

Question 3 c) updated

For all simulations, the variance of disturbance was set as 0.1

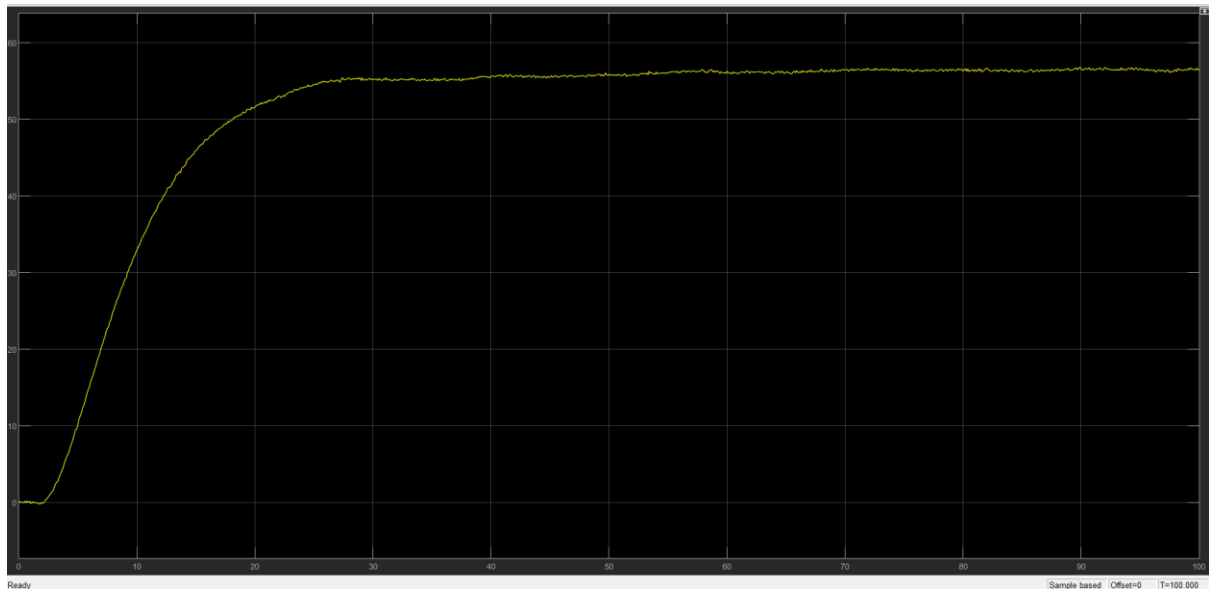


Figure: Plot of step response of the closed loop system for $K_c = 0.7636$ (part-a)

We see that G_{C1} has an offset of about 55.

For controller design using Pade's second order approximation, we use the rltool on L to get -0.2 as real part of the dominant pole as shown in the below figure

Gp_pade_second =

$$\frac{64 s^3 - 128 s^2 + 1024}{32 s^4 + 192 s^3 + 416 s^2 + 128 s - 768}$$

Continuous-time transfer function.

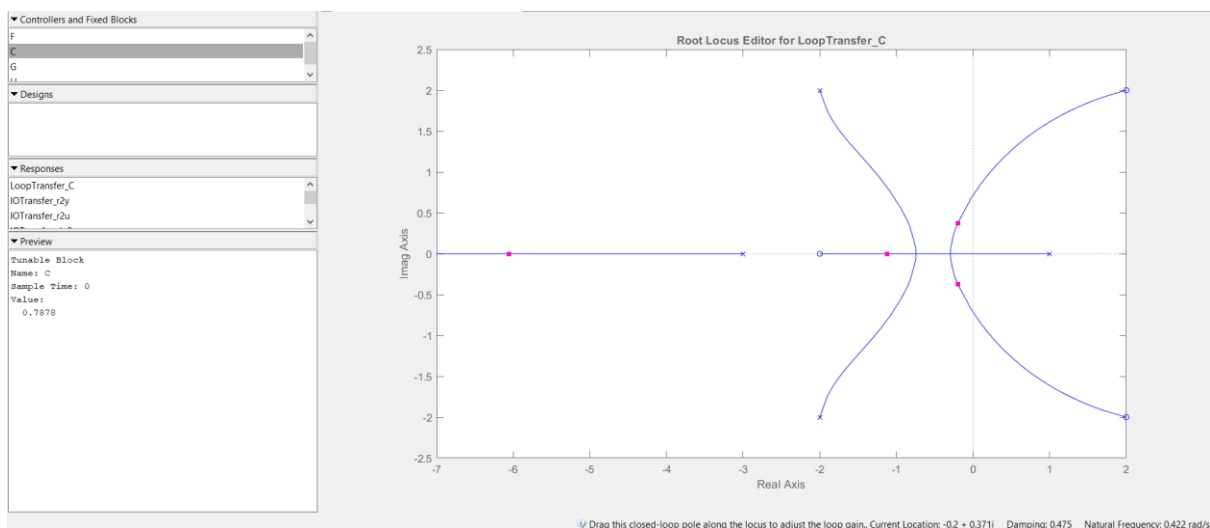


Figure: RL plot with the required roots marked. (along with the K_C value)

$K_C = 0.7878$

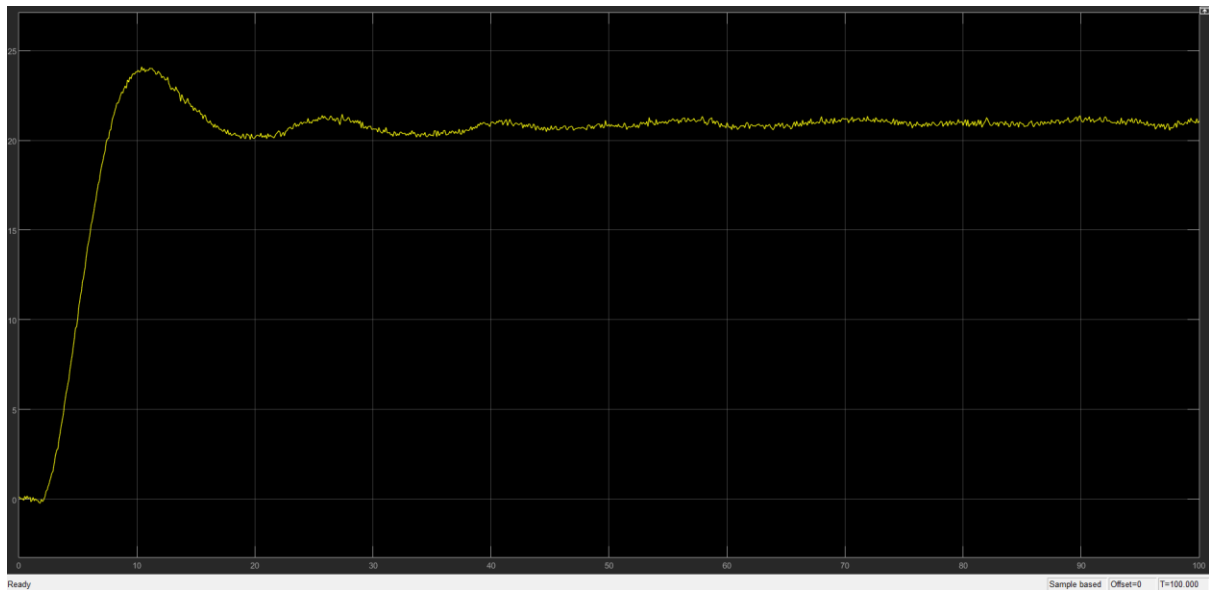


Figure: step response of the closed loop system with $K_C = 0.7878$

Conclusion: Closed loop system with controller from part b) is unstable as shown earlier. We see that the offset with controller from part a) (~55) is much greater than controller from part c) (~21). So we conclude that controller proposed by utilizing Pade's second order approximation has proven to be more effective in dealing with the actual system.

Code:

```
clear; close all;
%% Setup the system
s = tf('s');
Gp = 2*(s+2)/(s^2+2*s-3)*exp(-s);
%% 3a
Gp_pade = 2*(2-s)/(s^2+2*s-3);
f = @(s)(2*(2-s)/(s^2+2*s-3));
Kc_a = -1/(f(-0.2));
poles_parta = pole(1/(1+Kc_a*Gp_pade))
%% 3c
Gp_pade_second = 2*(s+2)*(1-s/2+s^2/8)/((s^2+2*s-3)*((1+s/2+s^2/8)));
rltool(Gp_pade_second)
%0.7878
```