CH 3050 PDC ASSUN-6

BY18-VUHAL CH18B020

For stability SCO (All CHPpoles) pole, 3 = 1 (1+1) My 19/ 30.2 J. 1. 2 - 0.2 = 27-1 . The pole remains in LHP urrespectful of Free to choose any to 70 even when K is uncertain 1.15 Grd = 55-11 GP = 80 524 (554) SUSZEUS EL (BID Controller) H & PIDboth are in combination Copy + Ord Do - 0 Orc (R-Y) + Orff Do - 3 whose boff =

y (1-e Cichip) = Giphill + (Giph) Do Do Strhpfhol (følter added to make it realisally Here Green - Gran (15-11) = - (105-(1) (125-11)(1.15) reporter Den (Cyther had) d (21-1.1) (21-11) (21-11) For fettling tim 715, TXZ. But here tominant 7 3.

So the bust toething we can get is around 25 minuts. the same was confirmed by sease! trying to solve the prethi må | trette - (5). Leane to be done to D (15⁻³) lowester band 141631 of reach faethe u 25 minuts

(H30570 Augn-6 BY: S.VISHAL CA (813050 (2) α Some court flure is no delay or inverse Jupponse, al can fit a Sevond order model the model is estimated my legarifit on 1-781 = L 4. Zrtr2 Step vespost model as, = Kpx KIVX K 4. 70552 + 4.361 +1 Kis the estimate from I MC the language tc = mon(t, 1t2) = 21/81 the step response 1.094 2-23857 T1-1[2 2 3 All relations = 4-3611 from table 12.1 tit2 = 1.0903 TILLZ 2-238 (1+ 1 - 1.095)

Vnig Shugestad's bull rule me : faller are available only $\frac{1}{679^{2}}$ $\frac{e^{-2.1731}}{(2.188+2.1731)}$ s+1for Hom B GAP, FORTA = 1.781 & 3.2675+1 From table 12.4, [ITAE Set point] A = 0.965, B = -0.85, KC= A (D) xet. 1 2 1.3734 · A = 3-796, B: -0.1465, TI = -4. D: A= 0-308 10-929 1 to= A () B3 XT . Gic 15 - 1-8734 1 + 1 - 0.36428

C) From take 12.4, [I TAE disturbance] P: A=1.357 B=-0.947, KC= 2.1475 Z: A= 0.842 B=-0.738/ tz = Z-3101 D: #=0.381, B=0.995, TD=0.4191 $\frac{1}{2-315} = \frac{1}{2-315} =$ CH3050 HSSGN-6

(3) a) viilt of gain: K/vadran $\frac{1}{6} = \frac{105}{(55-(1))} = \frac$ All pars factorisator: CP -(0.5) (+10541) (-10541) e (22-1) (32-1) [102-1] Ormii Graini . . 6 = Giff = + 1 Gimii (55-11) (55-11) [15-11] filter added

(55-11) (55-11) [15-11] to ensure that

(-0.5) (105-11) (15-11) it is hiproper

Here,
$$\Delta G = O(g)$$
 has $G_{r} = O(g)$ has $G_{r} =$

Some it is proper we won't trace a j'ung.
But me have i) selay

(i) Inverse Perpert (ii) RAP

$$=\frac{10(5)(10)(4)}{(-0.5)(10)(4)}=-\frac{30}{30}$$

We want this to be less than 251 - Type 7) - 30 / C - A 96° T -) 1 2 4 120 T (. . tumediately control affort

le lus than 25%)

CH 3050 ASSGN-6

S. VIS HAL

(418B122)

(4) a) From the given data 1

Gp = 0.4 c -7.55

(ru= emp(-10s) (0.52)
(305+1)

Q = - Gd

But we have non-mustible compart Use fade's fust order approximation.

 $\Rightarrow 60.6 = - 80.5 = \frac{0.5 = -10.5}{3.05 + 1} (0.4) (3.755 + 1)$

-2005² + 40572 e 2405² - 405-1.6

Question-1

```
Code
```

```
clear; close all;
tc = 5;
s = tf('s');
Gp = tf(1.15, [50 15 1]);
Gm = tf(1, [50 15 1]);
% PID controller
Gc = tf([50 \ 15 \ 1],[tc \ 0]);
% Disturbance tf
Gd = tf(1, [5 1]);
lambdavec = 0.001:0.001:0.5;
r1 = ones(length(lambdavec),1);
r2 = r1;
for k = 1:length(lambdavec)
    % Feedforward controller
    Gff = -Gd*1/(lambdavec(k)*s+1)/Gp;
    % sys is Y/Do
    sys = (Gff*Gp+Gd)/(1+Gp*Gc);
    S = stepinfo(sys);
    % get settling time as close as possible to 15
    r2(k) = S.SettlingTime;
    r1(k) = abs(S.SettlingTime-15);
end
[val, loc] = min(r1);
lambda = lambdavec(loc);
```

Question-2

Tables

Table 12.1 IMC Controller Settings for Parallel-Form PID Controller (Chien and Fruehauf, 1990)

Case	Model	K_cK	$ au_I$	$ au_D$
A	$\frac{K}{\tau s + 1}$	$\frac{\tau}{\tau_c}$	τ	-
В	$\frac{K}{(\tau_1 s + 1)(\tau_2 s + 1)}$	$\frac{\tau_1 + \tau_2}{\tau_c}$	$\tau_1 + \tau_2$	$\frac{\tau_1\tau_2}{\tau_1+\tau_2}$

Table 12.4 Controller Design Relations Based on the ITAE Performance Index and a First-Order-plus-Time-Delay Model (Lipták, 2006)*,†

Type of Input	Type of Controller	Mode	A	В
Disturbance	PI	P	0.859	-0.977
		I	0.674	-0.680
Disturbance	PID	P	1.357	-0.947
		I	0.842	-0.738
		D	0.381	0.995
Set point	PI	P	0.586	-0.916
		I	1.03^{\dagger}	-0.165^{\dagger}
Set point	PID	P	0.965	-0.85
		I	0.796^{\dagger}	-0.1465^{\dagger}
		D	0.308	0.929

^{*}Design relation: $Y = A(\theta/\tau)^B$ where $Y = KK_c$ for the proportional mode, τ/τ_I for the integral mode, and τ_D/τ for the derivative mode.

Code

```
clear; close all;
s = tf('s');
%% Given Data
Kv = 0.9; Kip = 0.75;
t = (0:1:11)';
T =
([12,12.5,13.4,14,14.8,15.4,16.1,16.4,16.8,16.9,17,16.9]'
-12)/2;
plot(t,T);
% Can't see any inverse response, so mostly no zero
assume first order plus
% time delay.
%% Model Estimation
[X,RESNORM,RESIDUAL,EXITFLAG] = lsqcurvefit(@resp,[5 2
1],t,T);
K = X(1) * Kv * Kip;
tau1 = X(2);
tau2 = X(3);
Gp = tf(K, conv([tau1 1], [tau2 1]));
%% Part a) IMC
tauc = max(tau1, tau2)/2;
Kc = (tau1 + tau2) / (K*tauc);
tauI = tau1 + tau2;
tauD = (tau1*tau2)/(tau1 + tau2);
Gc imc = Kc*(1+1/(tauI*s)+tauD*s);
%% Part b) ITAE (setpoint)
% FOPTD approximation
D = tau2/2;
```

 $^{^\}dagger$ For set-point changes, the design relation for the integral mode is $au/ au_I=A+B(\theta/ au)$.

```
tau = tau1 + tau2/2;
% Use tables
AP = 0.965;
BP = -0.85;
Kc b = AP*(D/tau)^BP/K;
AI = 0.796;
BI = -0.1465;
tauI b = tau/(AI + BI*(D/tau));
AD = 0.308;
BD = 0.929;
tauD b = AD*(D/tau)^BD*tau;
Gc b = Kc b*(1+1/(tauI b*s)+tauD b*s);
%% Part c) ITAE (disturbance)
AP = 1.357;
BP = -0.947;
Kc c = AP*(D/tau)^BP/K;
AI = 0.842;
BI = -0.738;
tauI c = tauI/(AI*(D/tau)^BI);
AD = 0.381;
BD = 0.995;
tauD c = AD*(D/tau)^BD*tau;
Gc c = Kc c*(1+1/(tauI c*s)+tauD c*s);
%% Function to give step response for lsqcurvefit
function Y = resp(params, tvec)
    K = params(1);
    tau = params(2);
    tau2 = params(3);
    Gp = tf(K, conv([tau 1], [tau2 1]));
    Y = step(Gp, tvec);
end
```

Question-4

Part a) Feedforward controller

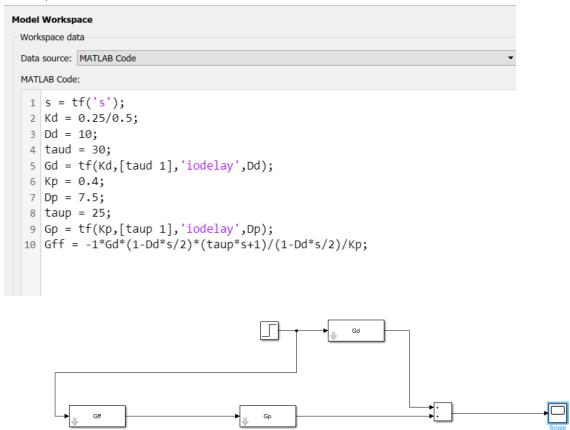


Figure 1: SIMULINK DIAGRAM of the system with just a feed-forward controller

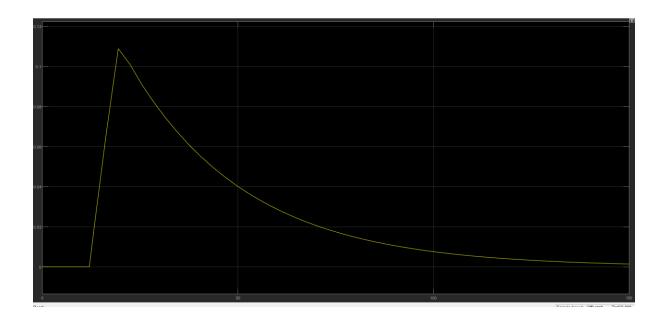


Figure 2: Disturbance rejection performance

Part b) Tuned PID Controller

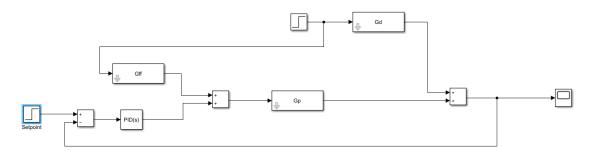


Figure 3: Feedforward in combination with a PID controller

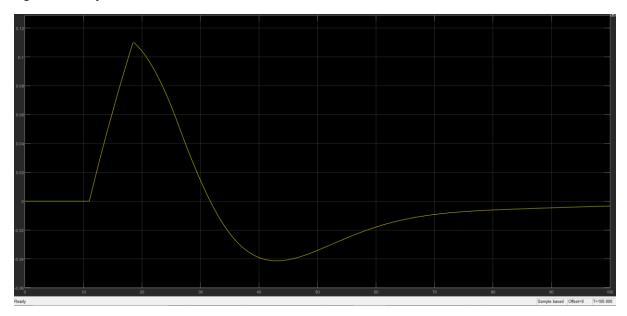


Figure 4: Response for combined efforts of feedforward and PID controller

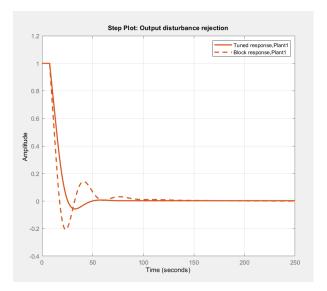


Figure 5: Tuning of the PID Controller (It linearizes the closed loop, and then we manually tune it on the basis of the responses/settling time requirements)

```
1 - model = 'mixing_vessel';
2 - load_system(model);
3 - out = sim(model);
4 - y = out.simout.data;
5 - t = out.tout;
6 - iae = trapz(t,abs(y));
```

Code for computing IAE

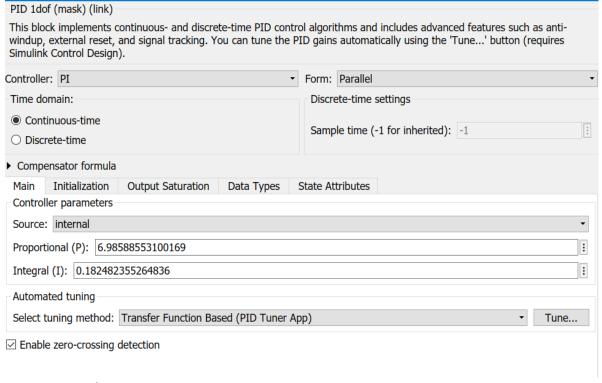


Figure 6: Tuned parameters

IAE with FF controller alone was obtained to be 3.5326

IAE with FF + PID controller was obtained to be 2.3346

As expected, we see an improvement when we use a PID controller in addition.

Part c) MPC

- Firstly, I will obtain the step response models of the process and disturbance using the corresponding transfer functions we have.
- Given the time delay and time constants, I will choose a sampling interval of about 2.5 minutes.
- In this way I can obtain step response model length as about 5*25/2.5 = 50.
- Given this n, and multiple delays involved I would want to have larger prediction horizon, p =
 25. Roughly half of what we have for n. (Note that obviously if we go for p > n, the system might exhibit instability)

- It is always safe to have the control horizon to be smaller than the predictive horizon. We can probably have **m** = **10-15**. And tune as per the response we get.
- Higher m is more aggressive but we need more computational power (because we need to optimize more variables).
- Input constraints can be decided based on the expected disturbance inputs that might occur. Let's say if 0.5 is the maximum expected disturbance (this causes a change of 0.25 in output) we can constrain the valve to have absolute value of input moves within 0.25/0.4 = 0.625 psig.