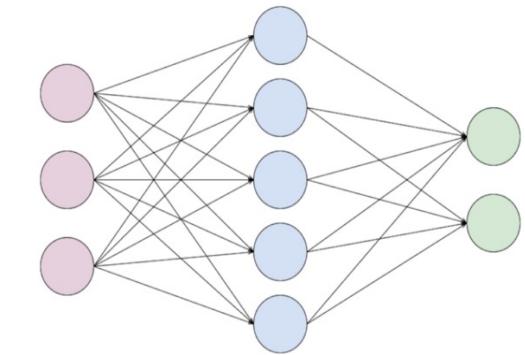
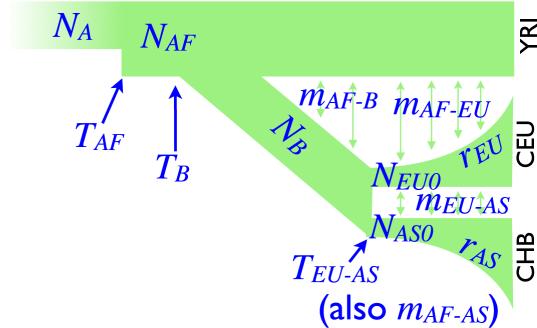
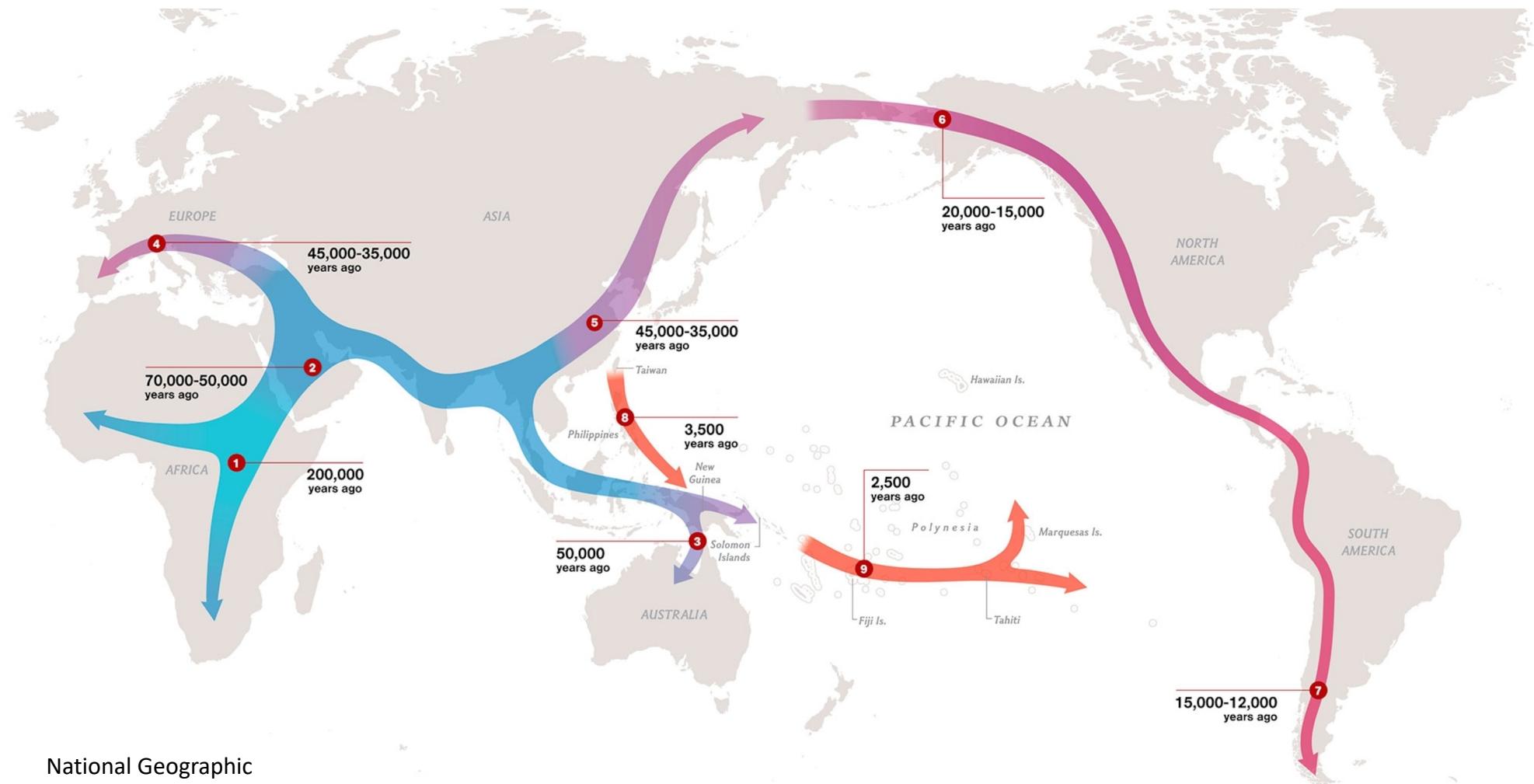


# Computationally Efficient Demographic Inference with Supervised Machine Learning



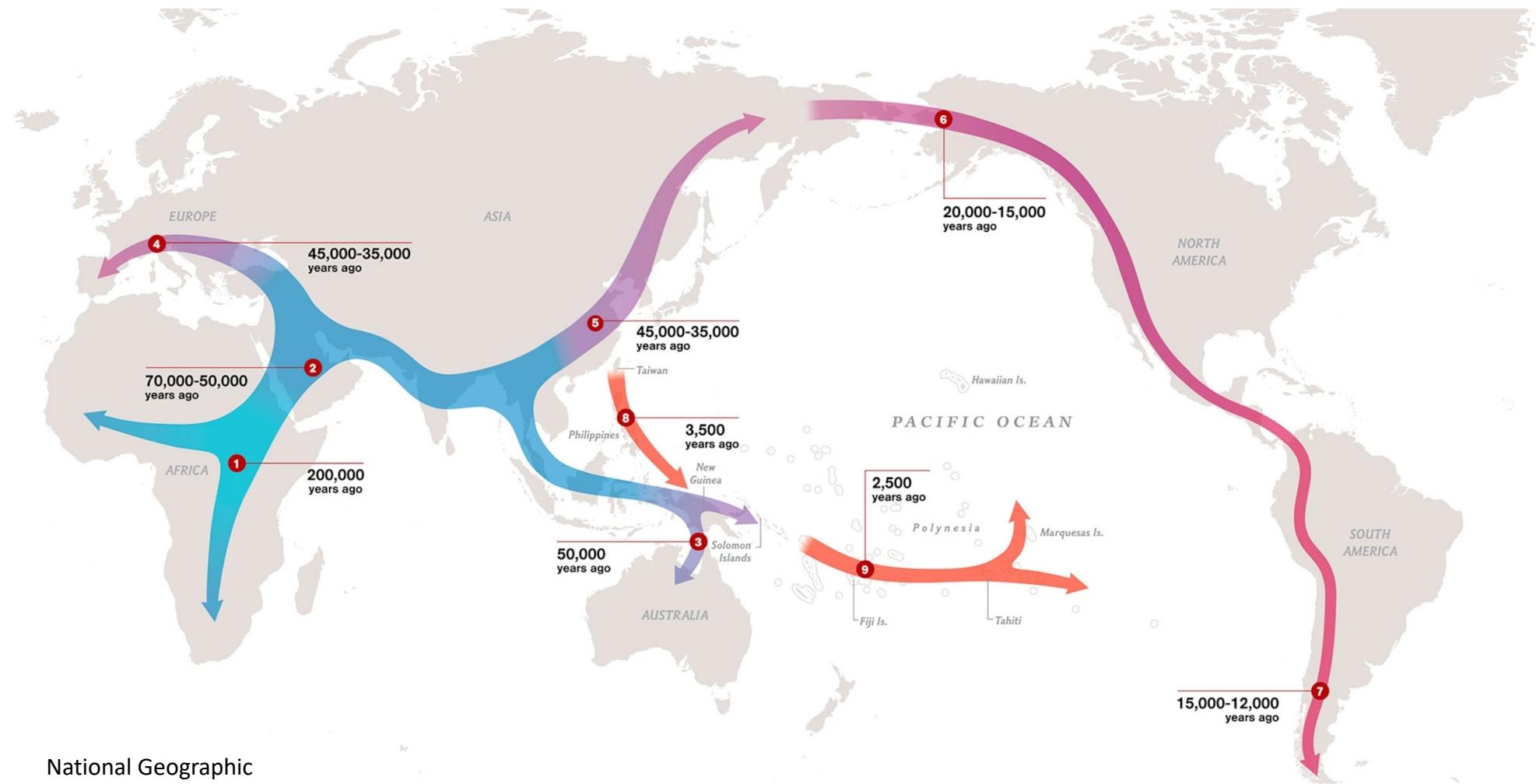
Linh N. Tran, Connie Sun, Mathews Sajan, Ryan Gutenkunst  
University of Arizona

# Demographic history inference



# Demographic history inference – Motivation

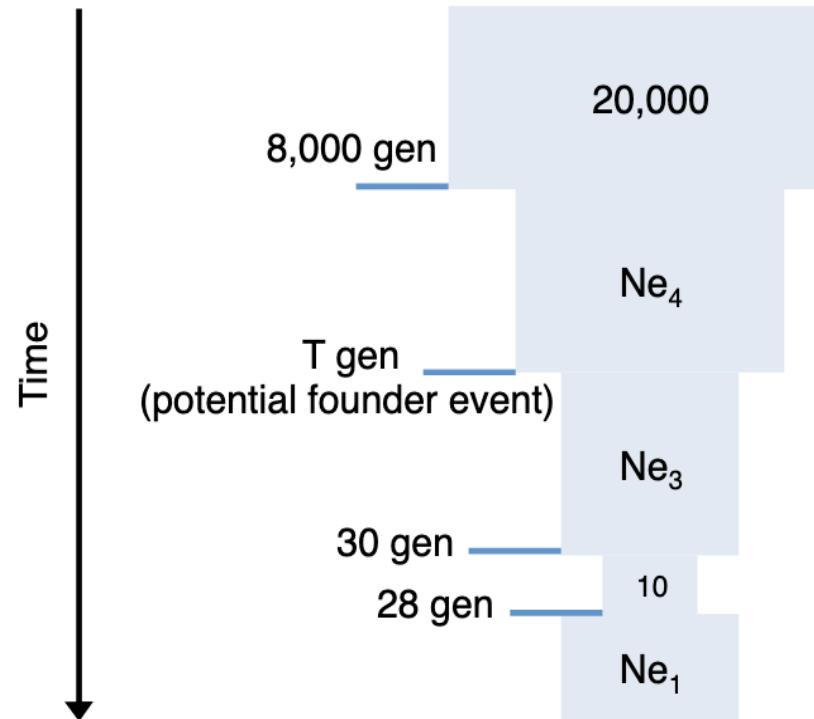
- Understand population history:  
bottlenecks, gene flow, etc.



# Demographic history inference – Motivation

National Geographic

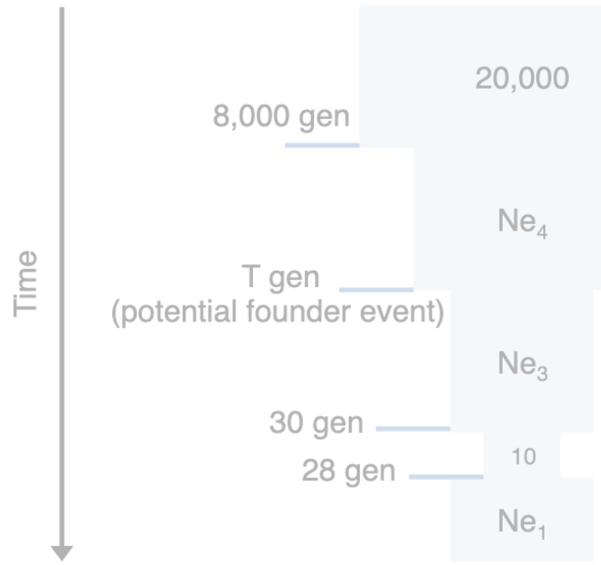
- Understand population history: bottlenecks, gene flow, etc.
- Conservation: historical genetic diversity of endangered species



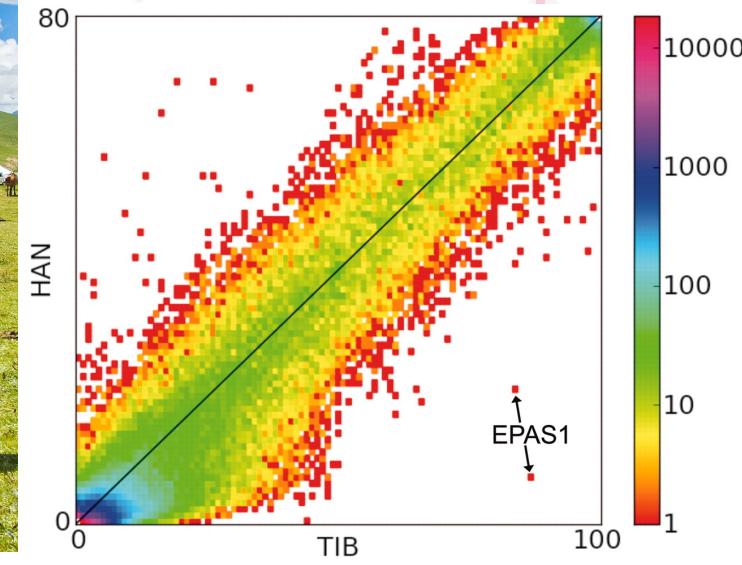
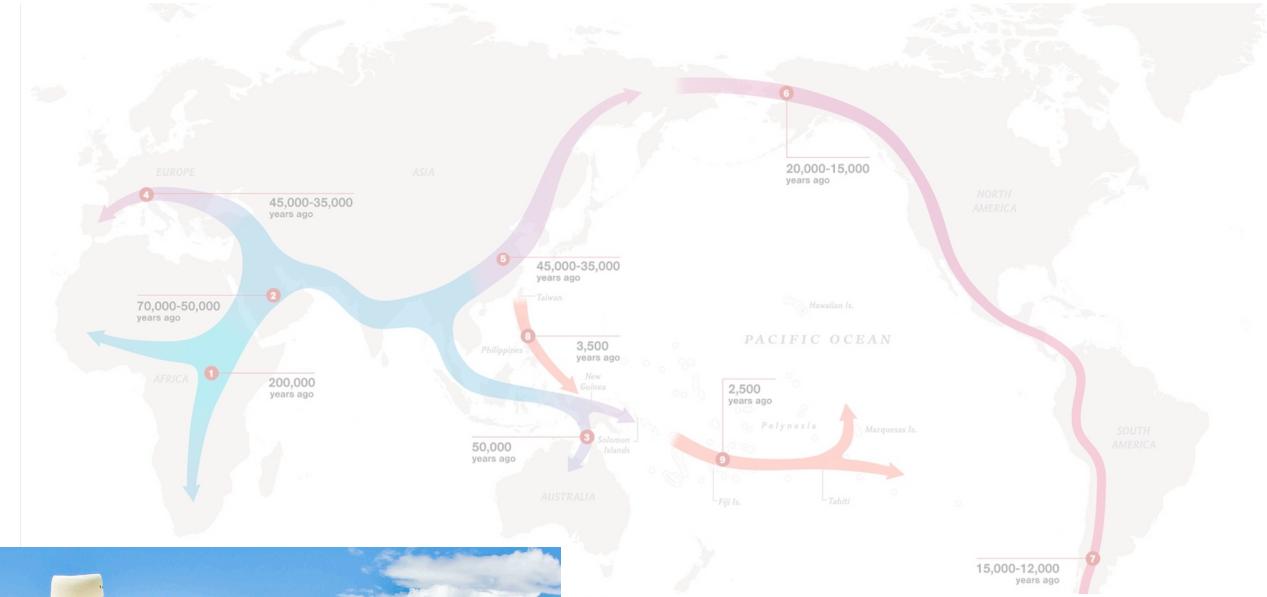
# Demographic history inference – Motivation

National Geographic

- Understand population history: bottlenecks, gene flow, etc.
- Conservation: historical genetic diversity of endangered species
- Selection: sets neutral background for detecting adaptation



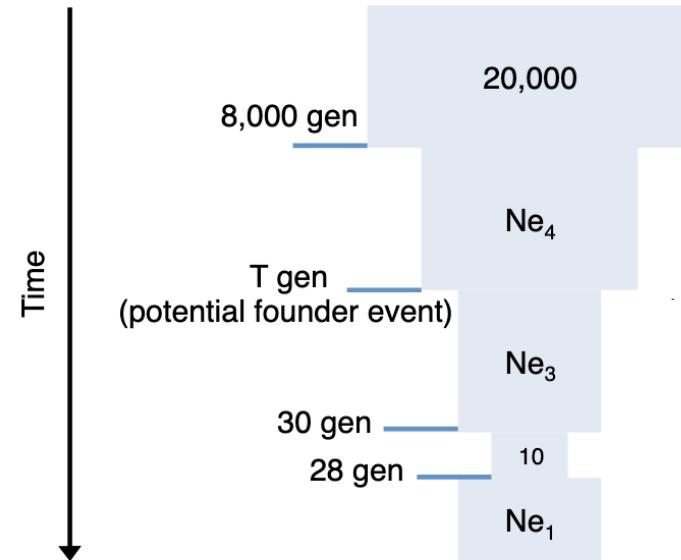
Robinson et al. (2016) *Current Biology*



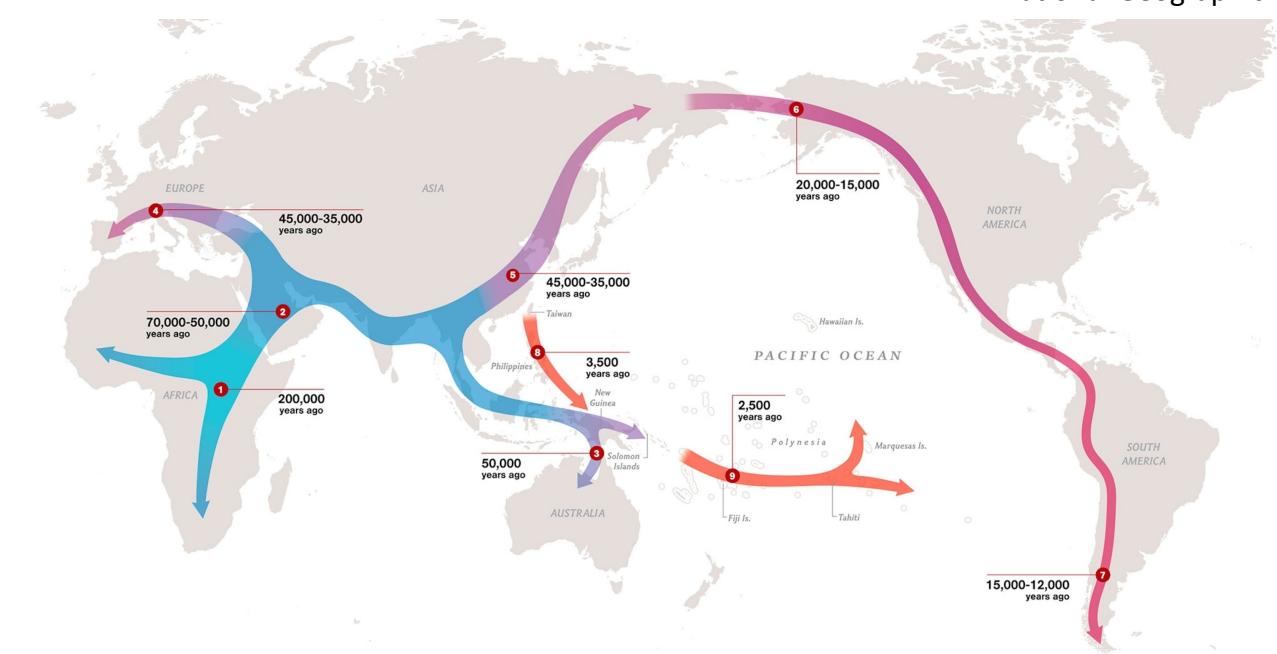
Yi et al. (2010) *Science*

# Demographic history inference – Motivation

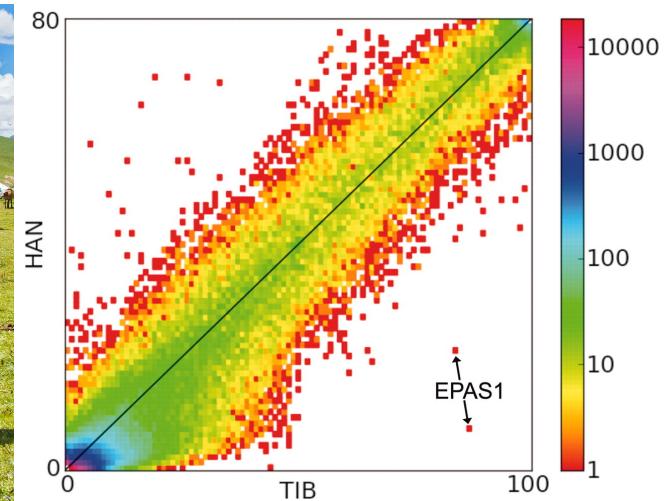
- Understand population history: bottlenecks, gene flow, etc.
- Conservation: historical genetic diversity of endangered species
- Selection: sets neutral background for detecting adaptation



Robinson et al. (2016) *Current Biology*



National Geographic



Yi et al. (2010) *Science*

# Diffusion approximation for demographic inference (dadi)

PLOS GENETICS

BROWSE PUBLISH ABOUT SEARCH  advanced search

OPEN ACCESS  PEER-REVIEWED

RESEARCH ARTICLE

## Inferring the Joint Demographic History of Multiple Populations from Multidimensional SNP Frequency Data

Ryan N. Gutenkunst , Ryan D. Hernandez, Scott H. Williamson, Carlos D. Bustamante

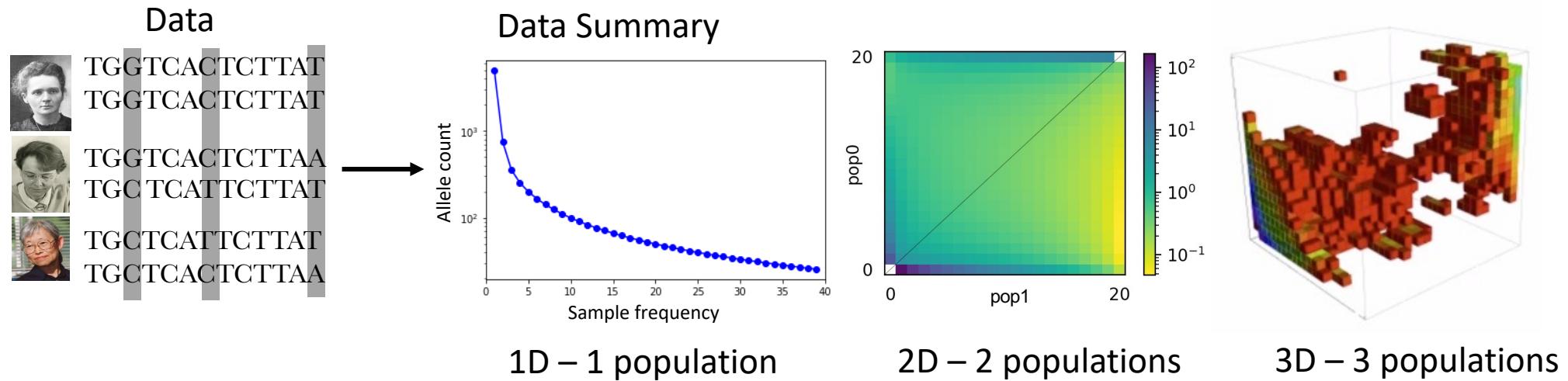
Published: October 23, 2009 • <https://doi.org/10.1371/journal.pgen.1000695>



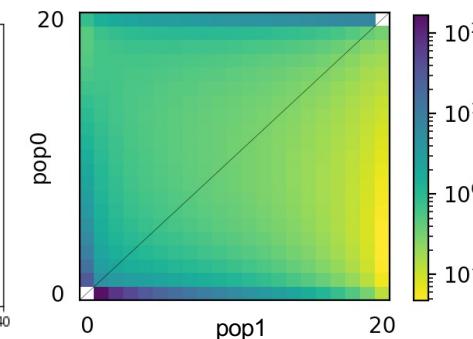
≡  Groups

☆ dadi-user 391 members

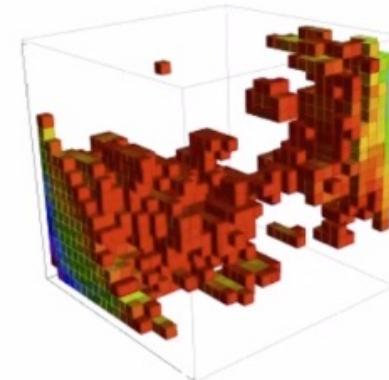
# Diffusion approximation for demographic inference (dadi)



1D – 1 population

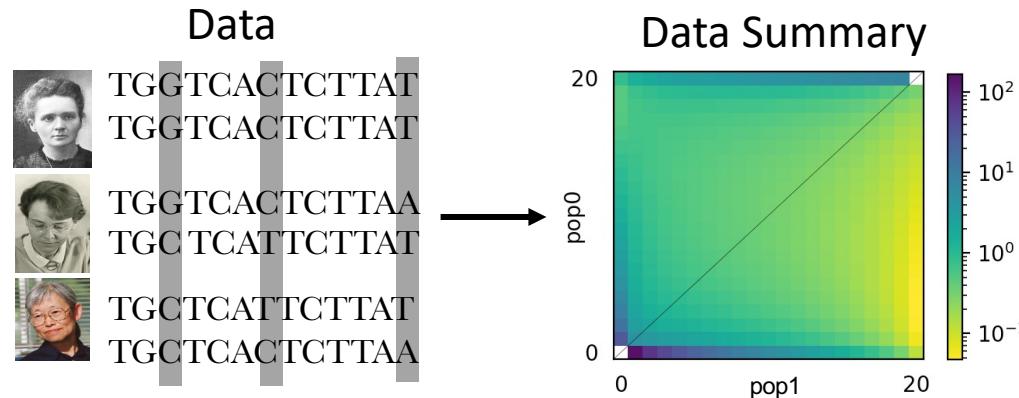


2D – 2 populations

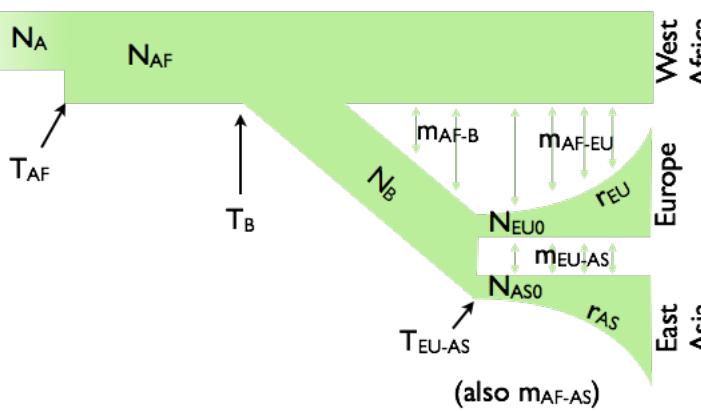


3D – 3 populations

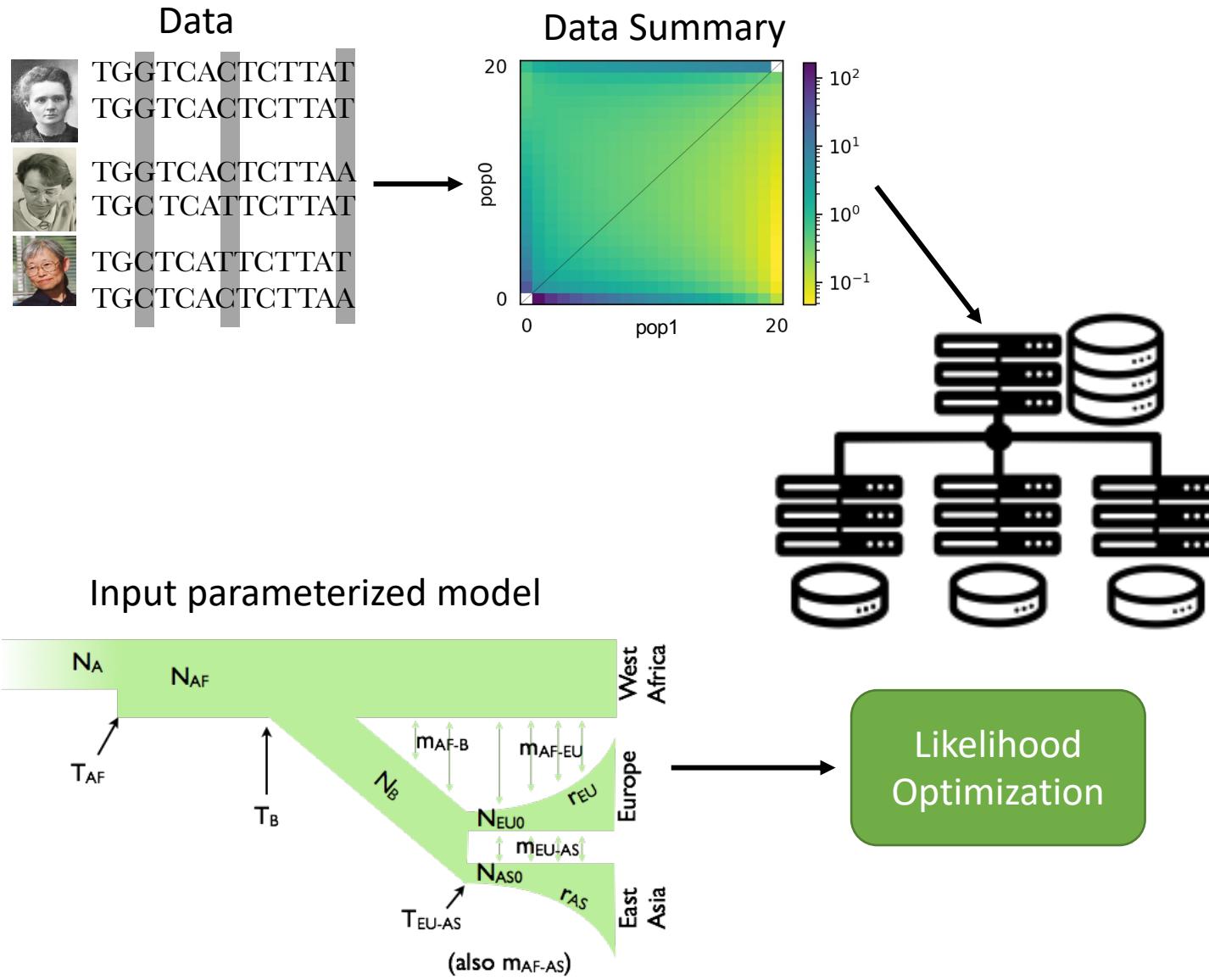
# Diffusion approximation for demographic inference (dadi)



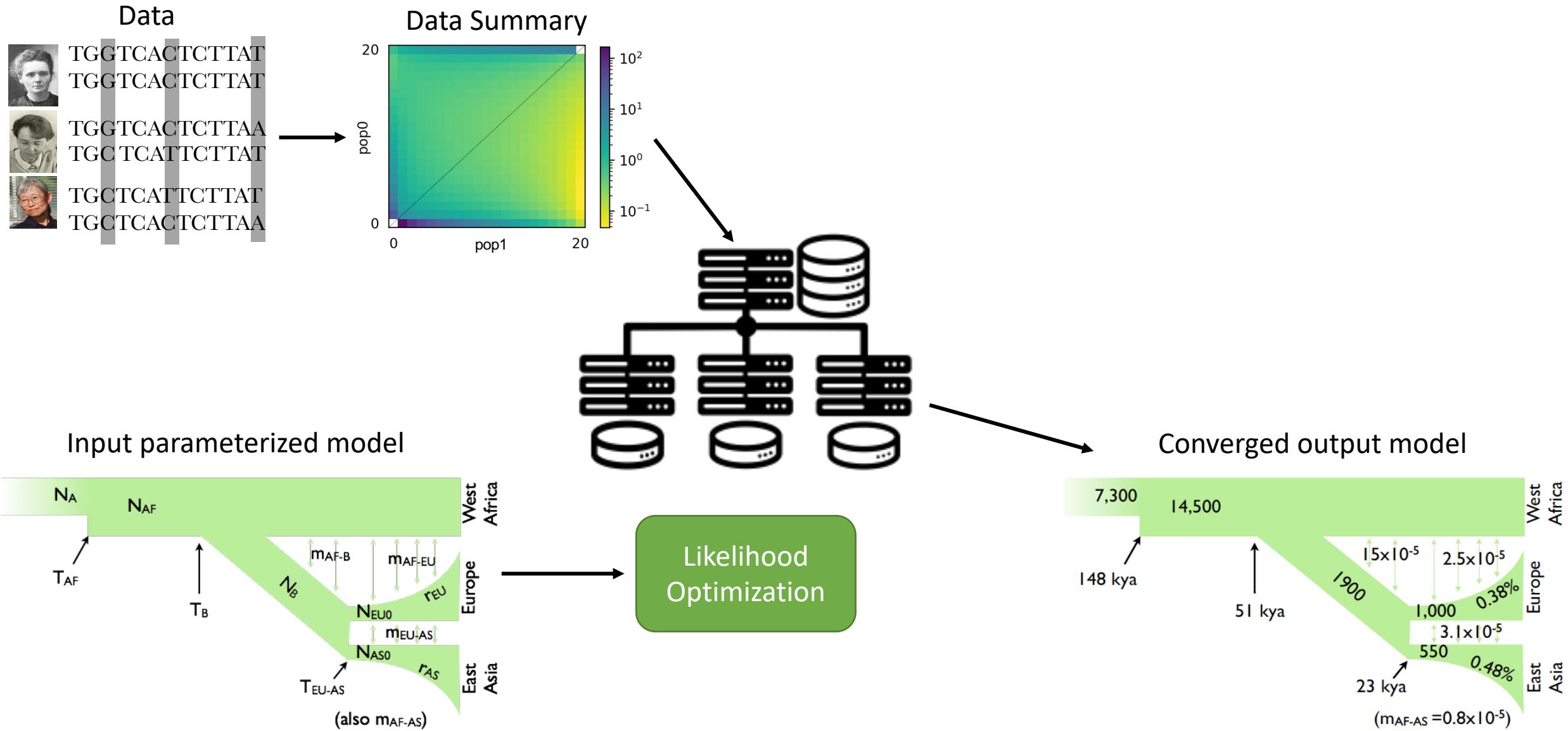
Input parameterized model



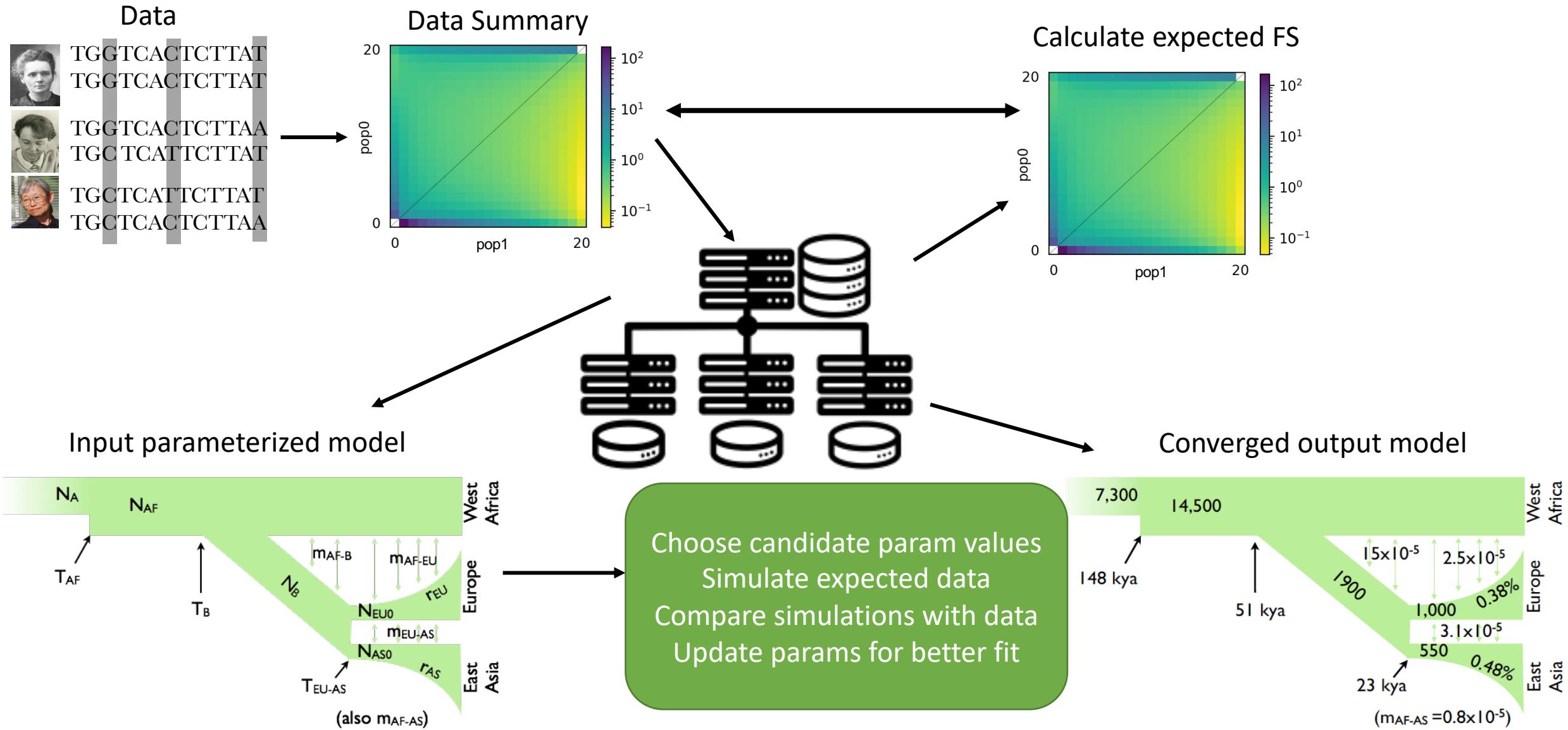
# Diffusion approximation for demographic inference (dadi)



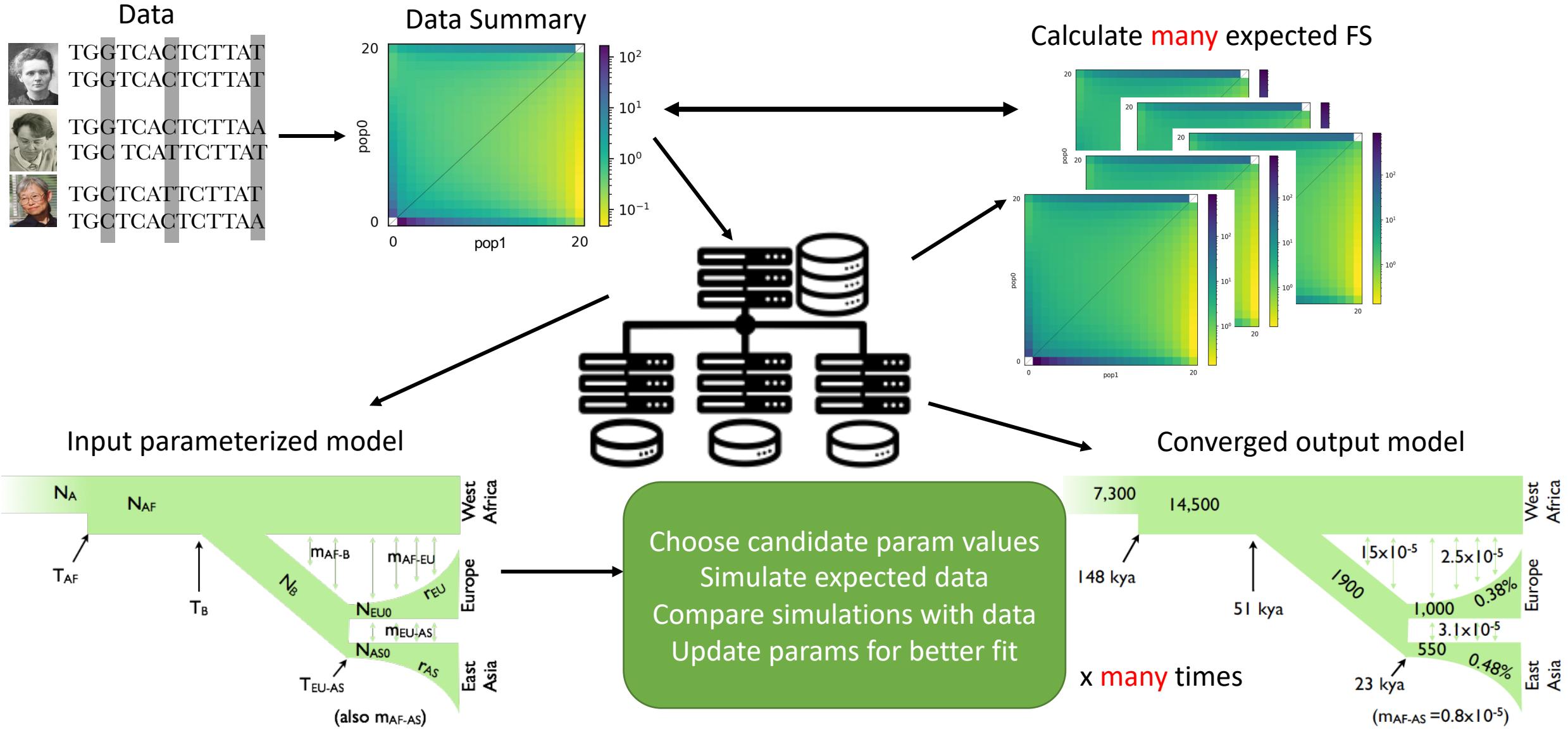
# Diffusion approximation for demographic inference (dadi)



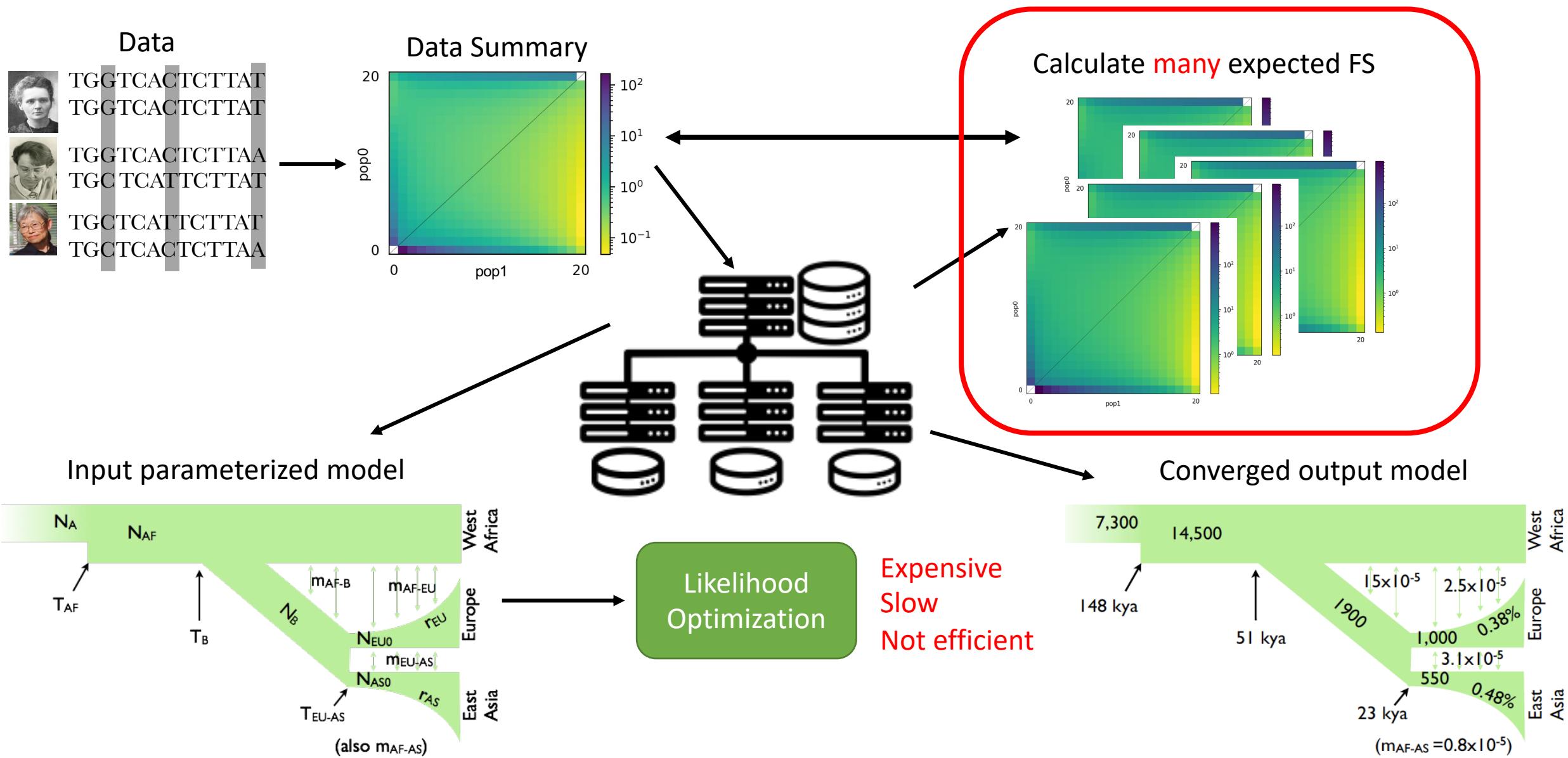
# Diffusion approximation for demographic inference (dadi)



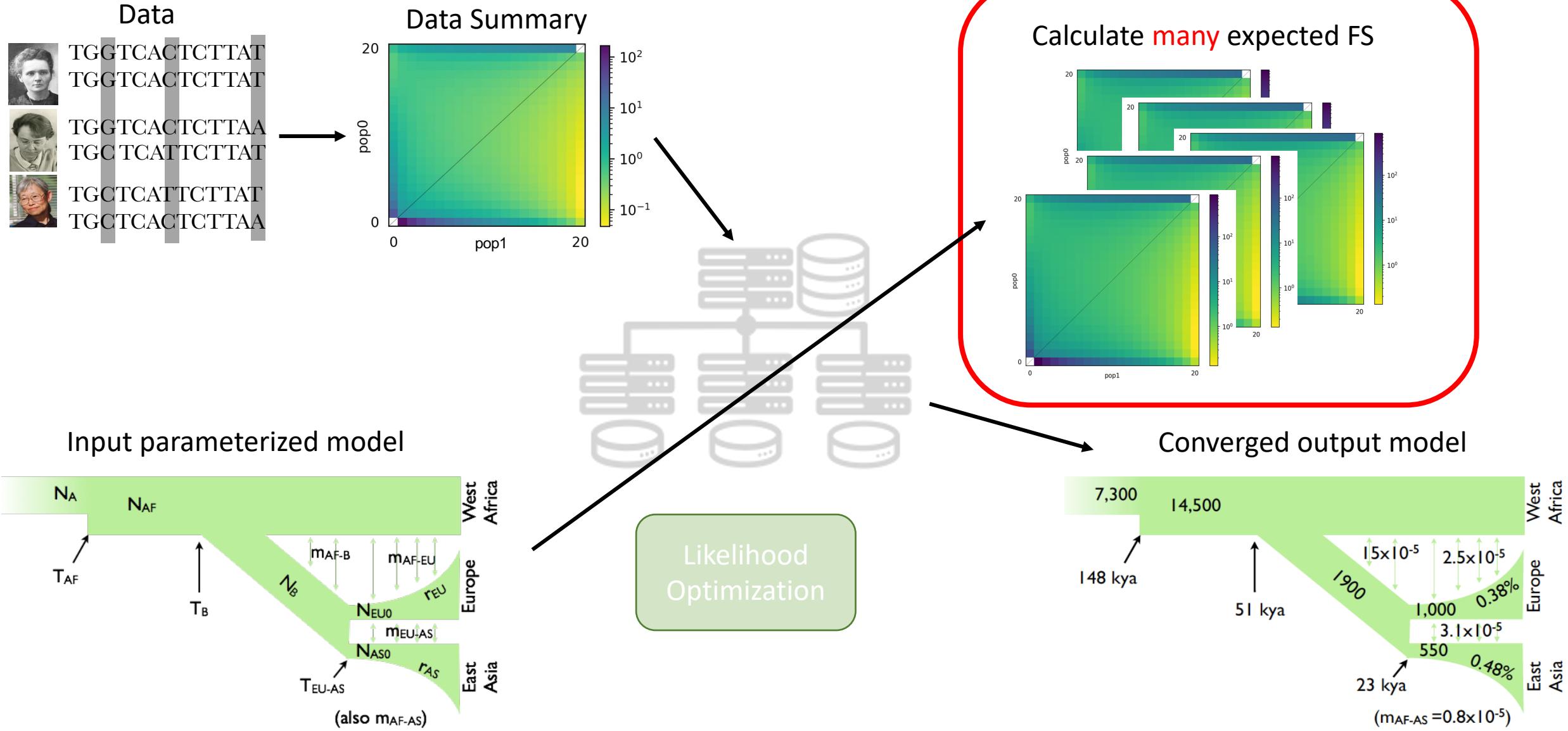
# Diffusion approximation for demographic inference (dadi)



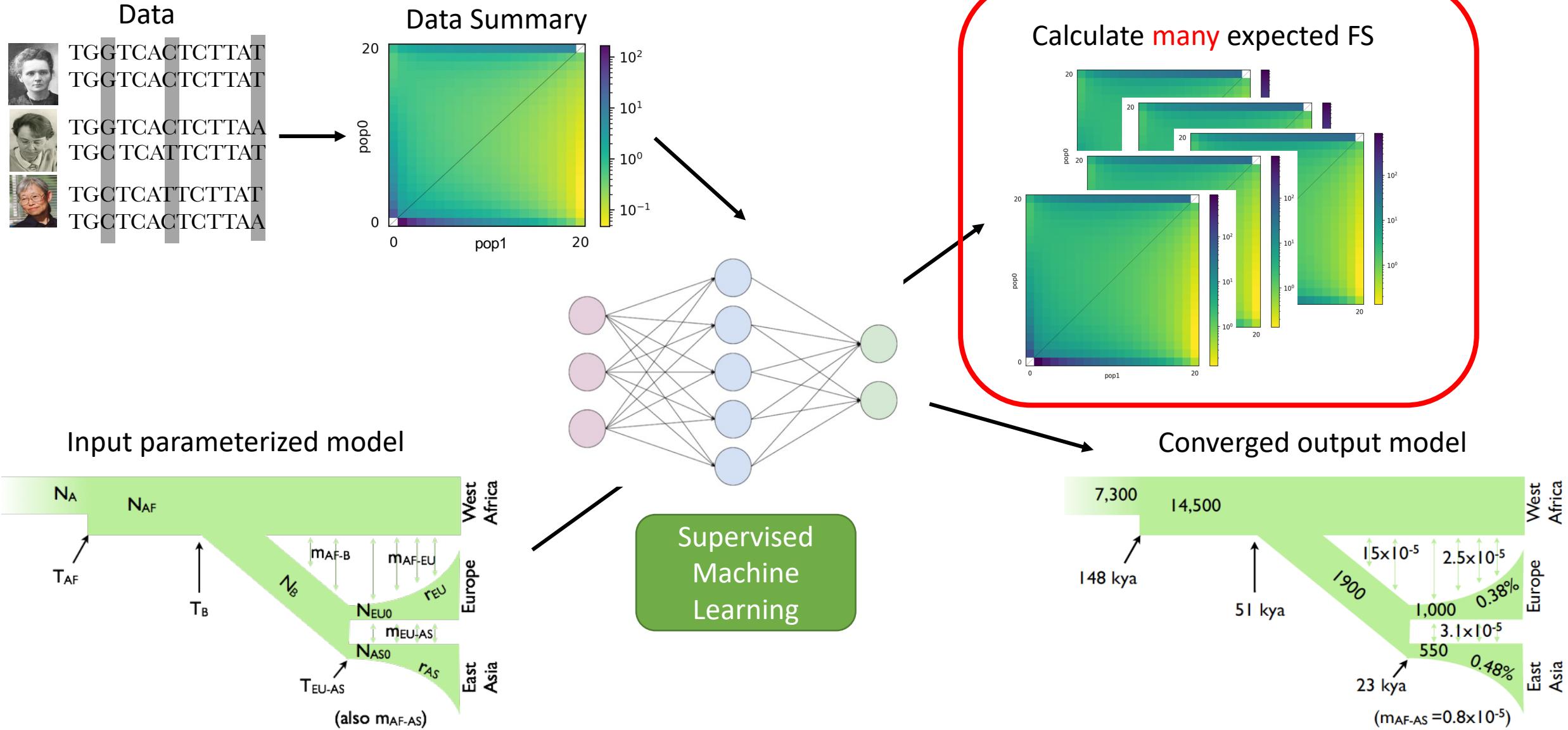
# Diffusion approximation for demographic inference (dadi)



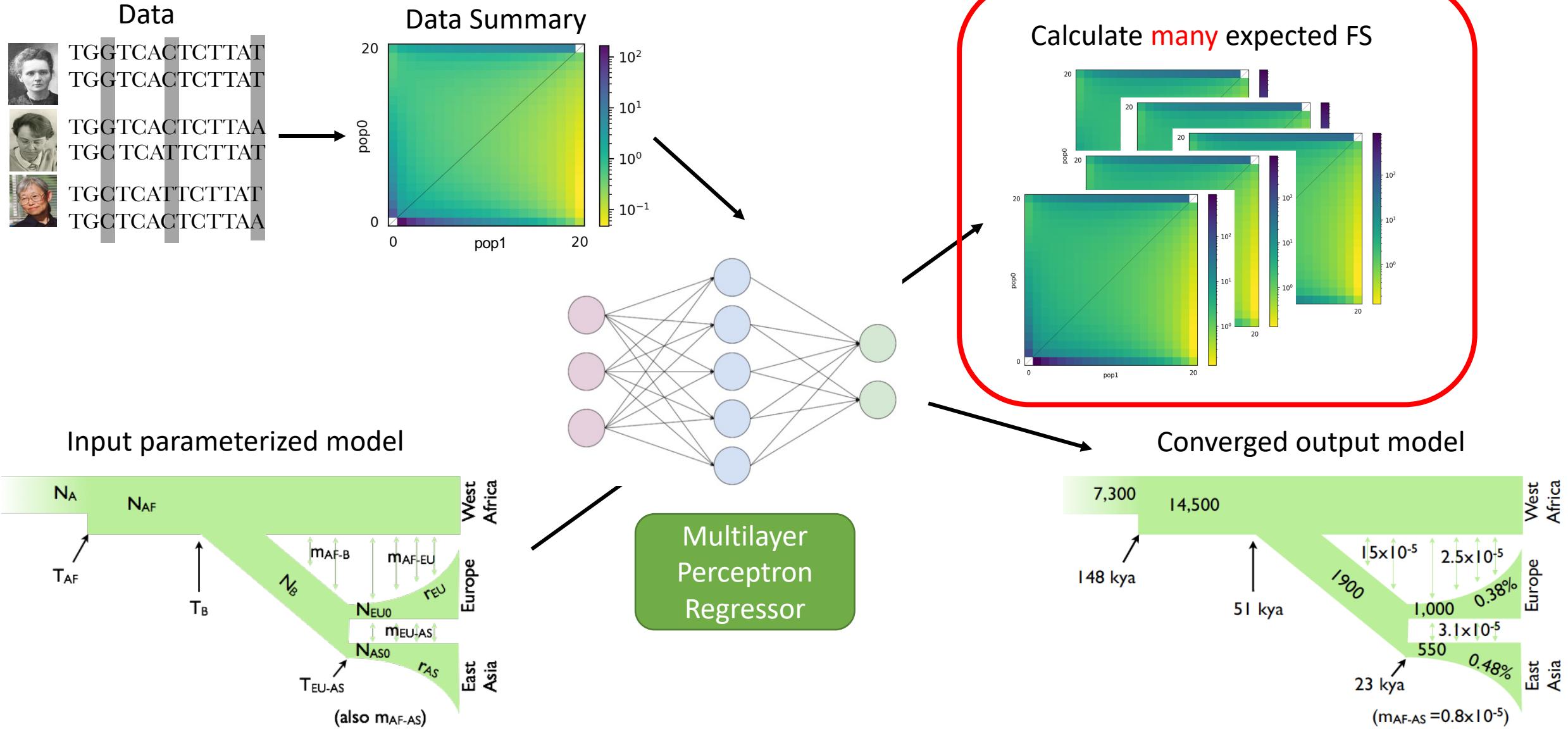
# Diffusion approximation for demographic inference (dadi)



# Diffusion approximation for demographic inference (dadi)



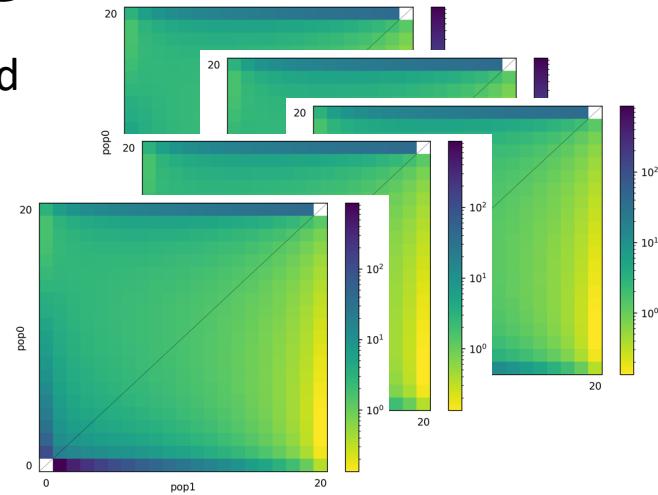
# Diffusion approximation for demographic inference (dadi)



# dadi-machine learning workflow

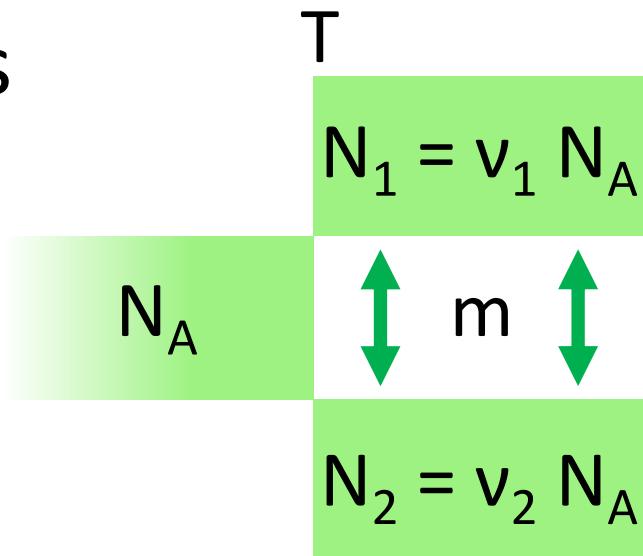
## Training data

dadi-simulated  
spectra  
(1000)



## Labels

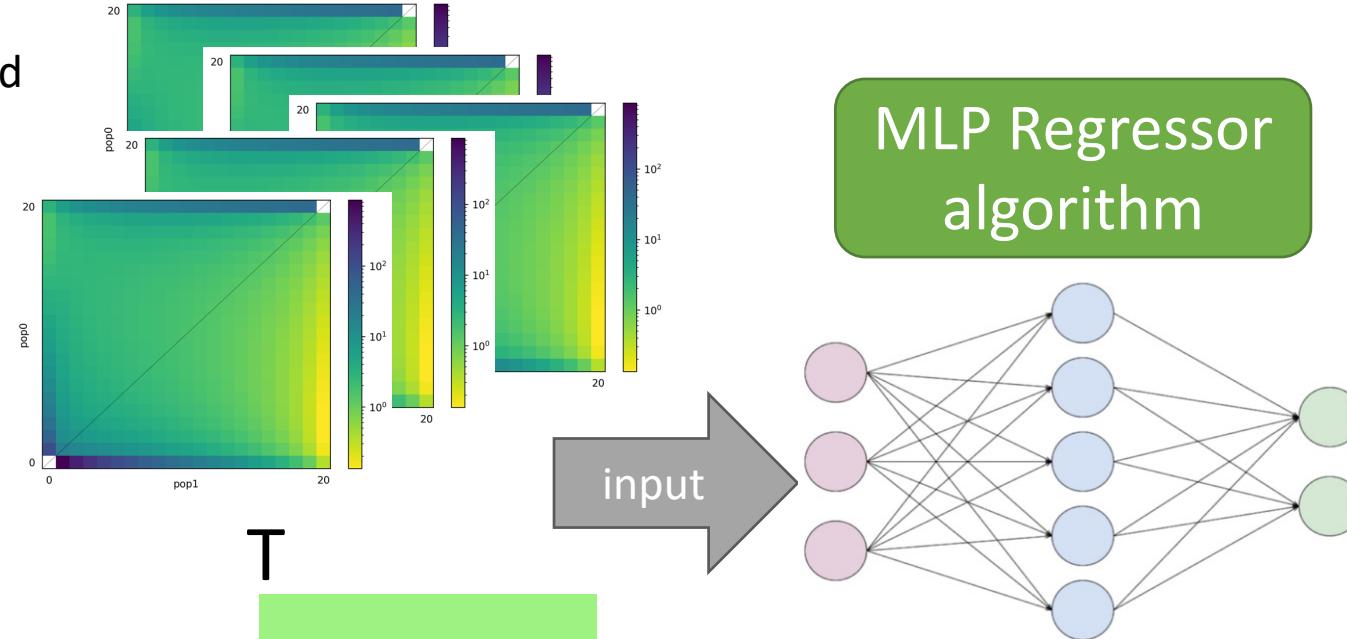
parameter  
values



# dadi-machine learning workflow

## Training data

dadi-simulated  
spectra  
(1000)



## Labels

parameter  
values

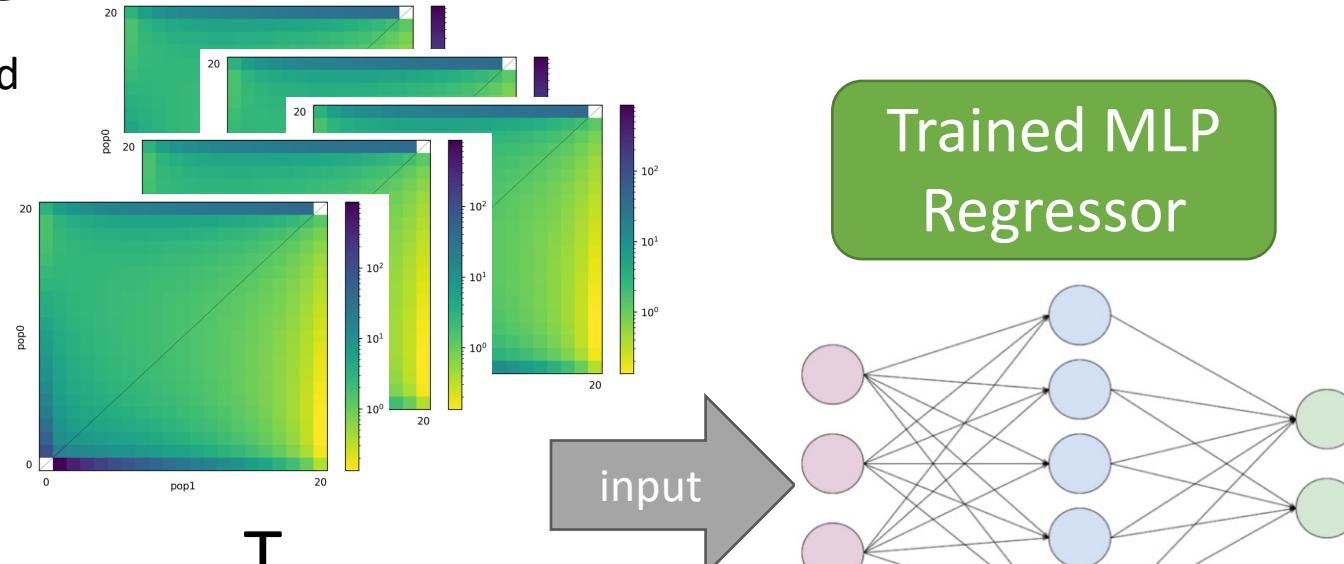
$$\begin{matrix} & T \\ N_1 = v_1 N_A & \end{matrix}$$
$$\begin{matrix} N_A & m \\ \uparrow \downarrow & \uparrow \downarrow \\ N_2 = v_2 N_A & \end{matrix}$$

Learns:  
Finds pattern  
of association

# dadi-machine learning workflow

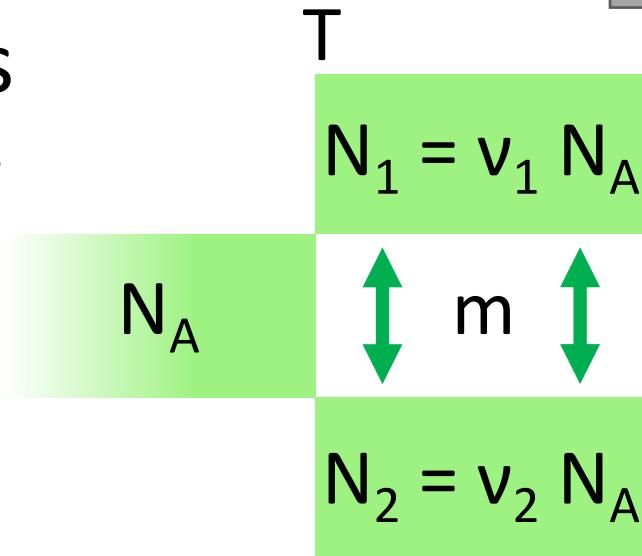
## Training data

dadi-simulated  
spectra  
(1000)



## Labels

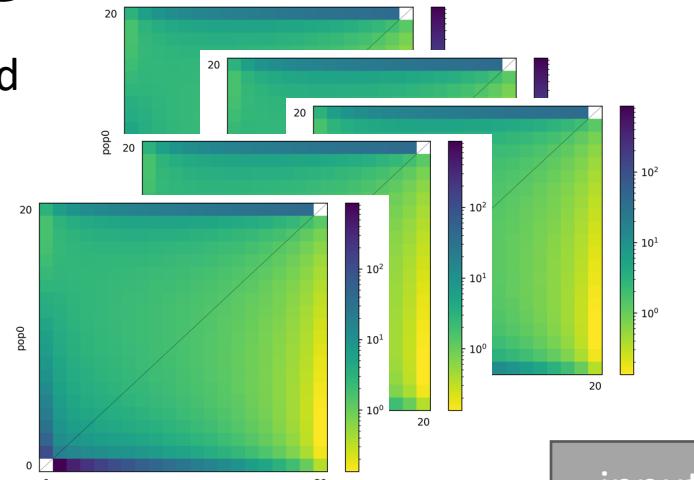
parameter  
values



# dadi-machine learning workflow

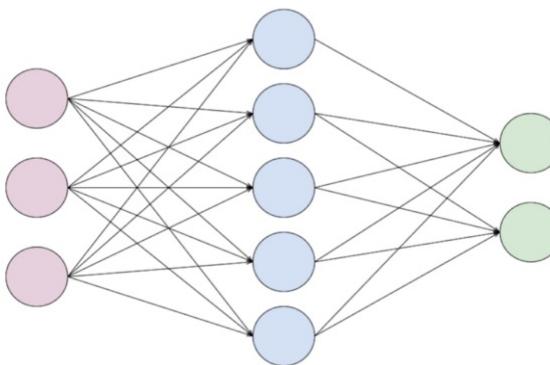
## Training data

dadi-simulated  
spectra  
(1000)



Trained MLP  
Regressor

input



## Labels

parameter  
values

$$\begin{matrix} & T \\ N_1 = v_1 N_A & \\ \uparrow \downarrow & m \\ N_A & \\ \uparrow \downarrow & \\ N_2 = v_2 N_A & \end{matrix}$$

**Strength** of frequency spectra simulation with dadi:

- Faster and less expensive than coalescent simulations
- Organism-agnostic and transferability

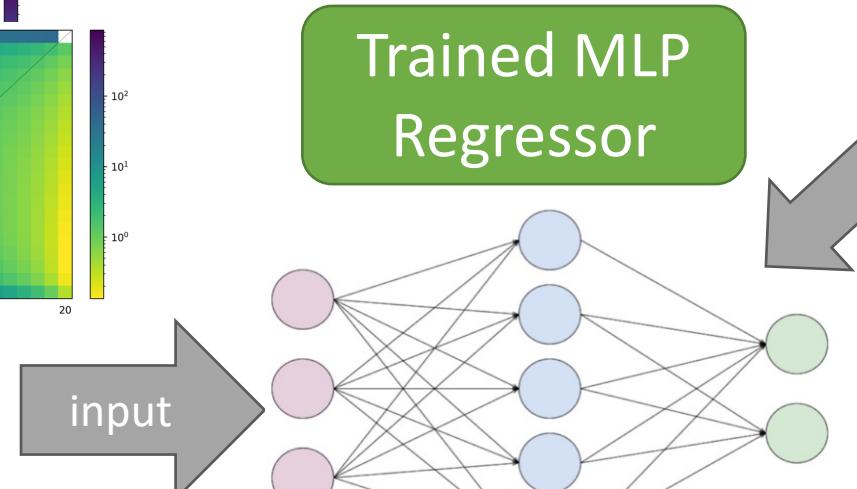
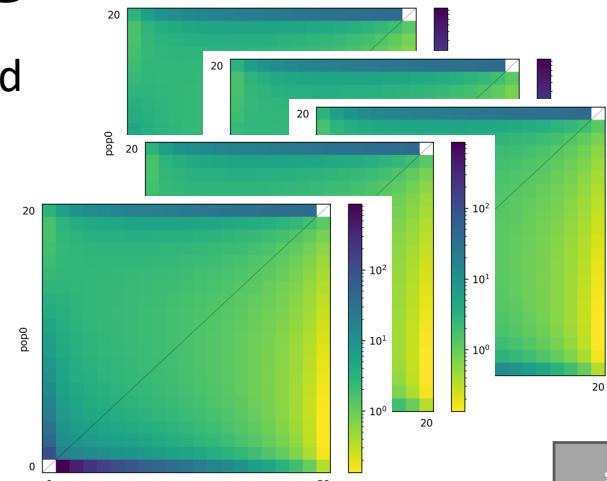
**Weakness:**

- Ignores linkage

# dadi-machine learning workflow

## Training data

dadi-simulated  
spectra  
(1000)

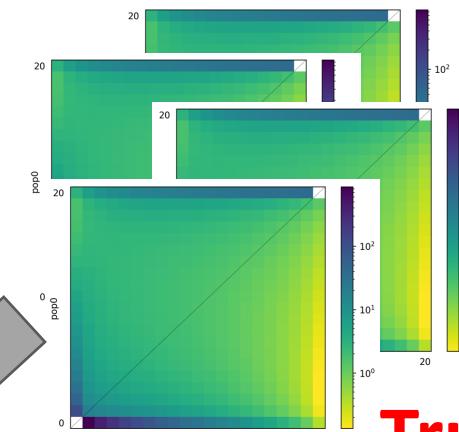


## Labels

parameter  
values

$$\begin{matrix} & T \\ & \downarrow \\ N_1 = v_1 N_A & \\ \hline N_A & \leftrightarrow m \leftrightarrow \\ & \downarrow \\ N_2 = v_2 N_A & \end{matrix}$$

## Test data



dadi- and  
msprime-  
simulated  
spectra  
(100-200)

**True params:**  
set aside for  
comparison

**Strength** of frequency spectra simulation with dadi:

- Faster and less expensive than coalescent simulations
- Organism-agnostic and transferability

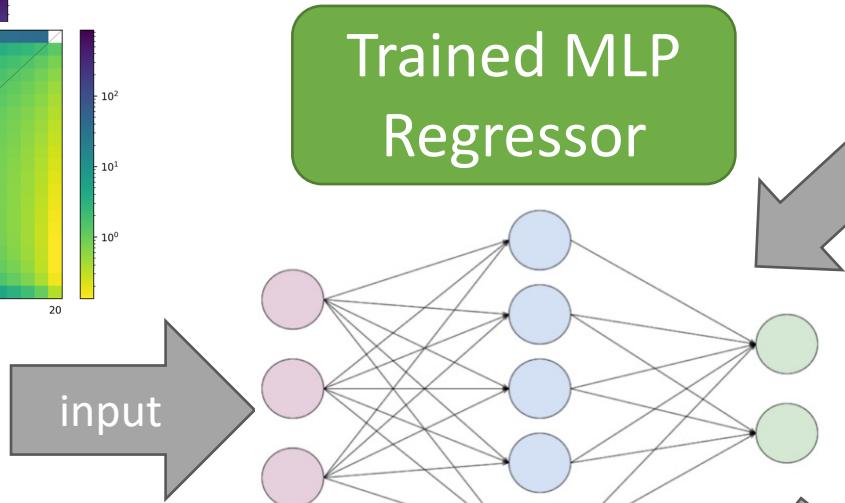
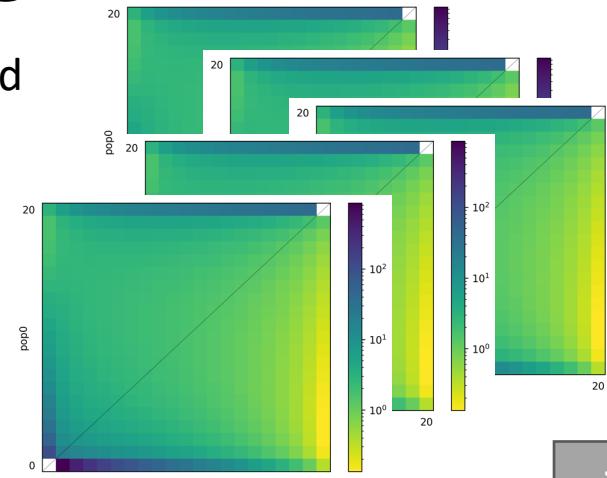
**Weakness:**

- Ignores linkage

# dadi-machine learning workflow

## Training data

dadi-simulated  
spectra  
(1000)



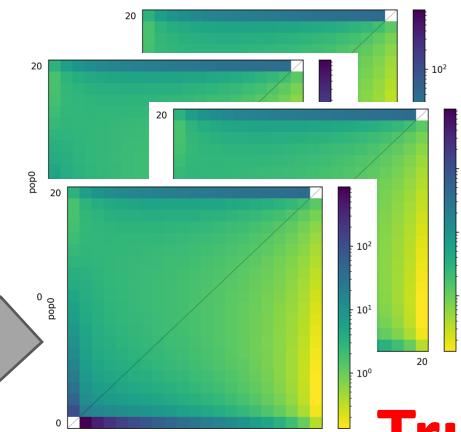
Trained MLP  
Regressor

## Labels

parameter  
values

$$\begin{matrix} & T \\ & \downarrow \\ N_1 = v_1 N_A & \\ \uparrow & m & \downarrow \\ N_A & & \\ \uparrow & m & \downarrow \\ N_2 = v_2 N_A & \end{matrix}$$

## Test data



dadi- and  
msprime-  
simulated  
spectra  
(100-200)

**True params:**  
set aside for  
comparison

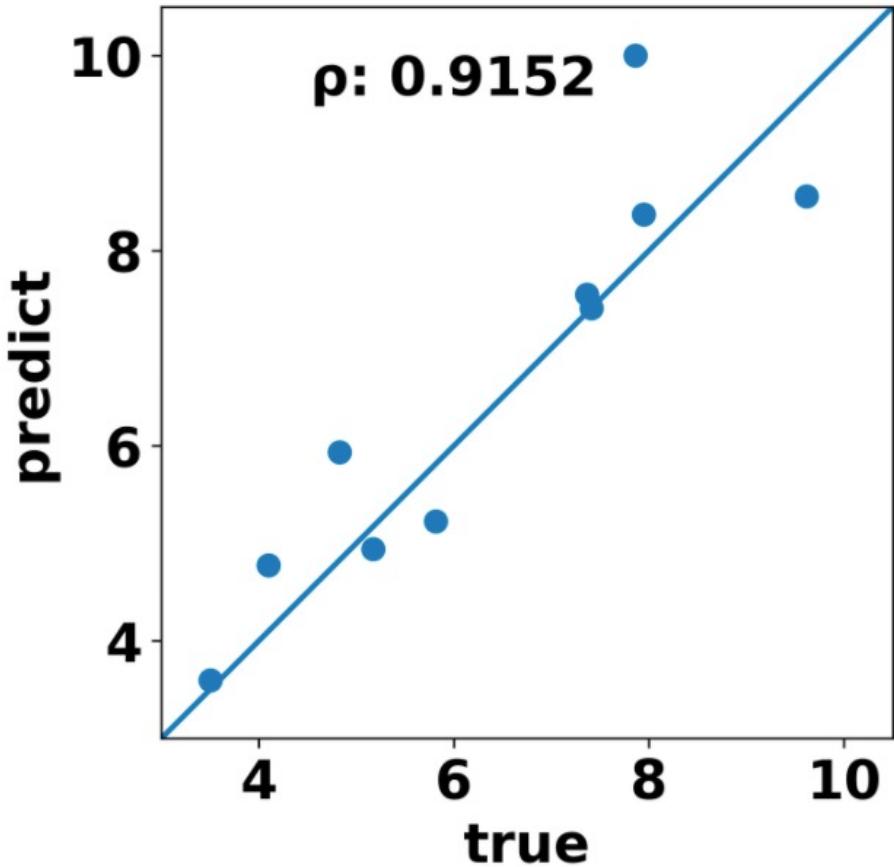
## Prediction

param values for  
each test spectrum

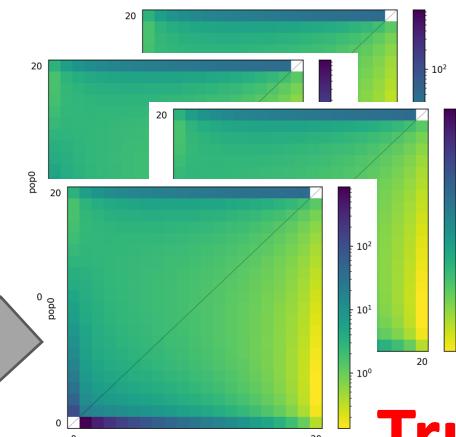
**Predict :**  
 $v_1 = 0.1$   
 $v_2 = 0.5$   
 $T = 1.3$   
 $m = 5$

# Testing and validation

## Prediction accuracy

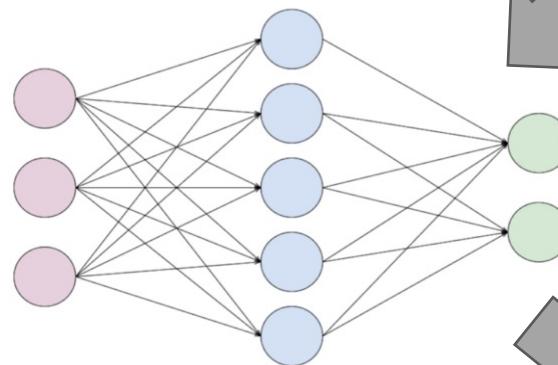


## Test data



dadi- and  
msprime-  
simulated  
spectra  
(100-200)

Trained MLP  
Regressor



True params:  
set aside for  
comparison

## Prediction

param values for  
each test spectrum

**Predict :**  
 $v_1 = 0.1$   
 $v_2 = 0.5$   
 $T = 1.3$   
 $m = 5$

# Results – prediction accuracy

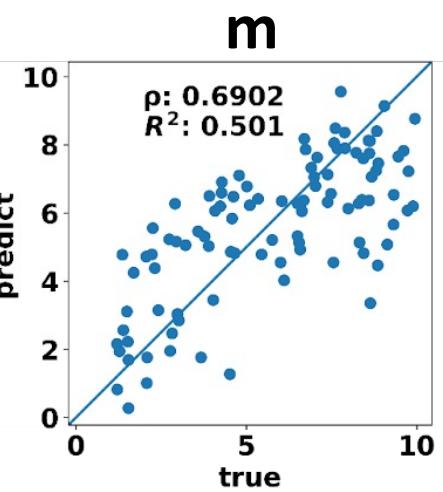
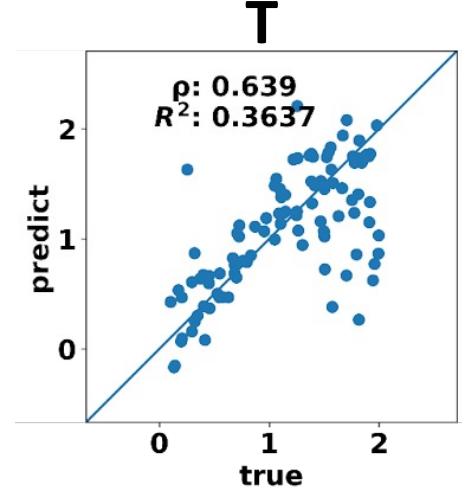
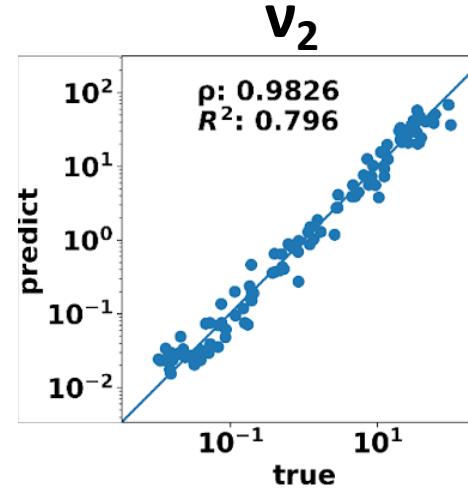
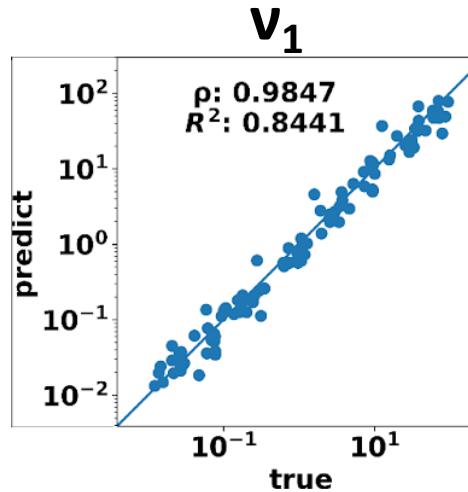
two-population  
split-migration model

$$N_1 = v_1 N_A$$

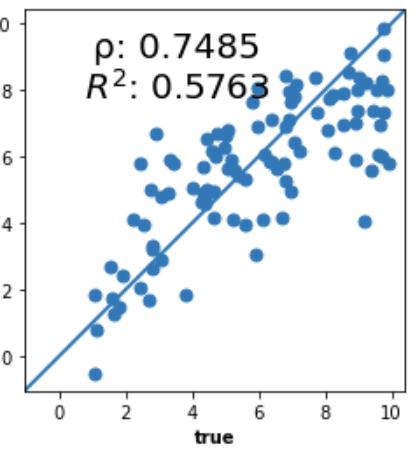
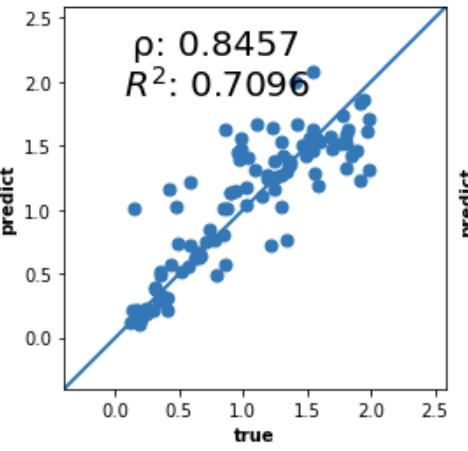
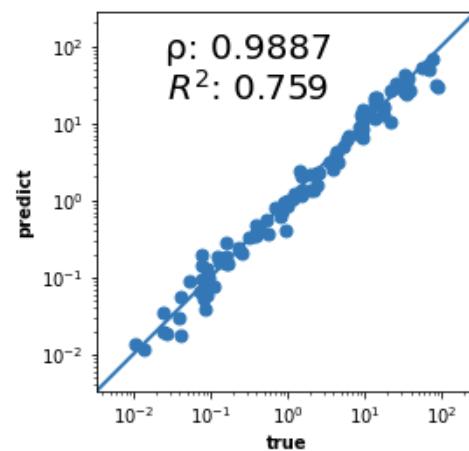
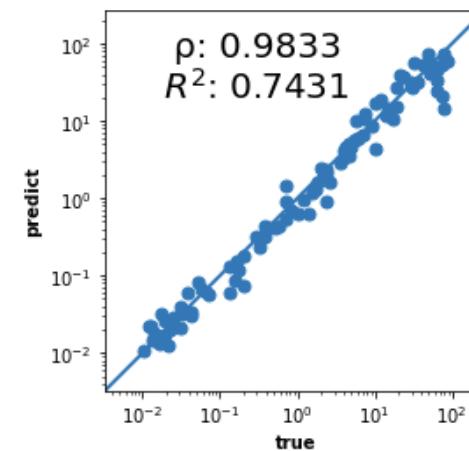
$$N_A \uparrow \downarrow m \uparrow \downarrow$$

$$N_2 = v_2 N_A$$

MLPR



dadi-simulated  
data sets



msprime-simulated  
data sets

# Results – prediction accuracy

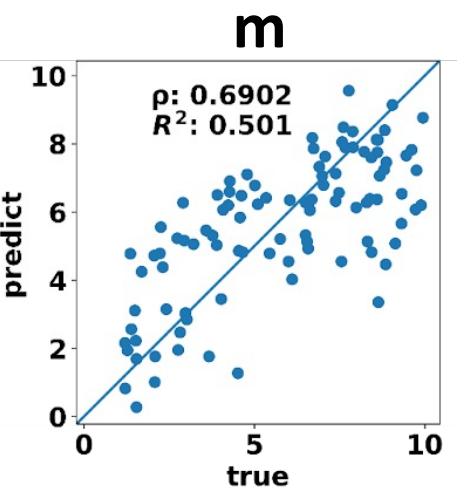
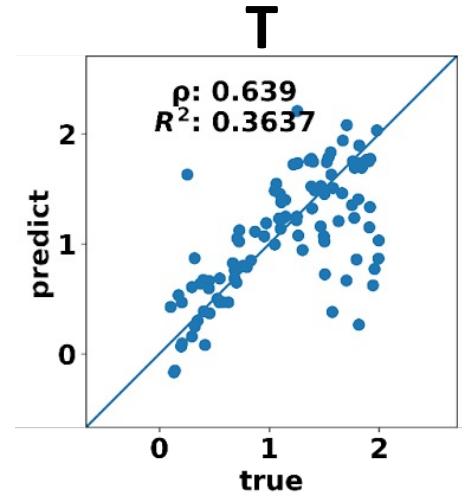
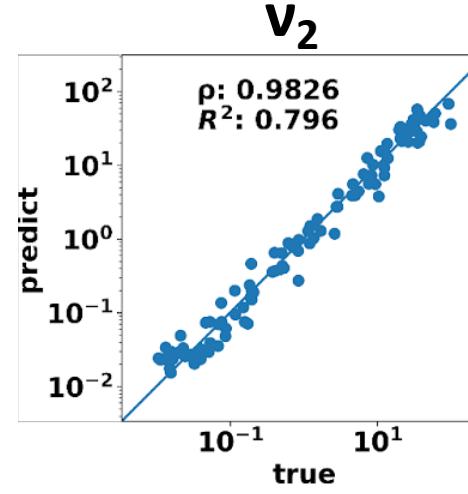
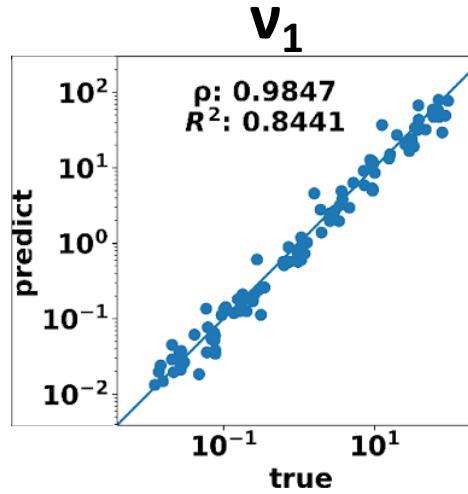
two-population  
split-migration model

$$N_1 = v_1 N_A$$

$$N_A \uparrow \downarrow m \uparrow \downarrow$$

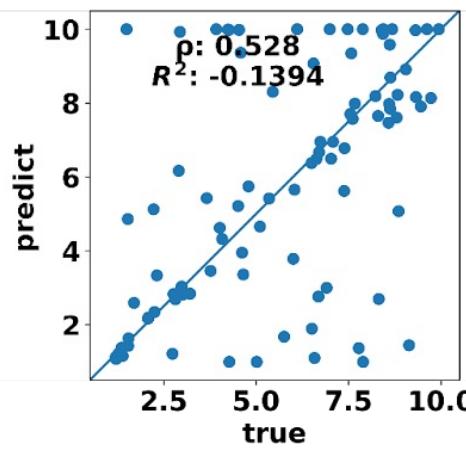
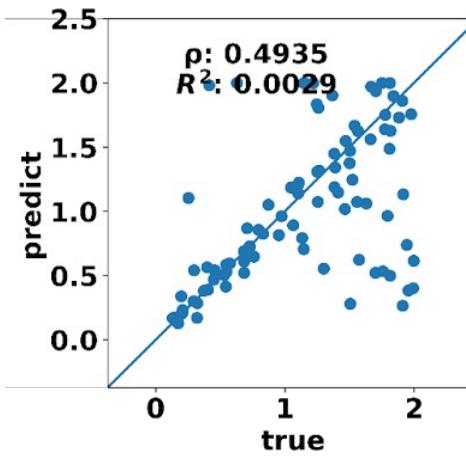
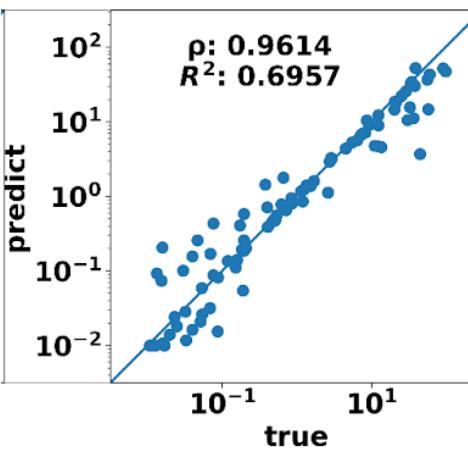
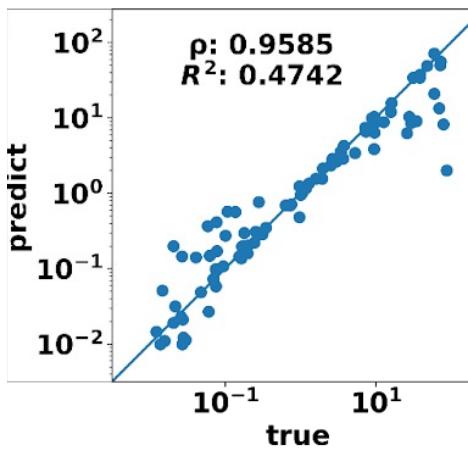
$$N_2 = v_2 N_A$$

MLPR



dadi-simulated  
data sets

dadi



dadi-simulated  
data sets

# Results – prediction accuracy and computational efficiency

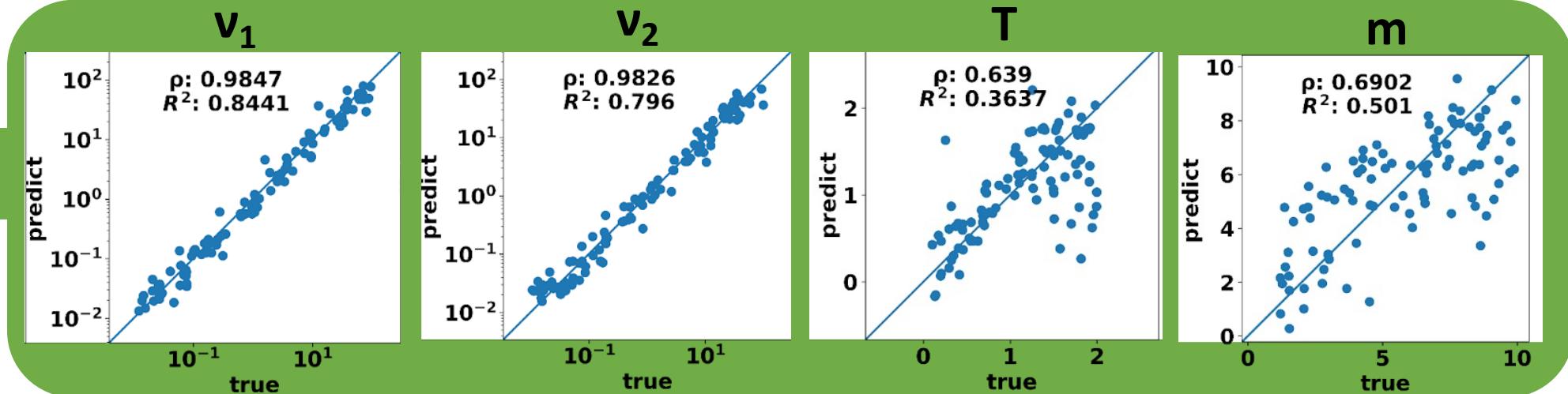
two-population  
split-migration model

$$N_1 = v_1 N_A$$

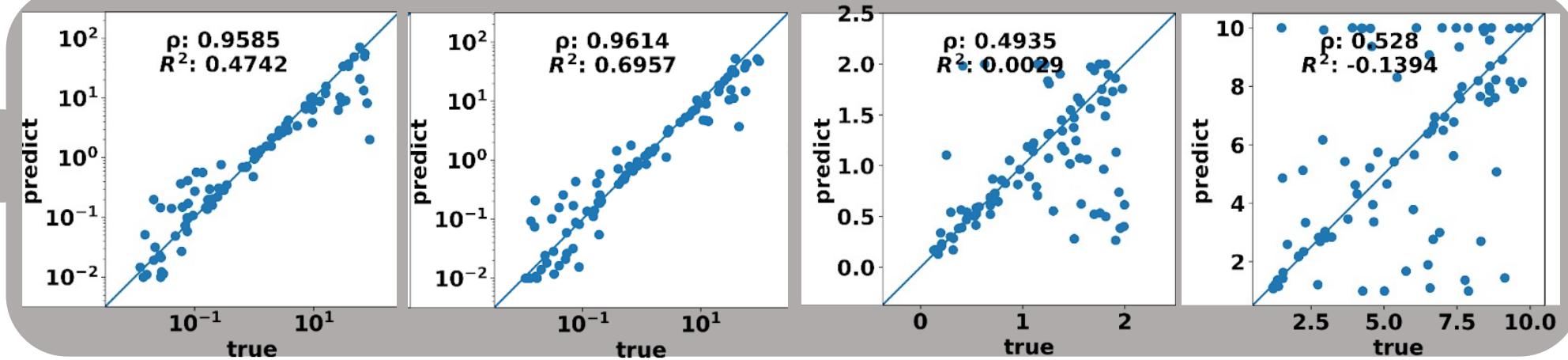
$$\uparrow \downarrow m \uparrow \downarrow$$

$$N_2 = v_2 N_A$$

MLPR



dadi



# Summary

- Machine learning approach to improve the computational efficiency of a widely used likelihood-based demographic inference method
- Comparable accuracy with significantly reduced computational cost & complexity
- Robust to test simulations generated with linkage
- Accompanying uncertainty quantification method that provides prediction intervals
- Trained MLPs for frequently used demographic models and workflow will be distributed



@LnTran26

<http://gutengroup.arizona.edu>

