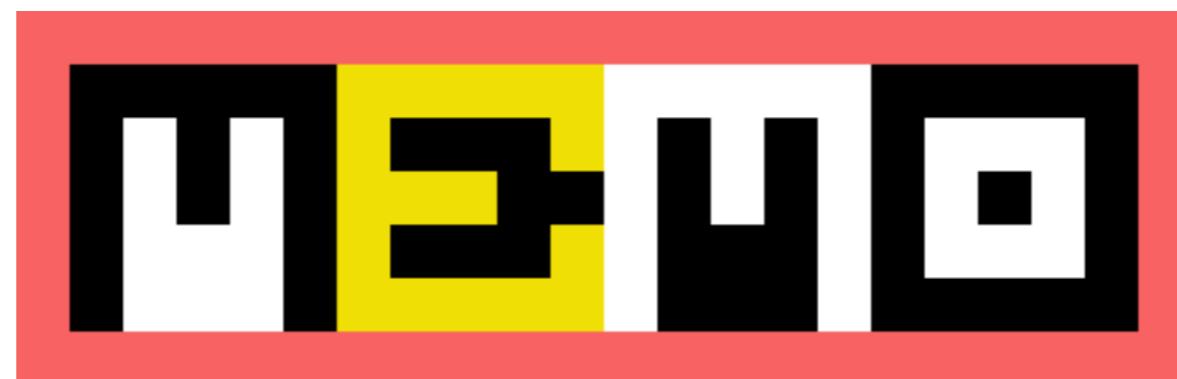
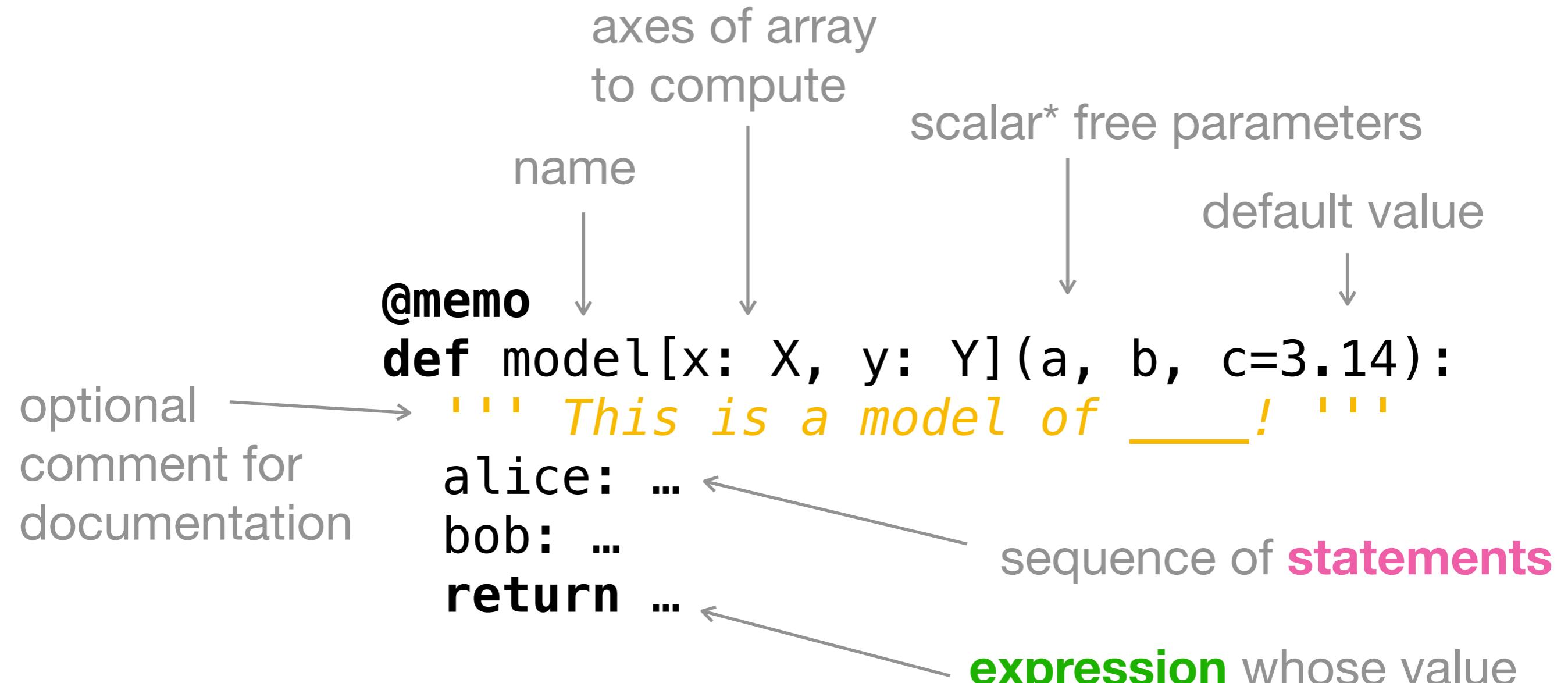


The memo handbook

v1.2.0



Anatomy of a memo



*You can pass arrays, too, but array-valued parameters must be declared with an ellipsis annotation (a: ...).

Statements

chooses

Domain of choice (name of Python list/enum or JAX array)

Agent making choice

```
bob: chooses(a in Actions, wpp=exp(β*utility(a)))
```

Name of choice

"With probability proportional to"
For softmax, use `wpp=exp(...)`
For uniform choice, use `wpp=1`

Can make multiple choices simultaneously

```
bob: chooses(x in X, y in Y, wpp=joint(x, y))
```

more ways to choose

```
bob: chooses(a in Actions, to_maximize=utility(a))
```



For argmax use to_maximize
For argmin use to_minimize

Aliases of "chooses" that don't imply agency/goal-orientation



(These all mean the same, but can make your model easier to read.)

```
bob: given(r in Roles, wpp=1)
bob: draws(r in Roles, wpp=1)
bob: assigned(r in Roles, wpp=1)
bob: guesses(r in Roles, wpp=1)
```

thinks

Agent doing the thinking



```
bob: thinks[  
    alice: chooses(...),  
    charlie: chooses(...),  
    ...]
```



What that agent thinks
(notice the commas!)

observes

Agent observing

↓
bob: observes [alice.x] is y

Choice being observed (square brackets are a mnemonic for "someone else's choice")



What the choice is observed to actually be.
Can create false beliefs this way!

bob: observes [alice.x] is charlie.y



This value can also be
another agent's choice.

advanced use of observes

Agent observing



Condition that was observed
(boolean expression)



like "condition(...)"
in WebPPL

Agent observing



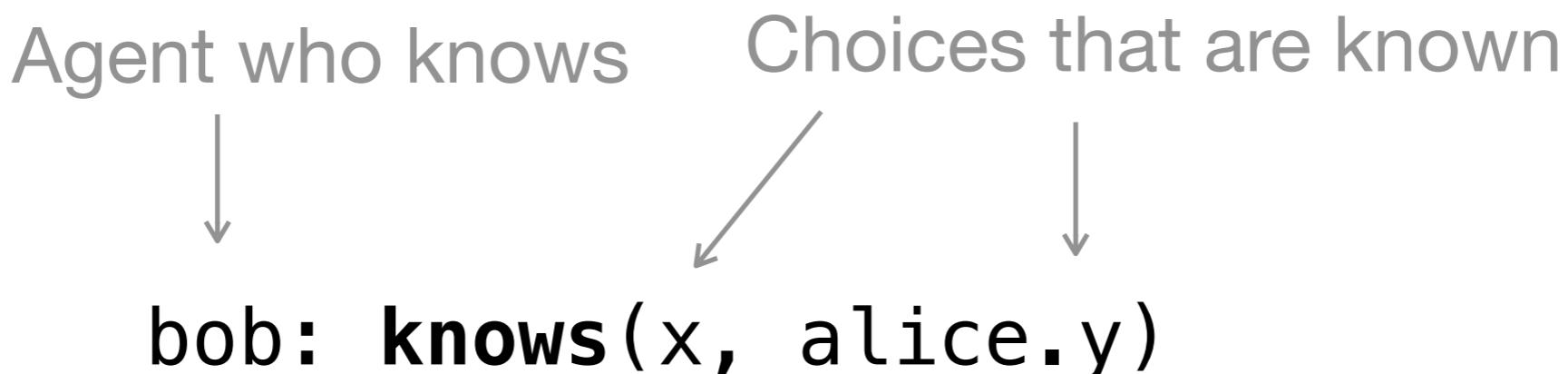
Probability of event observed



You generally shouldn't need these advanced constructs — most models should only use `observes` as documented on the previous page.

like "factor(log(...))"
in WebPPL

knows



This utility is useful for the common case of "pushing" a variable into an agent's frame of mind. Roughly shorthand for this:

```
graph TD; A["bob: thinks[ alice: chooses(y in Y, wpp=...)]\nbob: observes [alice.y] is alice.y"] --> B["bob: knows(x, alice.y)"]
```

The diagram shows the expansion of the `knows` utility. At the top, two lines of code are shown: `bob: thinks[alice: chooses(y in Y, wpp=...)]` and `bob: observes [alice.y] is alice.y`. An arrow points downwards from this code to the simplified expression `bob: knows(x, alice.y)`.

snapshots_self_as

Agents can remember "snapshots" of their past selves.
Useful for counterfactuals and hypotheticals, especially
when used with "imagine" expressions (see below...).

Agent who snapshots



alice: **snapshots_self_as(past_alice, ...)**

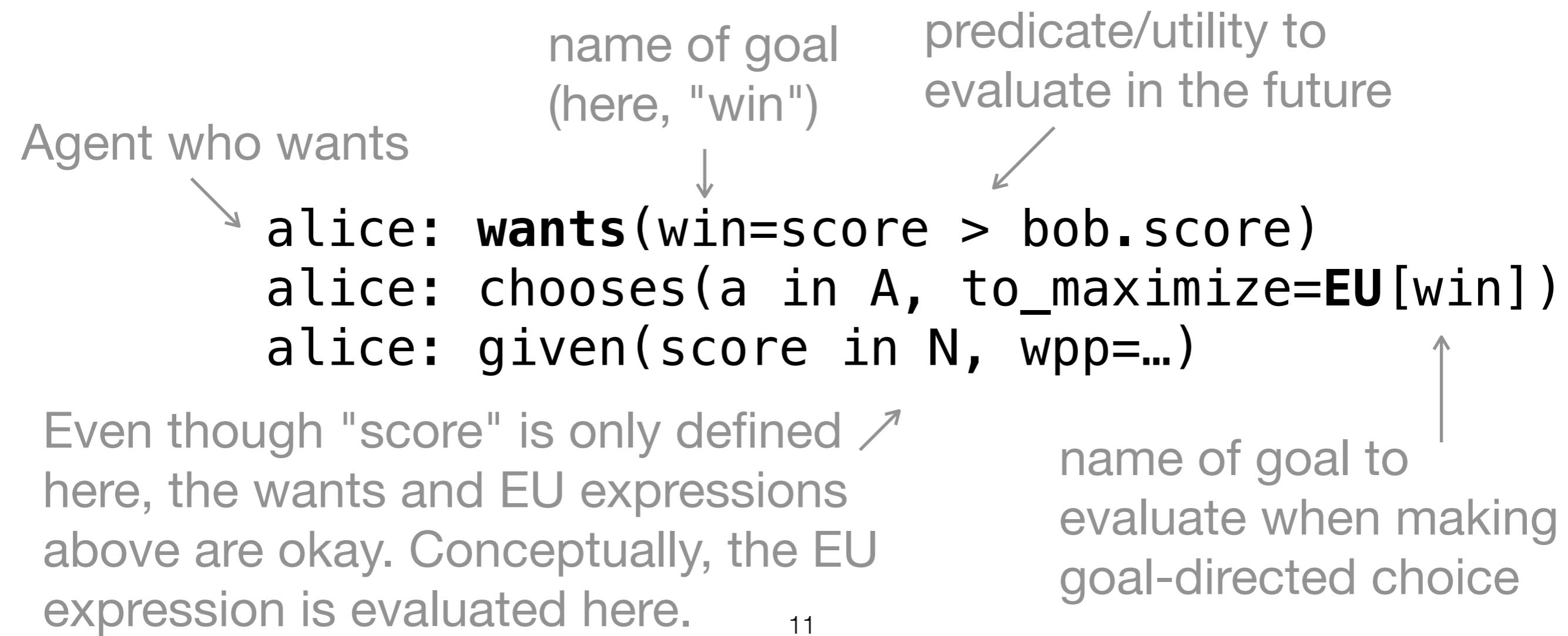
"aliases" of snapshots
↓

```
alice: observes [bob.x] is x
return alice[ past_alice[ E[bob.x] ] ]
```

not affected by "observe" statement
↑

wants / EU

wants sets up a predicate or utility function ("goal") that is defined over *future* states of the world. You can reference choices that have not yet been made yet. The expected future value of the goal expression can be evaluated using an EU expression.



INSPECT

At compile-time, print out the current state of an agent.
This can be helpful for debugging tricky models.

Agent to inspect

alice: **INSPECT()**

Expressions

literals

floating-point numbers only



3.14

also references to declared free parameters



a, b, c, ...

operators

memo supports most Python unary/binary ops



`1 + 1`

also some free bonus functions



`exp(...), log(...), abs(...)`

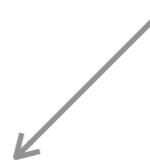
can also call any function tagged
with `@jax.jit`



```
@jax.jit
def f(x):
    return np.cos(x)
```

useful for calling deep learning, etc.

JAX is a big ecosystem



note: can only take scalar inputs
and can only return one scalar output

choices

alice: chooses(x in X , wpp=1)

alice: chooses(y in Y , wpp= $f(x, y)$)



you can refer to an agent's own
choice as if it were simply a variable

or refer to other agents' choices with "dot" notation

alice.x + alice.y

equivalent to either of these

alice[x] + alice[y]
alice[x + y]

probabilistic operators

expectation

$$\mathbf{E}[\text{alice.x} + \text{bob.z}]$$

variance

$$\mathbf{Var}[\text{alice.y} * 2]$$

probability

$$\begin{aligned}\mathbf{Pr}[\text{alice.y} \geq 0] \\ \mathbf{Pr}[\text{a.x} > 0, \text{b.y} < 2]\end{aligned}$$

can use both
commas and
"and" for joint

information-theoretic operators

(mutual) entropy between choices



H[alice.x, bob.y, ...]

KL divergence



KL[alice.x | bob.y]

queries

```
Var [alice[abs(x) * 2]]  
alice[bob.y == 7]
```



can "query" another agent for the value
of an expression using square brackets

hypotheticals

set up hypothetical world by
running statements

```
→ imagine[  
    bob: chooses(y in Y, wpp=1),  
    alice: observes [bob.y] is bob.y,  
    alice[Pr[bob.x == 7]]  
]
```



last line = expression to
evaluate in that world

memo calls

```
@memo  
def f[x: X](a, b, c): ...
```

can reference one memo from another. (don't forget to pass parameters!)

```
@memo  
def g():  
    alice: chooses(x in X, wpp=f[x](1.0, 0.0, 3.1))
```

shorthand: can use "..." if f should be called with all of g's parameters; in this case, (a, b, c).

```
@memo  
def g(a, b, c):  
    alice: chooses(x in X, wpp=f[x](...))
```

cost reflection

```
@memo def f[...](a, b, c): ...
```

```
cost @ f(3, 4, 5)
```



get number of FLOPs needed
to evaluate f
(note: no axes, params only!)

reference to Python variable

```
class Action(IntEnum): WAIT = 0; ...
```

```
@memo def f(...):  
    return {Action.WAIT}
```



use braces for inline reference
to a global Python variable

```
@memo def f(...)(x):  
    return {x[0] << 4}
```



You can also refer to model parameters, and write raw Python expressions. You cannot refer to memo constructs, e.g. agents or their choices, in curly braces.

Things to do with a memo

Running a memo

call it like a function with params
(returns an array with prescribed axes)



`f(a, b)`

pretty-print table of results



`f(a, b, print_table=True)`

`f(a, b, return_pandas=True)`

`f(a, b, return_xarray=True)`

get outputs in other formats

save "comic book" visualization of model via graphviz



`f(a, b, save_comic="file")`

@memo def options

cache results (keyed by scalar parameters)



@memo(cache=True)

trace execution, showing time taken



@memo(debug_trace=True)

Automatic differentiation (useful for fitting by gradient descent)

```
@memo  
def f [...] (a, b): ...
```

returns tuple of value + gradient wrt params a & b



```
jax.value_and_grad(f)(a, b)
```