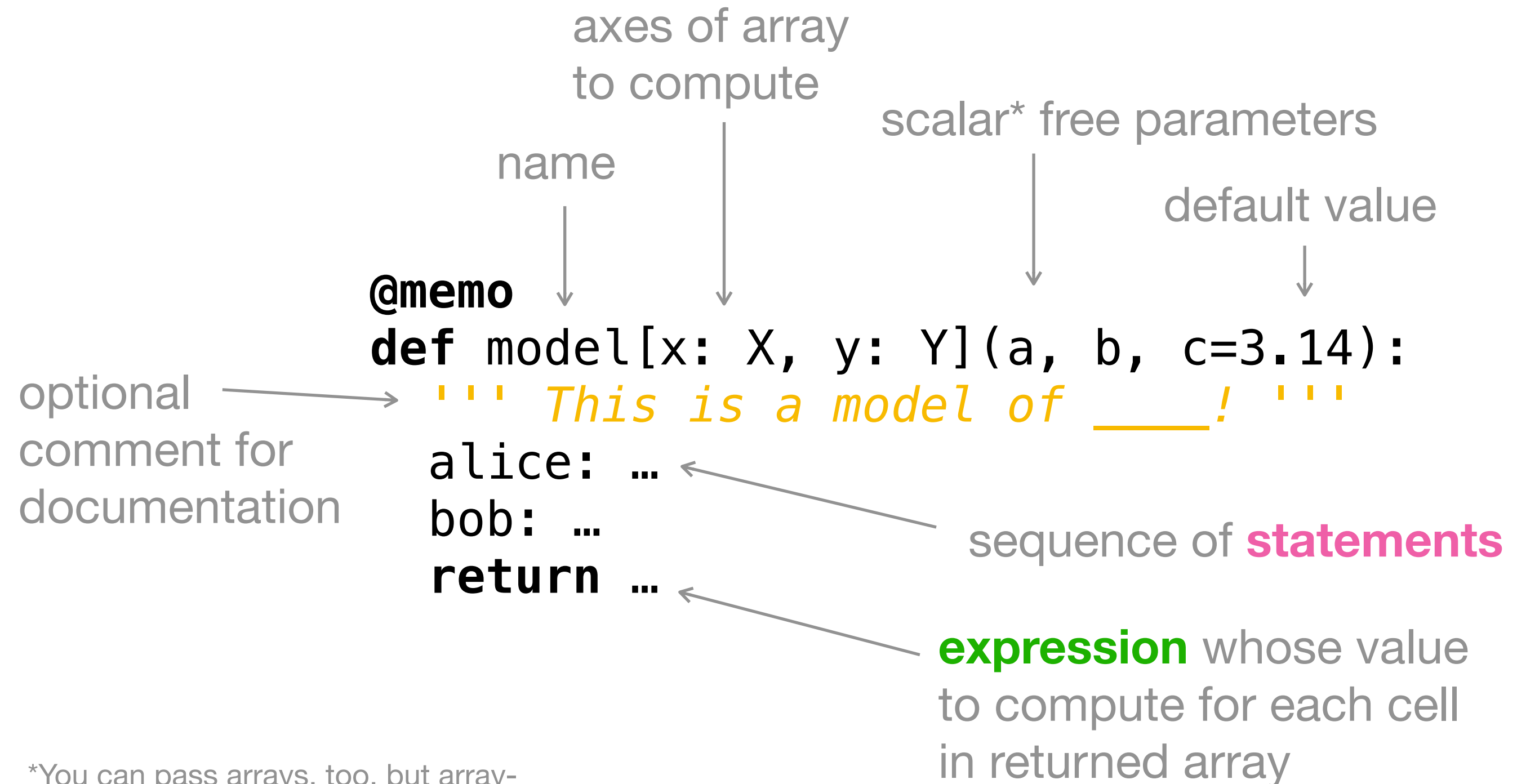


The memo handbook

v1.2.0



Anatomy of a memo



*You can pass arrays, too, but array-valued parameters must be declared with an ellipsis annotation (`a: ...`).

Statements

chooses

Domain of choice (name of Python list/enum or JAX array)

Agent making choice

bob: chooses(a in Actions, wpp=exp(β *utility(a)))

Name of choice

"With probability proportional to"
For softmax, use wpp=exp(...)
For uniform choice, use wpp=1

Can make multiple choices simultaneously

bob: chooses(x in X, y in Y, wpp=joint(x, y))

more ways to choose

```
bob: chooses(a in Actions, to_maximize=utility(a))
```

↑
For `argmax` use `to_maximize`
For `argmin` use `to_minimize`

Aliases of "chooses" that don't imply agency/goal-orientation
(These all mean the same, but can make your model easier to read.)

↓

```
bob: given(r in Roles, wpp=1)  
bob: draws(r in Roles, wpp=1)  
bob: assigned(r in Roles, wpp=1)  
bob: guesses(r in Roles, wpp=1)
```

thinks

Agent doing the thinking



```
bob: thinks[  
    alice: chooses(...),  
    charlie: chooses(...),  
    ...  
]
```

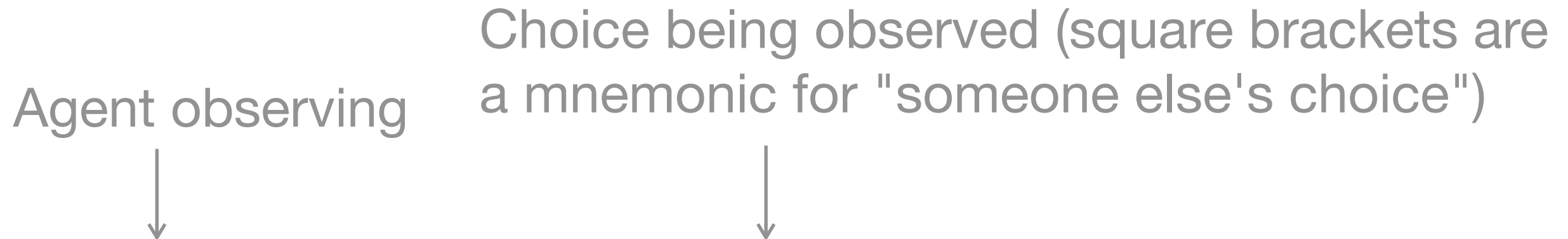


What that agent thinks
(notice the commas!)

observes

Agent observing

Choice being observed (square brackets are a mnemonic for "someone else's choice")



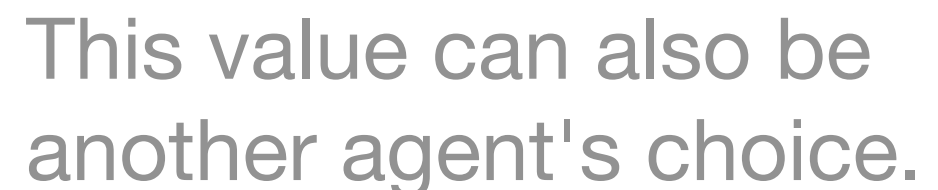
bob: observes [alice.x] is y

What the choice is observed to actually be.
Can create false beliefs this way!

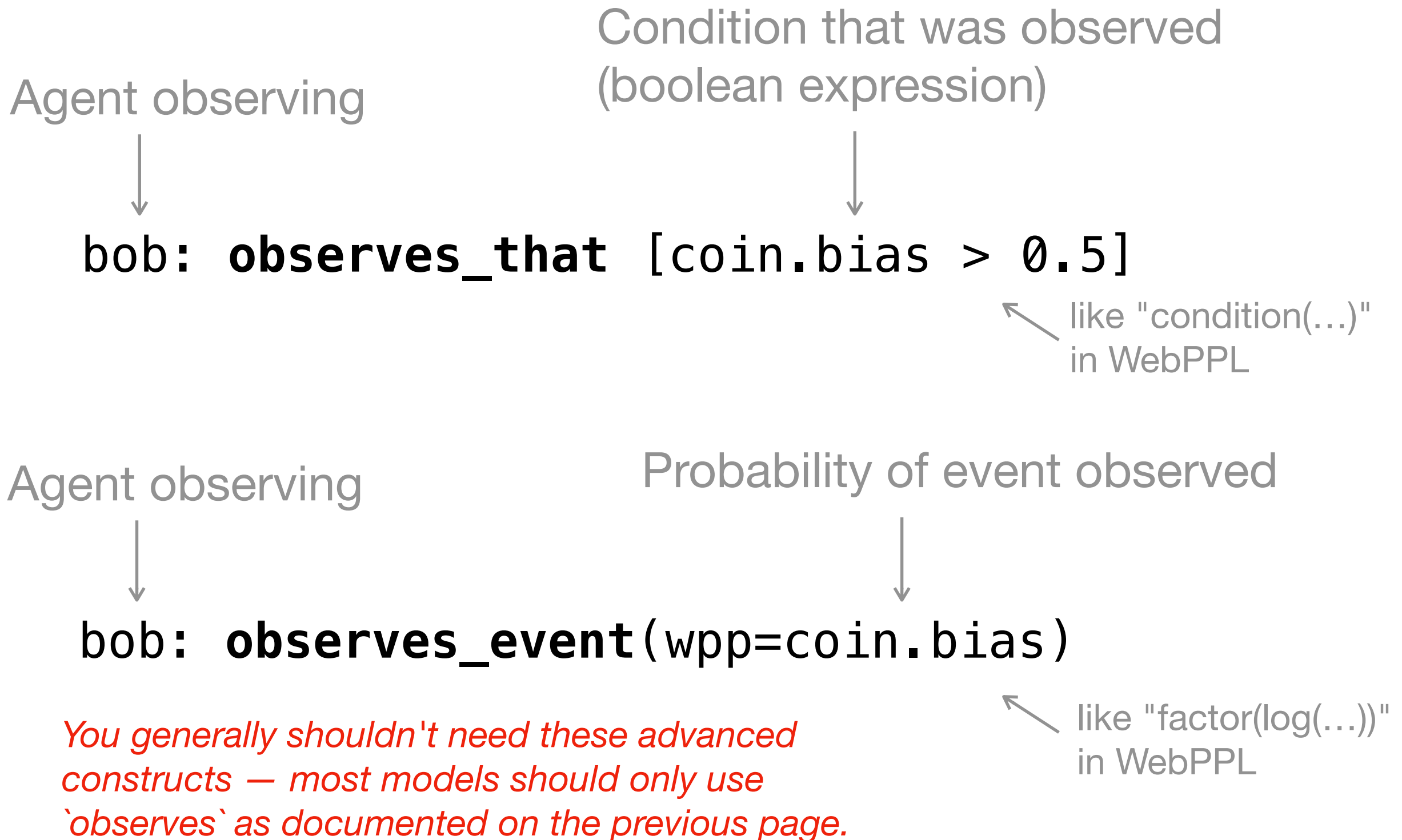


bob: observes [alice.x] is charlie.y

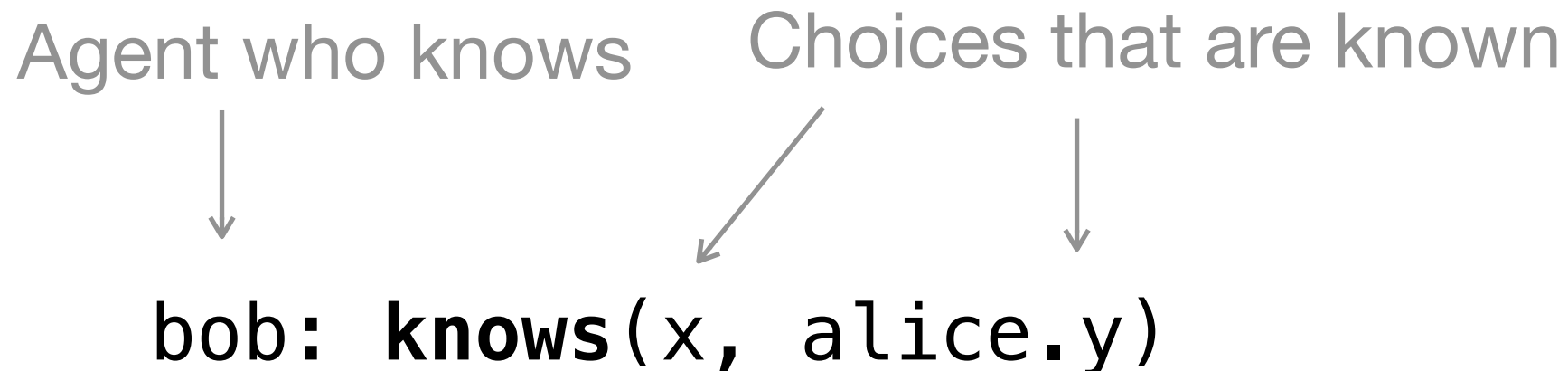
This value can also be
another agent's choice.



advanced use of observes



knows



This utility is useful for the common case of "pushing" a variable into an agent's frame of mind. Roughly shorthand for this:

bob: thinks[alice: chooses(y in Y, wpp=...)]
bob: observes [alice.y] is alice.y

snapshots_self_as

Agents can remember "snapshots" of their past selves.
Useful for counterfactuals and hypotheticals, especially
when used with "imagine" expressions (see below...).

Agent who snapshots "aliases" of snapshots
↓ ↓
alice: **snapshots_self_as**(past_alice, ...)

```
alice: observes [bob.x] is x  
return alice[ past_alice[ E[bob.x] ] ]
```

not affected by "observe" statement

wants / EU

wants sets up a predicate or utility function ("goal") that is defined over *future* states of the world. You can reference choices that have not yet been made yet. The expected future value of the goal expression can be evaluated using an EU expression.

Agent who wants name of goal (here, "win") predicate/utility to evaluate in the future

↓ ↙

```
alice: wants(win=score > bob.score)
alice: chooses(a in A, to_maximize=EU[win])
alice: given(score in N, wpp=...)
```

Even though "score" is only defined here, the wants and EU expressions above are okay. Conceptually, the EU expression is evaluated here.

↑
name of goal to evaluate when making goal-directed choice

INSPECT

At compile-time, print out the current state of an agent.
This can be helpful for debugging tricky models.

Agent to inspect



`alice: INSPECT()`

Expressions

literals

floating-point numbers only



3.14

also references to declared free parameters



a, b, c, ...

operators

memo supports most Python unary/binary ops

↓
`1 + 1`

also some free bonus functions

↓
`exp(...), log(...), abs(...)`

can also call any function tagged
with `@jax.jit`

↓
`@jax.jit`
`def f(x):`

`return np.cos(x)`

useful for calling deep learning, etc.

JAX is a big ecosystem

← note: can only take scalar inputs
and can only return one scalar output

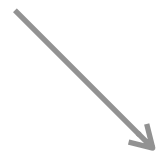
choices

```
alice: chooses(x in X, wpp=1)  
alice: chooses(y in Y, wpp=f(x, y))
```



you can refer to an agent's own
choice as if it were simply a variable

or refer to other agents' choices with "dot" notation



```
alice.x + alice.y
```

equivalent to either of these



```
alice[x] + alice[y]  
alice[x + y]
```


probabilistic operators

expectation



E[alice.x + bob.z]

variance



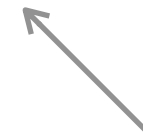
Var[alice.y * 2]

probability



Pr[alice.y >= 0]

Pr[a.x > 0, b.y < 2]



can use both
commas and
"and" for joint

information-theoretic operators

(mutual) entropy between choices



H[alice.x, bob.y, ...]

KL divergence



KL[alice.x | bob.y]

queries

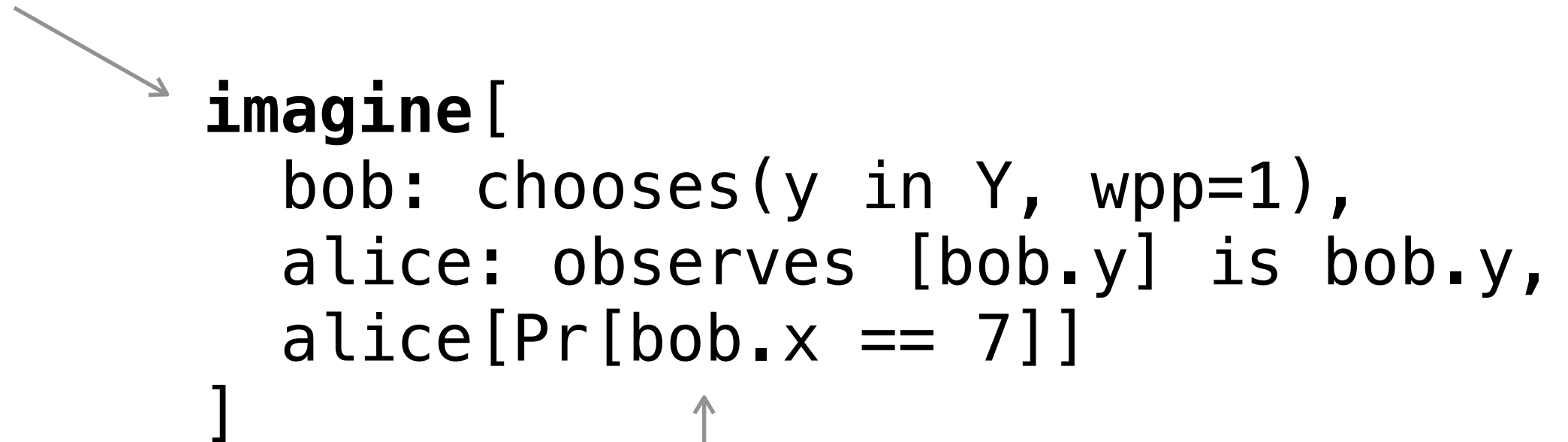
```
Var[alice[abs(x) * 2]]  
alice[bob.y == 7]
```



can "query" another agent for the value
of an expression using square brackets

hypotheticals

set up hypothetical world by
running statements



The diagram illustrates the setup of a hypothetical world. It features a code block with the following lines: `imagine[`, `bob: chooses(y in Y, wpp=1),`, `alice: observes [bob.y] is bob.y,`, `alice[Pr[bob.x == 7]]`, and `]`. An arrow points from the text 'set up hypothetical world by running statements' to the `imagine[` line. Another arrow points from the text 'last line = expression to evaluate in that world' to the `alice[Pr[bob.x == 7]]` line.

```
imagine[  
    bob: chooses(y in Y, wpp=1),  
    alice: observes [bob.y] is bob.y,  
    alice[Pr[bob.x == 7]]  
]
```


last line = expression to
evaluate in that world

memo calls

```
@memo  
def f[x: X](a, b, c): ...
```



can reference one memo from another. (don't forget to pass parameters!)

```
@memo  
def g():  
  alice: chooses(x in X, wpp=f[x](1.0, 0.0, 3.1))
```



shorthand: can use "..." if f should be called with all of g's parameters; in this case, (a, b, c).

```
@memo  
def g(a, b, c):  
  alice: chooses(x in X, wpp=f[x](...))
```



cost reflection

```
@memo def f[...](a, b, c): ...
```

```
cost @ f(3, 4, 5)
```



get number of FLOPs needed
to evaluate f
(note: no axes, params only!)

reference to Python variable

```
class Action(IntEnum): WAIT = 0; ...
```

```
@memo def f[...](...):  
    return {Action.WAIT}
```



use braces for inline reference
to a global Python variable

```
@memo def f[...](x):  
    return {x[0] << 4}
```



You can also refer to model parameters, and write raw Python expressions. You cannot refer to memo constructs, e.g. agents or their choices, in curly braces.

Things to do with a memo

Running a memo

call it like a function with params
(returns an array with prescribed axes)



`f(a, b)`

pretty-print table of results



`f(a, b, print_table=True)`

`f(a, b, return_pandas=True)`

`f(a, b, return_xarray=True)`

get outputs in other formats

save "comic book" visualization of model via graphviz



`f(a, b, save_comic="file")`

@memo def options

cache results (keyed by scalar parameters)



```
@memo ( cache=True )
```

trace execution, showing time taken



```
@memo ( debug_trace=True )
```

Automatic differentiation

(useful for fitting by gradient descent)

```
@memo  
def f[...](a, b): ...
```

returns tuple of value + gradient wrt params a & b



```
jax.value_and_grad(f)(a, b)
```