	48	44	76	34	19	17	10	27	96
							(b)	Measi	ıre N	umber	of T	Γrio					
		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
	1	81	57	67	2	90	41	24	56	94	47	62	72	25	64	48	87
D	2	78	45	30	65	14	33	10	73	40	55	46	17	31	85	11	76
i	3	8	69	26	53	43	95	88	63	79	5	3	60	54	21	42	82
e 1	4	84	6	4	22	51	12	83	92	58	93	66	23	15	13	27	32
_																	
	5	39	28	18	35	89	75	61	96	7	91	70	1	74	44	52	50

Table 1: Measure number to be looked-up in the Table of Measures (see Figures 1, 2, 3, 4, and 5 in Section 2.3) corresponding to each one-die outcome per bar for the minuet and trio. Measure number in **bold blue font** indicates identical measures under that column (see https://opus-infinity.org for more info).

Although the body of Table 1 includes $6 \times 16 + 6 \times 16 = 192$ bar numbers, the Tables of Measures for Minuets and Trios (Figures 1 to 4) contain only $6 \times 14 + 6 \times 13 + 5 = 167$ different measures. This is so since in Table 1: a) for the minuet bars, all the measures under bar 8 and all the measures under bar 16 are identical giving only two (2) unique measures; b) for the trio bars, all the measures under bar 7 and all the measures under bars 15 and 16 are identical, giving three (3) unique measures; c) there are six (6) different measures for each of the remaining 14 bars of the minuet and six (6) diffrent measures for each of the remaining 13 bars of the trio: $6 \times 14 + 6 \times 13 = 162$ additional bars. These also explain why the total number of unique minuet-trios that can be generated is $(6^{14} \times 6^{13} \times 1 \times 1 \times 1 \times 1 \times 1) = 6^{27}$.

2.3 Table of Measures

Der allezeit fertige Polonoisen und Menuettencomponist (Minuet)

 $[\textbf{from} \ \texttt{https://imslp.org/wiki/Der_allezeit_fertige_Polonoisen-_und_Menuettencomponist_(\texttt{Kirnberger\%2C_Johann_Philipp)}]$

Johann Philipp Kirnberger J = 90

Figure 1: Table of Measures for Minuets (Part I)



Figure 2: Table of Measures for Minuets (Part II)

[from https://imslp.org/wiki/Der_allezeit_fertige_Polonoisen-_und_Menuettencomponist_(Kirnberger%2C_Johann_Philipp)]



Figure 3: Table of Measures for Trios (Part III)



Figure 4: Table of Measures for Trios (Part IV)



Figure 5: Table of Measures for Trios (Part V)

3 Related Links

The following are very interesting sites in that they allow the online rendering of MDGs:

- Mozart A site maintained by Marian Aldenhövel allows the visitor to generate a MDG (user-specified or randomly-generated) and the corresponding audio (midi, wav) and image files (pdf, png) based on Musikalisches Würferspiel, K. 516f.
- Opus Infinity Collaborative work of Robbert Harms, Hein Moors, and Suus van Petegem whose goal is to unravel the mystery behind the tables used for generating MDGs. Site visitors can generate MDGs based on works of Kirnberger, Mozart, Stadler/Haydn, and Bach. Corresponding audio files (mid, ogg, and/or mp3) and image files (pdf or png) are also made available for listening, viewing, or downloading.
- Mozart A site maintained by John Chuang that allows the site visitor to generate MDGs based on the work of Stadler/Haydn.
- mozart.zip This is a Windows software (©1995 VisionSoft) by John Chuang and Stephen Goodwin that generates MDG based on input from user and is available for *free* from Amaranth Publishing.
- "Mozart Musical Game in C K. 516f," Mozart Studies Online The site of Hideo Noguchi that offers an explanation linking Musikalisches Würferspiel, K. 516f, and K. 294d (K. Anh. C 30.01).

4 Acknowledgments

My sincerest gratitude to Chris Walshaw et al. for the ABC music notation; Jean-Francois Moine for abcm2ps and the accompanying examples, templates, and pointers for the appropriate use of these resources; Guido Gonzato for the ABC Plus Project and the abcmidi resources available there, more especially for the ABC resource book Making Music with ABC 2; James R. Allwright and Seymour Shlien for abcmidi source and binaries; Artifex, Inc. for Ghostscript v.10.00.0 (includes the ps2pdf converter); Inkscape v.1.2.2 for the tool for converting SVGs to PDFs for inclusion into IATEX documents; William Schelter for Maxima v.5.47.0—used for computing the permutation number; Colomban Wendling et. al for Geany 2.0 IDE; and User: Martin H for his reply to a TFX / IATFX Stack Exchange question on including SVGs into LATEX documents. Special thanks also to the International Music Score Library Project (IMSLP) for making available the score for Der allezeit fertige Polonoisen- und Menuettencomponist (1757) and Amaranth Publishing for a copy of mozart.zip. Ditto to Machtelt Garrels for the book Bash Guide for Beginners, Vivek Gite for the book Linux Script Shell Tutorial, and Steve Parker for the Unix/Linux Shell Cheatsheet. John Fogarty's GitHub Site: Latex CreateSpace BookCover and Peter Wilson's reply in T_FX / L^AT_FX Stack Exchange on designing a book cover, were sources of ideas, information, and materials for creating the book cover and title page, thanks to both of them; LibreOffice Calc for its use in the image creation of the book cover. Many thanks, too, to the Debian Project for the Debian 12 (Bookworm) GNU/Linux OS, TexLive 2024 for providing the T_FX distribution, and GitHub for its generosity in providing space for the project.

5 Selected Waltzes

$2 \hbox{-} 1 \hbox{-} 3 \hbox{-} 4 \hbox{-} 5 \hbox{-} 2 \hbox{-} 3 \hbox{-} 2 \hbox{-} 3 \hbox{-} 1 \hbox{-} 4 \hbox{-} 3 \hbox{-} 1 \hbox{-} 6 \hbox{-} 3 \hbox{-} 6 \hbox{-} 4 \hbox{-} 6 \hbox{-} 4 \hbox{-} 2 \hbox{-} 2 \hbox{-} 1 \hbox{-} 1 \hbox{-} 4 \hbox{-} 5 \hbox{-} 3 \hbox{-} 6 \hbox{-} 1 \hbox{-} 5 \hbox{-} 1 \hbox{-} 3$

knbgr::63:77:42:74:18:37:52:90:4:60:80:9:45:10:66:96:84:71:4:65:14:41:24:56:58:91:3:29:25:44:48:82::



 $For \ audio \ (midi): \ knbgr-2-1-3-4-5-2-3-2-3-1-4-3-1-6-3-6-4-6-4-2-2-1-1-4-5-3-6-1-5-1-3.mid$

2 - 1 - 4 - 1 - 2 - 2 - 1 - 6 - 4 - 6 - 6 - 5 - 1 - 5 - 3 - 3 - 5 - 2 - 5 - 5 - 3 - 3 - 4 - 1 - 5 - 5 - 5 - 2 - 6 - 4 - 3 - 4

knbgr::63:77:64:70:41:37:59:48:95:76:34:92:45:61:66:24:39:45:18:35:43:95:83:56:7:91:70:17:80:13:42:32::
Perm. No.: 662409663186092164958



 $For \ audio \ (midi): \ knbgr-2-1-4-1-2-2-1-6-4-6-5-1-5-3-3-5-2-5-5-3-3-4-1-5-5-2-6-4-3-4.mid$

$2 \hbox{-} 1 \hbox{-} 5 \hbox{-} 5 \hbox{-} 5 \hbox{-} 6 \hbox{-} 4 \hbox{-} 5 \hbox{-} 2 \hbox{-} 3 \hbox{-} 2 \hbox{-} 1 \hbox{-} 3 \hbox{-} 6 \hbox{-} 6 \hbox{-} 2 \hbox{-} 1 \hbox{-} 1 \hbox{-} 6 \hbox{-} 1 \hbox{-} 4 \hbox{-} 4 \hbox{-} 2 \hbox{-} 5 \hbox{-} 5 \hbox{-} 4 \hbox{-} 3 \hbox{-} 1 \hbox{-} 1 \hbox{-} 5 \hbox{-} 5 \hbox{-} 2$

knbgr::63:77:86:31:18:49:67:58:55:12:88:14:25:10:27:81:81:57:37:2:51:12:10:96:7:93:3:72:25:44:52:76::



 $For \ audio \ (midi): \ knbgr-2-1-5-5-5-6-4-5-2-3-2-1-3-6-6-2-1-1-6-1-4-4-2-5-5-4-3-1-1-5-5-2.mid$

2 - 2 - 1 - 3 - 6 - 3 - 6 - 5 - 4 - 2 - 1 - 4 - 4 - 4 - 6 - 6 - 5 - 2 - 3 - 4 - 2 - 5 - 6 - 1 - 2 - 3 - 4 - 5 - 2 - 3

knbgr::63:54:62:5:22:69:56:48:38:78:88:14:1:51:82:96:59:71:18:65:43:12:10:96:38:47:46:60:15:44:11:82::
Perm. No.: 778010641294556413448



 $For \ audio \ (midi): \ knbgr-2-2-1-3-6-3-6-6-5-4-2-1-4-4-6-6-6-5-2-3-4-2-5-6-1-2-3-4-5-2-3.mid$

2-2-4-6-6-2-6-1-5-3-5-1-3-5-2-1-1-4-4-1-5-5-4-1-4-3-1-2-5-6-3-5



 $For \ audio \ (midi): \ knbgr-2-2-4-6-6-2-6-1-5-3-5-1-3-5-2-1-1-4-4-1-5-5-4-1-4-3-1-2-5-6-3-5.mid$

2 - 2 - 5 - 2 - 6 - 5 - 6 - 3 - 6 - 1 - 5 - 4 - 5 - 2 - 6 - 1 - 1 - 1 - 4 - 3 - 2 - 3 - 2 - 4 - 6 - 5 - 1 - 4 - 3 - 6 - 4 - 6



 $For \ audio \ (midi): \ knbgr-2-2-5-2-6-5-6-3-6-1-5-4-5-2-6-1-1-1-4-3-2-3-2-4-6-5-1-4-3-6-4-6.mid$

2-2-5-4-4-6-1-3-4-2-5-2-6-4-5-4-5-6-4-5-2-5-3-2-6-2-2-1-6-2-3



 $For \ audio \ (midi): \ knbgr-2-2-5-4-4-4-6-1-3-4-2-5-2-6-4-5-4-5-6-4-5-2-5-3-2-6-2-2-1-6-2-3.mid$

2-2-6-2-1-3-6-1-5-6-3-5-2-5-6-2-3-6-2-4-3-6-6-6-4-1-5-4-2-5-3-3



 $For \ audio \ (midi): \ knbgr-2-2-6-2-1-3-6-1-5-6-3-5-2-5-6-2-3-6-2-4-3-6-6-6-4-1-5-4-2-5-3-3.mid$

2 - 2 - 6 - 5 - 4 - 1 - 2 - 1 - 3 - 6 - 2 - 2 - 5 - 1 - 1 - 2 - 4 - 5 - 6 - 5 - 1 - 4 - 6 - 6 - 5 - 6 - 2 - 1 - 6 - 6 - 3 - 3



For audio (midi): knbgr-2-2-6-5-4-1-2-1-3-6-2-2-5-1-1-2-4-5-6-5-1-4-6-6-5-6-2-1-6-6-3-3.mid

2-3-5-5-3-2-4-1-4-4-3-1-2-1-1-4-4-6-2-4-2-5-6-4-2-1-2-6-2-5-4



 $For \ audio \ (midi): \ knbgr-2-3-5-5-3-2-4-1-4-4-3-1-2-1-1-4-4-6-2-4-2-5-6-4-2-1-2-6-2-5-4.mid$

2-4-1-3-5-4-5-4-1-3-6-4-1-5-6-4-1-2-1-3-2-4-5-3-3-5-6-4-4-4-5-4



 $For \ audio \ (midi): \ knbgr-2-4-1-3-5-4-5-4-1-3-6-4-1-5-6-4-1-2-1-3-2-4-5-3-3-5-6-4-4-4-5-4.mid$

2 - 4 - 1 - 4 - 5 - 2 - 6 - 4 - 3 - 1 - 5 - 4 - 1 - 3 - 3 - 1 - 6 - 1 - 4 - 1 - 4 - 1 - 3 - 2 - 4 - 3 - 5 - 1 - 3 - 2 - 6 - 4



 $For \ audio \ (midi): \ knbgr-2-4-1-4-5-2-6-4-3-1-5-4-1-3-3-1-6-1-4-1-4-1-3-2-4-3-5-1-3-2-6-4.mid$

2-4-1-5-5-4-2-3-5-4-6-6-5-1-6-1-1-6-6-6-3-3-2-2-5-4-6-6-5-5-2-3

knbgr::63:57:62:31:18:3:71:8:38:78:34:19:28:68:27:40:81:71:37:16:43:95:10:73:7:93:19:29:74:44:11:82::



 $For \ audio \ (midi): \ knbgr-2-4-1-5-5-4-2-3-5-4-6-6-5-1-6-1-1-6-6-6-3-3-2-2-5-4-6-6-5-5-2-3.mid$

2-4-2-1-1-1-1-2-1-5-5-6-4-6-5-3-4-1-4-1-5-4-6-3-3-1-1-6-3-2-6

knbgr::63:57:2:70:29:83:59:36:55:60:15:92:17:51:27:85:8:6:67:22:90:75:83:20:79:5:62:72:80:21:11:9:: Perm. No.: 483642784470122444216



 $For \ audio \ (midi): \ knbgr-2-4-2-1-1-1-1-2-1-5-5-6-4-6-5-3-4-1-4-1-5-4-6-3-3-1-1-6-3-2-6.mid$

2-4-4-1-6-5-1-4-5-2-4-5-3-2-2-6-1-1-6-3-3-4-1-6-5-2-6-3-6-1-5-2

knbgr::63:57:64:70:22:89:59:73:38:46:80:92:25:6:91:96:81:57:37:53:43:12:24:20:7:55:19:60:80:64:52:76::

Perm. No.: 155816583414403648592



 $For \ audio \ (midi): \ knbgr-2-4-4-1-6-5-1-4-5-2-4-5-3-2-2-6-1-1-6-3-3-4-1-6-5-2-6-3-6-1-5-2.mid$

2 - 4 - 6 - 2 - 6 - 5 - 5 - 6 - 1 - 2 - 5 - 2 - 4 - 1 - 4 - 6 - 3 - 6 - 3 - 2 - 3 - 1 - 2 - 1 - 2 - 3 - 5 - 1 - 2 - 2 - 1 - 2

knbgr::63:57:84:53:22:89:87:48:33:46:15:39:1:68:82:96:8:71:26:65:43:41:10:56:40:5:70:72:31:85:48:76::

Perm. No.: 202456345696866234992



 $For \ audio \ (midi): \ knbgr-2-4-6-2-6-5-5-6-1-2-5-2-4-1-4-6-3-6-3-2-3-1-2-1-2-3-5-1-2-2-1-2.mid$

2-5-1-1-5-4-6-6-6-6-6-5-4-4-1-6-3-5-2-5-2-2-3-3-4-2-6-6-4-4-6-6



For audio (midi): knbgr-2-5-1-1-5-4-6-6-6-6-6-5-4-4-1-6-3-5-2-5-2-3-3-4-2-6-6-4-4-6-6.mid

2 - 5 - 2 - 1 - 5 - 4 - 2 - 1 - 2 - 3 - 1 - 1 - 2 - 5 - 1 - 6 - 6 - 5 - 5 - 4 - 5 - 1 - 2 - 6 - 3 - 3 - 2 - 6 - 5 - 1 - 3



 $For \ audio \ (midi): \ knbgr-2-5-2-1-5-4-2-1-2-2-3-1-1-2-5-1-6-6-5-5-4-5-1-2-6-3-3-2-6-5-1-3.mid$

2 - 5 - 3 - 6 - 5 - 6 - 5 - 5 - 1 - 6 - 2 - 6 - 5 - 5 - 3 - 6 - 4 - 2 - 6 - 1 - 2 - 2 - 1 - 3 - 4 - 3 - 1 - 5 - 5 - 6 - 1 - 4



 $For \ audio \ (midi): \ knbgr-2-5-3-6-5-6-5-5-1-6-2-6-5-5-3-6-4-2-6-1-2-2-1-3-4-3-1-5-5-6-1-4.mid$

2-5-5-4-1-5-1-1-6-2-4-6-6-1-1-6-5-6-3-2-4-2-6-4-2-6-3-5-2-6-1-6



 $For \ audio \ (midi): \ knbgr-2-5-5-4-1-5-1-1-6-2-4-6-6-1-1-6-5-6-3-2-4-2-6-4-2-6-3-5-2-6-1-6.mid$

2 - 5 - 6 - 4 - 2 - 1 - 3 - 2 - 6 - 5 - 4 - 3 - 1 - 3 - 1 - 2 - 6 - 6 - 6 - 3 - 2 - 4 - 3 - 5 - 1 - 1 - 3 - 5 - 6 - 3 - 2 - 3

knbgr::63:7:84:74:41:83:52:90:44:93:80:9:45:35:26:81:59:71:37:53:14:12:88:96:94:47:3:1:80:21:11:82::



 $For \ audio \ (midi): \ knbgr-2-5-6-4-2-1-3-2-6-5-4-3-1-3-1-2-6-6-6-3-2-4-3-5-1-1-3-5-6-3-2-3.mid$

2 - 6 - 2 - 2 - 5 - 3 - 2 - 4 - 1 - 5 - 5 - 6 - 5 - 4 - 2 - 4 - 1 - 5 - 3 - 3 - 6 - 6 - 4 - 2 - 2 - 5 - 2 - 1 - 4 - 2 - 2 - 5



 $For \ audio \ (midi): \ knbgr-2-6-2-2-5-3-2-4-1-5-5-6-5-4-2-4-1-5-3-3-6-6-4-2-2-5-2-1-4-2-2-5.mid$

2 - 6 - 3 - 6 - 1 - 6 - 1 - 3 - 4 - 1 - 3 - 6 - 6 - 1 - 1 - 5 - 2 - 6 - 2 - 4 - 1 - 4 - 3 - 4 - 2 - 2 - 6 - 1 - 3 - 4 - 1 - 6



For audio (midi): knbgr-2-6-3-6-1-6-1-3-4-1-3-6-6-1-1-5-2-6-2-4-1-4-3-4-2-2-6-1-3-4-1-6.mid

2-6-4-5-1-2-5-2-1-6-2-6-1-2-4-2-1-2-2-5-5-1-6-2-5-2-1-3-5-3-3-4



 $For \ audio \ (midi): \ knbgr-2-6-4-5-1-2-5-2-1-6-2-6-1-2-4-2-1-2-5-5-1-6-2-5-2-1-3-5-3-3-4.mid$

2-6-5-1-6-1-2-3-5-2-6-5-6-5-1-2-2-4-3-2-2-4-4-3-4-4-6-6-2-3-1

knbgr::63:47:86:70:22:83:71:8:38:46:34:92:17:61:26:81:78:6:26:65:14:12:83:63:58:93:66:29:80:85:42:87::



 $For \ audio \ (midi): \ knbgr-2-6-5-1-6-1-2-3-5-2-6-5-6-5-1-2-2-4-3-2-2-4-3-4-4-6-6-2-3-1.mid$

2 - 6 - 5 - 2 - 2 - 1 - 1 - 2 - 1 - 6 - 1 - 3 - 1 - 2 - 1 - 3 - 5 - 1 - 2 - 1 - 3 - 5 - 2 - 1 - 4 - 6 - 2 - 1 - 5 - 2 - 3



 $For \ audio \ (midi): \ knbgr-2-6-5-2-2-1-1-2-1-6-1-3-1-2-1-3-5-1-2-1-3-5-2-1-4-6-2-1-5-2-3.mid$

$2 \hbox{-} 6 \hbox{-} 6 \hbox{-} 3 \hbox{-} 3 \hbox{-} 6 \hbox{-} 6 \hbox{-} 5 \hbox{-} 5 \hbox{-} 5 \hbox{-} 4 \hbox{-} 2 \hbox{-} 5 \hbox{-} 1 \hbox{-} 6 \hbox{-} 6 \hbox{-} 6 \hbox{-} 6 \hbox{-} 6 \hbox{-} 5 \hbox{-} 4 \hbox{-} 1 \hbox{-} 4 \hbox{-} 5 \hbox{-} 4 \hbox{-} 6 \hbox{-} 4 \hbox{-} 3 \hbox{-} 5 \hbox{-} 3 \hbox{-} 1 \hbox{-} 3 \hbox{-} 1$

knbgr::63:47:84:5:50:49:56:58:38:93:80:39:28:68:27:96:59:71:18:22:90:12:61:92:38:93:3:1:54:64:42:87::

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 $For \ audio \ (midi): \ knbgr-2-6-6-3-3-6-6-5-5-5-4-2-5-1-6-6-6-6-5-4-1-4-5-4-6-4-3-5-3-1-3-1.mid$

2 - 6 - 6 - 5 - 6 - 4 - 3 - 1 - 5 - 4 - 5 - 6 - 5 - 4 - 1 - 4 - 3 - 3 - 4 - 6 - 1 - 5 - 1 - 2 - 1 - 6 - 1 - 2 - 2 - 5 - 4 - 5



 $For \ audio \ (midi): \ knbgr-2-6-6-5-6-4-3-1-5-4-5-6-5-4-1-4-3-3-4-6-1-5-1-2-1-6-1-2-5-4-5.mid$

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References

Ivars Peterson. Mozart's Melody Machine, 2001. URL https://www.sciencenews.org/article/mozarts-melody-machine-0. Retrieved Tuesday, 08 August, 2017 11:36:00 AM +08. 3

Wikipedia: Musikalisches Würferspiel. Wikipedia, The Free Encyclopedia, 2017. URL https://en.wikipedia.org/w/index.php?title=Musikalisches_W%C3%BCrfelspiel&oldid=787418377. Retrieved Tuesday, 08 August, 2017 12:56:17 AM +08. 3