

The LNM Institute of Information Technology

Experiment No. # 9 Digital Filter Design: Windowing, Linear phase FIR

- 1) **Aim:**
 - a) Digital Filter Design.
- 2) Software used:
 - a) MATLAB.
- 3) Theory
 - a) J. Proakis and D. Manolakis, Digital signal processing: principles, algorithms, and applications
- 4) Procedure
 - a) Windowing Based design: Rectangle, Hamming, Blackman
 - i) Let's consider a low pass filter, whose response is given by

$$H_d(w) = e^{\left(-j \cdot w \cdot \left(\frac{M-1}{2}\right)\right)} \dots, 0 \le |w| \le w_c$$

$$H_d(w) = 0, \dots Otherwise.$$
(1)

where M is corresponding delay in time domain.

ii) The corresponding filter impulse response can be found by

$$h_d(n) = \frac{1}{2\pi} \int_{-w_c}^{w_c} e^{\left(-j \cdot w \cdot \left(n - \frac{M-1}{2}\right)\right)} dw \tag{2}$$

and is given by

$$h_d(n) = \frac{\sin\left(w_c\left(n - \left(\frac{M-1}{2}\right)\right)\right)}{\left(\pi\left(n - \left(\frac{M-1}{2}\right)\right)\right)} \tag{3}$$

- iii) This impulse response is windowed using the windows mentioned below.
 - A) Rectangle Window: w(n) = 1
 - B) Hamming Window: $w(n) = 0.42 0.5 \cdot cos(\frac{2\pi n}{M-1}) + 0.08 \cdot cos(\frac{4\pi n}{M-1})$ C) Blackman Window: $w(n) = 0.54 0.46 \cdot cos(\frac{2\pi n}{M-1})$
 - where $n = 0, 1, \dots M 1$
- iv) The finite impulse response h(n) is then windowed impulse response given by

$$h(n) = h_d(n) \cdot w(n) \tag{4}$$

where n = 0,1,2, ... M - 1.

b) Filtering Hamming sound using filtering:

- i) Let's read an audio file and sample it using 32 Khz. Let's also consider this audio file has a hamming sound or Hiss having frequency greater than $(\frac{\pi}{2})$ 8 KHz. Follow the steps and remove the hissing sound.
- ii) Steps:
 - Take 256 samples of the audio file and locate the hissing frequency (Approximately at 66^{th} and 192^{th} sample).
 - Use the low pass filter designed in previous exercise, having cut off frequency $\frac{\pi}{2}$ i.e (or ideal filter having ones for first 64 samples and zeros for next 64 sample over a span of 0 to π frequency).
 - Multiply the filter response and spectrum of audio signal for N=256 samples.
 - Repeat above step for the whole audio file.
 - Check whether hiss sound removed and also conclude for distortion audible if any.

c) Notch Filtering of Hiss:

- i) Let's read an audio file and sample it using 32 Khz. Let's also consider this audio file has a hissing sound at 8 KHz. Follow the steps and remove the hissing sound.
- ii) Steps:
 - Take 8 samples of the audio file and locate the hissing frequency (Approximately at 3^{rd} and 7^{th} sample).
 - Design a notch filter at frequency $\frac{\pi}{4}$ i.e (By placing complex conjugate pairs of zeros at $\pm \frac{\pi}{4}$ frequency).
 - Convolve the impulse response h(n) with the distorted file Or Multiply the filter response H(w)(Having zero values at corresponding frequencies) and spectrum of audio signal for N=8 samples. Here the transfer function H(w) and the impulse response h(n) having complex conjugate zeros at frequencies $\frac{\pi}{4}$ is given by

$$H(Z) = (1 - exp(j \cdot \frac{\pi}{4})Z^{-1})(1 - exp(-j \cdot \frac{\pi}{4})Z^{-1}) = 1 - 2\cos(\frac{\pi}{4})Z^{-1} + Z^{-2}$$
 (5)

$$h(n) = [1, -2\cos(\frac{\pi}{4}), 1] \tag{6}$$

• Check whether hiss sound removed and also conclude for distortion audible if any.

5) Tasks and Observations:

- a) Window Based Filtering: Use Eq.(1),(2),(3),(4)
 - i) Simulate vaious window(rectangle, hamming, blackman's) based Low pass FIR filter with cutoff frequncies $w_c = \frac{\pi}{2}, \frac{\pi}{4}, \frac{\pi}{6}$, show the frequncy response of the windowing functions and plot the magnitude(in dB), phase response of the designed FIR filter.
 - ii) Simulate vaious window(rectangle, hamming, blackman's) based High pass FIR filter with cutoff frequncies $w_c = \frac{\pi}{2}, \frac{\pi}{4}, \frac{\pi}{6}$, show the frequncy response of the windowing functions and plot the magnitude, phase response of the designed FIR filter.
 - iii) Simulate vaious window(rectangle, hamming, blackman's) based band pass FIR filter with cutoff frequncies $w_c(low) = \frac{\pi}{4}$, $w_c(high) = \frac{\pi}{2}$, show the frequncy response of the windowing functions and plot the magnitude, phase response of the designed FIR filter.
- b) Remove the hissing sound using above generated filter.
- c) Remove the hissing sound using Notch filter.
- d) Repeat the experiment in simulink.
- 6) Plot all the signals in all of the above steps and justify them.
- 7) **Conclusion** Write/plot your own.