



Experiment No. # 4

LTI System Characterization II: Circular convolution and DFT makes Fourier Transform pair

1) Objectives:

- a) Circular convolution and DFT Multiplication for two sequences.
- b) Simulink based circular convolution.

2) Software used:

- a) MATLAB.

A. Pre-Lab

- a) Read about circular convolution.
- b) practice simulink.

I. CIRCULAR CONVOLUTION \Leftrightarrow DFT

A. Theory

- 1) J. Proakis and D. Manolakis, Digital signal processing: principles, algorithms, and applications

B. Procedure

- 1) Circular Convolution: Write a MATLAB function myCirConvMat.m that takes in the impulse response $h(n)$ of an LSI system and the length of input sequence $x(n)$ and provides in output the matrix representing the circular convolution operator H . Compute and plot the convolution results for the following:

$$h_1(n) = \{2, 1, 2, 1\}$$

$$x_1(n) = \{1, 2, 3, 4\}$$

$$x_2(n) = 0.5^n$$

Here $n = 0, 1, \dots, 9$ samples.

The circular convolution sum for a system with $h(n)$ system response and $x(n)$ input is given by (both padded with zeros to make the length equal of both the sequences).

$$y(n) = \sum_{i=0}^{N-1} h(i) \cdot x((n-i))_N$$

Where N , the sequence length is greater or equal to length of the larger sequence and taken as multiple of 2. $N = 2^i$ $i = 2, 3, 4, \dots$

Also, $x((n-i))_N$ represents the index ' $((n-i) \text{ modulo } N) = N - i + n$ '.

- 2) Change of basis: For an LSI system, let the impulse response be given by $h(n) = h(0), \dots, h(7)$. The 8-point input to this system is a finite duration sequence $x(n) = x(0) \dots x(7)$. Now, to verify Circular Convolution \Leftrightarrow DFT, perform the following steps.
- Use your myCirConvMat.m to find circular convolution of $h(n)$ and $x(n)$ given by $y(n)$.
 - Use myDFT function to generate 8-Point DFT matrix.
 - Find out 8-point DFT of sequence $h(n)$ and $x(n)$ given by $H(k)$ and $X(k)$.
 - Multiply both above DFT sequence point by point and generate $Y(k) = H(k) \cdot X(k)$.
 - Find inverse DFT of $Y(k)$ using myDFT function and compare the result with the first step.

Let's verify it using matrix multiplication.

- Use your myCirConvMat.m to find convolution matrix H .
 - Use myDFT function to generate 8-Point DFT matrix D_8 .
 - Find out 8-point DFT of sequence $x(n)$ given by $X_F(k)$.
 - Calculate $H_F = D_8 \cdot H \cdot D_8^{-1}$. Is this matrix Diagonal? Compute $Y_F = H_F \cdot X_F$. Find $y = D_8^{-1} \cdot Y_F$.
 - Compare the above result with the circular convolution of $h(n)$ and $x(n)$.
- 3) **Observation:**
- Generate Circular Convolution matrix H .
 - Perform circular convolution code and compare your results with MATLAB built in command for circular convolution.
 - Generate myIDFT using myDFT function. Verify 'Circular convolution \Leftrightarrow DFT multiplication are fourier transform pair' using first five steps of change of basis section.
 - Verify the above answers using the matrix multiplication steps given in the change of basis section.
 - Repeat the experiment in simulink.
- 4) **Conclusion:** Conclude the experiment.

II. CONVOLUTION IN SIMULINK

- Open simulink and create a model file with .slx extension.
- Read input data $x = [1, 2, 3, 4]$ through command window.
- Take channel coefficients $h = [2, 1, 2, 1]$.
- Perform the circular convolution using matlab function in simulink.
- Repeat all the 'Procedure' steps and recreate all functional blocks into simulink.

Well Done
