


# Unconstrained Still/Video-Based Face Verification with Deep Convolutional Neural Networks

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**Abstract** Over the last 5 years, methods based on Deep Convolutional Neural Networks (DCNNs) have shown impressive performance improvements for object detection and recognition problems. This has been made possible due to the availability of large annotated datasets, a better understanding of the non-linear mapping between input images and class labels as well as the affordability of GPUs. In this paper, we present the design details of a deep learning system for unconstrained face recognition, including modules for face detection, association, alignment and face verification. The quantitative performance evaluation is conducted using the IARPA Janus Benchmark A (IJB-A), the JANUS Challenge Set 2 (JANUS CS2), and the Labeled Faces in the Wild (LFW) dataset. The IJB-A dataset includes real-world unconstrained faces of 500 subjects with significant pose and illumination variations which are much harder than the LFW and Youtube Face datasets. JANUS CS2 is the extended version of IJB-A which contains not only all the images/frames of IJB-A but also includes the original videos. Some open issues regarding DCNNs for face verification problems are then discussed.

**Keywords** Deep learning · Face detection/association · Fiducial detection · Face verification · Metric learning

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## 1 Introduction

Face verification is a challenging problem in computer vision and has been actively researched for over two decades (Zhao et al. 2003). In face verification, given two videos or images, the objective is to determine whether they belong to the same person. Many algorithms have been shown to work well on images and videos that are collected in controlled settings. However, the performance of these algorithms often degrades significantly on images that have large variations in pose, illumination, expression, aging, and occlusion. In addition, for an automated face verification system to be effective, it also needs to handle errors that are introduced by algorithms for automatic face detection, face association, and facial landmark detection.

Existing methods have focused on learning robust and discriminative representations from face images and videos. One approach is to extract an over-complete and high-dimensional feature representation followed by a learned metric to project the feature vector onto a low-dimensional space and then compute the similarity scores. For example, high-dimensional multi-scale local binary pattern (LBP) (Chen et al. 2013) features extracted from local patches around facial landmarks and Fisher vector (FV) (Simonyan et al. 2013; Chen et al. 2015c) features have been shown to be effective for face recognition. Despite significant progress, the performance of these systems has not been adequate for deployment. However, given the availability of millions of annotated data, faster GPUs and a better understanding of the nonlinearities, DCNNs are providing much better performance on tasks such as object recognition (Krizhevsky et al. 2012; Szegedy et al. 2014), object/face detection (Girshick et al. 2014a; Ranjan et al. 2015), face verification/recognition (Schroff et al. 2015; Parkhi et al. 2015). It has been shown that DCNN models can not only characterize large data variations

but also learn a compact and discriminative representation when the size of training data is sufficiently large. In addition, it can be generalized to other vision tasks by fine-tuning the pre-trained model on the new task (Donahue et al. 2013).

In this paper, we present an automated face verification system. Due to the robustness of DCNNs, we build each component of our system based on separate DCNN models. Modules for detection and face alignment use the DCNN architecture proposed in Krizhevsky et al. (2012). For face verification, we train two DCNN models trained using the CASIA-WebFace (Yi et al. 2014) dataset. Finally, we compare the performance of our approach with many face matchers on the IJB-A dataset which are being carried out or have been recently reported ([http://biometrics.nist.gov/cs\\_links/face/face\\_challenges/IJBA\\_reports.zip](http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip)).<sup>1</sup> The proposed system is fully automatic. Although the IJB-A dataset contains significant variations in pose, illumination, expression, resolution and occlusion which are much harder than the Labeled Faces in the Wild (LFW) datasets, we present verification results for the LFW dataset too.

The system described in this paper, which integrates DCNN-based face detection (Ranjan et al. 2015) and fiducial point detection (Kumar et al. 2016) modules differs from its predecessor (Chen et al. 2015b) in the following ways: (1) uses more robust features from two networks which take faces as input with different resolutions (Sect. 3.4) are used and (2) employs a more efficient metric learning method (Sankaranarayanan et al. 2016b) which uses inner-products based constraints between triplets to optimize for the embedding matrix as opposed to norm-based constraints used in other methods (Sect. 3.5). In the experimental section, we also demonstrate the improvement due to media-sensitive pooling and the fusion of two networks.

The rest of the paper is organized as follows. We briefly review closely related works in Sect. 2. In Sect. 3, we present the design details of a deep learning system for unconstrained face verification and recognition, including face detection, face association, face alignment, and face verification. Experimental results using IJB-A, CS2, and LFW datasets are presented in Sect. 4. Some open issues regarding the use of DCNNs for face recognition/verification problems are discussed in Sect. 5. Finally, we conclude the paper in Sect. 6 with a brief summary and discussion.

## 2 Related Work

A typical face verification system consists of the following components: (1) face detection and (2) face association

across video frames, (3) facial landmark detection to align faces, and (4) face verification to verify a subject's identity. Due to the large number of published papers in the literature, we briefly review some relevant works for each component.

### 2.1 Face Detection

The face detection method introduced by Viola and Jones (2004) is based on cascaded classifiers built using Haar wavelet features. Since then, a variety of sophisticated cascade-based face detectors such as Joint Cascade (Chen et al. 2014), SURF Cascade (Li and Zhang 2013) and CascadeCNN (Li et al. 2015) have demonstrated improved performance. Zhu and Ramanan (2012) improved the performance of face detection algorithm using the deformable part model (DPM) approach, which treats each facial landmark as a part and uses HOG features to simultaneously perform face detection, pose estimation, and landmark localization. A recent face detector, Headhunter (Mathias et al. 2014), demonstrated competitive performance using a simple DPM. However, the key challenge in unconstrained face detection is that features like Haar wavelets and HOG do not capture the salient facial information at different poses and illumination conditions. To overcome these limitations, several deep CNN-based face detection methods have been proposed in the literature such as Faceness (Yang et al. 2015a), DDFD (Farfadi et al. 2015) and CascadeCNN (Li et al. 2015). It has been shown in Donahue et al. (2013) that a deep CNN pre-trained with the Imagenet dataset can be used as a meaningful feature extractor for various vision tasks. The method based on Regions with CNN (R-CNN) (Ross 2015) computes region-based deep features and attains state-of-art face detection performance. In addition, since the deep pyramid (Girshick et al. 2014b) removes the fixed-scale input dependency in deep CNNs, it is attractive to be integrated with the DPM approach to further improve the detection accuracy across scale (Ranjan et al. 2015).

### 2.2 Face Association

Video-based face verification systems (Chen et al. 2012b) requires consistently-tracked faces to capture diverse pose and spatial-temporal information for analysis. In addition, there is usually more than one person present in the videos, and thus multiple face images from different individuals should be correctly associated across the video frames. Several recent techniques have tracked multiple objects by modeling the motion context (Yoon et al. 2015), track management (Duffner and Odobez 2013), and guided tracking using the confidence map of the detector (Breitenstein et al. 2009). Multi-object tracking methods based on tracklet linking (Huang et al. 2008b; Roth et al. 2012; Bae and Yoon 2014)

<sup>1</sup> While this paper was under review, several recent works have also reported improved numbers on the IJB-A dataset (Ranjan et al. 2016b) and its successive version Janus Challenge Set 3 (CS3) (Bodla et al. 2017). We refer the interested readers to these works for more details.

usually rely on the Hungarian algorithm (Ahuja et al. 1993) to optimally assign the detected bounding boxes to existing tracklets. Roth et al. (2012) adapted the framework of multi-object tracking methods based on tracklet linking approach to track multiple faces; Several face-specific metrics and constraints have been introduced to enhance the reliability of face trackers. A recent study Comaschi et al. (2015) proposed to manage the tracks generated by a continuous face detector without relying on long-term observations. In unconstrained scenarios, the camera can undergo abrupt movements, which makes persistent tracking a challenging task. Du et al. proposed a conditional random field (CRF) framework for face association in two consecutive frames by utilizing the affinity of facial features, location, motion, and clothing appearance (Du and Chellappa 2012). Our face association method utilizes the KLT tracker to track a face initiated from the face detection. We continuously update the face tracking results for every fifth frame using the detected faces. The tracklet linking (Bae and Yoon 2014) is utilized to link the fragmented tracklet. We present a robust face association method based on existing works in Everingham et al. (2009), Bae and Yoon (2014) and Shi and Tomasi (1994). In addition, recently developed object trackers (Babenko et al. 2009; Henriques et al. 2015; Kalal et al. 2012) and face trackers (Wang and Ji 2008; Lui et al. 2010) can be integrated to potentially improve the robustness of face association method. More details are presented in Sect. 3.2.

### 2.3 Facial Landmark Detection

Facial landmark detection is an important component to align the faces into canonical coordinates and to improve the performance of verification algorithms. Pioneering works such as Active Appearance Models (AAM) (Cootes et al. 2001) and Active Shape Models (ASM) (Cootes et al. 1995) are built using the PCA constraints on appearance and shape. Cristinacce and Cootes (2006) generalized the ASM model to a Constrained Local Model (CLM), in which every landmark has a shape constrained descriptor to capture the appearance. Zhu and Ramanan (2012) used a part-based model for face detection, pose estimation and landmark localization assuming the face shape to be a tree structure. Asthana et al. (2013) combined the discriminative response map fitting with CLM. In addition, Cao et al. (2014) followed the cascaded pose regression (CPR) proposed by Dollár et al. (2010): feature extraction followed by a regression stage. However, unlike CPR which uses pixel difference as features, it trains a random forest based on local binary patterns. In general, these methods learn a model that directly maps the image appearance to the target output. Nevertheless, the performance of these methods depends on the robustness of local descriptors. In Krizhevsky et al. (2012), the deep

features are shown to be robust to different challenging variations. Sun et al. (2013) proposed a cascade of carefully designed CNNs, in which at each level, outputs of multiple networks are fused for landmark estimation and achieve good performance. Unlike (Sun et al. 2013), we use a single CNN, carefully designed to provide a unique key-point descriptor and achieve better performance. Besides using a 2D transformation for face alignment, Hassner et al. (2015) proposed an effective method to frontalize faces with the help of generic 3D face model. However, the effectiveness of the method also highly relies on the quality of the detected facial landmarks (i.e., the method usually introduces undesirable artifacts when the quality of facial landmarks is poor).

### 2.4 Feature Representation for Face Recognition

Learning invariant and discriminative feature representations is a critical step in designing a face verification system. Ahonen et al. (2006) showed that the Local Binary Pattern (LBP) is effective for face recognition. Chen et al. (2013) demonstrated good results for face verification using high-dimensional multi-scale LBP features extracted from patches extracted around facial landmarks. However, recent advances in deep learning methods have shown that compact and discriminative representations can be learned using a DCNN trained with very large datasets. Taigman et al. (2014) built a DCNN model on the frontalized faces generated with a general 3D shape model from a large-scale face dataset and achieved better performance than many traditional methods. Sun et al. (2014) achieved results that surpass human performance for face verification on the LFW dataset using an ensemble of 25 simple DCNN with fewer layers trained on weakly aligned face images from a much smaller dataset than (Taigman et al. 2014). Schroff et al. (2015) adapted a state-of-the-art object recognition network to face recognition and trained it using a large-scale unaligned private face dataset with triplet loss. Parkhi et al. (2015) trained a very deep convolutional network based on VGGNet for face verification and demonstrated impressive results. These studies essentially demonstrate the effectiveness of the DCNN model for feature learning and detection/recognition/verification problems.

### 2.5 Metric Learning

Learning a similarity measure from data is the other key component for improving the performance of a face verification system. Many approaches have been proposed in the literature that essentially exploit label information from face images or face pairs. For instance, Weinberger and Saul (2009) used the Large Margin Nearest Neighbor

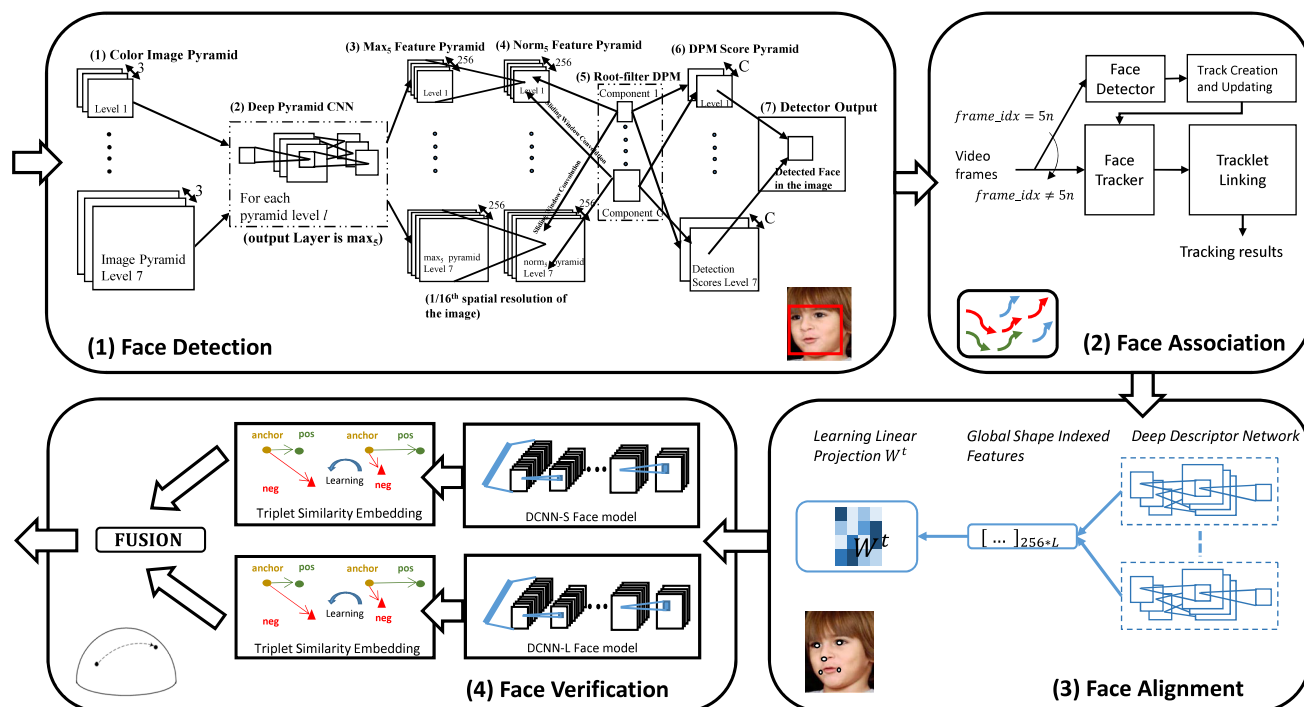
(LMNN) metric which enforces the large margin constraint among all triplets of labeled training data. [Guillaumin et al. \(2009\)](#) proposed two robust distance measures: Logistic Discriminant-based Metric Learning (LDML) and Marginalized kNN (MkNN). The LDML method learns a distance by performing a logistic discriminant analysis on a set of labeled image pairs and the MkNN method marginalizes a k-nearest-neighbor classifier to both images of the given test pair using a set of labeled training images. [Mignon and Jurie \(2012\)](#) proposed an algorithm for learning distance metrics from sparse pairwise similarity/dissimilarity constraints in high dimensional input space. The method exhibits good generalization properties when projecting the features from a high-dimensional space to a low-dimensional one. [Nguyen and Bai \(2010\)](#) used an efficient and simple metric learning method based on the cosine similarity measure instead of the widely adopted Euclidean distance. [Taigman et al. \(2009\)](#) employed the Mahalanobis distance using the Information Theoretic Metric Learning (ITML) method ([Davis et al. 2007](#)). [Chen et al. \(2012a\)](#) used a joint Bayesian approach for face verification which models the joint distribution of a pair of face images and uses the ratio of between-class and within-class probabilities as the similarity measure. [Hu et al. \(2014\)](#) learned a discriminative metric within the deep neural network framework. [Schroff et al. \(2015\)](#) and [Parkhi et al. \(2015\)](#) optimized the DCNN parameters based on the triplet loss which directly embeds the DCNN features into a discriminative subspace and presented promising results for face verification.

### 3 Proposed System

The proposed system is a complete pipeline for performing *automatic* face verification. We first perform face detection to localize faces in each image and video frame. Then, we associate the detected faces with the common identity across video frames and align the faces into canonical coordinates using the detected landmarks. Finally, we perform face verification to compute the similarity between a pair of images/videos. The system is illustrated in Fig. 1. The details of each component are presented in the following sections.

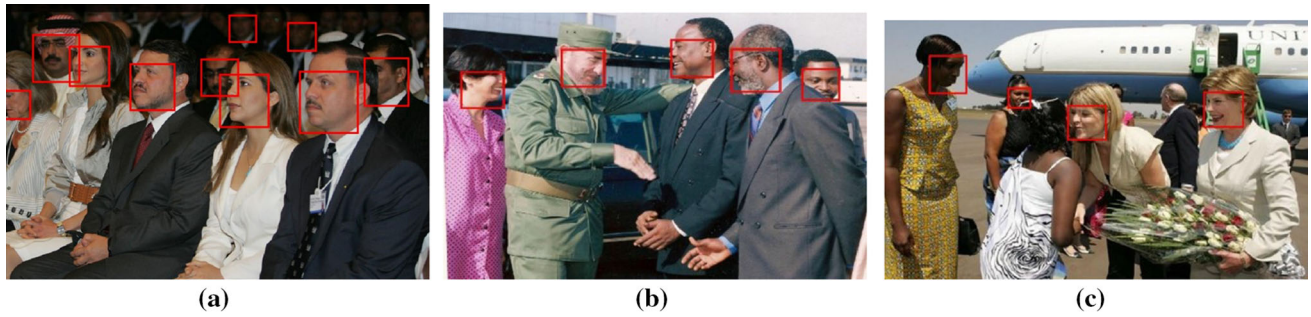
#### 3.1 Face Detection

All the faces in the images/video frames are detected using a DCNN-based face detector, called the Deep Pyramid Deformable Parts Model for Face Detection (DP2MFD) ([Ranjan et al. 2015](#)), which consists of two modules. The first module generates a seven level normalized deep feature pyramid for any input image of arbitrary size, as illustrated in the first part of Fig. 1. The architecture of Alexnet ([Krizhevsky et al. 2012](#)) is adopted for extracting the deep features. This image pyramid network generates a pyramid of 256 feature maps at the fifth convolution layer (conv<sub>5</sub>). A  $3 \times 3$  max filter is applied to the feature pyramid at a stride of one to obtain the max<sub>5</sub> layer. Typically, the activation magnitude for a face region decreases with the size of the pyramid level. As a result, a large face detected by a fixed-size sliding window at a lower pyramid level will have a high detection score



**Fig. 1** An overview of the proposed DCNN-based face verification system





**Fig. 2** Sample detection results on an IJB-A image using the deep pyramid method

compared to a small face getting detected at a higher pyramid level. In order to reduce this bias to face size, we apply a z-score normalization step on the  $\max_5$  features at each level. For a 256-dimensional feature vector  $x_{i,j,k}$  at the pyramid level  $i$  and location  $(j, k)$ , the normalized feature  $x_{i,j,k}$  is computed as:

$$x_{i,j,k} = \frac{x_{i,j,k} - \mu_i}{\sigma_i}, \quad (1)$$

where  $\mu_i$  is the mean feature vector, and  $\sigma_i$  is the standard deviation for the pyramid level  $i$ . We refer to the normalized  $\max_5$  features as  $norm_5$ . Then, the fixed-length features from each location in the pyramid are extracted using the sliding window approach.

The second module is a linear SVM, which takes these features as inputs to classify each location as face or non-face, based on their scores. A root-only DPM is trained on the  $norm_5$  feature pyramid using a linear SVM. In addition, the deep pyramid features are robust to not only pose and illumination variations but also to different scales. The DP2MFD algorithm works well in unconstrained settings as shown in Fig. 2. We also present the face detection performance results under the face detection protocol of the IJB-A dataset in Sect. 4.

### 3.2 Face Association

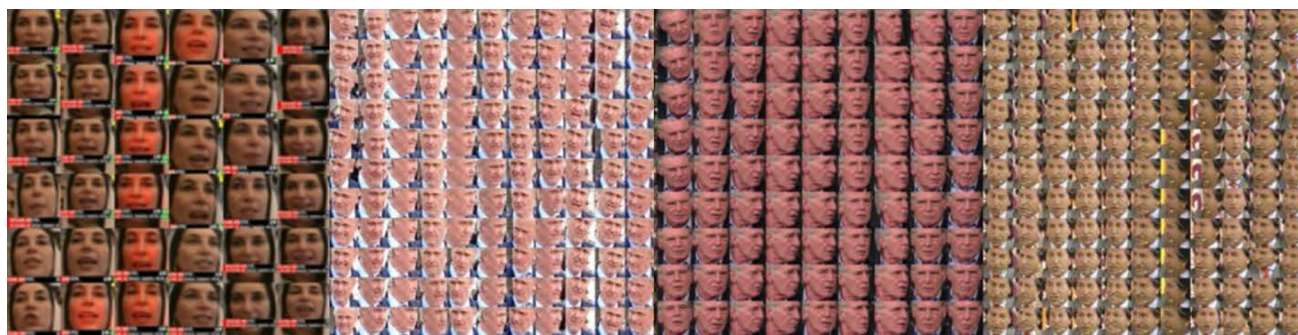
Because there are multiple subjects appearing in the frames of each video of the IJB-A dataset, performing face association to assign each face to its corresponding subject is an important step to pick the correct subject for face verification. Thus, once the faces in the images and video frames are detected, we track multiple faces by integrating results from the face detector, face tracker, and a tracklet linking step. The second part of Fig. 1 shows the block diagram of the multiple face tracking system. We apply the face detection algorithm in every fifth frame using the face detection method presented in Sect. 3.1. The detected bounding box is considered as a novel detection if it does not have an

overlap ratio with any bounding box in the previous frames larger than  $\gamma$ . The overlap ratio of a detected bounding box  $\mathbf{b}_d$  and a bounding box  $\mathbf{b}_{tr}$  in the previous frames is defined as

$$s(\mathbf{b}_d, \mathbf{b}_{tr}) = \frac{\text{area}(\mathbf{b}_d \cap \mathbf{b}_{tr})}{\text{area}(\mathbf{b}_{tr})}. \quad (2)$$

We empirically set the overlap threshold  $\gamma$  to 0.2. A face tracker is created from a detection bounding box that is treated as a novel detection. We set the face detection confidence threshold to  $-1.0$  to select bounding boxes of face detection of high confidence. For face tracking, we use the Kanade–Lucas–Tomasi (KLT) feature tracker (Shi and Tomasi 1994) to track the faces between two consecutive frames. To avoid the potential drift of trackers, we update the bounding boxes of the tracker by those provided by the face detector in every fifth frame. The detection bounding box  $\mathbf{b}_d$  replaces the tracking bounding boxes  $\mathbf{b}_{tr}$  of a tracklet in the previous frame if  $s(\mathbf{b}_d, \mathbf{b}_{tr}) \leq \gamma$ . A face tracker is terminated if there is no corresponding face detection overlapping with it for more than  $t$  frames. We set  $t$  to 4 based on empirical grounds.

In order to handle the fragmented face tracks resulting from occlusions or unreliable face detection, we use the tracklet linking method proposed by Bae and Yoon (2014) to associate the bounding boxes in the current frames with tracklets in the previous frames. The tracklet linking method consists of two stages. The first stage is to associate the bounding boxes provided by the tracker or the detector in the current frame with the existing tracklet in previous frames. This stage consists of local and global associations. The local association step associates the bounding boxes with the set of tracklets, having high confidence. The global step associates the remaining bounding boxes with the set of tracklets of low confidence. The second stage is to update the confidence of the tracklets, which will be used for determining the tracklets for local or global association in the first stage. We show sample face association results for some videos from the CS2 dataset in Fig. 3.



**Fig. 3** Sample results of our face association method for videos of JANUS CS2 which is the extension dataset of IJB-A

### 3.3 Facial Landmark Detection

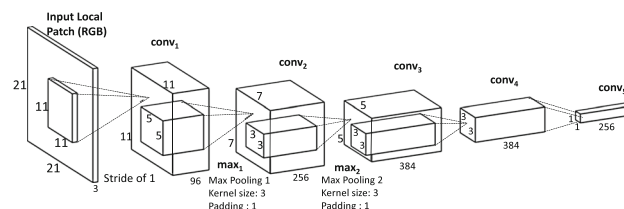
Once the faces are detected or associated, we perform facial landmark detection for face alignment. The DCNN-based facial landmark detection algorithm module, local deep descriptor regression (LDDR) (Kumar et al. 2016), works in two stages. We model the task as a regression problem, where beginning with the initial mean shape, the target shape is reached through regression. The first step is to perform feature extraction of a patch around a point of the shape followed by linear regression as described in Ren et al. (2014) and Cao et al. (2014). Given a face image  $I$  and the initial shape  $S^0$ , the regressor computes the shape increment  $\Delta S$  from the deep descriptors and updates the face shape using (3).

$$S^t = S^{t-1} + W^t \Phi^t(I, S^{t-1}) \quad (3)$$

The CNN features (represented as  $\Phi$  in 3) carefully designed with the proper number of strides and pooling (refer to Table 1 for more details), are used as features to perform regression. We use the same CNN architecture as Alexnet (Krizhevsky et al. 2012) with the pretrained weights for the ImageNet dataset as shown in Fig. 4. Then, we further fine-tuned it with AFLW (Koestinger et al. 2011) dataset for face detection task. The fine-tuning step helps the network to learn features specific to faces. Furthermore, we adopt the cascade regression, in which the output generated by the first stage is used as an input for the next stage. The number of stages is fixed at 5 in our system. The patches selected for feature extraction are reduced subsequently in later stages to

**Table 1** Input size and the number of strides in conv1, max1, conv2 and max2 layers for 4 stages of regression (Kumar et al. 2016)

Stage	Input size (pixels)	conv1	max1	conv2	max2
Stage 1	$92 \times 92$	4	2	1	1
Stage 2	$68 \times 68$	3	2	1	1
Stage 3	$42 \times 42$	2	1	1	2
Stage 4	$21 \times 21$	1	1	1	1



**Fig. 4** The DCNN architecture used to extract the local descriptors for the facial landmark detection task (Kumar et al. 2016)

improve the localization of facial landmarks. After the facial landmark detection is completed, each face is aligned into the canonical coordinate using the similarity transform and seven landmark points (i.e., two left eye corners, two right eye corners, nose tip, and two mouth corners).

### 3.4 Deep Convolutional Face Representation

In this work, we train two deep convolutional networks. One is trained using tight face bounding boxes (DCNN<sub>S</sub>), and the other using large bounding boxes which include more contextual (DCNN<sub>L</sub>) information. In Sect. 4, we present results which show that both networks capture discriminative information and complement each other. In addition, the fusion of two networks does significantly improve the final performance. The architectures of both networks are summarized in Tables 2 and 3.

Stacking small filters to approximate large filters and building very deep convolutional networks reduces the number of parameters but also increases the nonlinearity of the network as discussed in Simonyan and Zisserman (2014) and Szegedy et al. (2014). In addition, the resulting feature representation is compact and discriminative. Therefore, for (DCNN<sub>S</sub>), we use the same network architecture presented in Chen et al. (2015a) and train it using the CASIA-WebFace dataset (Yi et al. 2014). The dimensionality of the input layer is  $100 \times 100 \times 3$  for RGB images. The network includes ten convolutional layers, five pooling layers, and one fully connected layer. Each convolutional layer is followed by a parametric rectified linear unit (PReLU) (He et al. 2015),

**Table 2** The architectures of DCNN<sub>S</sub>

Name	Type	Filter size/stride	#Params
conv11	Convolution	$3 \times 3/1$	0.84 K
conv12	Convolution	$3 \times 3/1$	18 K
pool1	Max pooling	$2 \times 2/2$	
conv21	Convolution	$3 \times 3/1$	36 K
conv22	Convolution	$3 \times 3/1$	72 K
pool2	Max pooling	$2 \times 2/2$	
conv31	Convolution	$3 \times 3/1$	108 K
conv32	Convolution	$3 \times 3/1$	162 K
pool3	Max pooling	$2 \times 2/2$	
conv41	Convolution	$3 \times 3/1$	216 K
conv42	Convolution	$3 \times 3/1$	288 K
pool4	Max pooling	$2 \times 2/2$	
conv51	Convolution	$3 \times 3/1$	360 K
conv52	Convolution	$3 \times 3/1$	450 K
pool5	Avg pooling	$7 \times 7/1$	
Dropout	Dropout (40%)		
fc6	Fully connected	10,548	3296 K
Loss	Softmax	10,548	
Total			5 M

**Table 3** The architecture of DCNN<sub>L</sub>

Name	Type	Filter size/stride	#Params
conv1	Convolution	$11 \times 11/4$	35 K
pool1	Max pooling	$3 \times 3/2$	
conv2	Convolution	$5 \times 5/2$	614 K
pool2	Max pooling	$3 \times 3/2$	
conv3	Convolution	$3 \times 3/2$	885 K
conv4	Convolution	$3 \times 3/2$	1.3 M
conv5	Convolution	$3 \times 3/1$	885 K
conv6	Convolution	$3 \times 3/1$	590 K
pool6	Max pooling	$3 \times 3/2$	
fc6	Fully connected	1024	9.4 M
Dropout	Dropout (50%)		
fc7	Fully connected	512	524 K
Dropout	Dropout (50%)		
fc8	Fully connected	10,548	5.5 M
Loss	Softmax	10,548	
Total			19.8 M

except the last one, conv52. Moreover, two local normalization layers are added after conv12 and conv22, respectively, to mitigate the effect of illumination variations. The kernel size of all filters is  $3 \times 3$ . The first four pooling layers use the max operator, and pool<sub>5</sub> uses average pooling. The feature dimensionality of pool<sub>5</sub> is thus equal to the number of channels of conv52 which is 320. The dropout ratio is set as 0.4

to regularize Fc6 due to the large number of parameters (i.e.,  $320 \times 10,548$ <sup>2</sup>). The pool<sub>5</sub> feature is used for face representation. The extracted features are further  $L_2$ -normalized to unit length before the metric learning stage. If there are multiple images and frames available for the subject template, we use the average of pool<sub>5</sub> features as the overall feature representation.

On the other hand, for DCNN<sub>L</sub>, the deep network architecture closely follows the architecture of the AlexNet (Krizhevsky et al. 2012) with some notable differences: reduced number of parameters in the fully connected layers; use of Parametric Rectifier Linear units (PReLU's) instead of ReLU, since they allow a negative value for the output based on a learnt threshold and have been shown to improve the convergence rate (He et al. 2015).

The reason for using the AlexNet architecture in the convolutional layers is due to the fact that we initialize the convolutional layer weights with weights from the AlexNet model which was trained using the ImageNet challenge dataset. Several recent works (Yosinski et al. 2014; Long and Wang 2015) have empirically shown that this transfer of knowledge across different networks, albeit for a different objective, improves performance and more significantly reduces the need to train using a large number of iterations. To learn more domain specific information, we add an additional convolutional layer, conv6 and initialize the fully connected layers fc6-fc8 from scratch. Since the network is used as a feature extractor, the last layer fc8 is removed during deployment, thus reducing the number of parameters to 15 M. When the network is deployed, the features are extracted from fc7 layers resulting in a dimensionality of 512. The network is trained using the CASIA-WebFace dataset (Yi et al. 2014). The dimensionality of the input layer is  $227 \times 227 \times 3$  for RGB images.

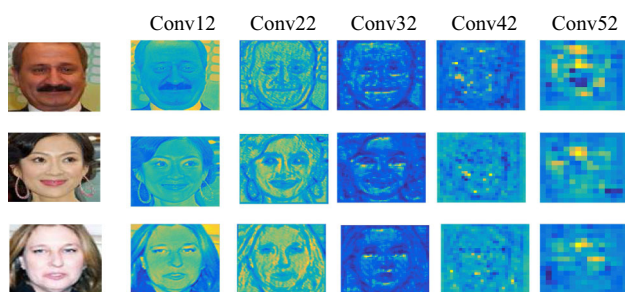
In Fig. 5, we show some feature activation maps of the DCNN<sub>S</sub> model. At upper layers, the feature maps capture more global shape features which are also more robust to illumination changes than Conv12 where the green pixels represent high activation values, and the blue pixels represent low activation values compared to the green.

### 3.5 Triplet Similarity Embedding

To further improve the performance of our deep features, we obtain a low-dimensional discriminative projection of the deep features, called the Triplet Similarity Embedding (TSE) that is learnt using the training data provided for each split of IJB-A. The output of the procedure is an embedding matrix  $\mathbf{W} \in \mathbf{R}^{n \times M}$  where  $M$  is the dimensionality of the deep descriptor (320 for DCNN<sub>S</sub> and 512 for DCNN<sub>L</sub>) and

<sup>2</sup> The list of overlapping subjects is available at [http://www.umi.acs.umd.edu/~pullpull/janus\\_overlap.xlsx](http://www.umi.acs.umd.edu/~pullpull/janus_overlap.xlsx).





**Fig. 5** An illustration of some feature maps of conv12, conv22, conv32, conv42, and conv52 layers of DCNN<sub>S</sub> trained for the face identification task. At *upper layers*, the feature maps capture more global shape features which are also more robust to illumination changes than conv12. The feature maps are rescaled to the same size for visualization purpose. The *green pixels* represent high activation values, and the *blue pixels* represent low activation values as compared to the *green* (Color figure online)

we set  $n = 128$ , thus achieving dimensionality reduction in addition to an improvement in performance.

In addition, for the TSE approach, the objective was twofold (1) to achieve as small dimensionality as possible for both networks (2) to obtain a more discriminative representation in the low dimensional space which means to push similar pairs together and dissimilar pairs apart in the low-dimensional space. For learning  $\mathbf{W}$ , we solve an optimization problem based on constraints involving triplets—each containing two similar samples and one dissimilar sample. Consider a triplet  $\{a, p, n\}$ , where  $a$  (anchor) and  $p$  (positive) are from the same class, but  $n$  (negative) belongs to a different class. Our objective is to learn a linear projection  $\mathbf{W}$  from the data such that the following constraint is satisfied:

$$(\mathbf{W}a)^T \cdot (\mathbf{W}p) > (\mathbf{W}a)^T \cdot (\mathbf{W}n) \quad (4)$$

In our case,  $\{a, p, n\} \in \mathbf{R}^M$  are deep descriptors which are normalized to unit length. As such,  $(\mathbf{W}a)^T \cdot (\mathbf{W}p)$  is the dot-product or the similarity between  $a, p$  under the projection  $\mathbf{W}$ . The constraint in (4) requires that the similarity between the anchor and positive samples should be higher than the similarity between the anchor and negative samples in the low dimensional space represented by  $\mathbf{W}$ . Thus, the mapping matrix  $\mathbf{W}$  pushes similar pairs closer and dissimilar pairs apart, with respect to the anchor point. By choosing the dimensionality of  $\mathbf{W}$  as  $n \times M$  where  $n < M$ , we achieve dimensionality reduction in addition to better performance. For our work, we fix  $n = 128$  based on cross validation.

Given a set of labeled data points, we solve the following optimization problem:

$$\underset{\mathbf{W}}{\operatorname{argmin}} \sum_{a, p, n \in \mathbb{T}} \max(0, \alpha + a^T \mathbf{W}^T \mathbf{W} n - a^T \mathbf{W}^T \mathbf{W} p) \quad (5)$$

where  $\mathbb{T}$  is the set of triplets and  $\alpha$  is a margin parameter chosen based on the validation set. In practice, the above problem

is solved in a Large-Margin framework using Stochastic Gradient Descent (SGD) and the triplets are sampled online. The update step for solving (5) with SGD is:

$$\mathbf{W}_{t+1} = \mathbf{W}_t - \eta * \mathbf{W}_t * (a(n - p)^T + (n - p)a^T) \quad (6)$$

where  $\mathbf{W}_t$  is the estimate at iteration  $t$ ,  $\mathbf{W}_{t+1}$  is the updated estimate,  $\{a, p, n\}$  is the triplet sampled at the current iteration and  $\eta$  is the learning rate which is set to 0.01 for the current work.

The entire procedure takes 3–5 min per split using a standard C++ implementation. More details regarding the optimization algorithm can be found in Sankaranarayanan et al. (2016b). At each iteration, we sample 1000 instances from the whole training set to choose the negatives. Since the training set is relatively small for the datasets considered in this experiment, the entire training set is held in memory. Going forward this could be made efficient by using a buffer which will be replenished periodically, thus requiring a constant memory requirement. The computational complexity of each iteration is  $O(M^2)$ , that is, the complexity varies quadratically with the dimension of the deep descriptor. The technique closest to the one presented in this section, which is used in recent works (Parkhi et al. 2015; Schroff et al. 2015) computes the embedding  $\mathbf{W}$  based on satisfying the distance constraints given below:

$$\underset{\mathbf{W}}{\operatorname{argmin}} \sum_{a, p, n \in \mathbb{T}} \max\{0, \alpha + (a - p)^T \mathbf{W}^T \mathbf{W} (a - p) - \quad (7)$$

$$(a - n)^T \mathbf{W}^T \mathbf{W} (a - n)\} \quad (8)$$

To be consistent with the terminology used in this paper, we call it Triplet Distance Embedding (**TDE**). It should be noted that the **TSE** formulation is different from **TDE**, in that, the current work uses inner-product based constraints between triplets to optimize for the embedding matrix as opposed to norm-based constraints used in the **TDE** method. To choose the dimensionality, we test the values 64, 128, 256 using a fivefold validation scheme for each split. The learning rate is chosen as 0.02 and is fixed throughout the procedure. The margin parameter is chosen as 0.1. We find from our experiments that the lower margin works better but since we perform hard negative mining at each step, the method is not particularly sensitive to the margin parameter.

In general, to learn a reasonable distance measure directly using pairwise or triplet metric learning approach requires huge amount of data [i.e., the state-of-the-art approach (Schroff et al. 2015) uses 200M images]. In addition, the proposed approach decouples the DCNN feature learning and metric learning steps due to memory constraints. To learn a reasonable distance measure requires generating the informative pairs or triplets. The batch size used for SGD is limited by the memory size of the graphics card. If the model is trained



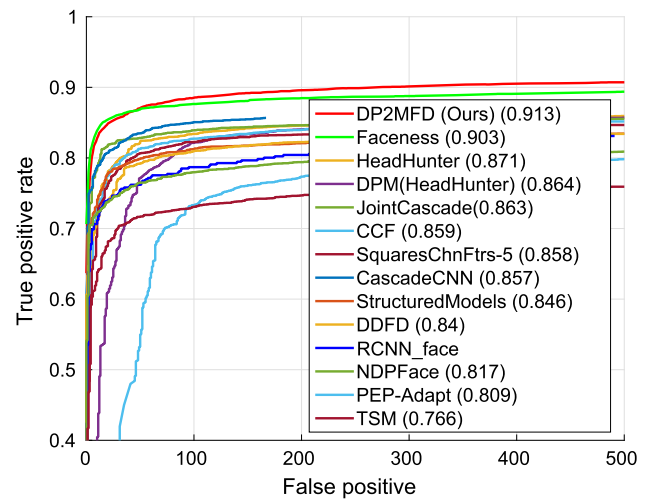
end-to-end, then only a small batch size is available for use. Thus, in this work, we perform DCNN model training and metric learning independently. In addition, for the publicly available deep model (Parkhi et al. 2015), it is also trained first with softmax loss and followed by finetuning the model with verification loss while freezing the convolutional and fully connected layers except the last one so that the transformation which is equivalent to the proposed approach can be learned.

## 4 Experimental Results

In this section, we present the results of the proposed automatic system for both face detection and face verification tasks on the challenging IARPA Janus Benchmark A (IJB-A) (Klare et al. 2015), its extended version Janus Challenging set 2 (JANUS CS2) dataset, and the LFW dataset. The JANUS CS2 dataset contains not only the sampled frames and images in the IJB-A, but also the original videos. In addition, the JANUS CS2 dataset<sup>3</sup> includes considerably more test data for identification and verification problems in the defined protocols than the IJB-A dataset. The receiver operating characteristic curves (ROC) and the cumulative match characteristic (CMC) scores are used to evaluate the performance of different algorithms for face verification. The ROC curve measures the performance in verification scenarios, where the vertical axis is true acceptance rate (TAR) which represents the degree to correctly match the face image (i.e., deep features) from the same person and the horizontal axis shows false acceptance rate (FAR) which represents the degree to falsely match the biometric information from one person to another. The CMC score measures the accuracy in closed set identification scenarios.

### 4.1 Face Detection on IJB-A

The IJB-A dataset contains images and sampled video frames from 500 subjects collected from online media (Klare et al. 2015; Cheney et al. 2015). For face detection task, there are 67,183 faces of which 13,741 are from images and the remaining are from videos. The locations of all faces in the IJB-A dataset have been manually annotated. The subjects were captured so that the dataset contains wide geographic distribution. Nine different face detection algorithms were evaluated on the IJB-A dataset (Cheney et al. 2015), and the algorithms compared in (Cheney et al. 2015) include one commercial off the shelf (COTS) algorithm, three government off the shelf (GOTS) algorithms, two open source face detection algorithms (OpenCV's Viola Jones and the detector provided in the Dlib library), and GOTS ver 4 and



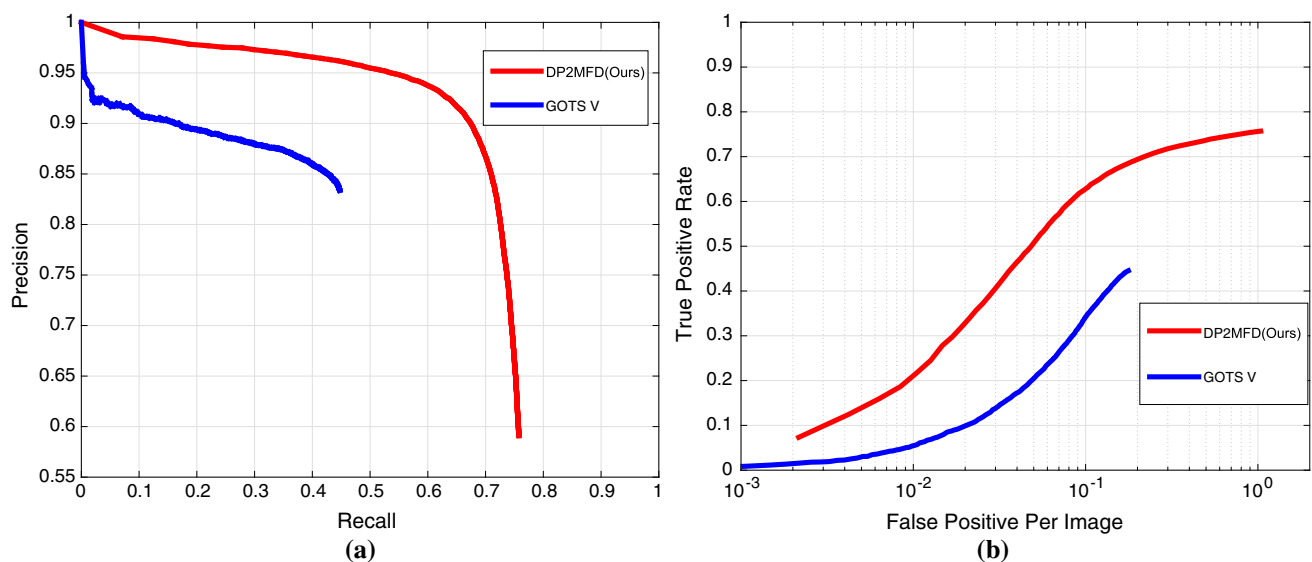
**Fig. 6** Face detection performance evaluation on the FDDB dataset (Ranjan et al. 2015)

5. In Fig. 7, we show the precision–recall (PR) curves and the ROC curves, respectively corresponding to the method used in our work and one of the best reported methods in Cheney et al. (2015). We see that the face detection algorithm used in our system outperforms the best performing method reported in Cheney et al. (2015) by a large margin. In Fig. 8b, we illustrate typical faces in the IJB-A dataset that are not detected by DP2MFD, and we can find the faces to be usually in very extreme conditions which contain limited information for face verification. However, in Fig. 8a, we also show that the DP2MFD algorithm can handle very difficult faces but relatively reasonable as compared to those in Fig. 8b. As shown in Fig. 6, the DP2MFD algorithm also achieves top performance in the challenging FDDB benchmark (Jain and Learned-Miller 2010) for face detection with a large performance margin compared to most algorithms. Some of the recent published methods compared in the FDDB evaluation include Faceness (Yang et al. 2015a), HeadHunter (Mathias et al. 2014), JointCascade (Chen et al. 2014), CCF (Yang et al. 2015b), Squares-ChnFtrs-5 (Mathias et al. 2014), CascadeCNN (Li et al. 2015), Structured Models (Yan et al. 2014), DDFD (Farfadi et al. 2015), NDPFace (Liao et al. 2016), PEP-Adapt (Li et al. 2013) and TSM (Zhu and Ramanan 2012). More comparison results with other face detection data sets are available in Ranjan et al. (2015). Since the CS2 dataset has not been released to public, we are not able to provide comparisons with other existing face detectors.

### 4.2 Facial Landmark Detection on IJB-A

We also evaluate the performance of our facial landmark detection method on the IJB-A dataset. For the training data, we take 3148 images in total from the LFPW (Belhumeur

<sup>3</sup> The JANUS CS2 dataset is not publicly available yet.

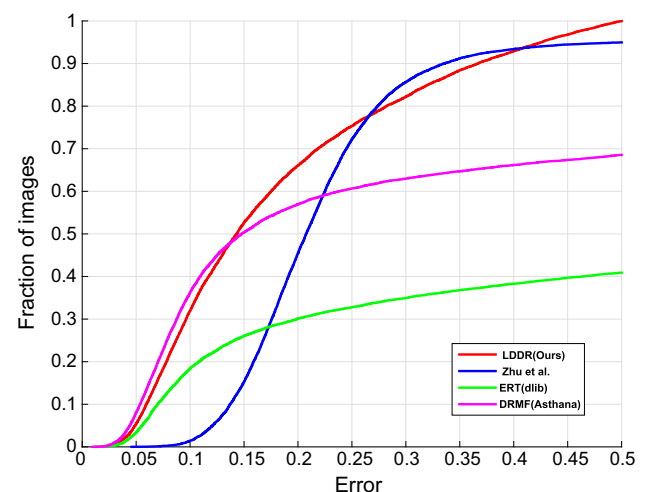


**Fig. 7** Face detection performance evaluation on the IJB-A dataset: **a** precision versus recall curves. **b** ROC curves (Ranjan et al. 2015)



**Fig. 8** **a** Difficult faces in the IJB-A dataset that are successfully detected by DP2MFD, and **b** faces that are not detected by DP2MFD. From the results, we can see that DP2MFD can handle difficult occlusion, partial face, large illumination and pose variations

et al. 2013), Helen (Le et al. 2012) and AFW (Zhu and Ramanan 2012) datasets and test on the IJB-A dataset. The subjects were captured so that the dataset contains wide geographic distribution. The challenge comes through the wide diversity in pose, illumination and resolution. Our method produces 68 facial landmark points following MultiPIE (Gross et al. 2010) markup format. We evaluate the performance using the normalized mean square error and average pt-pt error (normalized by face size) versus fraction



**Fig. 9** Average 3-pt error (normalized by eye-nose distance) versus fraction of images in the IJB-A dataset (Kumar et al. 2016)

of images plots of different methods. Since IJB-A is annotated only with 3 key-points on the faces (two eyes and nose base) by human annotators, the interocular distance error was normalized by the distance between nose tip and the midpoint of the eye centers. In Fig. 9, we present a comparison of our algorithm with Zhu and Ramanan (2012), Asthana et al. (2013) and Kazemi and Sullivan (2014). For the Helen dataset, we show the performance of 49-point and full 68-point results in Table 4. Our deep descriptor-based global shape regression method outperforms the above mentioned state-of-the-art methods in both high-quality (Helen) and low-quality (IJB-A) images. Samples of detected landmarks results are shown in Fig. 10. More evaluation results for landmark detection on other standard datasets may be found in Kumar et al. (2016). Once facial landmark detection

**Table 4** Averaged error comparison of different methods on the Helen dataset (Kumar et al. 2016)

Method	68-pts	49-pts
Zhu and Ramanan (2012)	8.16	7.43
DRMF (Asthana et al. 2013)	6.70	–
RCPR (Burgos-Artizzu et al. 2013)	5.93	4.64
SDM (Xiong and la Torre 2013)	5.50	4.25
GN-DPM (Tzimiropoulos and Pantic 2014)	5.69	4.06
CFAN (Zhang et al. 2014)	5.53	–
CFSS (Zhu et al. 2015)	<b>4.63</b>	3.47
LDDR (ours)	4.76	<b>2.36</b>

Bold values indicate the best performances achieved by different methods at each operating point

**Fig. 10** Sample facial landmark detection results

is completed, we choose seven landmark points (i.e., two left eye corners, two right eye corners, nose tip, and two mouth corners) out of the detected 68 points and apply the similarity transform to warp the faces into canonical coordinates.

### 4.3 IJB-A and JANUS CS2 for Face Verification

For face verification task, both IJB-A and JANUS CS2 datasets contain 500 subjects with 5397 images and 2042 videos split into 20,412 frames, 11.4 images and 4.2 videos per subject. Sample images and video frames from the datasets are shown in Fig. 11 (i.e., the videos are only released for the JANUS CS2 dataset). The IJB-A evaluation protocol consists of verification (1:1 matching) over 10 splits. Each split contains around 11,748 pairs of templates (1756 positive and 9992 negative pairs) on average. Similarly, the identification (1:N search) protocol also consists of 10 splits, which are used to evaluate the search performance. In each search split, there are about 112 gallery templates and 1763 probe templates (i.e., 1187 genuine probe templates and 576 impostor probe templates). On the other hand, for the JANUS CS2, there are about 167 gallery templates and 1763 probe templates and all of them are used for both identification and

verification. The training set for both datasets contains 333 subjects, and the test set contains 167 subjects without any overlapping subjects. Ten random splits of training and testing are provided by each benchmark, respectively. The main differences between IJB-A and JANUS CS2 evaluation protocols are that (1) IJB-A considers the open-set identification problem and the JANUS CS2 considers the closed-set identification and (2) IJB-A considers the more difficult pairs which are subsets of JANUS CS2 dataset.

Unlike the LFW and YTF datasets, which only use a sparse set of negative pairs to evaluate the verification performance, the IJB-A and JANUS CS2 datasets divide the images/video frames into gallery and probe sets so that all the available positive and negative pairs are used for the evaluation. Also, each gallery and probe set consist of multiple templates. Each template contains a combination of images or frames sampled from multiple image sets or videos of a subject. For example, the size of the similarity matrix for JANUS CS2 split1 is  $167 \times 1806$  where 167 are for the gallery set and 1806 for the probe set (i.e., the same subject reappears multiple times in different probe templates). Moreover, some templates contain only one profile face with a challenging pose with low quality imagery. In contrast to LFW and YTF datasets, which only include faces detected by the Viola Jones face detector (Viola and Jones 2004), the images in the IJB-A and JANUS CS2 contain extreme pose, illumination, and expression variations. These factors essentially make the IJB-A and JANUS CS2 challenging face recognition datasets (Klare et al. 2015).

### 4.4 Performance Evaluations of Face Verification on IJB-A and JANUS CS2

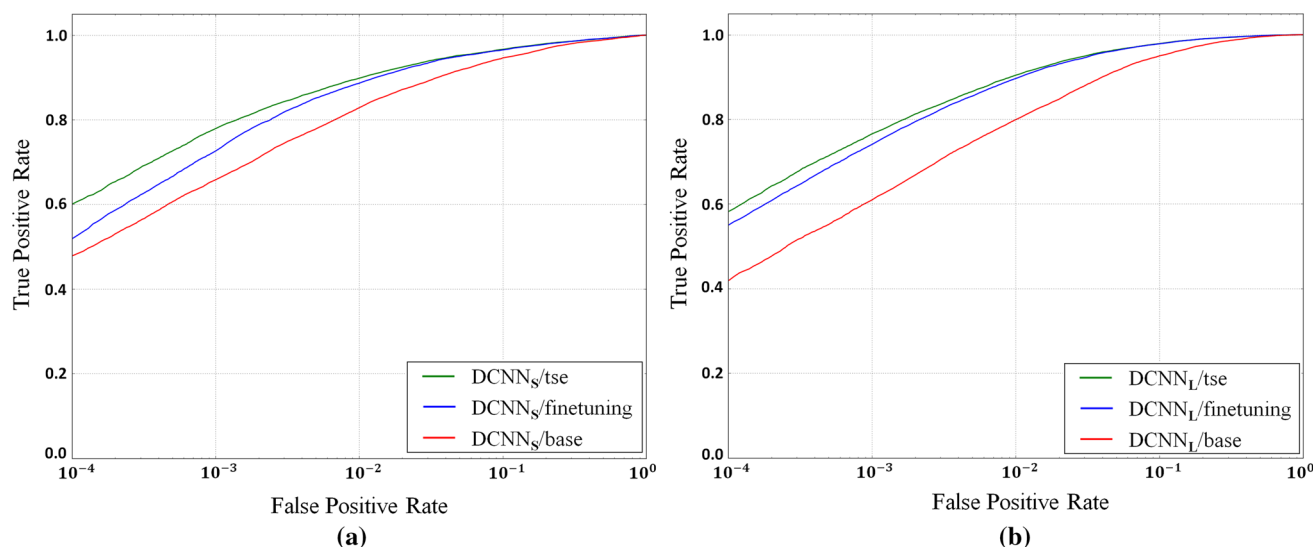
To take different situations into account, we have considered three modes of evaluations, manual, automatic and semi-automatic modes. This enables the handling of cases where we are unable to detect any of the faces (i.e., the failure of face detection.) in the images of the given template and also to compare the performance with the one using the metadata provided with the dataset. We describe the setups of performance evaluation in details as follows:

- **Setup 1 (manual mode)** Under this setup, we directly use the three facial landmarks and face bounding boxes provided along with the datasets.
- **Setup 2 (automatic mode)** In this setup when we get a video we use the face association method to detect and track the faces and to extract the bounding box to perform fiducial detection. If it is an image, we perform detection and facial landmark detection independently. For every image or frame in a template in which we are unable to detect the target face, we are unable to compare the template with others and thus assign all the corresponding





**Fig. 11** Sample images and frames from the IJB-A (*top*) and JANUS CS2 datasets (*bottom*). Challenging variations due to pose, illumination, resolution, occlusion, and image quality are present in these images



**Fig. 12** The performance evaluation for face verification tasks of **a**  $DCNN_S$  and **b**  $DCNN_L$  of before finetuning, with finetuning, and with finetuning and triplet similarity embedding for the JANUS CS2 dataset under Setup 3 (semi-automatic mode). Fine tuning is done only using the training data in each split

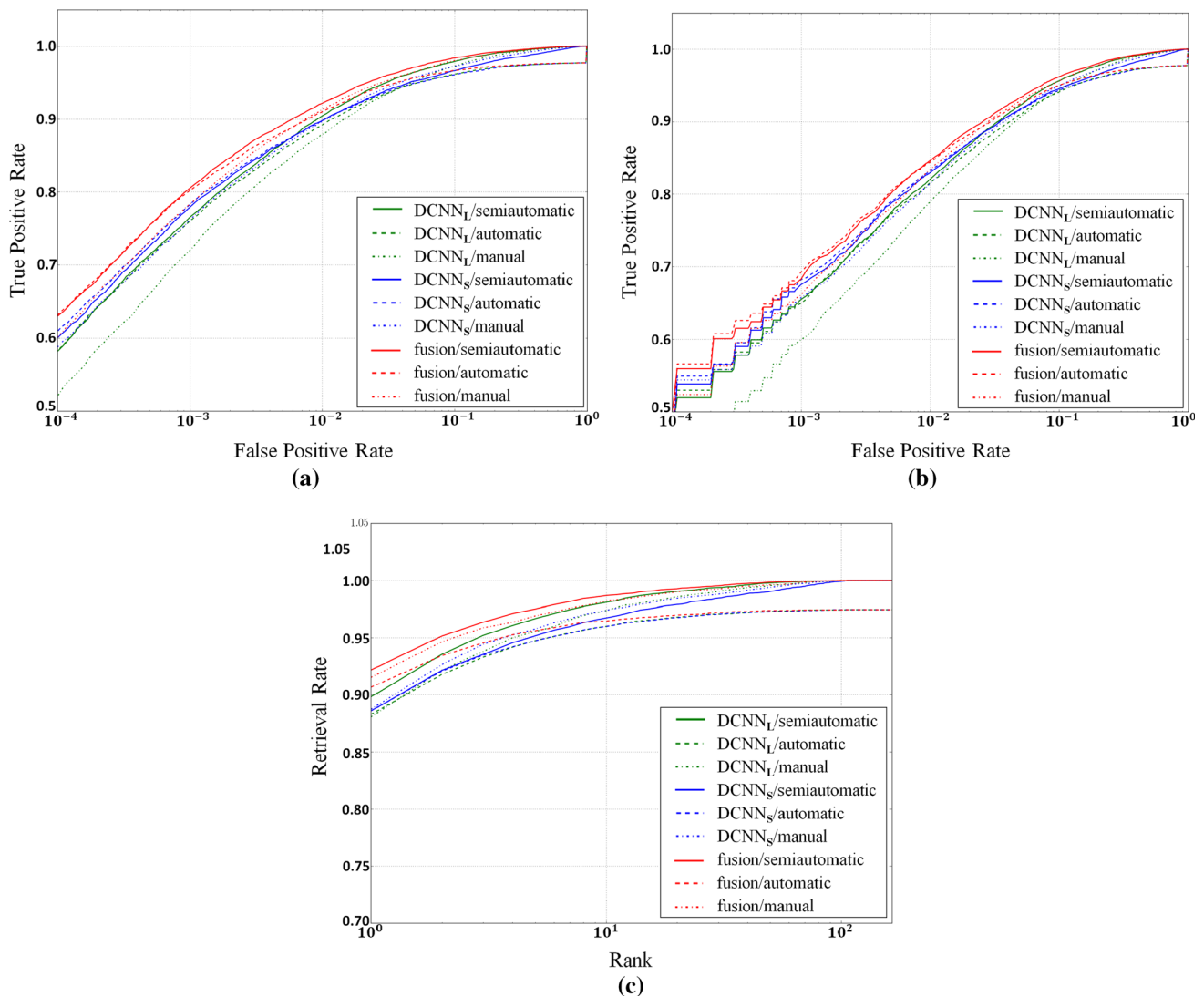
entries for the template in the similarity matrices to the lowest similarity scores,  $-\text{Inf}$ .

- **Setup 3 (semi-automatic mode)** In this setup if we are able to detect the target face in an image then we follow setup 2. Otherwise, we follow setup 1 to use the metadata of the dataset for the faces which are not detected and tracked by our algorithms.

To evaluate the performance of two networks individually, we present the ROC curves of  $DCNN_S$  and  $DCNN_L$  of the Setup 3 (i.e., semi-automatic mode) for the JANUS CS2 dataset in Fig. 12. As shown in the figures, the performances are consistently improved for both networks after fine-tuning the models previously trained using the CASIA-WebFace dataset on the training data of JANUS CS2. Triplet similarity embedding (TSE) further increase the performance for both networks, especially for the TAR number at the low FAR interval. For all the results presented here, fine tuning is done using only the training data in each split. The gallery dataset is not used for parameter fine tuning or for triplet similarity embedding. Then, we perform the fusion of the

two networks by adding the corresponding similarity scores together and demonstrate the fusion results of all the three setup for the verification task of both JANUS CS2 and IJB-A in Fig. 13a, b, respectively. In Fig. 13c, we present the CMC curve for the IJB-A identification task. From Fig. 13, it can be seen that even the simple fusion strategy used in this work significantly boosts the performance. Since  $DCNN_S$  is trained using tight face bounding boxes ( $DCNN_S$ ) and  $DCNN_L$  using the large ones which includes more context ( $DCNN_L$ ), one possible reason for the performance improvement is that the two networks contain discriminative information learned from different scales and complement each other. In addition, the figure also shows that the performance of our system in Setup 2 (the automatic mode) is comparable to Setup 1 (the manual mode) and Setup 3 (the semi-automatic mode). This demonstrates the robustness of each component of our system.

Besides using the average feature representation, we also perform media averaging which is to first average the features coming from the same media (image or video) and then further average the media average features to generate the final



**Fig. 13** **a, b** Face verification performance of the fusion model for JANUS CS2 and IJB-A (1:1) verification, respectively, and **c** face identification performance of the fusion model for IJB-A (1:N) identification for all the three setups. Fine tuning is done only using the training data in each split

feature representation. We show the results before and after media averaging for both IJB-A and JANUS CS2 dataset in Tables 5 and 6 respectively. It is clear that media averaging significantly improves the performance.

Tables 7 and 8 summarize the scores (i.e., both ROC and CMC numbers) produced by different face verification methods on the IJB-A and JANUS CS2 datasets, respectively. For the IJB-A dataset, we compare our fusion results (i.e., we perform finetuning and TSE in Setup 3.) with DCNN<sub>bl</sub> [bilinear CNN (RoyChowdhury et al. 2016)], DCNN<sub>pose</sub> [multi-pose DCNN models (AbdAlmageed et al. 2016)], NAN (Yang et al. 2016), DCNN<sub>3d</sub> (Masi et al. 2016), template adaptation (TP) (Crosswhite et al. 2016), DCNN<sub>lpe</sub> (Sankaranarayanan et al. 2016a) and the ones ([http://biometrics.nist.gov/cs\\_links/face/face\\_challenges/IJBA\\_reports.zip](http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip)) reported recently by NIST where JanusB-092015 achieved the best verification results,

and JanusD-071715 the best identification results. For the JANUS CS2 dataset, Table 8 includes, a DCNN-based method (Wang et al. 2015), Fisher vector-based method (Simonyan et al. 2013), DCNN<sub>pose</sub> (AbdAlmageed et al. 2016), DCNN<sub>3d</sub> (Masi et al. 2016), and two commercial off-the-shelf matchers, COTS and GOTS (Klare et al. 2015). From the ROC and CMC scores, we see that the fusion of DCNN methods significantly improve the performance. This can be attributed to the fact that the DCNN model does capture face variations over a large dataset and generalizes well to a new small dataset. In addition, the performance results of Janus B (Jan-usB-092015), Janus D (JanusD-071715), DCNN<sub>bl</sub> and DCNN<sub>pose</sub> systems have produced results for setup 1 (based on landmarks provided along with the dataset) only.

During the review period of the paper, newer results on IJB-A datasets have been reported. The interested readers

**Table 5** Results on the IJB-A dataset

	DCNN (setup 1)	DCNN (setup 2)	DCNN (setup 3)	DCNN <sub>m</sub> (setup 1)	DCNN <sub>m</sub> (setup 2)	DCNN <sub>m</sub> (setup 3)
<b>IJB-A-Verif</b>						
FAR = 1e−2	0.834 ± 0.036	0.844 ± 0.026	0.846 ± 0.029	0.863 ± 0.02	0.885 ± 0.014	<b>0.889 ± 0.016</b>
FAR = 1e−1	0.956 ± 0.008	0.95 ± 0.005	0.962 ± 0.007	0.966 ± 0.05	0.954 ± 0.003	<b>0.968 ± 0.005</b>
<b>IJB-A-Ident</b>						
Rank-1	0.915 ± 0.011	0.907 ± 0.011	0.922 ± 0.011	0.916 ± 0.009	0.923 ± 0.01	<b>0.942 ± 0.008</b>
Rank-5	0.969 ± 0.007	0.955 ± 0.007	0.975 ± 0.006	0.971 ± 0.007	0.961 ± 0.006	<b>0.98 ± 0.005</b>
Rank-10	0.982 ± 0.005	0.965 ± 0.005	0.987 ± 0.001	0.981 ± 0.005	0.969 ± 0.004	<b>0.988 ± 0.003</b>
<b>IJB-A-Ident</b>						
FPIR = 0.01	0.618 ± 0.05	0.64 ± 0.043	0.631 ± 0.041	0.639 ± 0.057	0.646 ± 0.055	<b>0.654 ± 0.001</b>
FPIR = 0.1	0.799 ± 0.014	0.806 ± 0.012	0.813 ± 0.014	0.816 ± 0.015	0.827 ± 0.012	<b>0.836 ± 0.01</b>

Bold values indicate the best performances achieved by different methods at each operating point

The TAR of all the approaches at FAR = 0.1 and 0.01 for the ROC curves (IJB-A 1:1 verification). The Rank-1, Rank-5, and Rank-10 retrieval accuracies of the CMC curves and TPIR at FPIR = 0.01 and 0.1 (IJB-A 1:N identification). We also show the results before and after media averaging where *m* means media averaging

**Table 6** Results on the JANUS CS2 dataset

	DCNN (setup 1)	DCNN (setup 2)	DCNN (setup 3)	DCNN <sub>m</sub> (setup 1)	DCNN <sub>m</sub> (setup 2)	DCNN <sub>m</sub> (setup 3)
<b>CS2-Verif</b>						
FAR = 1e−2	0.913 ± 0.008	0.91 ± 0.008	0.922 ± 0.007	0.92 ± 0.01	0.922 ± 0.008	<b>0.935 ± 0.007</b>
FAR = 1e−1	0.98 ± 0.004	0.967 ± 0.003	0.984 ± 0.003	0.981 ± 0.003	0.968 ± 0.003	<b>0.986 ± 0.002</b>
<b>CS2-Ident</b>						
Rank-1	0.9 ± 0.01	0.896 ± 0.008	0.909 ± 0.008	0.905 ± 0.007	0.915 ± 0.007	<b>0.931 ± 0.007</b>
Rank-5	0.963 ± 0.006	0.954 ± 0.006	0.969 ± 0.006	0.965 ± 0.004	0.959 ± 0.005	<b>0.976 ± 0.004</b>
Rank-10	0.977 ± 0.006	0.965 ± 0.004	0.981 ± 0.003	0.977 ± 0.004	0.967 ± 0.004	<b>0.985 ± 0.002</b>

Bold values indicate the best performances achieved by different methods at each operating point

The TAR of all the approaches at FAR = 0.1 and 0.01 for the ROC curves. The Rank-1, Rank-5, and Rank-10 retrieval accuracies of the CMC curves. We report average and standard deviation of the 10 splits. We also show the results before and after media averaging where *m* means media averaging

are referred to [Xiong et al. \(2017\)](#) and [Ranjan et al. \(2017\)](#) for more details. In addition, the NAN ([Yang et al. 2017](#)) results are based on an earlier version ([Yang et al. 2016](#)). More recent state of the art results are reported in [Ranjan et al. \(2017\)](#) obtained by employing the deep residual network and  $L_2$ -norm regularized softmax loss.

#### 4.5 Labeled Faces in the Wild

We also evaluate our approach on the well-known LFW dataset ([Huang et al. 2008a](#)) using the standard protocol which defines 3000 positive pairs and 3000 negative pairs in total and further splits them into 10 disjoint subsets for cross validation. Each subset contains 300 positive and 300 negative pairs. It contains 7701 images of 4281 subjects. We compare the mean accuracy of the proposed deep model with other state-of-the-art deep learning-based methods: Deep-Face ([Taigman et al. 2014](#)), DeepID2 ([Sun et al. 2014](#)), DeepID3 ([Sun et al. 2015](#)), FaceNet ([Schroff et al. 2015](#);

[Yi et al. 2014](#); [Wang et al. 2015](#); [Ding and Tao 2015](#); [Parkhi et al. 2015](#)), and human performance on the “funneled” LFW images. The results are summarized in Table 9. It can be seen that our approach performs comparable to other deep learning-based methods. Note that some of the deep learning-based methods compared in Table 9 use millions of data samples for training the model. In comparison, we use only the CASIA dataset for training our model which has less than 500 K images.

#### 4.6 Comparison with Methods Based on Annotated Metadata

Most systems compared in this paper produced the results for setup 1 which is based on landmarks provided along with the dataset only (i.e., except DCNN<sub>lpe</sub>). For DCNN<sub>3d</sub> ([Masi et al. 2016](#)), the number of face images is augmented along with the original CASIA-WebFace dataset by around 2 million using 3D morphable models. On the other hand,



**Table 7** Results on the IJB-A dataset

	Wang et al. (2015)	JanusB ( <a href="http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip">http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip</a> )	JanusD ( <a href="http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip">http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip</a> )	DCNN <sub>bl</sub> (RoyChowdhury et al. 2016)	NAN (Yang et al. 2016)	DCNN <sub>3d</sub> (Masi et al. 2016)
<b>IJB-A-Verif</b>						
FAR = 1e−3	0.514 ± 0.006	0.65	0.49	–	0.785 ± 0.028	0.725
FAR = 1e−2	0.732 ± 0.033	0.826	0.71	–	0.897 ± 0.01	0.886
FAR = 1e−1	0.895 ± 0.013	0.932	0.89	–	0.959 ± 0.005	–
<b>IJB-A-Ident</b>						
Rank-1	0.820 ± 0.024	0.87	0.88	0.895 ± 0.011	–	0.906
Rank-5	0.929 ± 0.013	–	–	0.963 ± 0.005	–	0.962
Rank-10	–	0.95	0.97	–	–	0.977
	DCNN <sub>pose</sub> (AbdAlmageed et al. 2016)	DCNN <sub>m</sub> (setup 1)	DCNN <sub>m</sub> (setup 2)	DCNN <sub>m</sub> (setup 3)	DCNN <sub>rpe</sub> (Sankaranarayanan et al. 2016a)	TP (Crosswhite et al. 2016)
<b>IJB-A-Verif</b>						
FAR = 1e−3	–	0.704 ± 0.037	0.762 ± 0.038	0.76 ± 0.038	<b>0.813 ± 0.02</b>	–
FAR = 1e−2	0.787	0.863 ± 0.02	0.885 ± 0.014	0.889 ± 0.016	0.9 ± 0.01	<b>0.939 ± 0.013</b>
FAR = 1e−1	0.911	0.966 ± 0.05	0.954 ± 0.003	<b>0.968 ± 0.005</b>	0.964 ± 0.01	–
<b>IJB-A-Ident</b>						
Rank-1	0.846	0.916 ± 0.009	0.923 ± 0.01	<b>0.942 ± 0.008</b>	0.932 ± 0.001	0.928 ± 0.01
Rank-5	0.927	0.971 ± 0.007	0.961 ± 0.006	<b>0.98 ± 0.005</b>	–	–
Rank-10	0.947	0.981 ± 0.005	0.969 ± 0.004	<b>0.988 ± 0.003</b>	0.977 ± 0.005	0.986 ± 0.003

Bold values indicate the best performances achieved by different methods at each operating point

The TAR of all the approaches at FAR = 0.1, 0.01, and 0.001 for the ROC curves (IJB-A 1:1 verification). The Rank-1, Rank-5, and Rank-10 retrieval accuracies of the CMC curves (IJB-A 1:N identification). We report average and standard deviation of the 10 splits. All the performance results reported in [http://biometrics.nist.gov/cs\\_links/face/face\\_challenges/IJBA\\_reports.zip](http://biometrics.nist.gov/cs_links/face/face_challenges/IJBA_reports.zip), Janus B (JanusB-092015), Janus D (JanusD-071715), DCNN<sub>bl</sub> (RoyChowdhury et al. 2016), DCNN<sub>3d</sub> (Masi et al. 2016), NAN (Yang et al. 2016), DCNN<sub>pose</sub> (AbdAlmageed et al. 2016), DCNN<sub>rpe</sub> (Sankaranarayanan et al. 2016a), and TP (Crosswhite et al. 2016) are included in the Table. Some of these systems have produced results for setup 1 (based on landmarks provided along with the dataset) only. In addition, we also compare the performance of the recent work, DCNN<sub>rpe</sub> (Sankaranarayanan et al. 2016a) where the performance difference mainly comes from the better preprocessing module and improved metric (Ranjan et al. 2016a)

NAN (Yang et al. 2016) and TP (Crosswhite et al. 2016) used datasets with more than 2 million face images to train the model. However, the networks used in this work were trained with the original CASIA-WebFace which contains around 500K images. In addition, TP adapted the one-shot similarity framework (Wolf et al. 2009) with linear support vector machine for set-based face verification and trained the metric on-the-fly with the help of a pre-selected negative set during testing. Although TP achieved significantly better results than other approaches, it takes more time during testing than the proposed method since our metric is trained off-line and requires much less time for testing than TP. We expect the performance of the proposed approach can also be improved by using the one-shot similarity framework. As shown in Table 7, the proposed approach achieves comparable results to other methods and strikes a balance between testing time and performance. In a recent work, DCNN<sub>rpe</sub> (Sankaranarayanan et al. 2016a), adopted a proba-

bilistic embedding for similarity computation and a new face preprocessing module, hyperface (Ranjan et al. 2016a), for improved face detection and fiducials where (Ranjan et al. 2016a) is a multi-task deep network trained for the tasks of gender classification, fiducial detection, pose estimation and face detection. We plan to incorporate hyperface into the current framework which may yield some improvement in performance.

#### 4.7 Run Time

The DCNN<sub>S</sub> model for face verification is trained on the CASIA-Webface dataset from scratch for about 4 days and for DCNN<sub>L</sub>, it takes 20h to train on the same face dataset which is initialized using the weights of Alexnet pretrained on the ImageNet dataset. The two networks are trained using NVidia Titan X with cudnn v4. The running time for face detection is around 0.7s per image. The facial

**Table 8** Results on the JANUS CS2 dataset

	COTS	GOTS	FV (Simonyan et al. 2013)	DCNN <sub>pose</sub> (AbdAlmageed et al. 2016)
CS2-Verif				
FAR = 1e−3	–	–	–	–
FAR = 1e−2	0.581 ± 0.054	0.467 ± 0.066	0.411 ± 0.081	0.897
FAR = 1e−1	0.767 ± 0.015	0.675 ± 0.015	0.704 ± 0.028	0.959
CS2-Ident				
Rank-1	0.551 ± 0.003	0.413 ± 0.022	0.381 ± 0.018	0.865
Rank-5	0.694 ± 0.017	0.571 ± 0.017	0.559 ± 0.021	0.934
Rank-10	0.741 ± 0.017	0.624 ± 0.018	0.637 ± 0.025	0.949
	DCNN <sub>3d</sub> (Masi et al. 2016)	DCNN (setup 1)	DCNN (setup 2)	DCNN (setup 3)
CS2-Verif				
FAR = 1e−3	0.824	0.81 ± 0.018	0.823 ± 0.013	<b>0.83 ± 0.014</b>
FAR = 1e−2	0.926	0.92 ± 0.01	0.922 ± 0.008	<b>0.935 ± 0.007</b>
FAR = 1e−1	–	0.981 ± 0.003	0.968 ± 0.003	<b>0.986 ± 0.002</b>
CS2-Ident				
Rank-1	0.898	0.905 ± 0.007	0.915 ± 0.007	<b>0.931 ± 0.007</b>
Rank-5	0.956	0.965 ± 0.004	0.959 ± 0.005	<b>0.976 ± 0.004</b>
Rank-10	0.969	0.977 ± 0.004	0.967 ± 0.004	<b>0.985 ± 0.002</b>

The TAR of all the approaches at FAR = 0.1, 0.01, and 0.001 for the ROC curves. The Rank-1, Rank-5, and Rank-10 retrieval accuracies of the CMC curves. We report average and standard deviation of the 10 splits. The performance results of DCNN<sub>pose</sub> have produced results for setup 1 only

**Table 9** Accuracy of different methods on the LFW dataset

Method	#Net	Training set	Metric	Mean accuracy ± SD
DeepFace (Taigman et al. 2014)	1	4.4 million images of 4030 subjects, private	Cosine	95.92 ± 0.29%
DeepFace	7	4.4 million images of 4030 subjects, private	Unrestricted, SVM	97.35 ± 0.25%
DeepID2 (Sun et al. 2014)	1	202,595 images of 10,117 subjects, private	Unrestricted, Joint-Bayes	95.43%
DeepID2	25	202,595 images of 10,117 subjects, private	Unrestricted, Joint-Bayes	99.15 ± 0.15%
DeepID3 (Sun et al. 2015)	50	202,595 images of 10,117 subjects, private	Unrestricted, Joint-Bayes	99.53 ± 0.10%
FaceNet (Schroff et al. 2015)	1	260 million images of 8 million subjects, private	L2	99.63 ± 0.09%
Yi et al. (2014)	1	494,414 images of 10,575 subjects, public	Cosine	96.13 ± 0.30%
Yi et al.	1	494,414 images of 10,575 subjects, public	Unrestricted, Joint-Bayes	97.73 ± 0.31%
Wang et al. (2015)	1	494,414 images of 10,575 subjects, public	Cosine	96.95 ± 1.02%
Wang et al.	7	494,414 images of 10,575 subjects, public	Cosine	97.52 ± 0.76%
Wang et al.	1	494,414 images of 10,575 subjects, public	Unrestricted, Joint-Bayes	97.45 ± 0.99%
Wang et al.	7	494,414 images of 10,575 subjects, public	Unrestricted, Joint-Bayes	98.23 ± 0.68%
Ding and Tao (2015)	8	471,592 images of 9000 subjects, public	Unrestricted, Joint-Bayes	99.02 ± 0.19%
Parkhi et al. (2015)	1	2.6 million images of 2,622 subjects, public	Unrestricted, TDE	98.95%
Human, funneled (Wang et al. 2015)	N/A	N/A	N/A	99.20%
Our DCNN <sub>S</sub>	1	490,356 images of 10,548 subjects, public	Cosine	97.7 ± 0.8%
Our DCNN <sub>L</sub>	1	490,356 images of 10,548 subjects, public	Cosine	96.8 ± 0.6%
Our DCNN <sub>S</sub> + DCNN <sub>L</sub>	2	490,356 images of 10,548 subjects, public	Cosine	98 ± 0.5%
Our DCNN <sub>S</sub> + DCNN <sub>L</sub>	2	490,356 images of 10,548 subjects, public	Unrestricted, TSE	98.33 ± 0.7%

landmark detection and feature extraction steps take about 1 and 0.006 s per face, respectively (i.e., To compare the speed difference, we run the feature extraction part using CPU. it takes around 0.7 s for feature extraction using a

core of 16-core 3.0GHz Intel Xeon CPU and math library atlas which is around 100 times as the GPU time.) The face association module for a video takes around 5 fps on average.

## 5 Open Issues

Given sufficient number of annotated data and GPUs, DCNNs have been shown to yield impressive performance improvements. Still many issues remain to be addressed to make the DCNN-based recognition systems robust and practical. These are briefly discussed below.

- **Reliance on large training data sets** One of the top performing networks in the MegaFace challenge needs 500 million faces of about 10 million subjects. Such large annotated training set may not be always available (e.g., expression recognition, age estimation). So networks that can perform well with reasonable-sized training data are needed.
- **Invariance** While limited invariance to translation is possible with existing DCNNs, networks that can incorporate more general invariances are needed.
- **Training time** The training time even when GPUs are used can be several tens of hours, depending on the number of layers used and the training data size. More efficient implementations of learning algorithms, preferably implemented using CPUs are desired.
- **Number of parameters** The number of parameters can be several tens of millions. Novel strategies that reduce the number of parameters need to be developed.
- **Handling degradations in training data** DCNNs robust to low-resolution, blur, illumination and pose variations, occlusion, erroneous annotation, etc. are needed to handle degradations in data.
- **Domain adaptation of DCNNs** While having large volumes of data may help with processing test data from a different distribution than that of the training data, systematic methods for adapting the deep features to test data are needed.
- **Theoretical considerations** While DCNNs have been around for a few years, detailed theoretical understanding is just starting to develop (Bruna and Mallat 2013; Mallat 2016; Giryes et al. 2014; Haeffele and Vidal 2015). Methods for deciding the number of layers, neighborhoods over which max pooling operations are performed are needed.
- **Incorporating domain knowledge** The current practice is to rely on fine tuning. For example, for the age estimation problem, one can start with one of the standard networks such as the AlexNet and fine tune it using aging data. While this may be reasonable for somewhat related problems (face recognition and facial expression recognition), such fine tuning strategies may not always be effective. Methods that can incorporate context may make the DCNNs more applicable to a wider variety of problems.

- **Memory** Although Recurrent CNNs are on the rise, they still consume a lot of time and memory for training and deployment. Efficient DCNN algorithms are needed to handle videos and other data streams as blocks.

We also discussed design considerations for each component of a full face verification system, including

- **Face detection** Face detection is challenging due to the wide range of variations in the appearance of faces. The variability is caused mainly by changes in illumination, facial expression, viewpoints, occlusions, etc. Other factors such as blurry images and low resolution are prominent in face detection task.
- **Fiducial detection** Most of the datasets only contain few thousands images. A large scale annotated and unconstrained dataset will make the face alignment system more robust to the challenges, including extreme pose, low illumination, small and blurry face images. Researchers have hypothesized that deeper layers can encode more abstract information such as identity, pose, and attributes; However, it has not yet been thoroughly studied which layers exactly correspond to local features for fiducial detection.
- **Face association** Since the video clips may contain media of low-quality images, the blurred and low-resolution image makes the face detection not reliable. This may lead to performance degradation of face association since a face track will not be initiated due to the missing of face detection. Besides, abrupt motion, occlusion, and crowded scene can lead to performance degradation of tracking and potential identity switching.
- **Face verification** For face verification, the performance can be improved by learning a discriminative distance measure. However, due to memory constraints limited by graphics cards, how to choose informative pairs or triplets and train the network end-to-end using online methods (e.g., stochastic gradient descent) on large-scale datasets are still open problems.

## 6 Conclusion

We presented the design and performance of our automatic face verification system, which automatically locates faces and performs verification/recognition on newly released challenging face verification datasets, IARPA Benchmark A (IJB-A) and its extended version, JANUS CS2. It is shown that the proposed DCNN-based system can not only accurately locate the faces across images and videos but also learn a robust model for face verification. Experimental results demonstrate that the performance of the proposed system on



the IJB-A dataset is much better than a FV-based method and some COTS and GOTS matchers.

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