Comparing Images Using Color Coherence Vectors

Greg Pass

Ramin Zabih*

Justin Miller

Computer Science Department
Cornell University
Ithaca, NY 14853
gregpass,rdz,jmiller@cs.cornell.edu
http://www.cs.cornell.edu/home/rdz/ccv.html

Abstract

Color histograms are used to compare images in many applications. Their advantages are efficiency, and insensitivity to small changes in camera viewpoint. However, color histograms lack spatial information, so images with very different appearances can have similar histograms. For example, a picture of fall foliage might contain a large number of scattered red pixels; this could have a similar color histogram to a picture with a single large red object. We describe a histogram-based method for comparing images that incorporates spatial information. We classify each pixel in a given color bucket as either coherent or incoherent, based on whether or not it is part of a large similarly-colored region. A color coherence vector (CCV) stores the number of coherent versus incoherent pixels with each color. By separating coherent pixels from incoherent pixels, CCV's provide finer distinctions than color histograms. CCV's can be computed at over 5 images per second on a standard workstation. A database with 15,000 images can be queried for the images with the most similar CCV's in under 2 seconds. We show that CCV's can give superior results to color histograms for image retrieval.

KEYWORDS: Content-based Image Retrieval, Processing, Color Histograms

INTRODUCTION

Many applications require simple methods for comparing pairs of images based on their overall appearance. For example, a user may wish to retrieve all images similar to a given image from a large database of images. Color histograms are a popular solution to this problem, and are used in systems like QBIC [4] and Chabot [11]. Color histograms are computationally efficient, and generally insensitive to small changes in camera position.

Color histograms also have some limitations. A color histogram provides no spatial information; it merely describes which colors are present in the image, and in what quantities. In addition, color histograms are sensitive to both compression artifacts and changes in overall image brightness.

In this paper we describe a color-based method for comparing images which is similar to color histograms, but which also takes spatial information into account. We begin with a

^{*}To whom correspondence should be addressed

review of color histograms. We then describe color coherence vectors (CCV's) and how to compare them. Examples of CCV-based image queries demonstrate that they can give superior results to color histograms. We contrast our method with some recent algorithms [8, 14, 15, 17] that also combine spatial information with color histograms. Finally, we present some possible extensions to CCV's.

COLOR HISTOGRAMS

Color histograms are frequently used to compare images. Examples of their use in multimedia applications include scene break detection [1, 7, 10, 12, 22] and querying a database of images [3, 4, 11, 13]. Their popularity stems from several factors.

- Color histograms are computationally trivial to compute.
- Small changes in camera viewpoint tend not to effect color histograms.
- Different objects often have distinctive color histograms.

Researchers in computer vision have also investigated color histograms. For example, Swain and Ballard [19] describe the use of color histograms for identifying objects. Hafner et al. [6] provide an efficient method for weighted-distance indexing of color histograms. Stricker and Swain [18] analyze the information capacity of color histograms, as well as their sensitivity.

Definitions

We will assume that all images are scaled to contain the same number of pixels M. We discretize the colorspace of the image such that there are n distinct (discretized) colors. A

color histogram H is a vector $\langle h_1, h_2, \ldots, h_n \rangle$, in which each bucket h_j contains the number of pixels of color j in the image. Typically images are represented in the RGB colorspace, and a few of the most significant bits are used from each color channel. For example, Zhang [22] uses the 2 most significant bits of each color channel, for a total of n=64 buckets in the histogram.

For a given image I, the color histogram H_I is a compact summary of the image. A database of images can be queried to find the most similar image to I, and can return the image I' with the most similar color histogram $H_{I'}$. Typically color histograms are compared using the sum of squared differences (L_2 -distance) or the sum of absolute value of differences (L_1 -distance). So the most similar image to I would be the image I' minimizing

$$||H_I - H_{I'}|| = \sum_{j=1}^n (H_I[j] - H_{I'}[j])^2,$$

for the L_2 -distance, or

$$|H_I - H_{I'}| = \sum_{j=1}^n |H_I[j] - H_{I'}[j]|,$$

for the L_1 -distance. Note that we are assuming that differences are weighted evenly across different color buckets for simplicity.

COLOR COHERENCE VECTORS

Intuitively, we define a color's *coherence* as the degree to which pixels of that color are members of large similarly-colored regions. We refer to these significant regions as *coherent regions*, and observe that they are of significant importance in characterizing images.



Figure 1: Two images with similar color histograms

For example, the images shown in figure 1 have similar color histograms, despite their rather different appearances.¹ The color red appears in both images in approximately the same quantities. In the left image the red pixels (from the flowers) are widely scattered, while in the right image the red pixels (from the golfer's shirt) form a single coherent region.

Our coherence measure classifies pixels as either coherent or incoherent. Coherent pixels are a part of some sizable contiguous region, while incoherent pixels are not. A color coherence vector represents this classification for each color in the image. CCV's prevent coherent pixels in one image from matching incoherent pixels in another. This allows fine distinctions that cannot be made with color histograms.

Computing CCV's

The initial stage in computing a CCV is similar to the computation of a color histogram. We first blur the image slightly by replacing

pixel values with the average value in a small local neighborhood (currently including the 8 adjacent pixels). This eliminates small variations between neighboring pixels. We then discretize the colorspace, such that there are only n distinct colors in the image.

The next step is to classify the pixels within a given color bucket as either coherent or incoherent. A coherent pixel is part of a large group of pixels of the same color, while an incoherent pixel is not. We determine the pixel groups by computing connected components. A connected component C is a maximal set of pixels such that for any two pixels $p, p' \in C$, there is a path in C between p and p'. (Formally, a path in C is a sequence of pixels $p = p_1, p_2, \dots, p_n = p'$ such that each pixel p_i is in C and any two sequential pixels p_i, p_{i+1} are adjacent to each other. We consider two pixels to be adjacent if one pixel is among the eight closest neighbors of the other; in other words, we include diagonal neighbors.) Note that we only compute connected components within a given discretized color bucket. This effectively segments the image based on the discretized colorspace.

Connected components can be computed in

 $^{^1{\}rm The~color~images}$ used in this paper can be found at http://www.cs.cornell.edu/home/rdz/ccv.html.

linear time (see, for example, [20]). When this is complete, each pixel will belong to exactly one connected component. We classify pixels as either coherent or incoherent depending on the size in pixels of its connected component. A pixel is coherent if the size of its connected component exceeds a fixed value τ ; otherwise, the pixel is incoherent.

For a given discretized color, some of the pixels with that color will be coherent and some will be incoherent. Let us call the number of coherent pixels of the j'th discretized color α_j and the number of incoherent pixels β_j . Clearly, the total number of pixels with that color is $\alpha_j + \beta_j$, and so a color histogram would summarize an image as

$$\langle \alpha_1 + \beta_1, \dots, \alpha_n + \beta_n \rangle$$
.

Instead, for each color we compute the pair

$$(\alpha_i, \beta_i)$$

which we will call the *coherence pair* for the j'th color. The *color coherence vector* for the image consists of

$$\langle (\alpha_1, \beta_1), \ldots, (\alpha_n, \beta_n) \rangle$$
.

This is a vector of coherence pairs, one for each discretized color.

In our experiments, all images were scaled to contain M=38,976 pixels, and we have used $\tau=300$ pixels (so a region is classified as coherent if its area is about 1% of the image). With this value of τ , an average image in our database consists of approximately 75% coherent pixels.

An example CCV

We next demonstrate the computation of a CCV. To keep our example small, we will let $\tau=4$ and assume that we are dealing with an image in which all 3 color components have

the same value at every pixel (in the RGB colorspace this would represent a grayscale image). This allows us to represent a pixel's color with a single number (i.e., the pixel with R/G/B values 12/12/12 will be written as 12).

Suppose that after we slightly blur the input image, the resulting intensities are as follows.

22	10	21	22	15	16
24	21	13	20	14	17
23	17	38	23	17	16
25	25	22	14	15	21
27	22	12	11	21	20
24	21	10	12	22	23

Let us discretize the colorspace so that bucket 1 contains intensities 10 through 19, bucket 2 contains 20 through 29, etc. Then after discretization we obtain

2	1	2	2	1	1
2	2	1	2	1	1
2	1	3	2	1	1
2	2	2	1	1	2
2	2	1	1	2	2
2	2	1	1	2	2

The next step is to compute the connected components. Individual components will be labeled with letters (A,B,\ldots) and we will need to keep a table which maintains the discretized color associated with each label, along with the number of pixels with that label. Of course, the same discretized color can be associated with different labels if multiple contiguous regions of the same color exist. The image may then become

and the connected components table will be

Label	A	B	C	D	E
Color	1	2	1	3	1
Size	12	15	3	1	5

The components A, B, and E have more than τ pixels, and the components C and D less than τ pixels. Therefore the pixels in A, B and E are classified as coherent, while the pixels in C and D are classified as incoherent.

The CCV for this image will be

Color	1	2	3
α	17	15	0
β	3	0	1

A given color bucket may thus contain only coherent pixels (as does 2), only incoherent pixels (as does 3), or a mixture of coherent and incoherent pixels (as does 1). If we assume there are only 3 possible discretized colors, the CCV can also be written

$$\langle (17,3), (15,0), (0,1) \rangle$$
.

Comparing CCV's

Consider two images I and I', together with their CCV's G_I and $G_{I'}$, and let the number of coherent pixels in color bucket j be α_j (for I) and α'_j (for I'). Similarly, let the number of incoherent pixels be β_j and β'_j . So

$$G_I = \langle (\alpha_1, \beta_1), \dots, (\alpha_n, \beta_n) \rangle$$

and

$$G_{I'} = \langle (\alpha'_1, \beta'_1), \dots, (\alpha'_n, \beta'_n) \rangle$$

Color histograms will compute the difference between I and I' as

$$\Delta_H = \sum_{j=1}^n \left| (\alpha_j + \beta_j) - (\alpha'_j + \beta'_j) \right|. \quad (1)$$

Our method for comparing is based on the quantity

$$\Delta_G = \sum_{j=1}^n \left| (\alpha_j - \alpha'_j) \right| + \left| (\beta_j - \beta'_j) \right|. \quad (2)$$

From equations 1 and 2, it follows that CCV's create a finer distinction than color histograms. A given color bucket j can contain the same number of pixels in I as in I', i.e.

$$\alpha_i + \beta_i = \alpha'_i + \beta'_i$$

but these pixels may be entirely coherent in I and entirely incoherent in I'. In this case $\beta_j = \alpha'_j = 0$, and while $\Delta_H = 0$, Δ_G will be large.

In general, $\Delta_H \leq \Delta_G$. This is true even if we use squared differences instead of absolute differences in the definitions of Δ_H and Δ_G . This is because both d(x) = |x| and $d(x) = x^2$ are metrics, so they satisfy the triangle inequality

$$d(x+y) \le d(x) + d(y). \tag{3}$$

If we rearrange the terms in equation 1 we get

$$\Delta_H = \sum_{j=1}^n \left| (\alpha_j - \alpha'_j) + (\beta_j - \beta'_j) \right|.$$

Applying the triangle inequality we have

$$\Delta_H \leq \sum_{j=1}^n \left| (\alpha_j - \alpha'_j) \right| + \left| (\beta_j - \beta'_j) \right| = \Delta_G.$$

EXPERIMENTAL RESULTS

We have implemented color coherence vectors, and have used them for image retrieval from a large database. Our database consists of 14,554 images, which are drawn from a variety of sources. Our largest sources include the 11,667 images used in Chabot [11], the 1,440 images used in QBIC [4], and a 1,005 image database available from Corel. In addition, we included a few groups of images in PhotoCD format. Finally, we have taken a number of MPEG videos from the Web and segmented

them into scenes using the method described in [21]. We have added one or two images from each scene to the database, totaling 349 images. The image database thus contains a wide variety of imagery. In addition, some of the imagery has undergone substantial lossy compression via JPEG or MPEG.

We have compared our results with a number of color histogram variations. These include the L_1 and L_2 distances, with both 64 and 512 color buckets. In addition, we have implemented Swain's opponent axis colorspace [19], and used the color discretization scheme he describes. In each case we include a small amount of smoothing as it improves the performance of color histograms. On our database, the L_1 distance with the 64-bucket RGB colorspace gave the best results, and is used as a benchmark against CCV's.

Hand examination of our database revealed 52 pairs of images which contain different views of the same scene. Examples are shown in figures 3 and 4. One image is selected as a query image, and the other represents a "correct" answer. In each case, we have shown where the second image ranks, when similarity is computed using color histograms versus CCV's. The color images shown are available at http://www.cs.cornell.edu/home/rdz/ccv.html

In 46 of the 52 cases, CCV's produced better results, while in 6 cases they produced worse results. The average change in rank due to CCV's was an improvement of just over 75 positions (note that this included the 6 cases where CCV's do worse). The average percentage change in rank was an improvement of 30%. In the 46 cases where CCV's performed better than color histograms, the average improvement in rank was 88 positions, and the average percentage improvement was 50%. In the 6 cases where color histograms performed better than CCV's, the average rank improvement was 21 positions, and the average per-

centage improvement was 48%. A histogram of the change in rank obtained by using CCV's is shown in figure 2.

When CCV's produced worse results, it was always due to a change in overall image brightness (i.e., the two images were almost identical, except that one was brighter than the other). Because CCV's use discretized color buckets for segmentation, they are more sensitive to changes in overall image brightness than color histograms. We believe that this difficulty can be overcome by using a better colorspace than RGB, as we discuss in the extensions section of this paper.

Efficiency

There are two phases to the computation involved in querying an image database. First, when an image is inserted into the database, a CCV must be computed. Second, when the database is queried, some number of the most similar images must be retrieved. Most methods for content-based indexing include these distinct phases. For both color histograms and CCV's, these phases can be implemented in linear time.

We ran our experiments on a 50 MHz SPARCstation 20, and provide the results from color histogramming for comparison. Color histograms can be computed at 67 images per second, while CCV's can be computed at 5 images per second. Using color histograms, 21,940 comparisons can be performed per second, while with CCV's 7,746 can be performed per second. The images used for benchmarking are 232×168 . Both implementations are preliminary, and the performance can definitely be improved.

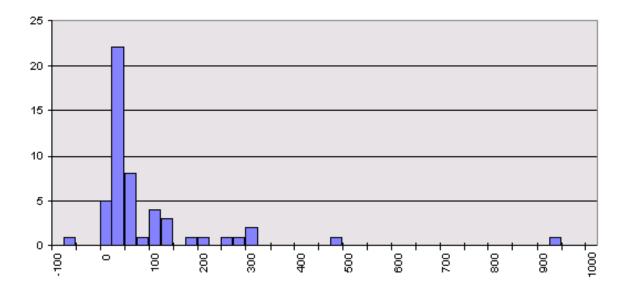


Figure 2: Change in rank due to CCV's. Positive numbers indicate improved performance.

RELATED WORK

Recently, several authors have proposed algorithms for comparing images that combine spatial information with color histograms. Hsu et al. [8] attempts to capture the spatial arrangement of the different colors in the image, in order to perform more accurate content-based image retrieval. Rickman and Stonham [14] randomly sample the endpoints of small triangles and compare the distributions of these triplets. Smith and Chang [15] concentrate on queries that combine spatial information with color. Stricker and Dimai [17] divide the image into five partially overlapping regions and compute the first three moments of the color distributions in each image. We will discuss each approach in turn.

Hsu [8] begins by selecting a set of representative colors from the image. Next, the image is partitioned into rectangular regions, where each region is predominantly a single

color. The partitioning algorithm makes use of maximum entropy. The similarity between two images is the degree of overlap between regions of the same color. Hsu presents results from querying a database with 260 images, which show that the integrated approach can give better results than color histograms.

While the authors do not report running times, it appears that Hsu's method requires substantially more computation than the approach we describe. A CCV can be computed in a single pass over the image, with a small number of operations per pixel. Hsu's partitioning algorithm in particular appears much more computationally intensive than our method. Hsu's approach can be extended to be independent of orientation and position, but the computation involved is quite substantial. In contrast, our method is naturally invariant to orientation and position.

Rickman and Stonham [14] randomly sample pixel triples arranged in an equilateral tri-

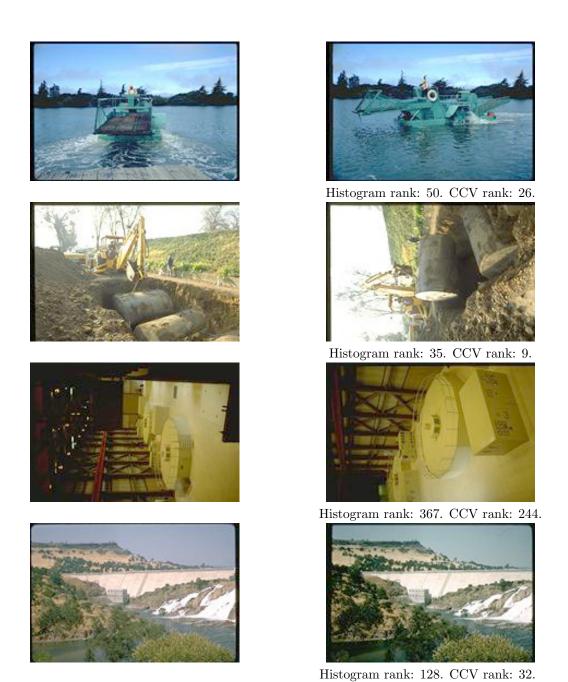


Figure 3: Example queries with their partner images











Histogram rank: 310. CCV rank: 205.



Histogram rank: 88. CCV rank: 38.



Histogram rank: 13. CCV rank: 5.



Histogram rank: 119. CCV rank: 43.

Figure 4: Additional examples

angle with a fixed side length. They use 16 levels of color hue, with non-uniform quantization. Approximately a quarter of the pixels are selected for sampling, and their method stores 372 bits per image. They report results from a database of 100 images.

Smith and Chang's algorithm also partitions the image into regions, but their approach is more elaborate than Hsu's. They allow a region to contain multiple different colors, and permit a given pixel to belong to several different regions. Their computation makes use of histogram back-projection [19] to back-project sets of colors onto the image. They then identify color sets with large connected components.

Smith and Chang's image database contains 3,100 images. Again, running times are not reported, although their algorithm does speed up back-projection queries by pre-computing the back-projections of certain color sets. Their algorithm can also handle certain kinds of queries that our work does not address; for example, they can find all the images where the sun is setting in the upper left part of the image.

Stricker and Dimai [17] compute moments for each channel in the HSV colorspace, where pixels close to the border have less weight. They store 45 floating point numbers per image. Their distance measure for two regions is a weighted sum of the differences in each of the three moments. The distance measure for a pair of images is the sum of the distance between the center regions, plus (for each of the 4 side regions) the minimum distance of that region to the corresponding region in the other image, when rotated by 0, 90, 180 or 270 degrees. Because the regions overlap, their method is insensitive to small rotations or translations. Because they explicitly handle rotations of 0, 90, 180 or 270 degrees, their method is not affected by these particular rotations. Their database contains over 11,000 images, but the performance of their method is only illustrated on 3 example queries. Like Smith and Chang, their method is designed to handle certain kinds of more complex queries that we do not consider.

EXTENSIONS

There are a number of ways in which our algorithm could be extended and improved. One extension involves generalizing CCV's, while another centers on improving the choice of colorspace.

Histogram refinement and effective feature extraction

Our approach can be generalized to features other than color and coherence. We are investigating histogram refinement, in which the pixels of a given color bucket are subdivided based on particular features (coherence, texture, etc.). CCV's can be viewed as a simple form of histogram refinement, in which histogram buckets are split in two based on coherence.

Histogram refinement also permits further distinctions to be imposed upon a CCV. In the same way that we distinguish between pixels of similar color by coherence, for example, we can distinguish between pixels of similar coherence by some additional feature. We can apply this method repeatedly; each split imposes an additional constraint on what it means for two pixels to be similar. If the initial histogram is a color histogram, and it is only refined once based on coherence, then the resulting refined histogram is a CCV. But there is no requirement that the initial histogram be based on color, or that the initial split be based on coherence.

Consider the example shown in figure 5. We begin with a color histogram and divide the

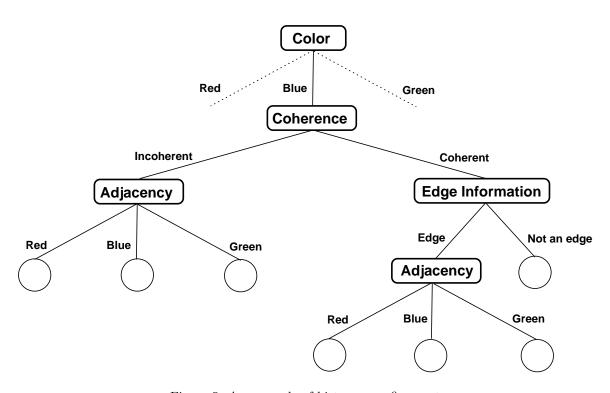


Figure 5: An example of histogram refinement.

pixels in each bucket based on coherence (i.e., generate a CCV). The incoherent pixels can be refined by tallying the colors of pixels adjacent to the incoherent pixels in a particular bin. The coherent pixels, in turn, can be further refined into those that lie on edges and those which do not. The coherent pixels on edges can then be further refined by recording what colors the coherent regions are adjacent to. The leaves of the tree, therefore, represent those images that satisfy these successive constraints. This set of refinements defines a compact summary of the image, and remains an efficient structure to compute and compare.

The best system of constraints to impose on the image is an open issue. Any combination of features might give effective results, and there are many possible features to choose from. However, it is possible to take advantage of the temporal structure of a successively refined histogram. One feature might serve as a filter for another feature, by ensuring that the second feature is only computed on pixels which already possess the first feature.

For example, the perimeter-to-area ratio can be used to classify the relative shapes of color regions. If we used this ratio as an initial refinement on color histograms, incoherent pixels would result in statistical outliers, and thus give questionable results. This feature is better employed after the coherent pixels have been segregated. We call the choice of a sensible structure of constraints effective feature extraction. Refining a histogram not only makes finer distinctions between pixels, but functions as a statistical filter for successive refinements.

Choice of colorspace

Many systems based on color histograms spend considerable effort on selecting a good set of colors. Hsu [8], for example, assumes that the colors in the center of the image are more important than those at the periphery,

while Smith and Chang [15] use several different thresholds to extract colors and regions. A wide variety of different colorspaces have also been investigated. For example, Swain and Ballard [19] make use of the opponent-axis colorspace, while QBIC [4] uses the Munsell colorspace.

The choice of colorspace is a particularly significant issue for CCV's, since they use the discretized color buckets to segment the image. A perceptually uniform colorspace, such as CIE Lab, should result in better segmentations and improve the performance of CCV's. A related issue is the color constancy problem [9], which causes objects of the same color to appear rather differently depending upon the lighting conditions. The simplest effect of color constancy is a change in overall image brightness, which is responsible for the negative examples obtained in our experiments. Standard histogramming methods are sensitive to image gain. More sophisticated methods, such as cumulative histograms [16] or color ratio histograms [5], might alleviate this problem.

In fact, most proposed improvements to color histograms can also be applied to CCV's. This includes improvements beyond the selection of better colorspaces. For example, some authors [17] suggest that color moments be used in lieu of histograms. Color moments could be computed separately for coherent and incoherent pixels.

CONCLUSIONS

We have described a new method for comparing pairs of images that combines color histograms with spatial information. Most research in content-based image retrieval has focused on query by example (where the system automatically finds images similar to an input image). However, other types of queries are also important. For example, it is often useful

to search for images in which a subset of another image (e.g. a particular object) appears. This would be particularly useful for queries on a database of videos. One approach to this problem might be to generalize histogram back-projection [19] to separate pixels based on spatial coherence.

It is clear that larger and larger image databases will demand more complex similarity measures. This added time complexity can be offset by using efficient, coarse measures that prune the search space by removing images which are clearly not the desired answer. Measures which are less efficient but more effective can then be applied to the remaining images. Baker and Nayar [2] have begun to investigate similar ideas for pattern recognition problems. To effectively handle large image databases will require a balance between increasingly fine measures (such as histogram refinement) and efficient coarse measures.

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