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# REVIEW ON SORTING ALGORITHMS

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Computational Thinking with Algorithms

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# I. Introduction

Sorting is a process of organising a list of elements in a particular order. The most used orders are lexicographical (alphabetic) or numeric (ascending or descending). Sorting increases efficiency of subsequent operations performed on the elements since it is easier to handle sorted elements than randomize data (S. Paira et al., 2014). While sorting is a simple concept, it is frequently used as an intermediate step by complex computer programs such as data compression, path finding, data search, media recovery etc. This makes sorting a fundamental operation in computer science.

Sorting algorithm is an algorithm that takes an array as input and outputs a permutation of that array that is sorted (Sorting Algorithms, n.d.). Enhancing the existing sorting algorithms or producing new algorithms can greatly optimize other algorithms. Thus, a large number of algorithms has been developed to improve sorting, each approaching the reordering of elements differently in order to increase the performance and efficiency of the practical applications (K. S. Al-Kharabsheh et al., 2013).

There are two categories of sorting algorithms: *comparison* and *non-comparison based* sorts. Comparison based sorting algorithms determine the sorted order by comparing input elements, whereas non-comparison based by performing operations other than comparisons. In other words, comparison sorts require a *comparator function* to define ordering, and thus can be used for sorting any object. On the other hand, non-comparison based sorting algorithms do not rely on having a *comparator function* so they can only be used to sort integers (T. Cormen et al., 2003).

Examples of comparison based sorts are simple comparison-based sorts (Bubble Sort, Selection Sort and Insertion Sort) and efficient comparison-based sort (Merge Sort, Quicksort and Heap Sort). Counting Sort, Bucket Sort or Radix Sort are examples on-comparison sorts.

When comparing various sorting algorithms, there are several factors that must be taken in consideration.

## 1. Time complexity.

Time complexity of an algorithm signifies the amount of time that required by an algorithm to run till its completion. The time complexity of an algorithm is generally written in form big  $O(n)$  notation, where the  $O$  represents the complexity of the algorithm and a value  $n$  represent the number of elementary operations performed by the algorithm (C. Scheideler, 2005). For example, a sorting algorithm has  $O(1)$ , or constant time complexity if it needs to operate on one element of input list (regardless of the size). Time complexity of  $O(n)$  means an algorithm operates on each of the  $n$  elements of input list only once, etc. There are three types of time complexity: *best*, *average*, and *worst-case* complexity ( $\cdot$ ).

## 2. Space complexity

Space complexity describes the amount of memory (or space) necessary to perform the task that the algorithm is expected to solve. For example, space complexity of  $O(1)$  means that the algorithm doesn't require extra memory allocation to sort the input list. The sorting in this case is done *in-place*. A sorting algorithm has a  $O(n)$  space complexity when it needs the allocation of new space in memory like creating a new array (or list). This is an *outplace* sorting technique. Sorting algorithms that use recursive techniques require more copies of sorting data which increases their space complexity (Space Complexity, n.d.).

## 3. Stability

The stability of a sorting algorithm concerns preserving the same relative order of elements with equal values in the output as they were in the input. Some sorting algorithms are stable by its nature (Bubble sort, Insertion sort, Merge sort) while some sorting algorithms are not (Selection sort, Heap Sort, Quicksort). However, any given unstable sort can be modified to be stable. (K. S. Al-Kharabsheh et al., 2013)

## II. Five Sorting Algorithms

In this report I examined five sorting algorithms: Insertion Sort, Quicksort, Heap Sort, Bucket Sort and Introsort.

### 1. Insertion Sort

Insertion sort is a simple comparison-based sort that builds a final list one element at a time. Consider the example below where an array [4, 1, 20, 3, 11, 5, 9] needs to be sorted.

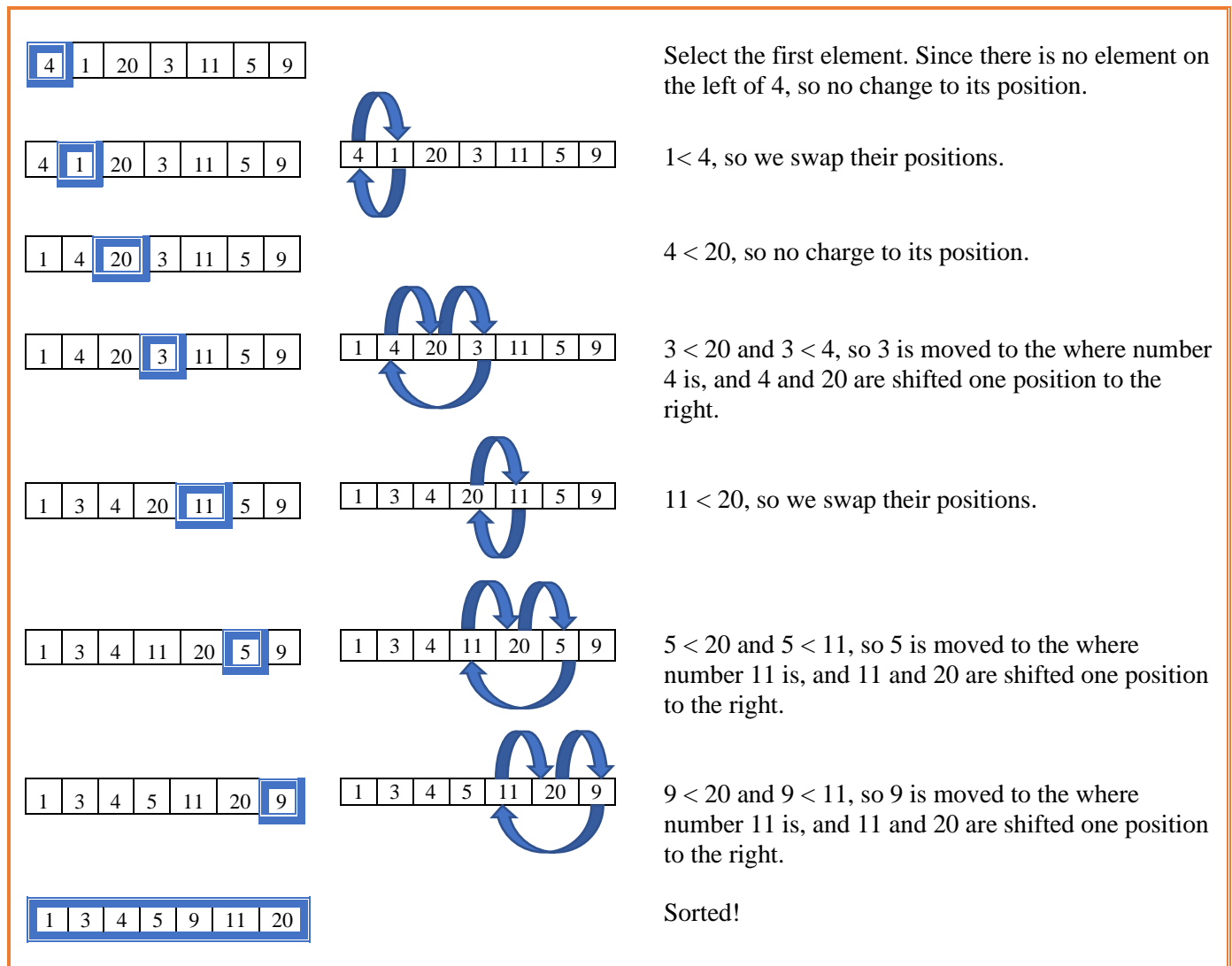


Table 1 Insertion Sort Diagram

Insertion sort is a stable in-place sort with  $O(1)$  space complexity. Regarding the time complexity, in the best case it is  $O(n)$ , in the worst and average cases -  $O(n^2)$ . The best case occurs when the data is already sorted, so insertion sort only compares  $O(n)$  elements without performing any swaps. The insertion sort runs in its worst when the elements in the list are sorted in decreasing order when for the last element insertion at most  $n-1$  comparisons and  $n-1$  swaps are needed, for the second to last element insertion – at most  $n-2$  comparisons and  $n-2$  swaps, etc. Hence the number of steps required come to  $2 \times (1+2 + \dots + n-2 + n-1)$  (Insertion Sort, n.d.).

Among the advantages of insertion sort are a tight code and efficiency when sorting small and nearly sorted data. However, it is much less efficient for sorting large and more unordered lists.

## 2. Quicksort

Quicksort is efficient comparison-based sort that utilizes a divide-and-conquer approach to sorting lists. Divide-and-conquer technique recursively breaks an algorithm down into two or more subproblems until they are simple enough to be solved, and then combining the results back together to solve the original problem (T. Cormen et al., 2003). In case of quicksort, a pivot is selected in order to divide the algorithm into subarrays. Consider the table below.

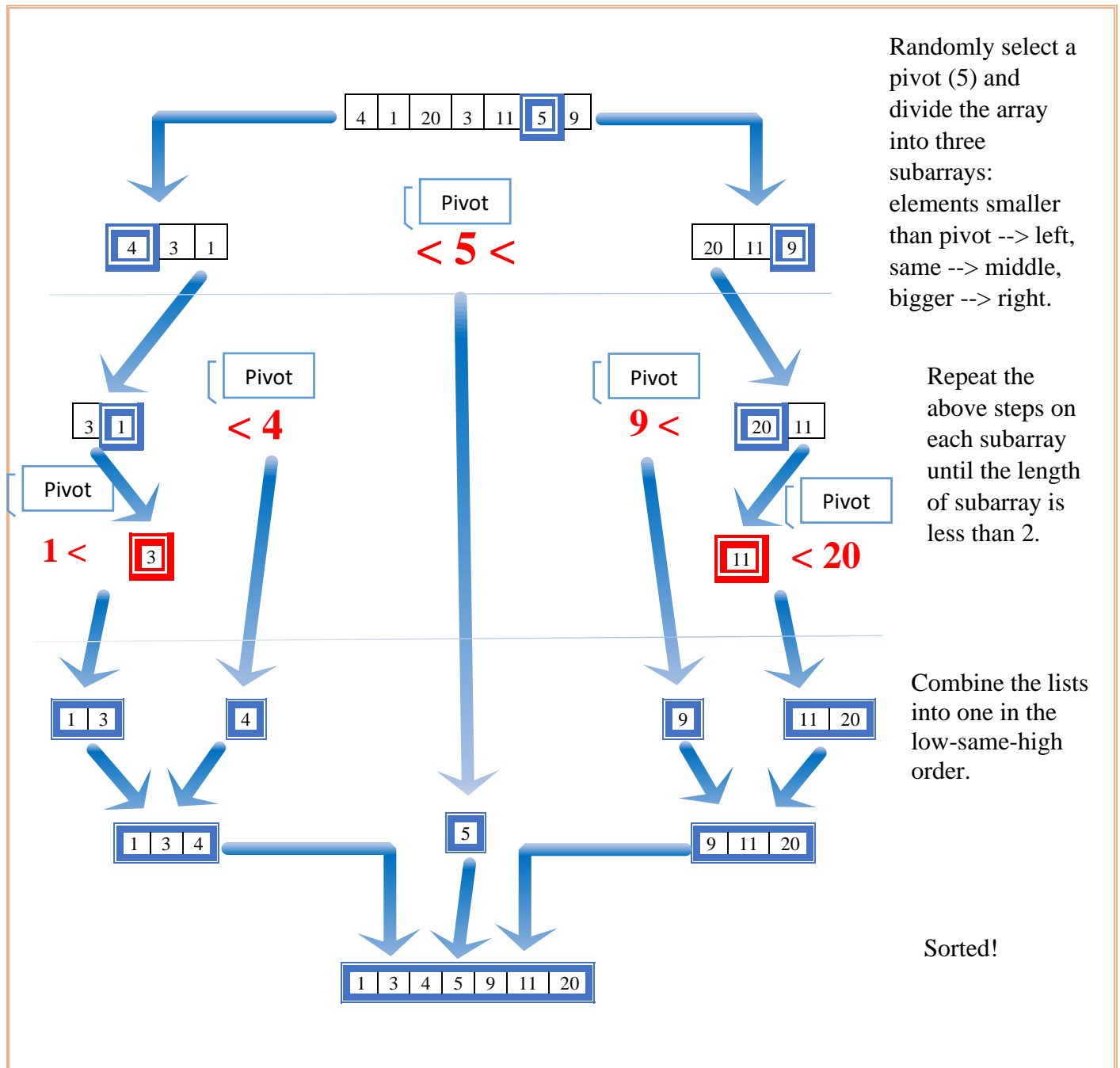


Table 2 Quicksort Diagram

Choosing a good pivot is the crucial part to a fast implementation of quicksort. The best pivot would split the input array in two even subarrays, which would halve the problem size (the best case time complexity). The example above depicts a random selection of a pivot. However, there are other ways of doing it:

- Select the leftmost or rightmost element as the pivot.
- Median-of-three method: take the first, middle, and last value of the array, and choose the median of those three numbers as the pivot.
- Use a median-finding algorithm such as the median-of-medians algorithm.

Quicksort is usually implemented as an unstable sort with a best-case space complexity of  $O(\log n)$  and an average-case space complexity of  $O(n)$ . In the best and average cases, the algorithm runs  $O(n \log n)$  time, in the worst case –  $O(n^2)$ . The worst case would be when the pivot is either the minimum or maximum element in the array (Quick Sort, n.d.).

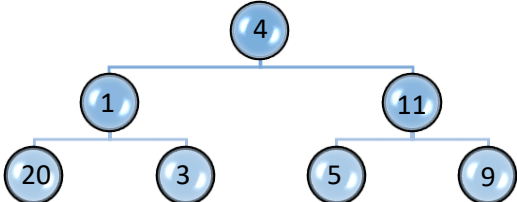
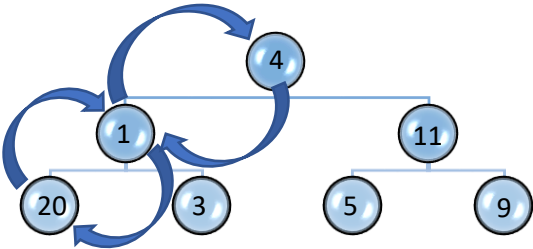
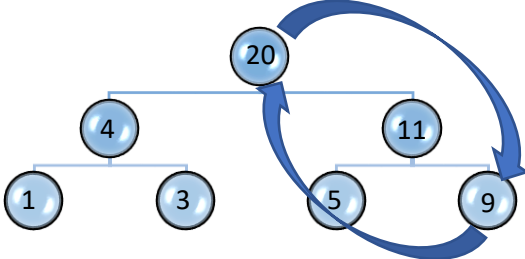
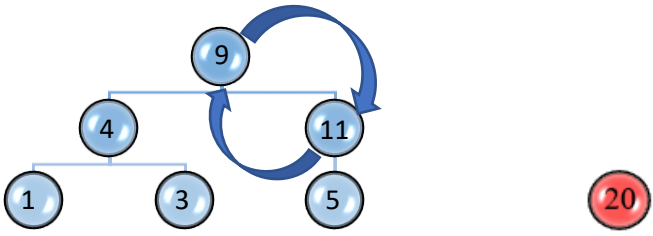
Quicksort usually outperforms other comparison based sorts, thus considered to be the best practical choice for sorting large data. Like insertion sort, it has simple implementation, and it sorts in-place, but it also can run as slow as insertion sort in its worst case (T. Cormen et al., 2003).

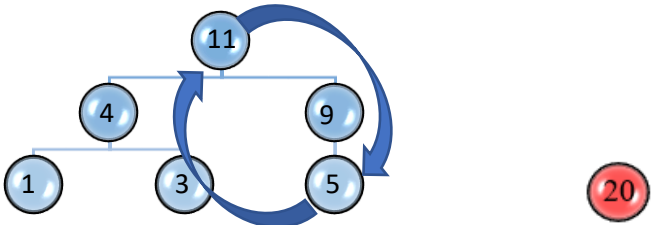
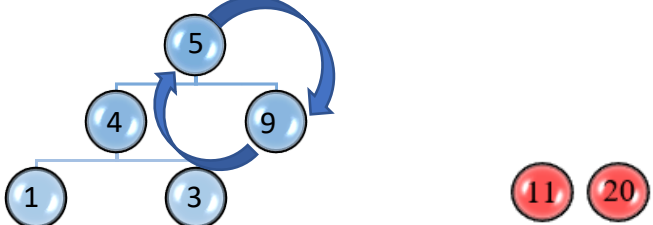
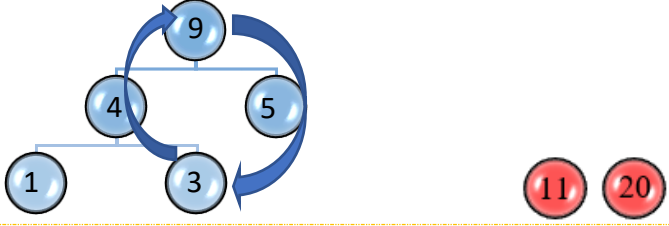

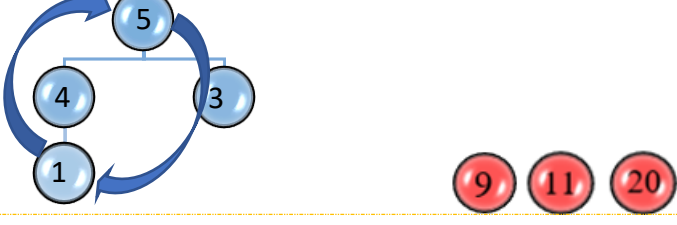
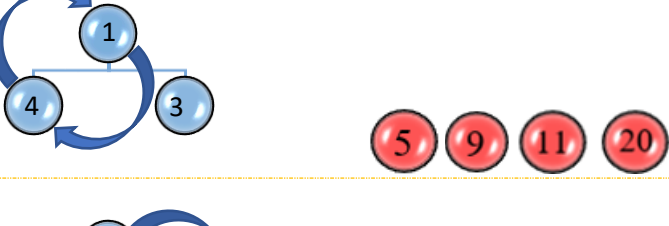
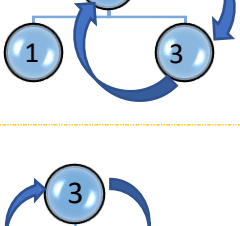
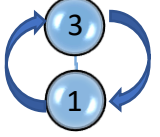
### 3. Heap Sort



Heapsort is a comparison-based [sorting algorithm](#) that uses a [binary heap](#) data structure.

The binary heap data structure allows the heapsort algorithm to take advantage of the heap's **heap properties** and the heapsort algorithm makes use of the efficient running time for inserting to and deleting from the heap. <https://brilliant.org/wiki/heap-sort/>

<https://www.hackerearth.com/practice/algorithms/sorting/heap-sort/tutorial/>

|   |  |
|---|--|
|   | <p>Initial array [4, 1, 20, 3, 11, 5, 9] as heap.</p>  |
|  | <p>Initially build a max heap of elements in the array</p>                                     |
|  | <p>20 is swapped with 9.</p>   |
|  | <p>20 is disconnected from heap as it is in correct position now.<br/>Max heap is created.</p> |
|   |  |

|   |  |
|---|--|
|    | <p>11 is swapped with 5.</p>   |
|    | <p>11 is disconnected from heap as it is in its correct position now.<br/>Max heap is created.</p>                     |
|    | <p>9 is swapped with 3.</p>  |
|   | <p>9 is disconnected from heap as it is in its correct position now.<br/>Max heap is created.</p>                      |
|  | <p>5 is swapped with 1.</p>  |
|  | <p>5 is disconnected from heap as it is in its correct position now.<br/>Max heap is created.</p>                      |
|  | <p>4 is swapped with 3.</p>  |
|  | <p>4 is disconnected from heap as it is in its correct position now. Max heap is created.<br/>3 is swapped with 1.</p> |

|   |  |
|---|--|
|  | <p>3 is disconnected from heap as it is in its correct position now.<br/>1 is in its own position now.</p> |
|  | <p>Sorted!</p>   |

#### 4. Bucket Sort

#### 5. Introsort

### III. Implementation & Benchmarking

This section will describe the process followed when implementing the application above, and will present the results of your benchmarking. Discuss how the measured performance of the algorithms differed – were the results similar to what you would expect, given the time complexity of each chosen algorithm?

All five sorting algorithms (Insertion Sort, Quicksort, Heap Sort, Bucket Sort and Introsort) were implemented in Python and tested for the random sequence input of length from 100 to 10000. All five sorting algorithms were executed on machine Operating System having Intel(R) Core(TM) i7-7700HQ CPU @ 2.80 GHz and installed memory (RAM) 8.00 GB. The Plot of length of input and CPU time taken (in milliseconds) is shown in Figure 1. The result shows that for small input the performance for the five algorithms is almost nearest, but for the large input Quicksort and Introsort are the fastest and the Insertion sort the slowest.

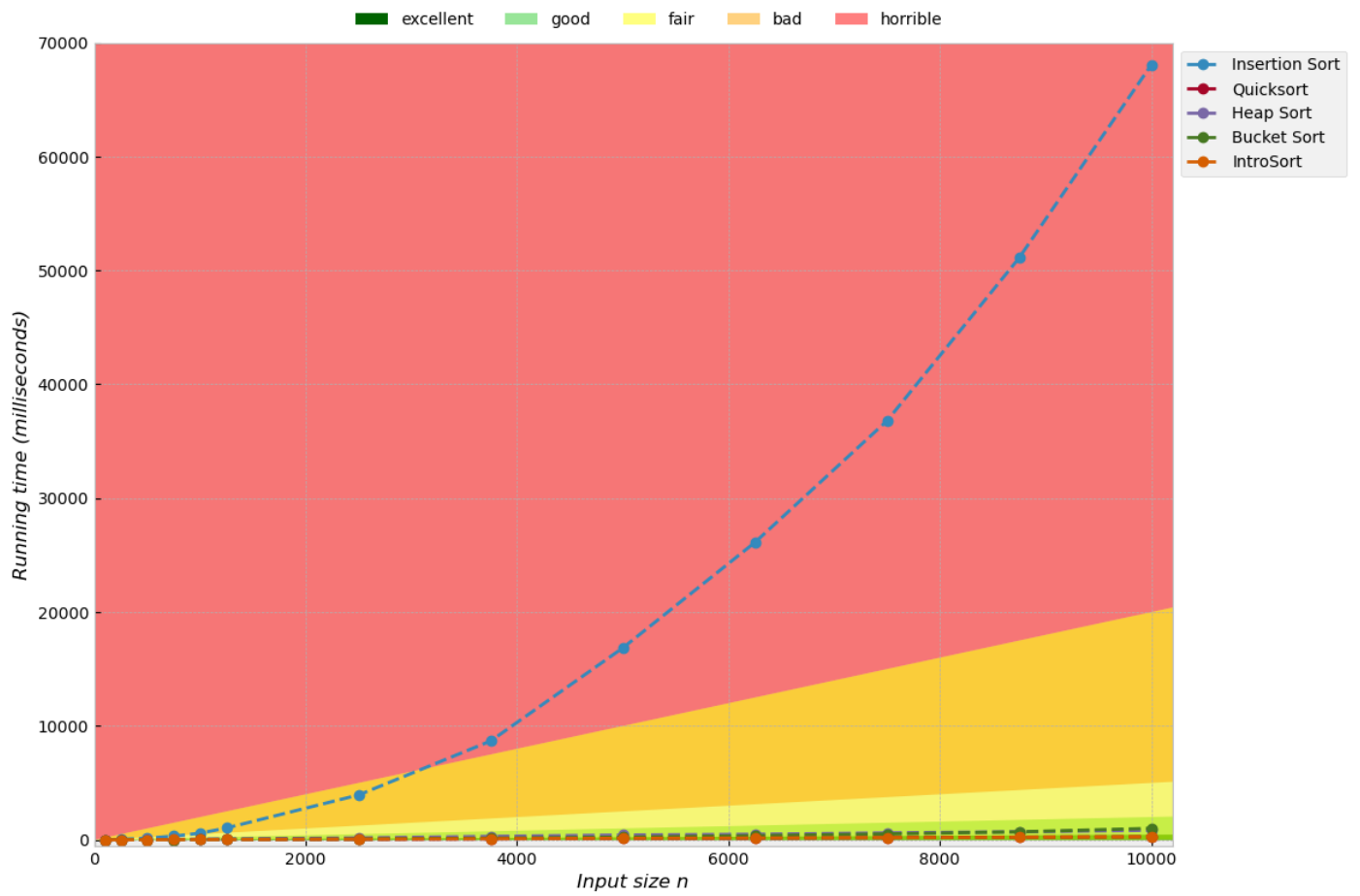
and measure the execution time of all programs with the same input data using the same computer. The built-in function (clock ()) in C++ is used to get the elapsed time of the implementing algorithms, execution time of a program is measured in milliseconds [6].The performances of GCS algorithm and a set of conventional sort algorithms are comparatively tested under average cases by using random test data from size 10000 to 30000. The result obtained is given in Table 1 to Table 6 for each Algorithm and the curves are shown in figure 1.

| <i>Sizes</i>          | <i>100</i> | <i>250</i> | <i>500</i> | <i>750</i> | <i>1000</i> | <i>1250</i> | <i>2500</i> | <i>3750</i> | <i>5000</i> | <i>6250</i> | <i>7500</i> | <i>8750</i> | <i>10000</i> |
|-----------------------|------------|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|--------------|
| <i>Insertion Sort</i> | 8.615      | 44.187     | 145.094    | 330.76     | 584.569     | 1038.718    | 3940.958    | 8683.307    | 16853.674   | 26118.586   | 36798.18    | 51102.482   | 68049.178    |
| <i>Quicksort</i>      | 2.132      | 3.994      | 8.788      | 14.288     | 18.977      | 23.661      | 52.62       | 91.082      | 131.531     | 148.987     | 185.526     | 240.117     | 270.273      |
| <i>Heap Sort</i>      | 3.938      | 14.024     | 29.678     | 49.135     | 71.095      | 83.327      | 174.13      | 309.035     | 428.624     | 495.514     | 612.139     | 708.832     | 836.248      |
| <i>Bucket Sort</i>    | 1.598      | 4.179      | 10.328     | 16.611     | 22.959      | 47.141      | 76.723      | 150.642     | 242.875     | 371.101     | 519.634     | 703.357     | 1007.795     |
| <i>Introsort</i>      | 1.674      | 5.043      | 11.098     | 20.134     | 23.068      | 33.364      | 67.835      | 103.779     | 136.952     | 166.592     | 203.662     | 233.689     | 279.067      |

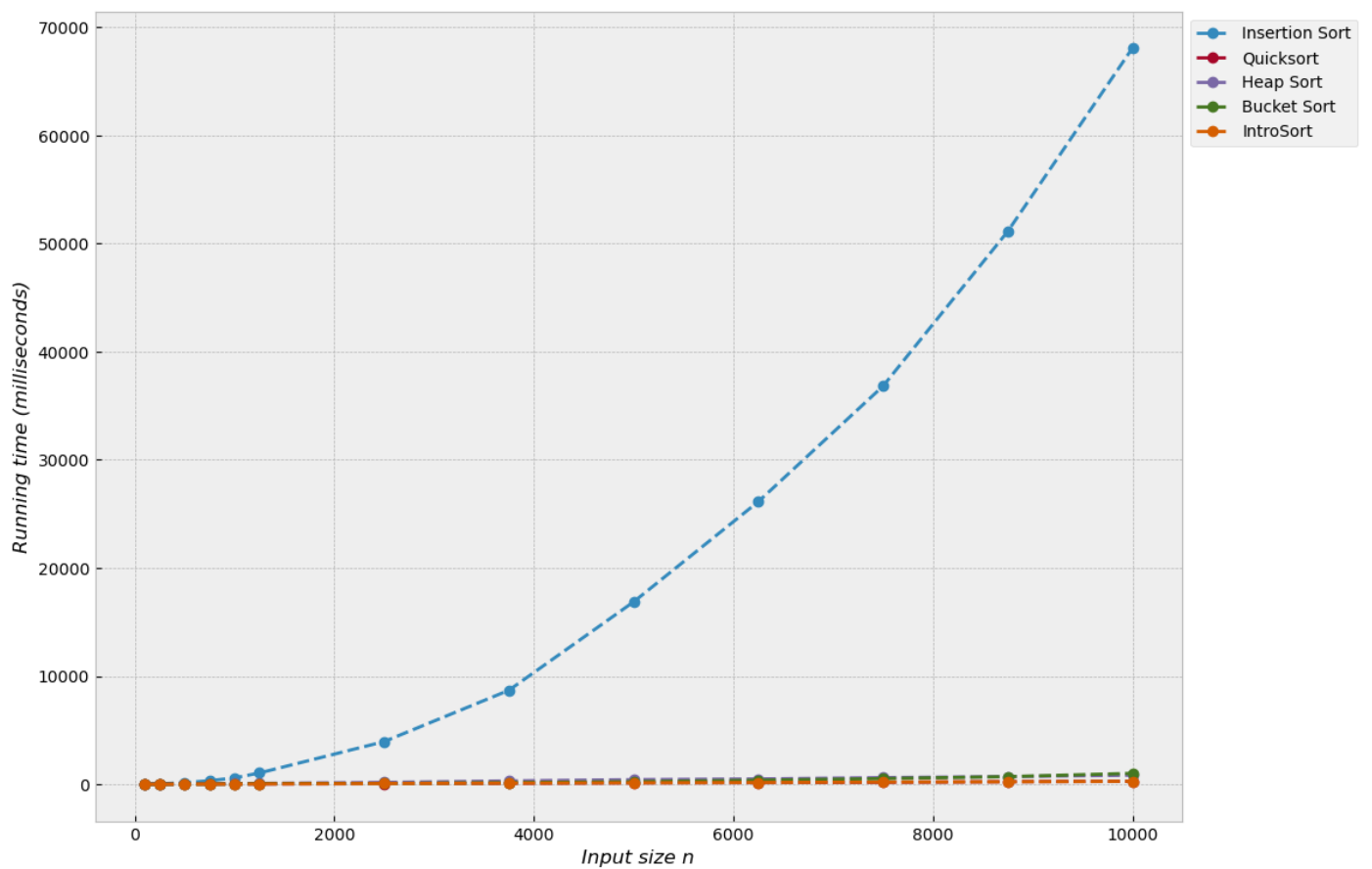
*Figure 1 Running time benchmark (the average of 10 repeated runs)*



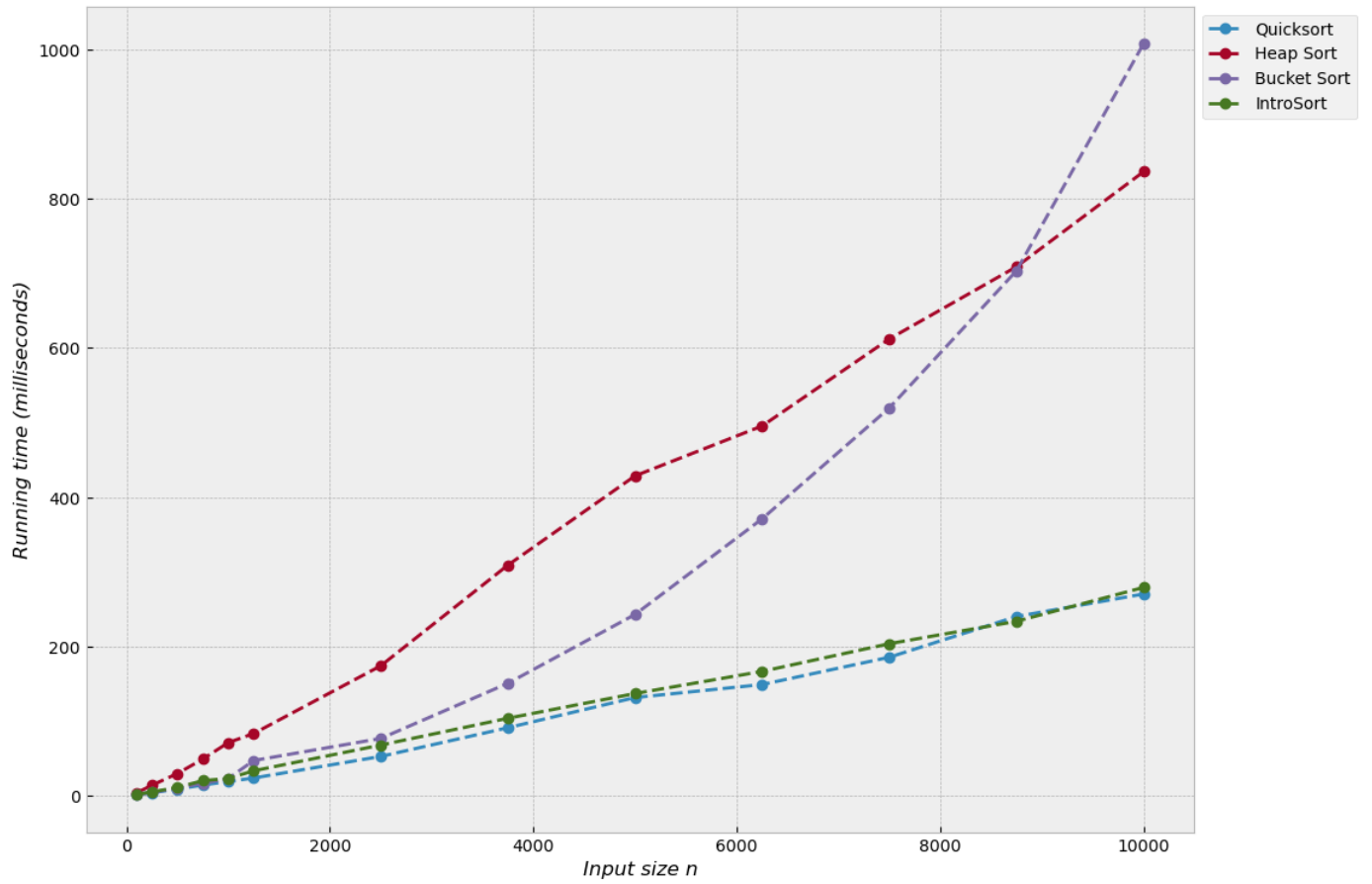
## Big O Notation



## Sorting Benchmark



### Sorting Benchmark



### Big O Notation



## IV. References

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