

GRAPH VISUALIZATION

KIRELL BENZI, PH.D.



Inspired by Lex

www.kirellbenzi.com

BIO

- Ph.D. in Data Science from EPFL
- CEO and founder of Kirelion, creative data science studio
- Data visualization lecturer @ EPFL
- Art exhibitions “Singular Networks” running in France, Switzerland, Brazil, etc.



@kirellb



@KirellBenzi

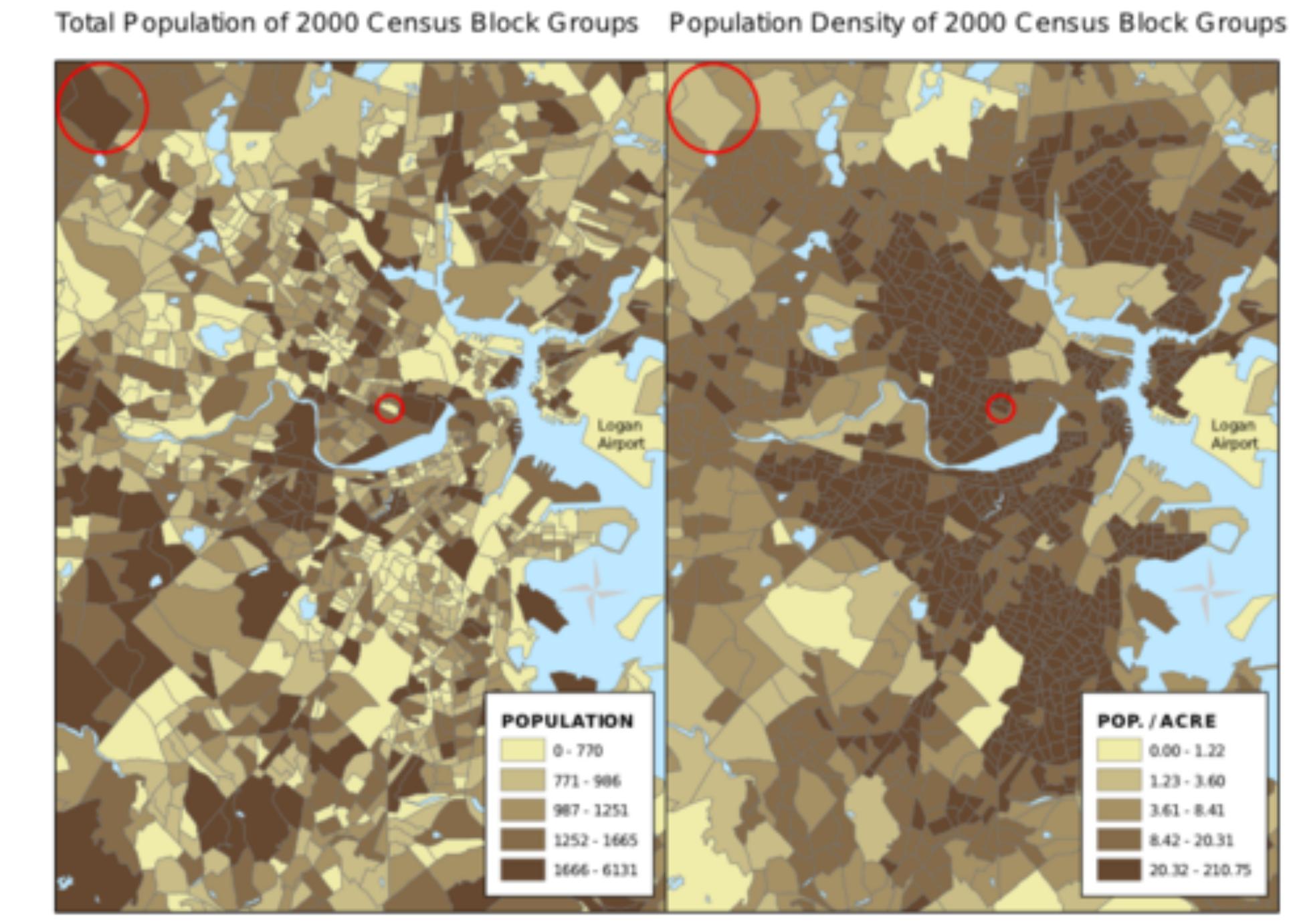
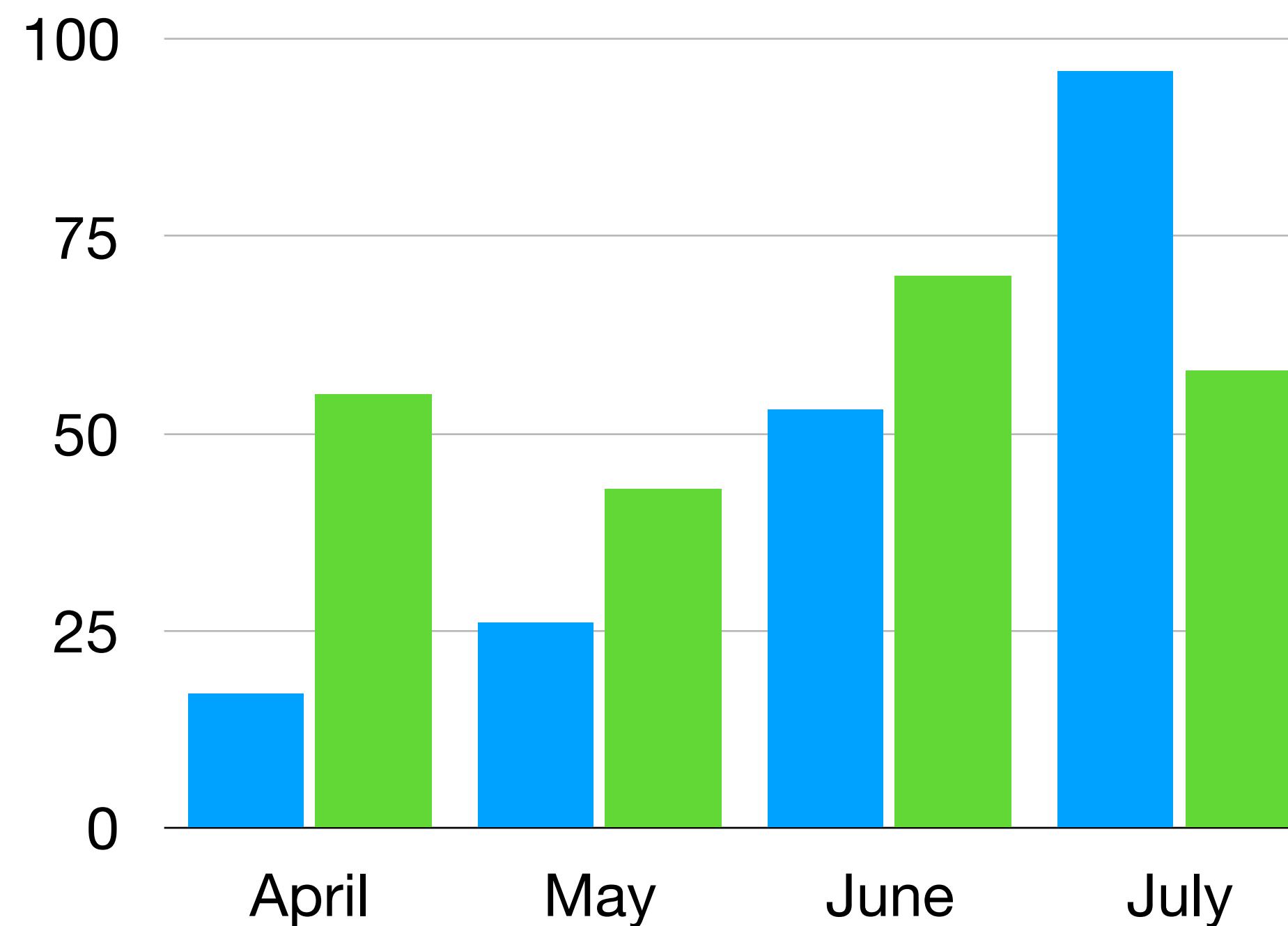


“The purpose of visualization is insight, not pictures.”

–Ben Shneiderman

Defining data visualization

Efficiently communicate information from **statistical** data using visual objects (such as bars, lines, points, etc.)



Wikipedia

Why visualize?

Communication

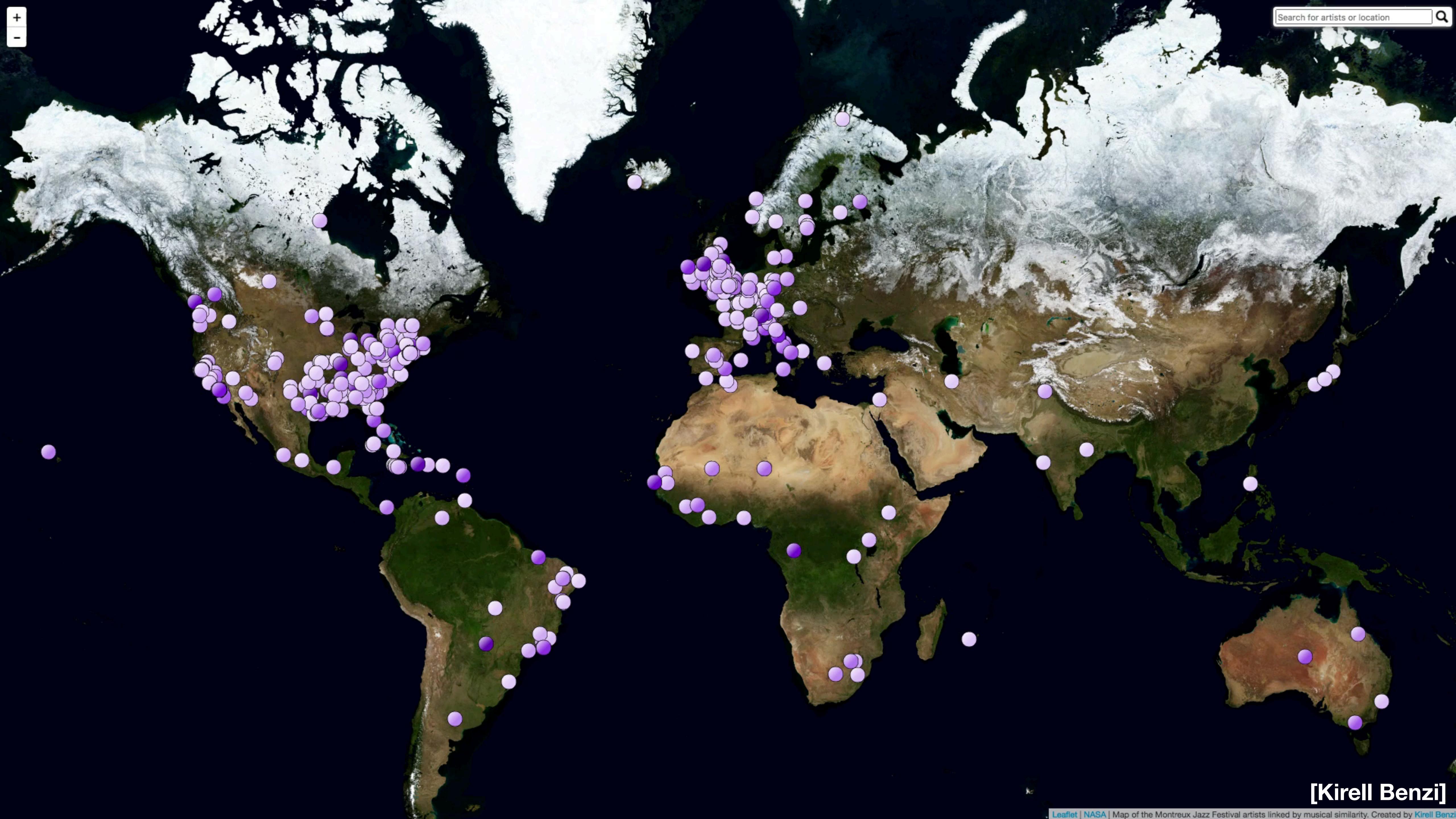
Transmit information to others

Exploration

Reveal previously hidden insights from the data

Cognition

Understand and reason about the data

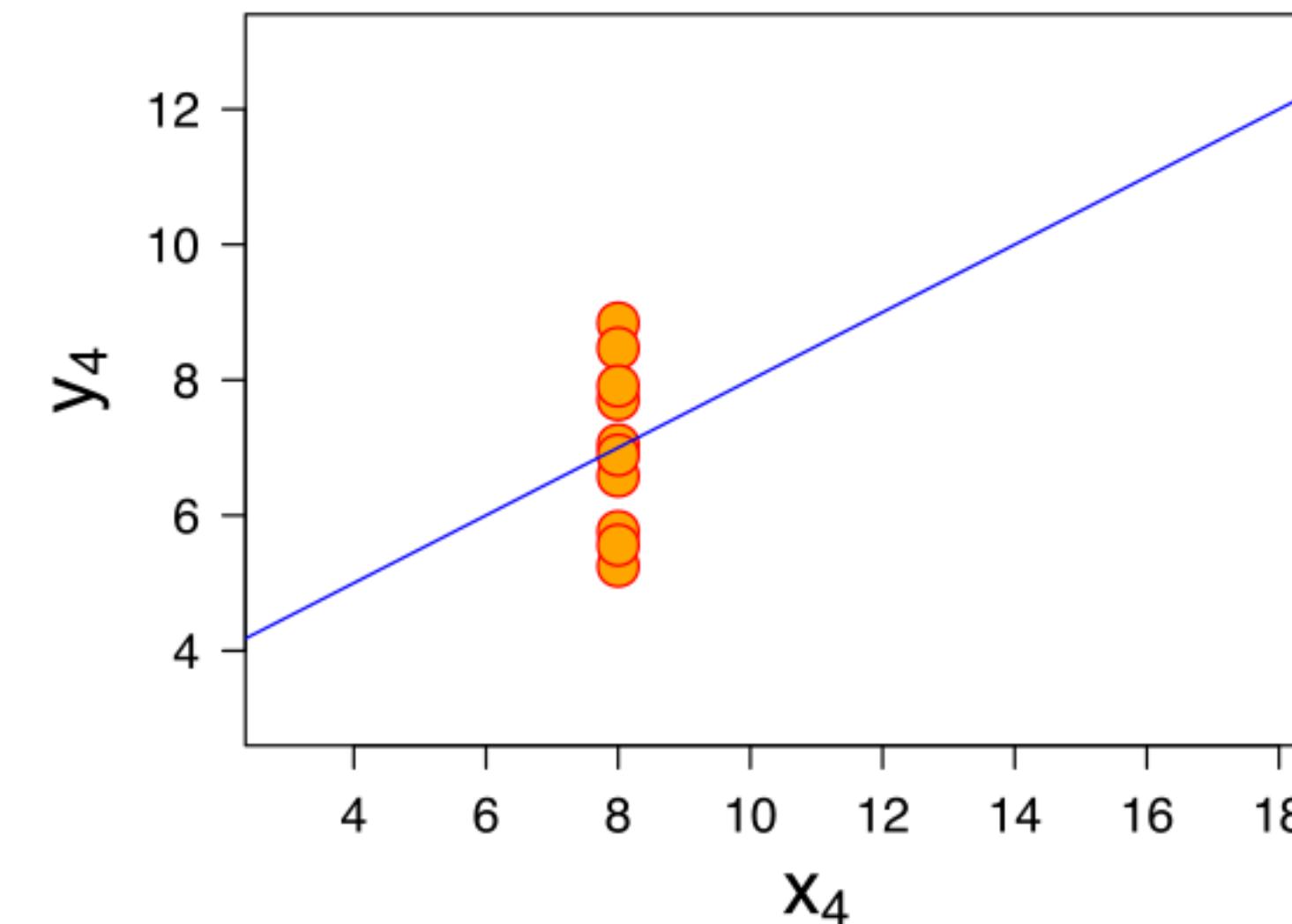
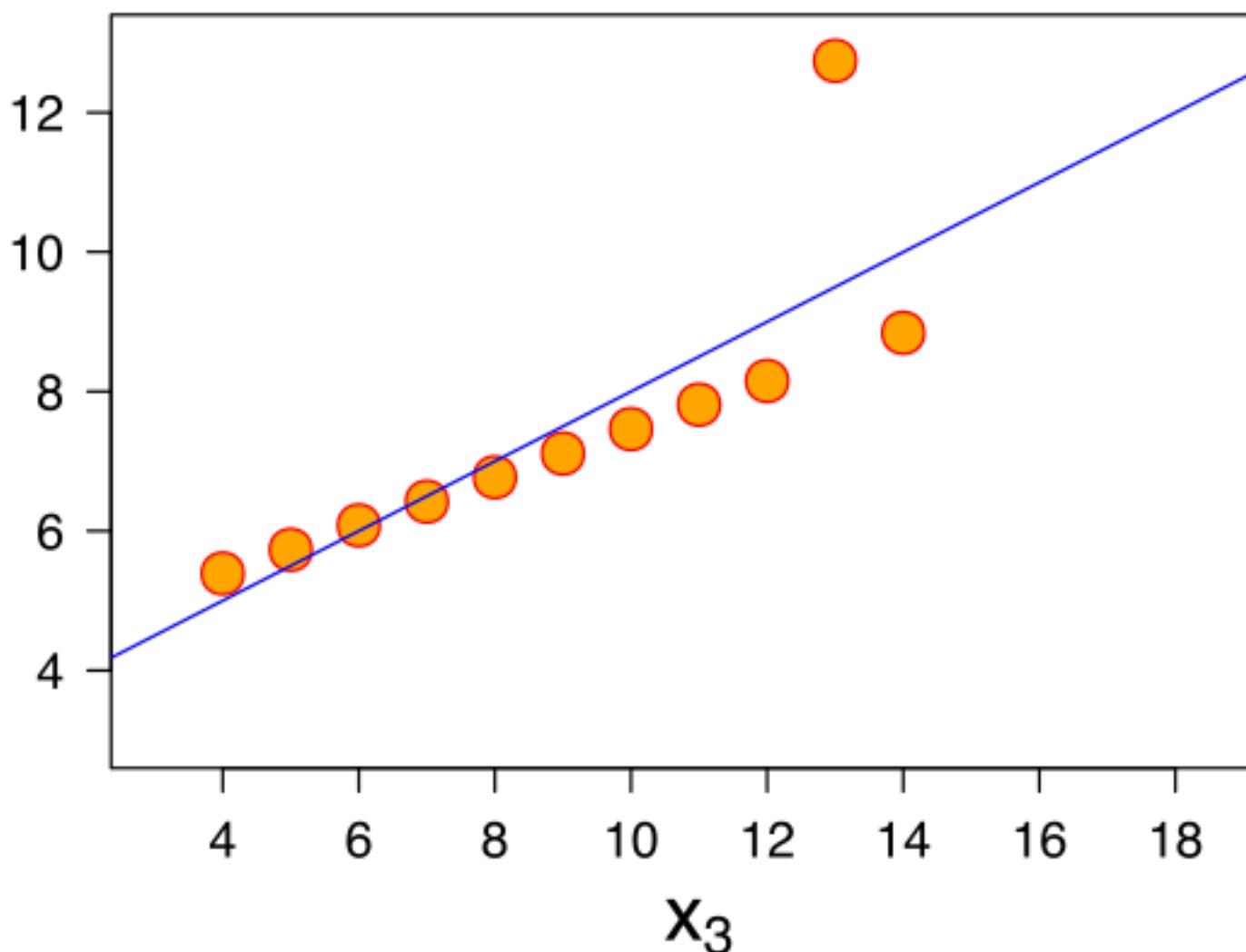
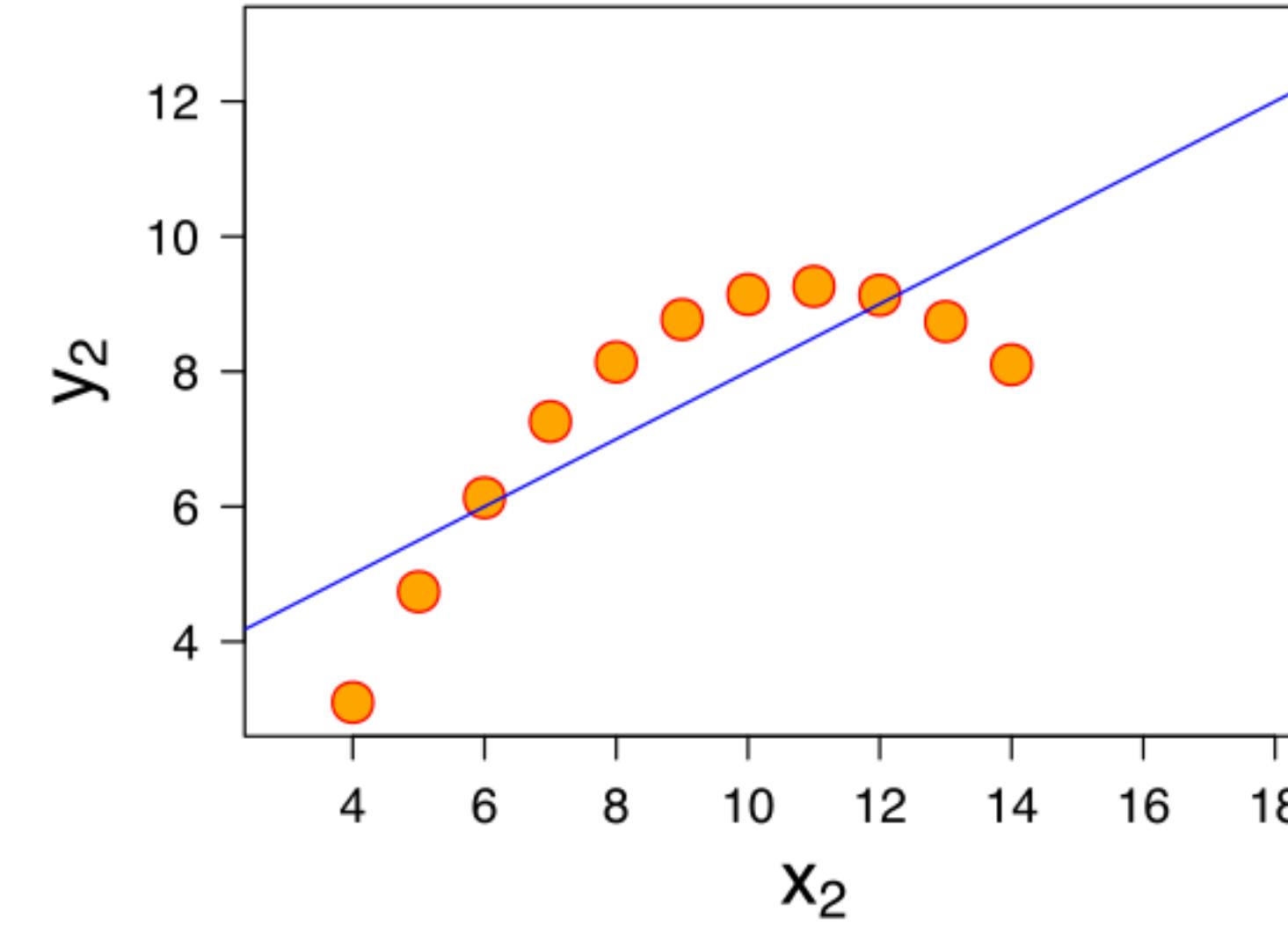
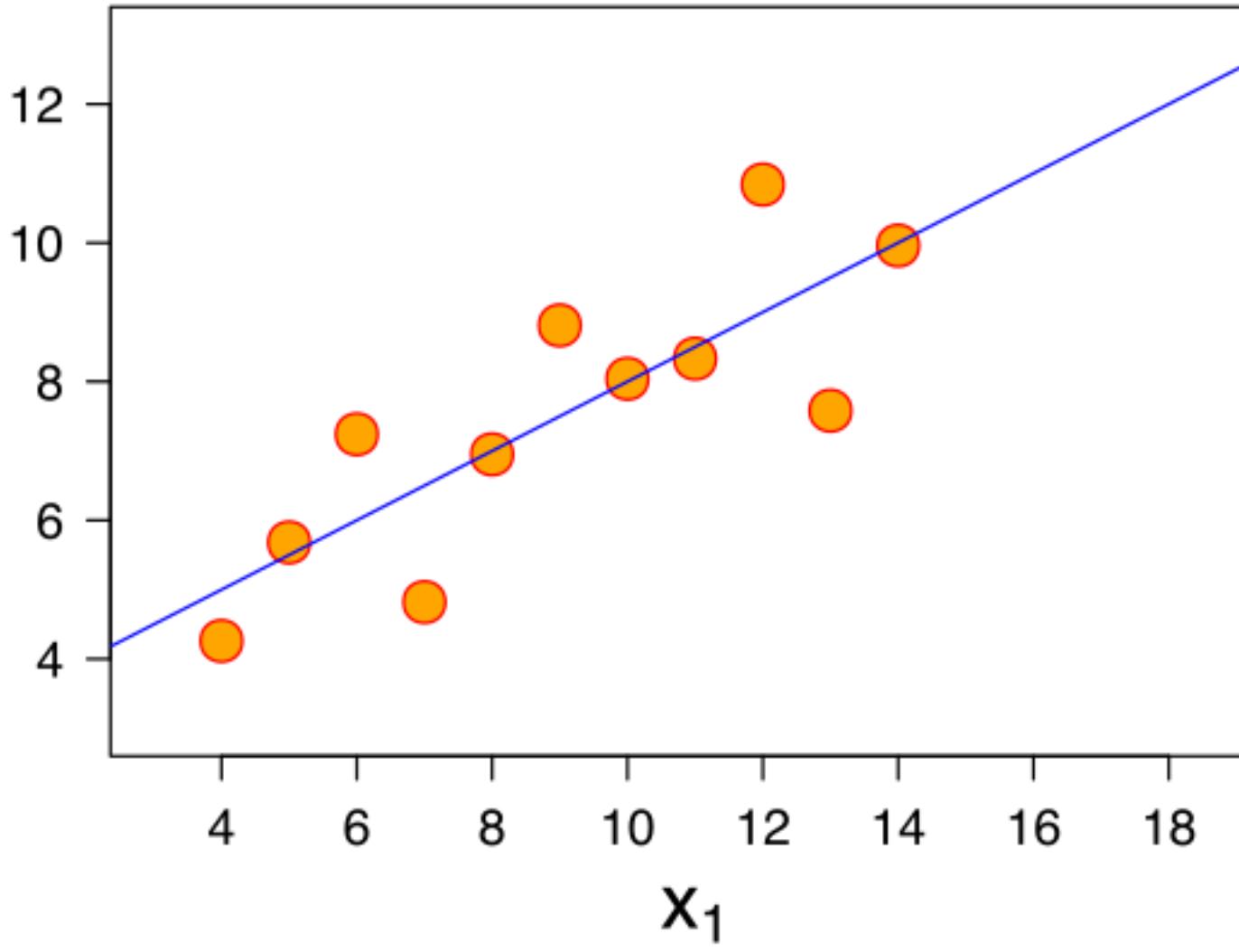


Search for artists or location



[Kirell Benzi]

Why not only use statistics?



Identical statistical properties

Property	
Mean of x	9
Sample variance of x	11
Mean of y	7.50
Sample variance of y	4.125
Correlation between x and y	0.816
Linear regression line	$y = 3.0 + 0.6x$
Coefficient of determination of the linear regression	0.67

[Anscombe's quartet]

Using a graphical representation

Figures are richer; provide more information with less clutter and in less space.

Figures provide the ***gestalt*** effect: they give an overview; make structure more visible.

Figures are more accessible, easier to understand, faster to grasp, more comprehensible, more memorable, more fun, and less formal.



Tor Nørretranders

Alexander Lex

Human visual system

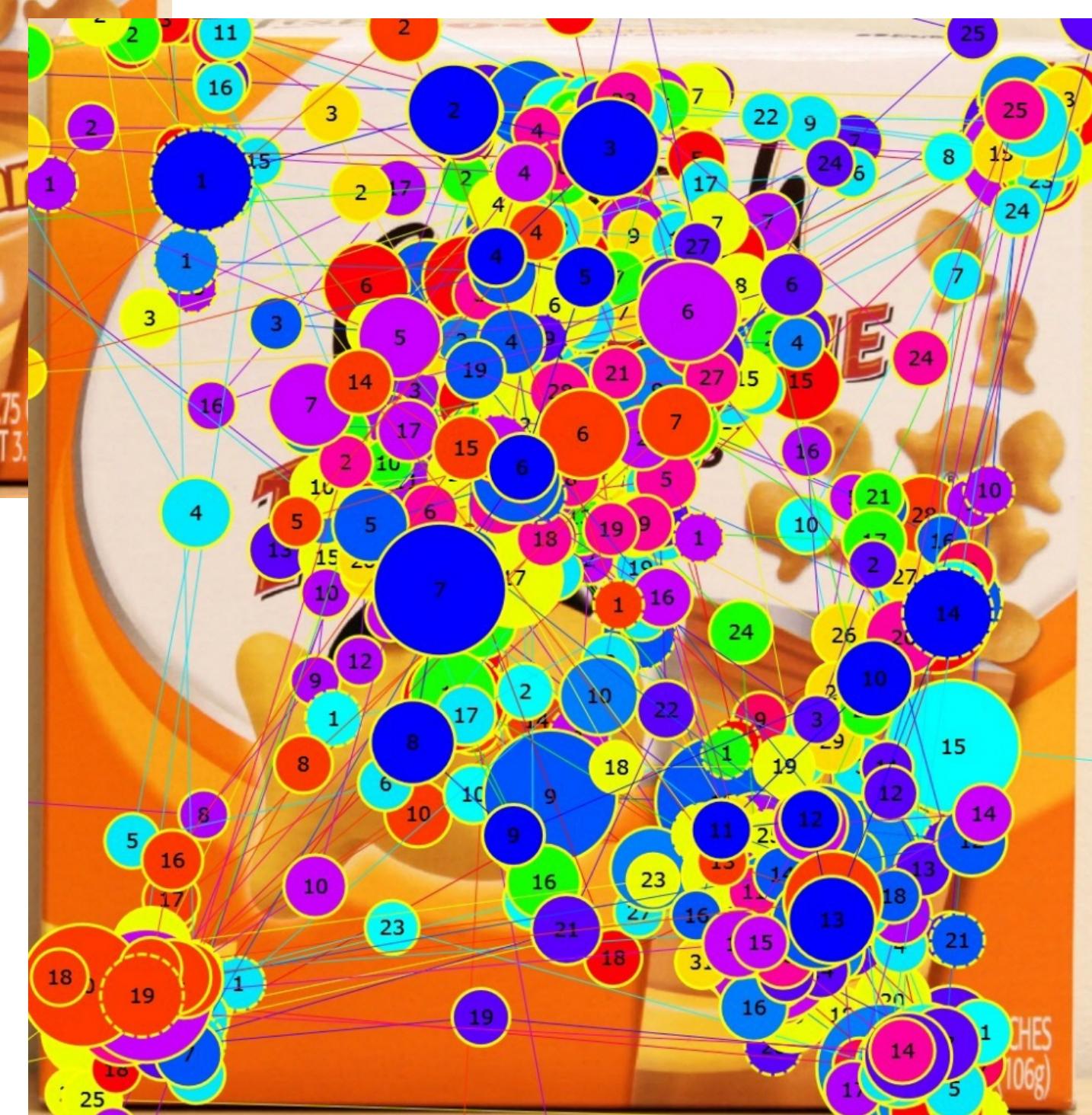
Vision works as a sequence of rapid eye movements: **fixations** and **saccades**

Fixation: maintaining gaze on a location during 200-600 ms

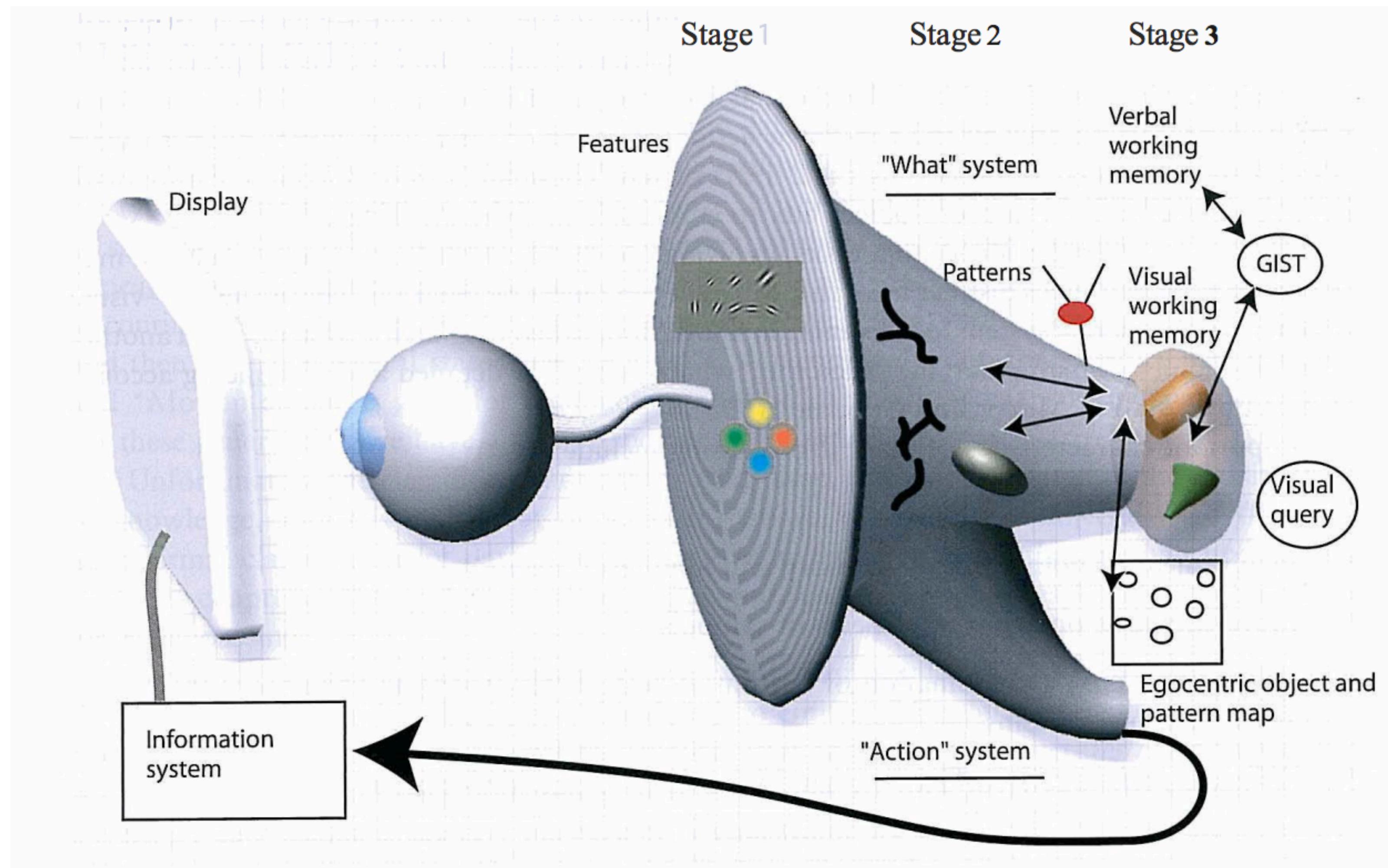
Saccade: quickly switching between different locations 20-100ms



Gaze plot example



Visual information processing model



A three-stage model of human visual information processing.

[Ware]

Visual popout

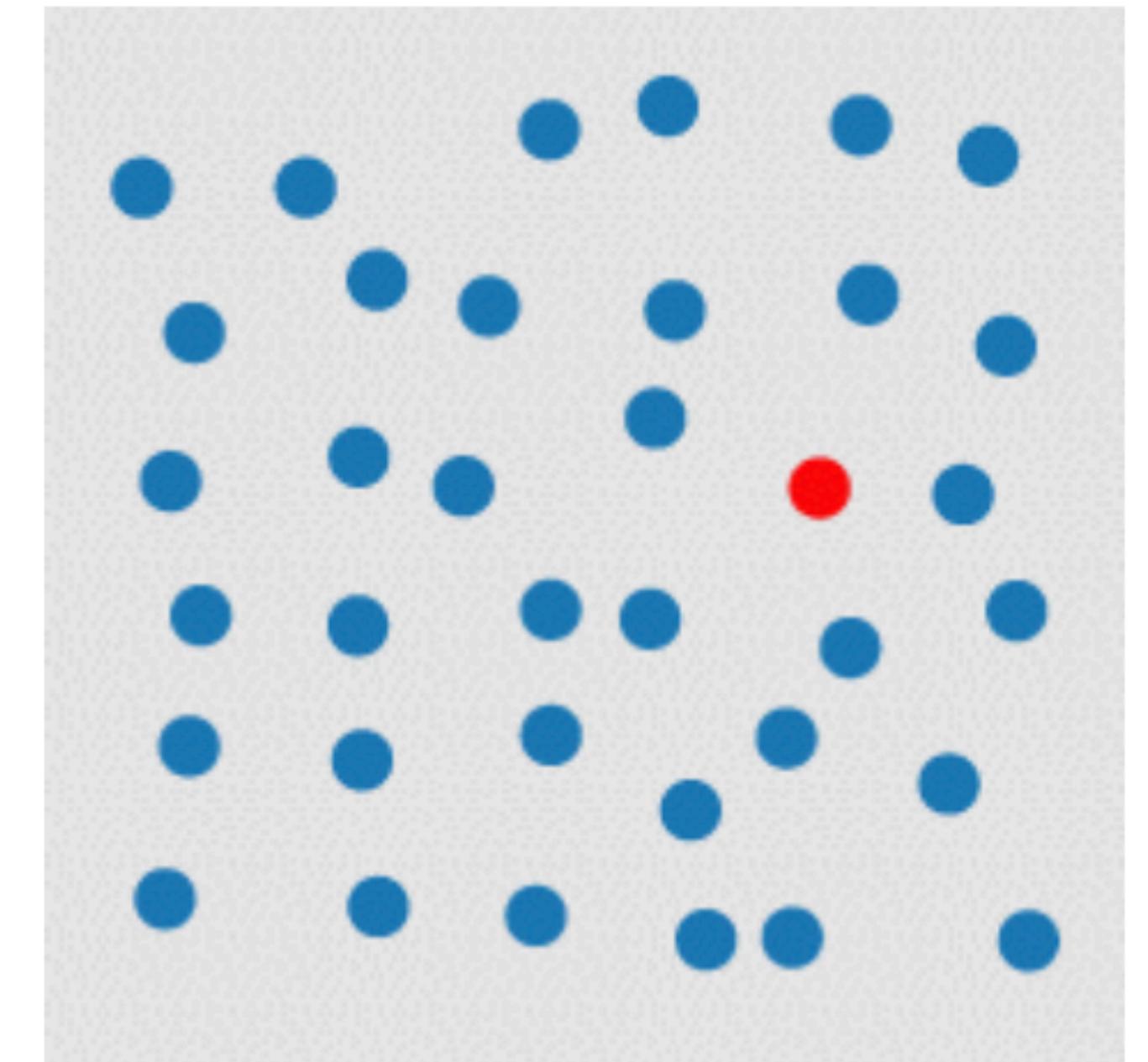
Properties detected by the low-level visual system:

very fast and very accurate (200-250 milliseconds)

processed in parallel

Happens before attention

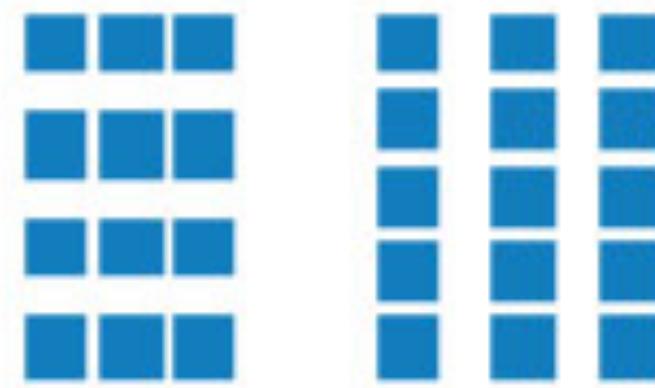
Also called: **preattentive processing features**



Difference in hue

Gestalt effect

PROXIMITY



Most people see rows on the left and columns on the right.

SIMILARITY



Most people see a larger group containing a sub-group.

FIGURE GROUND



Most people first see a vase or a face then flip between the two.

CONTINUATION



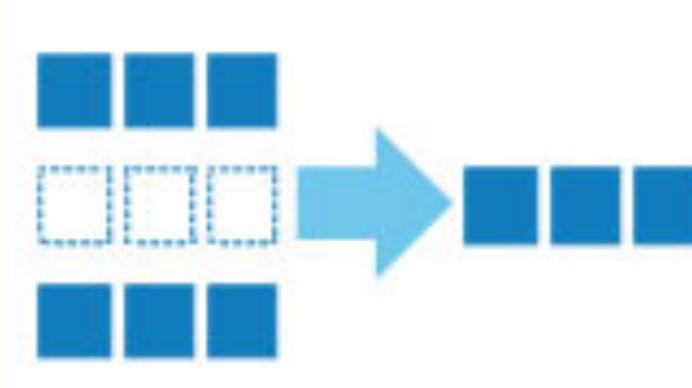
Most people see 2 rows crossing rather than for lines meeting at a single point.

CLOSURE



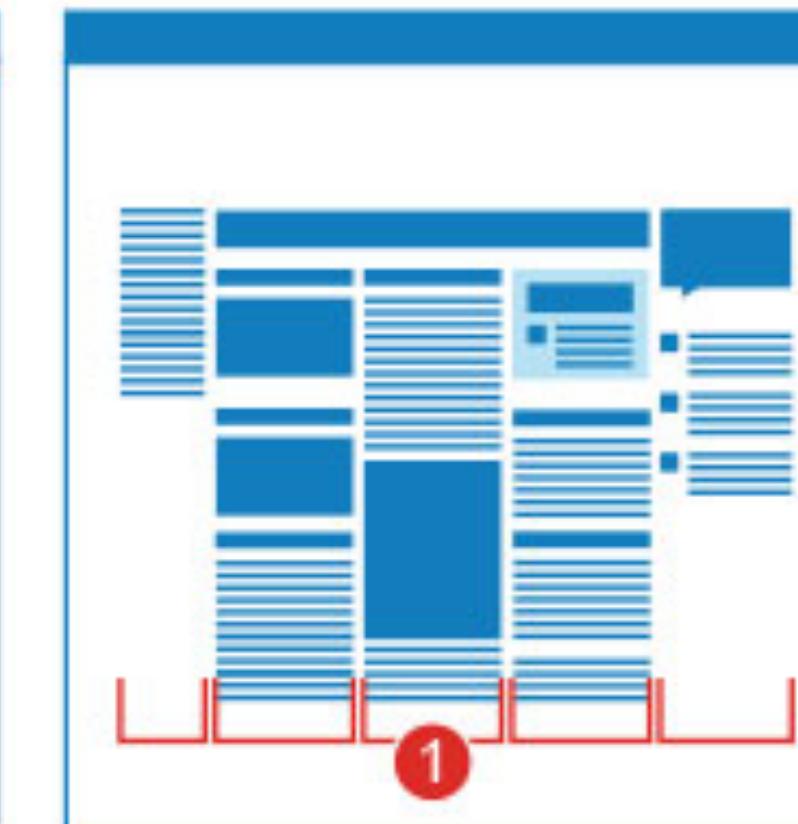
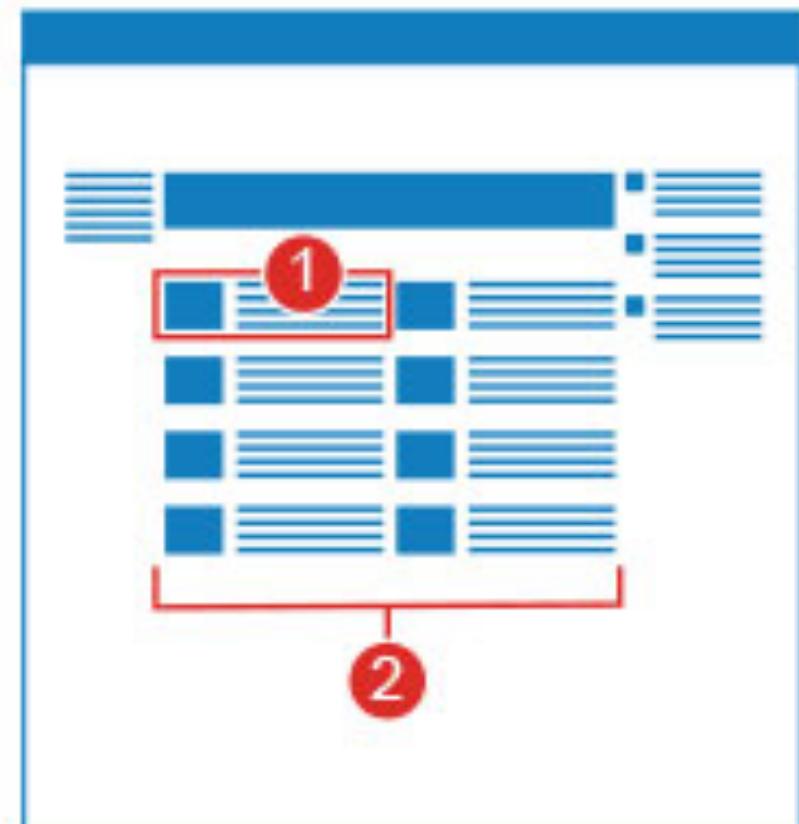
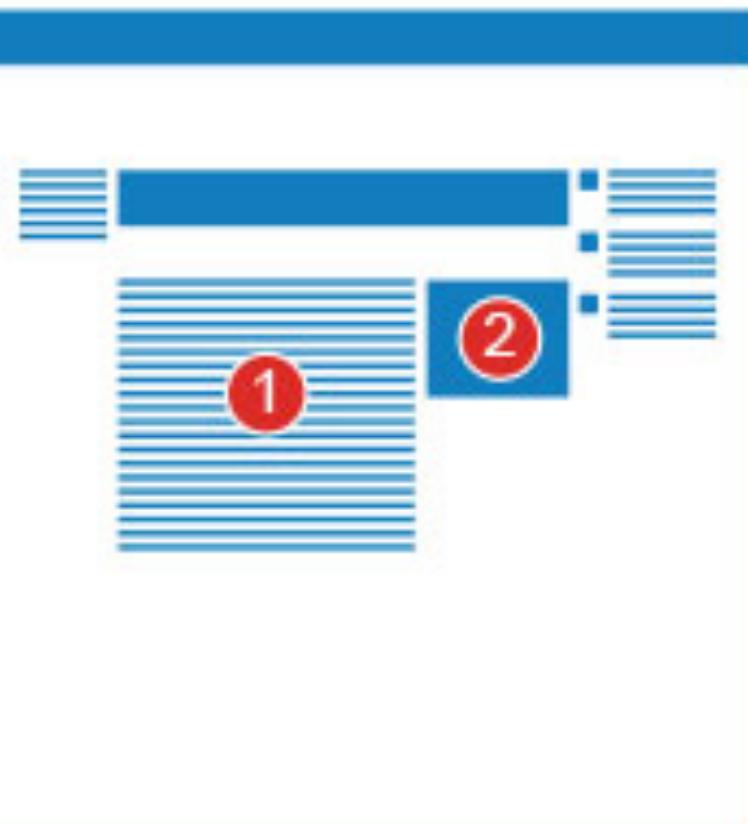
Most people see the white triangle not the 3 circles with segments missing.

COMMON FATE



Objects moving in a similar direction are perceived as belonging together.

Examples:



Elements that are closer together are perceived as being more related compared to those spaced further apart. In this

Web parts that look similar are perceived as being grouped together or related.

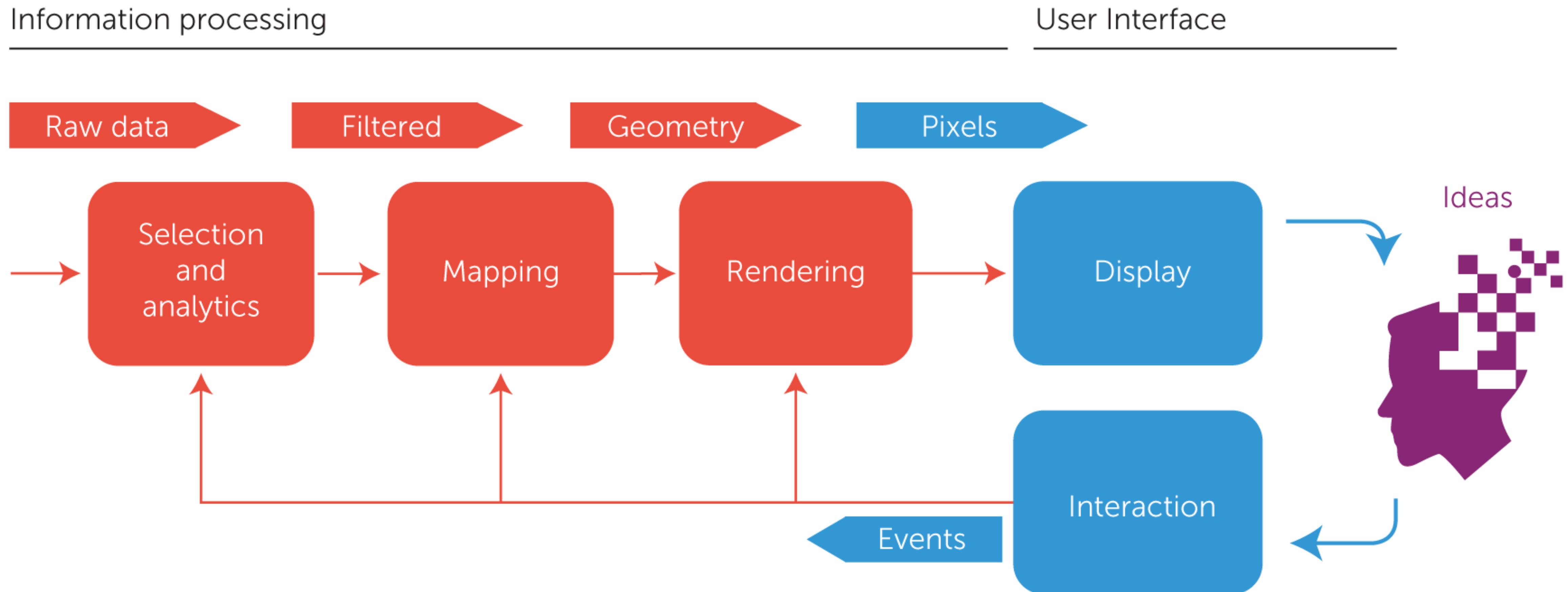
We automatically perceive objects as being in the foreground, (figure) or in the background (ground). Anything

We tend to perceive contours as objects. In this way we perceive lines continue in an established direction (even when they don't).

When we perceive a pattern the gaps (1) between the objects (negative or white space) are just as important as the objects

When objects move in the same direction we perceive them to be related and moving on an invisible path. Even if objects

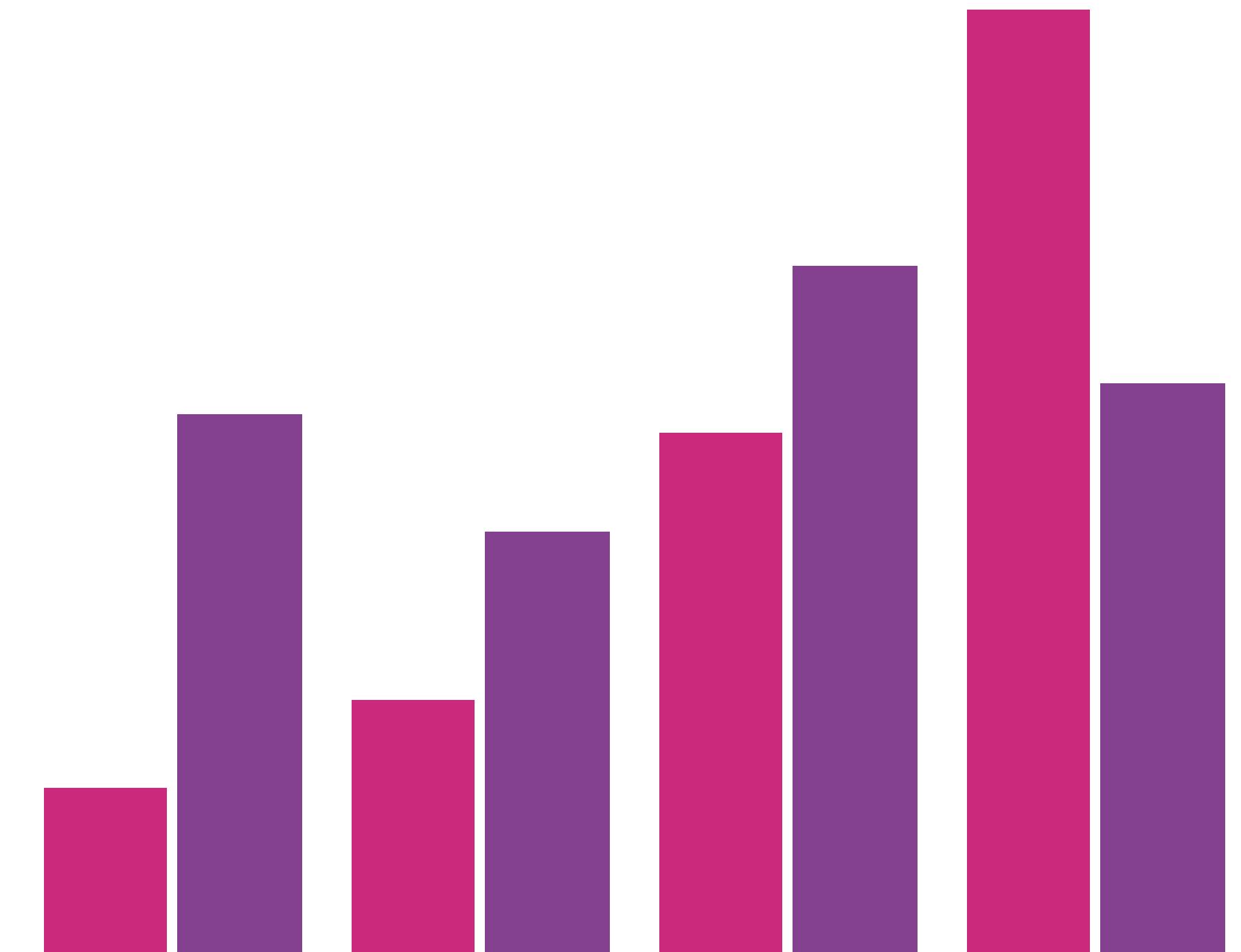
Visualization Pipeline



Definitions

Marks: basic geometric elements
to represent items or links

Channels: visual variable,
change the appearance of marks
based on attributes



Marks for items/nodes

→ Points



0D

sense of place

→ Lines



1D

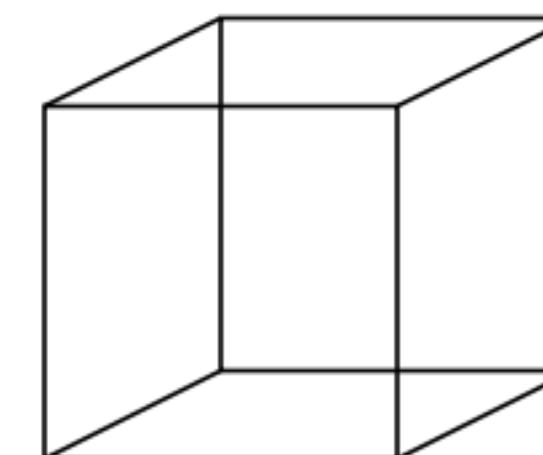
sense of length and direction

→ Areas



2D

sense of space and scale



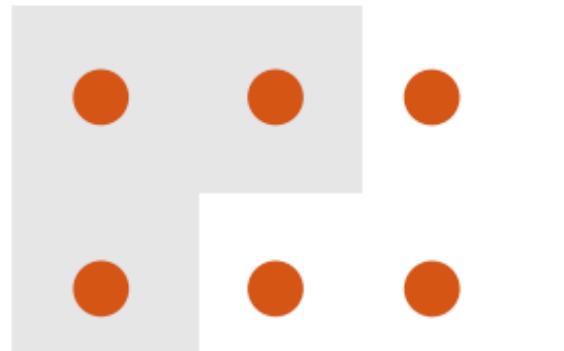
3D

sense of volume

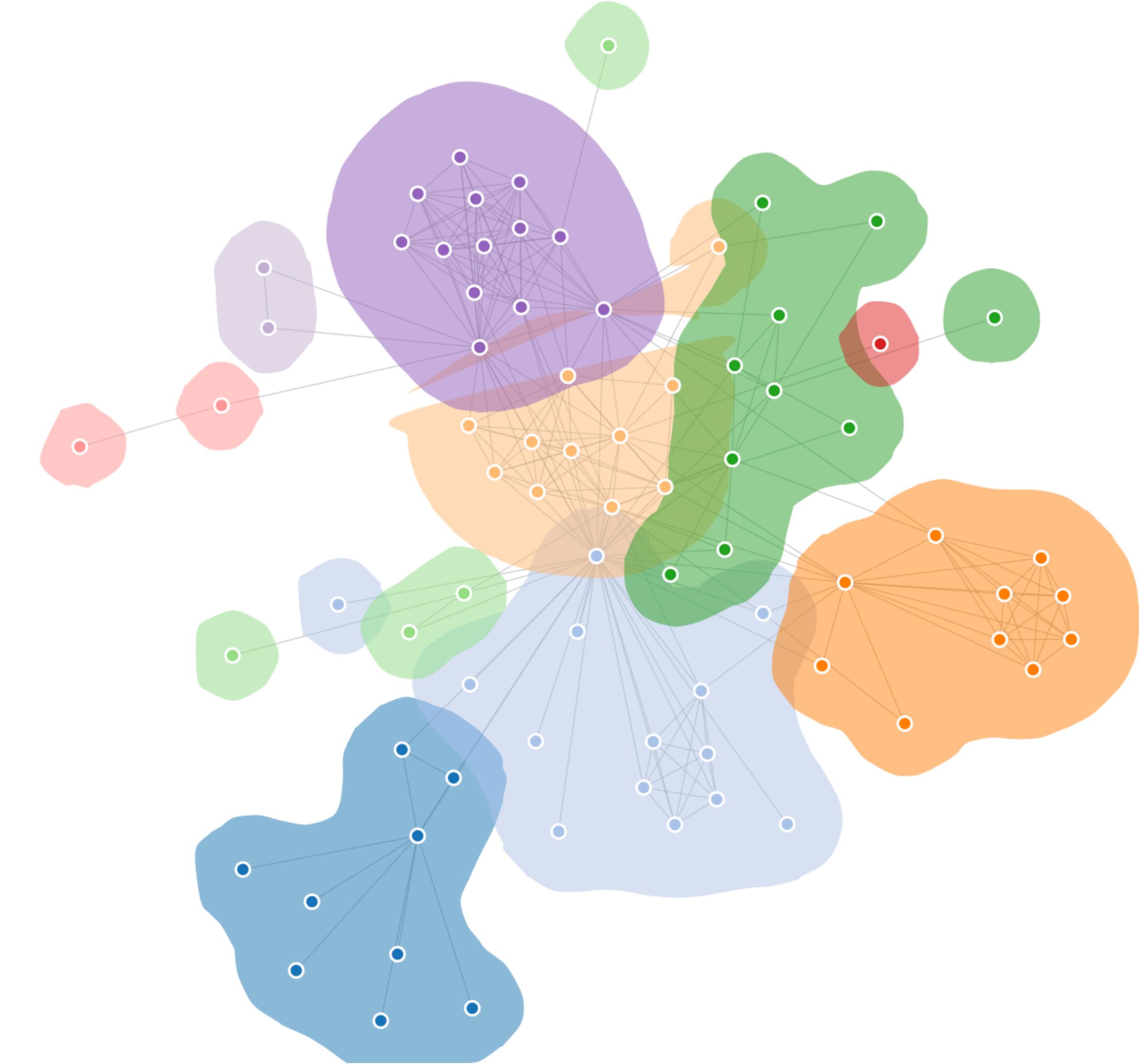
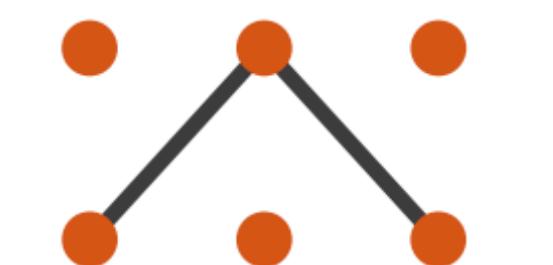
Marks for links

(Enclosure)

→ Containment



→ Connection



Channels (visual attributes)

④ Position

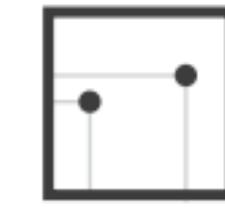
→ Horizontal



→ Vertical



→ Both



④ Color



④ Shape



④ Tilt



④ Size

→ Length



→ Area



→ Volume



**Control appearance
of marks**

Channel effectiveness

Accuracy: How well can a user read the information in the channel?

Discriminability: How easily can we perceive differences between attribute levels?

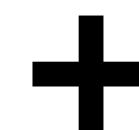
Separability: Can we use one channel independently of another? Do they interfere?

Popout: How can a channel trigger a visual popout when processing data?

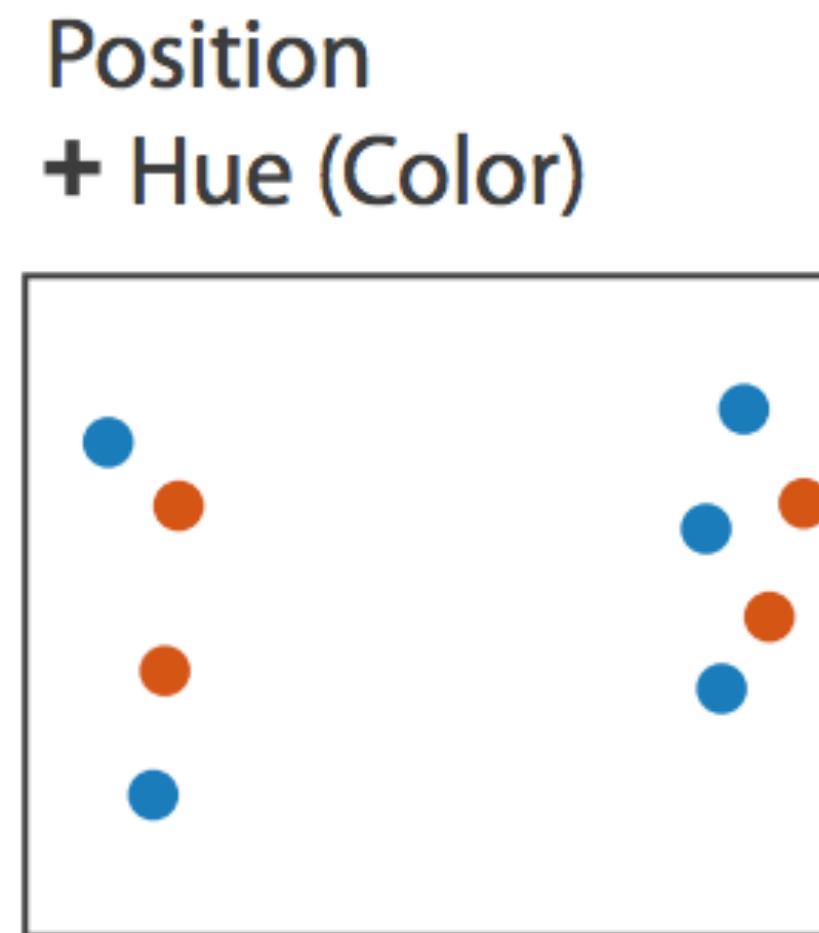
Grouping: How can a channel trigger some of the Gestalt principles?

Test of separability

Low-level preattentive processing features



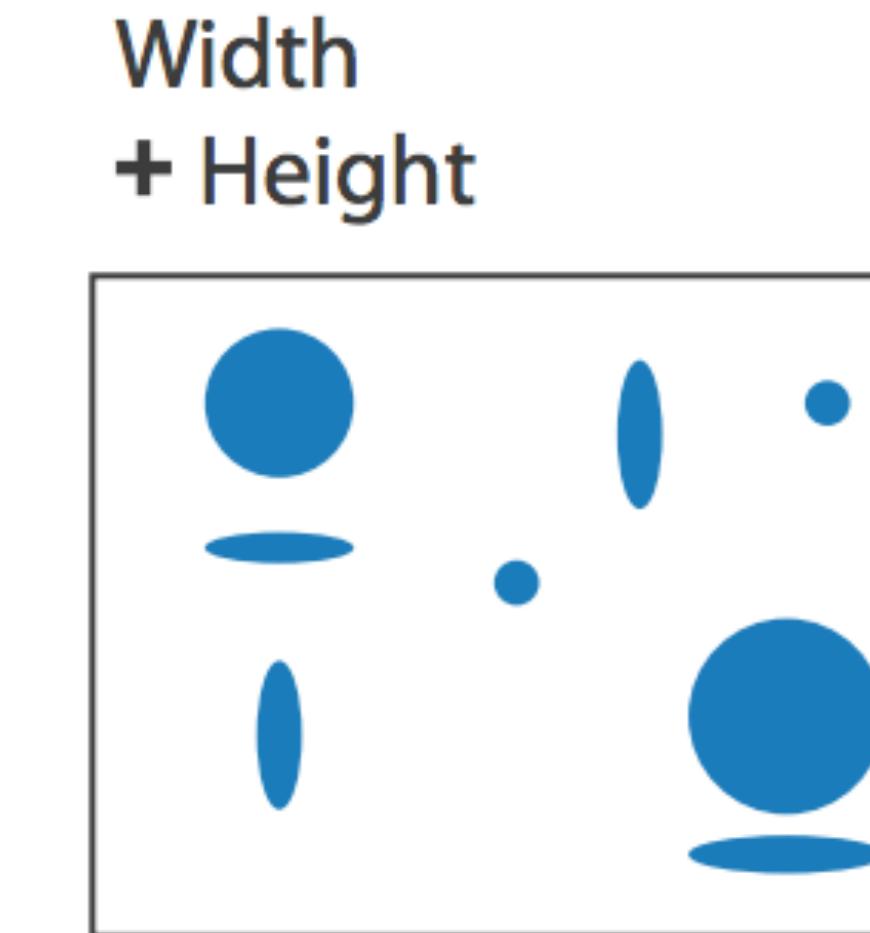
Gestalt principles



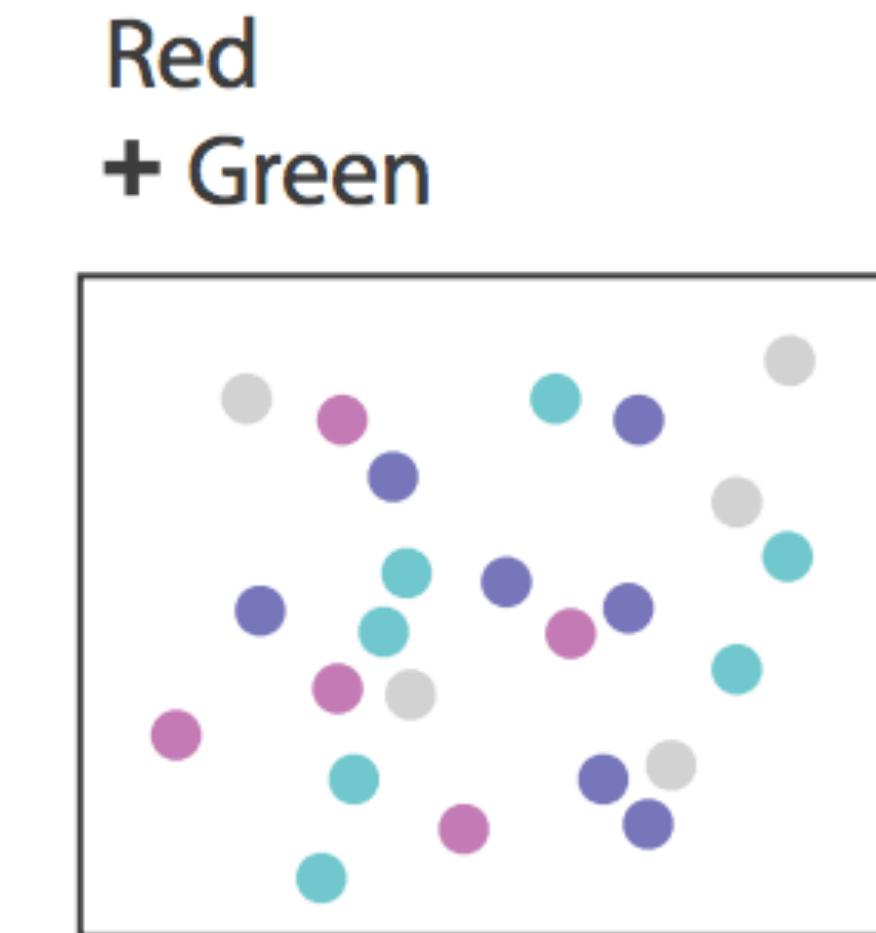
Fully separable



Some interference



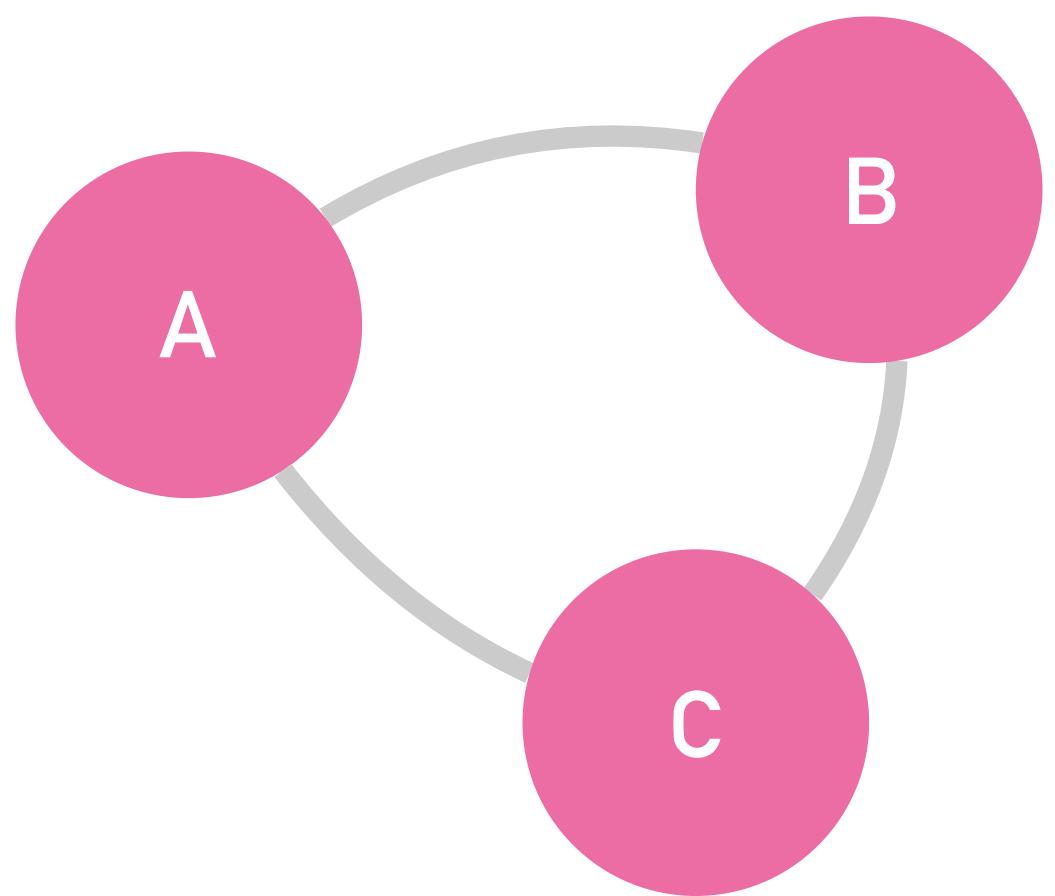
Some/significant
interference



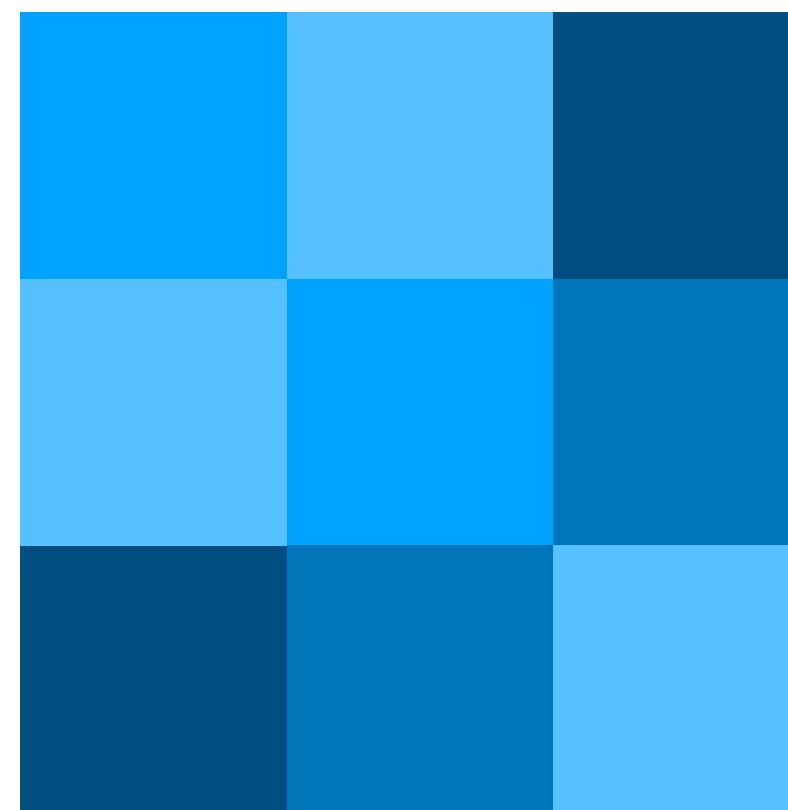
Major interference

Graph visualizations

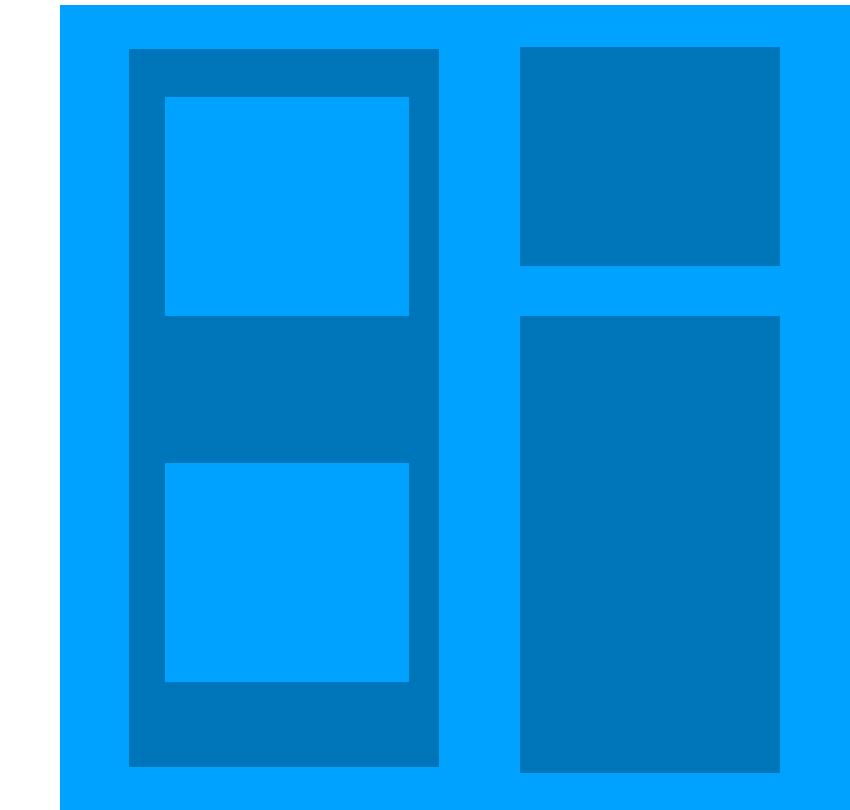
Graph visual encodings



Node-link diagram



Matrix form



Implicit form

Choosing the right representation?

Depends on the task, **attribute-based (ABT)** and/or **topology-based (TBT)**

Localize – find a single or multiple nodes/edges

- **ABT**: Find edges of a certain type
- **TBT**: Get the neighborhood of a given node

Quantify – count or estimate a numerical property of the graph

- **ABT**: Get number of edges
- **TBT**: Get the number of outbound links from a node

Sort/Order – enumerate the nodes/edges according to a given criterion

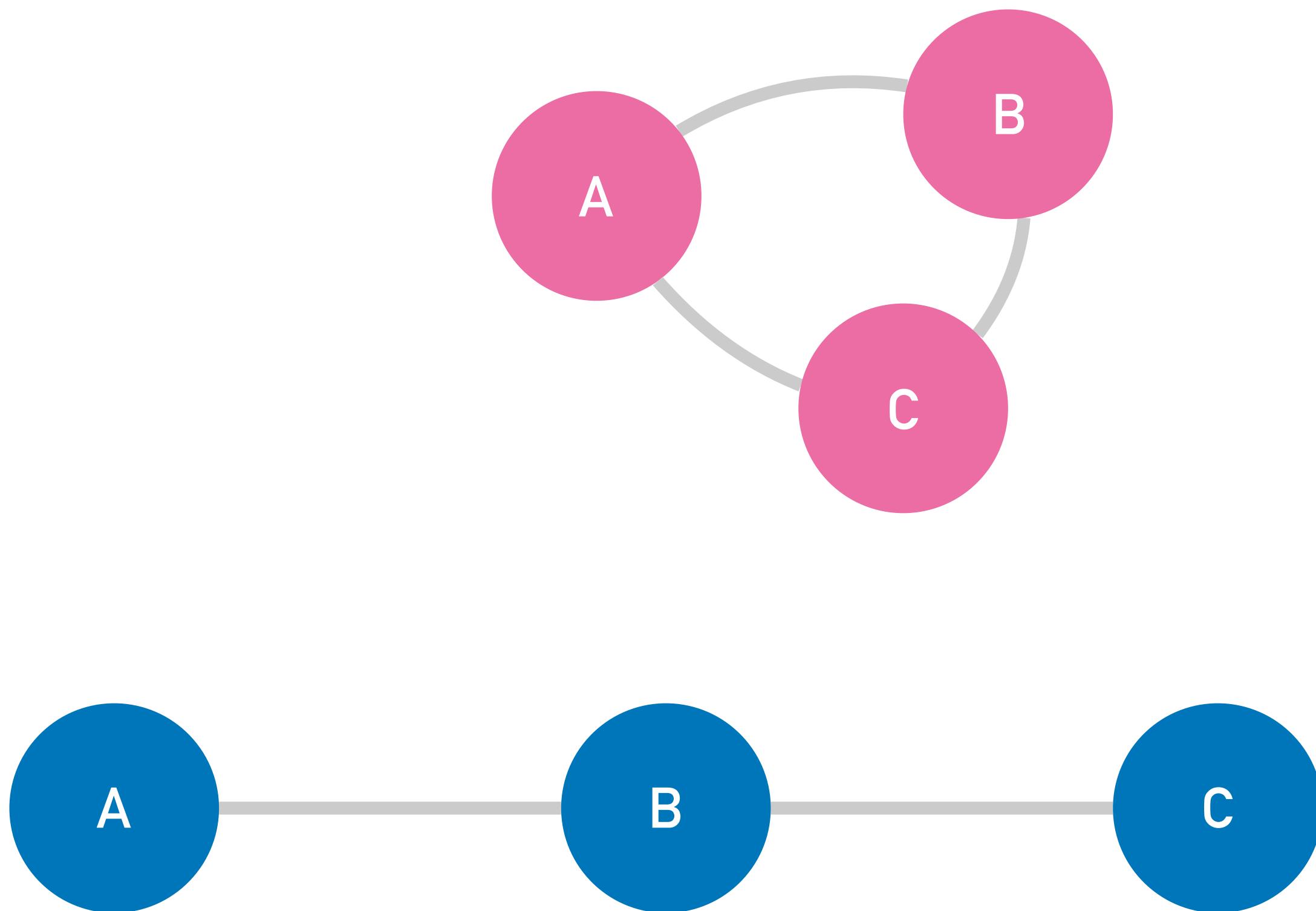
- **ABT**: Sort all edges by distance (or weight)
- **TBT**: Get the shortest paths from a given node

Node-link diagram

Explicit graph representation

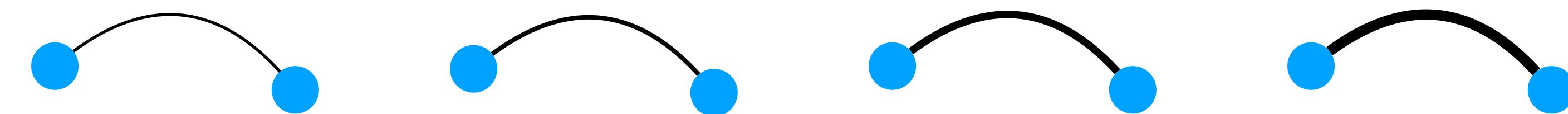
Vertex = point

Edge = line or arc

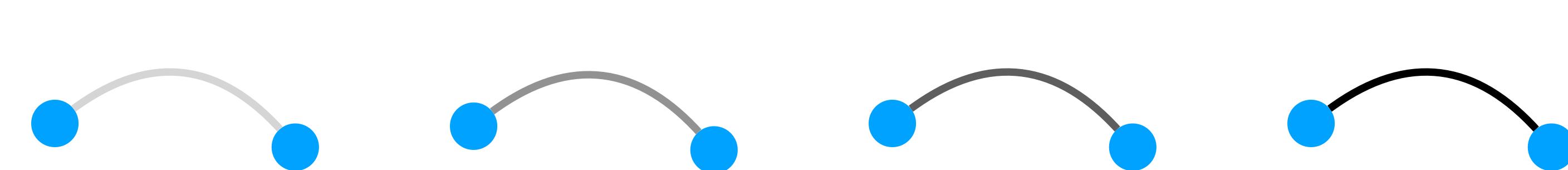


Edge attribute encoding

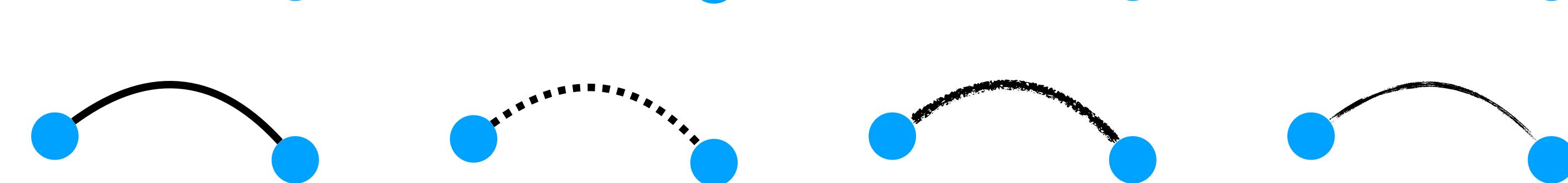
Width: quantitative



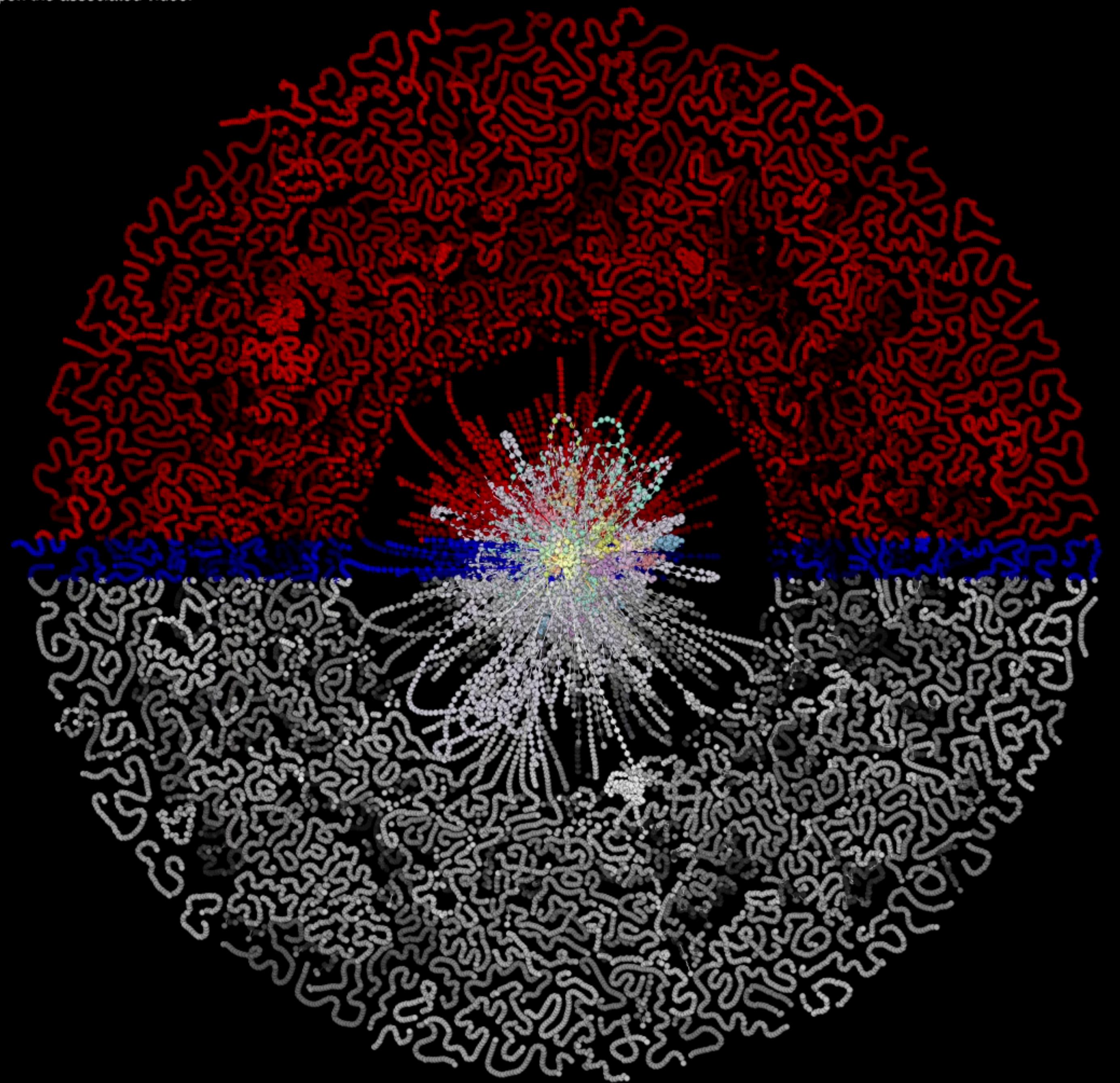
Saturation: ordinal



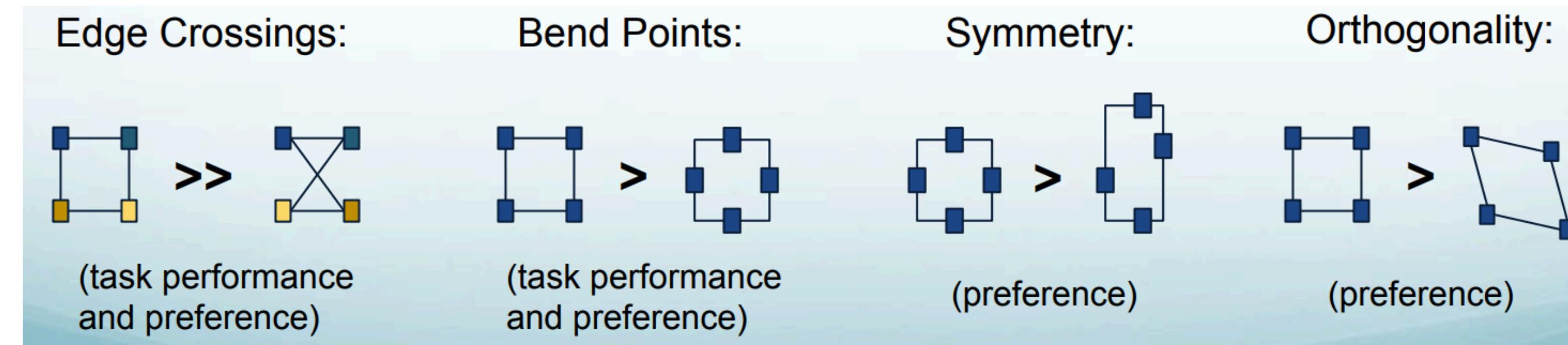
Style: nominal



Navigate using your mouse and double click on a node to open the associated video.



Criteria for good layout



[Hindalong]

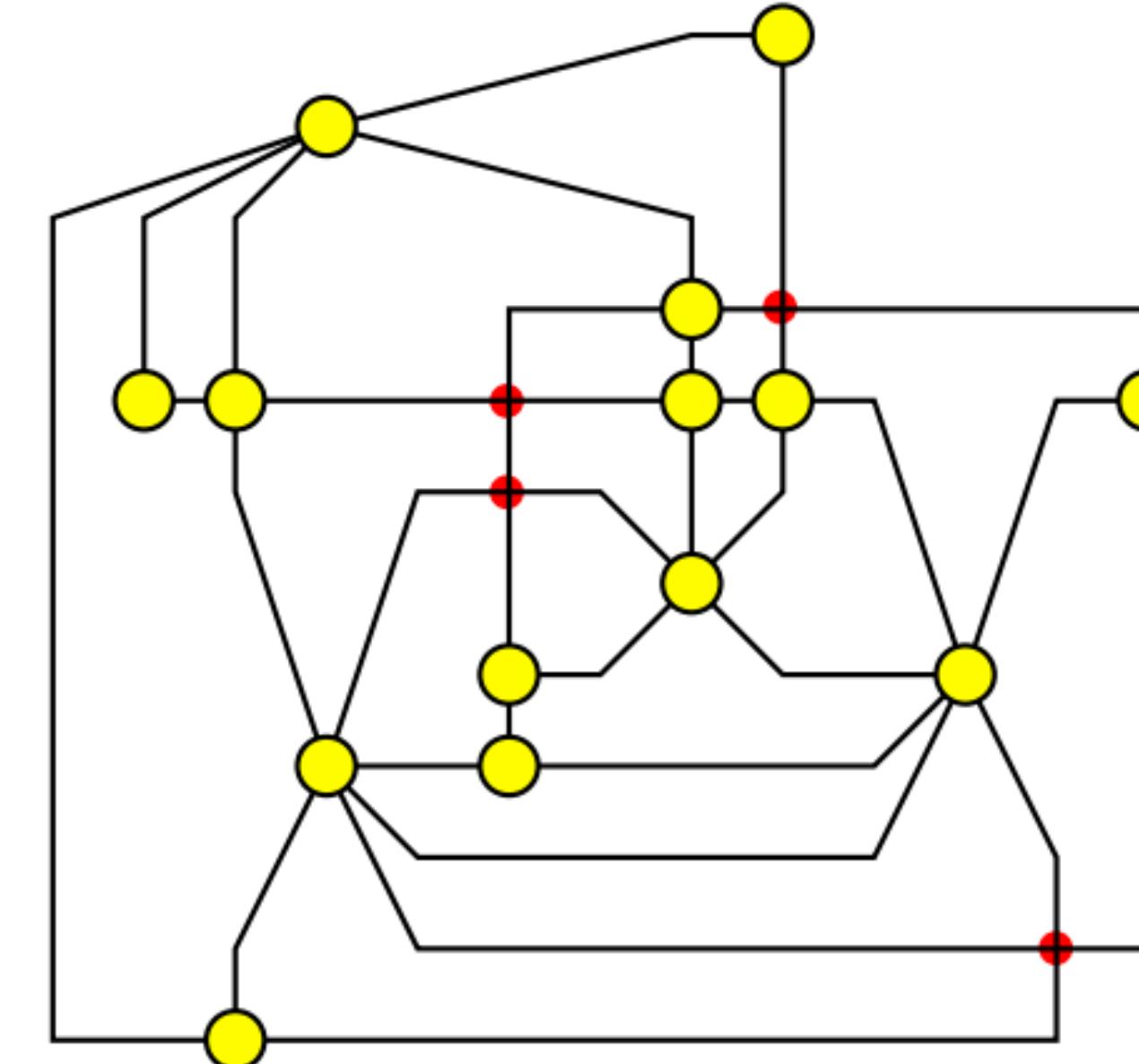
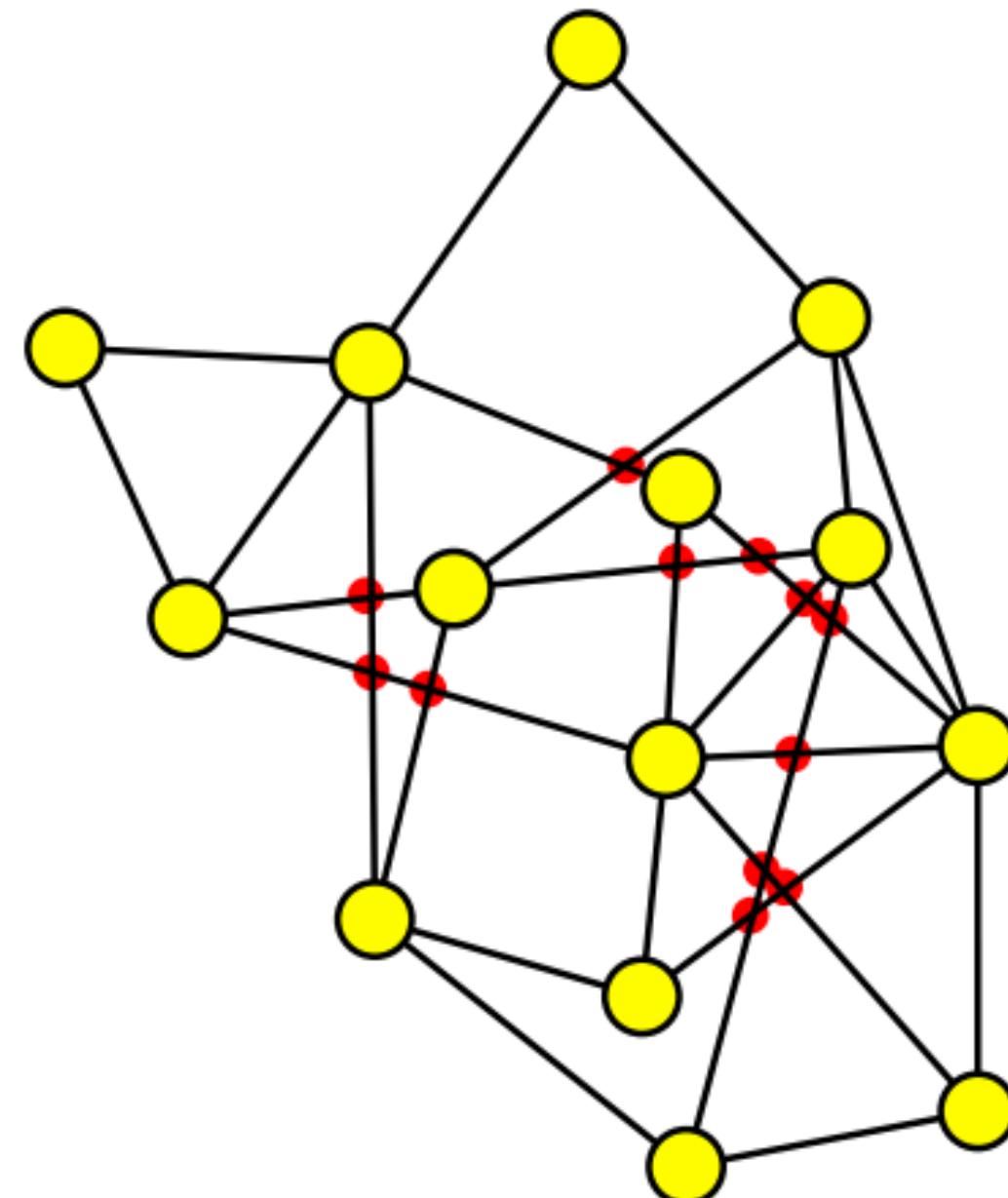
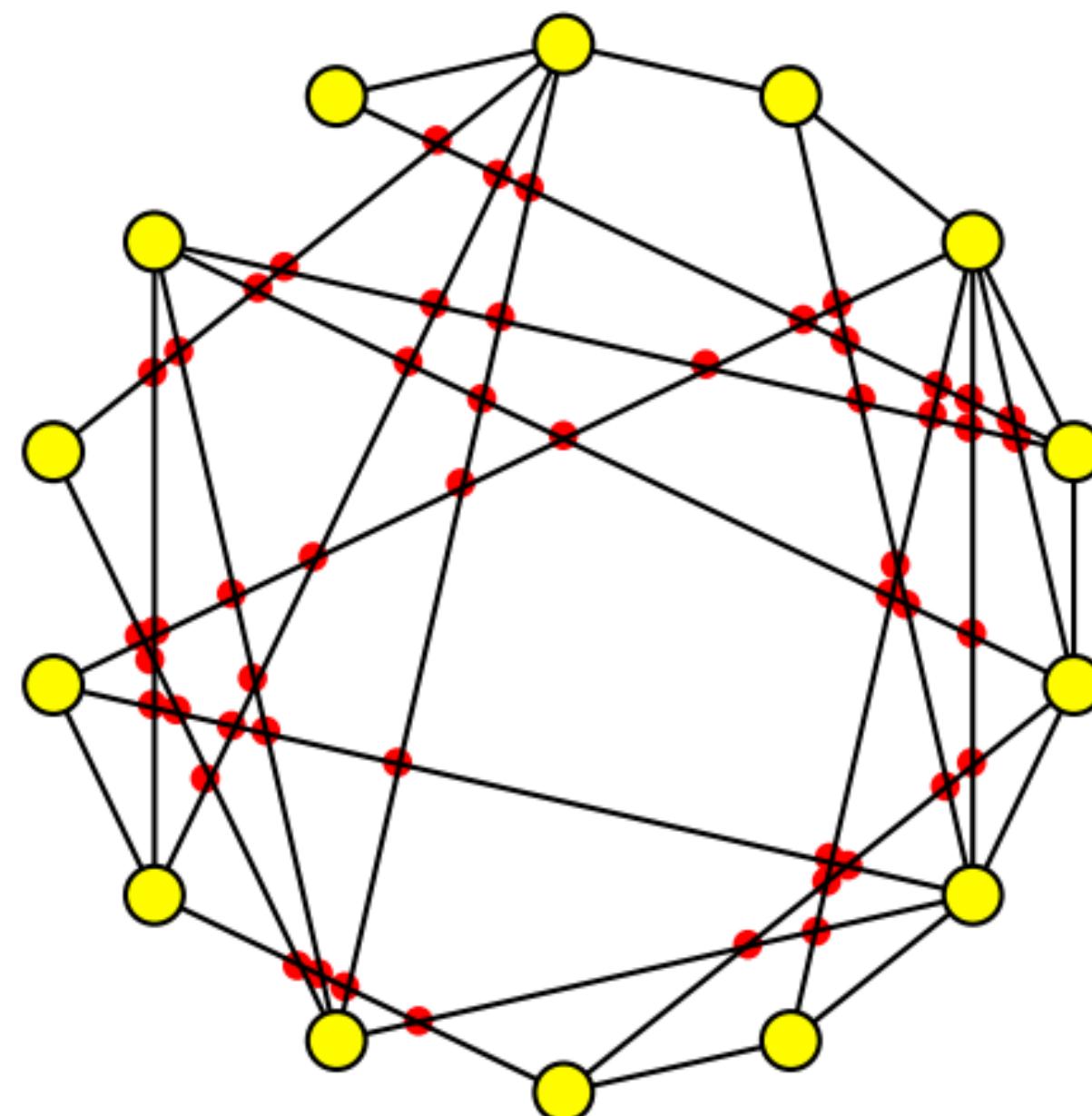
Minimized distance of neighboring nodes

Uniform edge length

Aspect ratio about 1 (not too long and not too wide)

Minimized drawing area

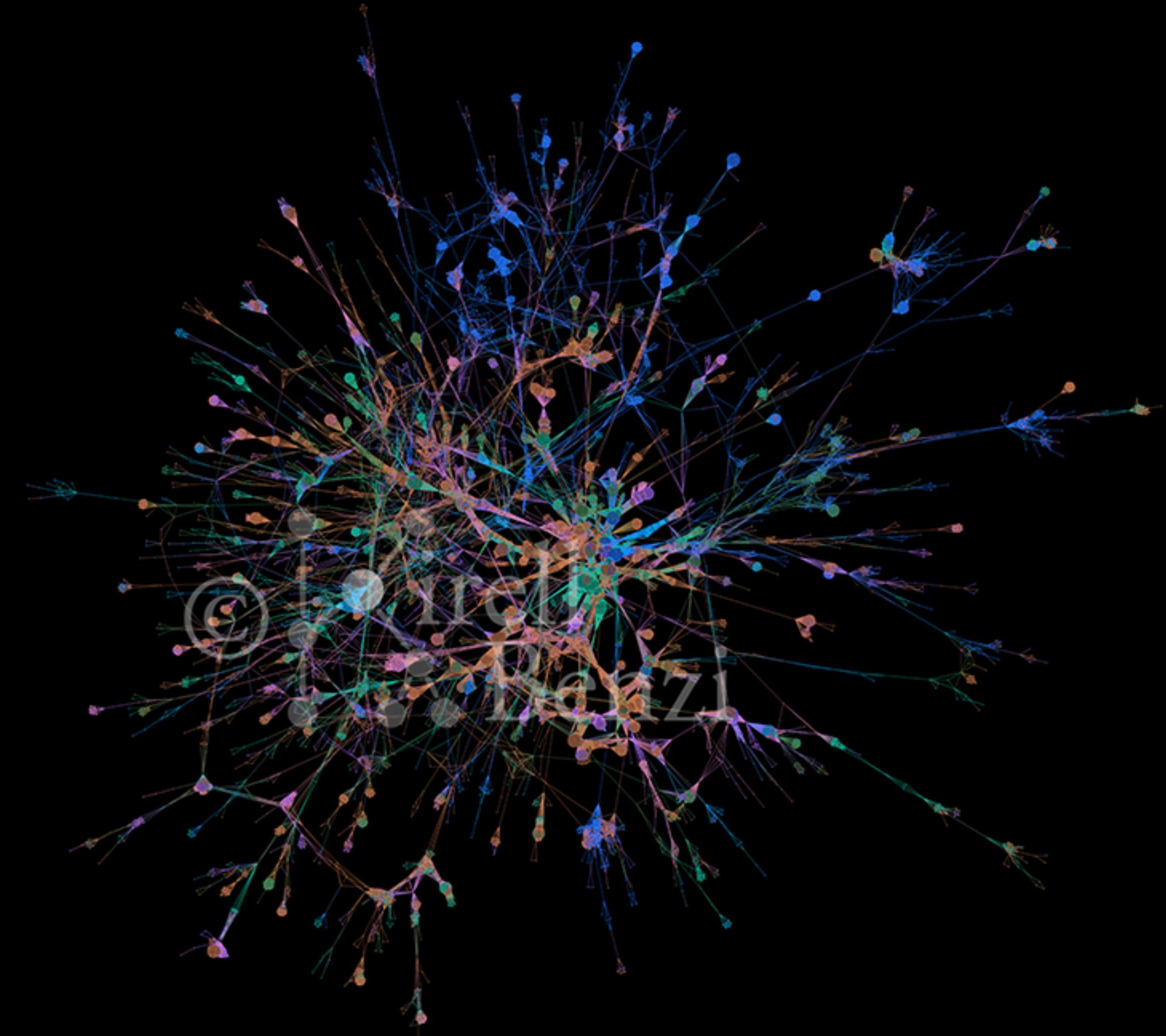
Conflicting criteria



Design critique



Kirell Benzi



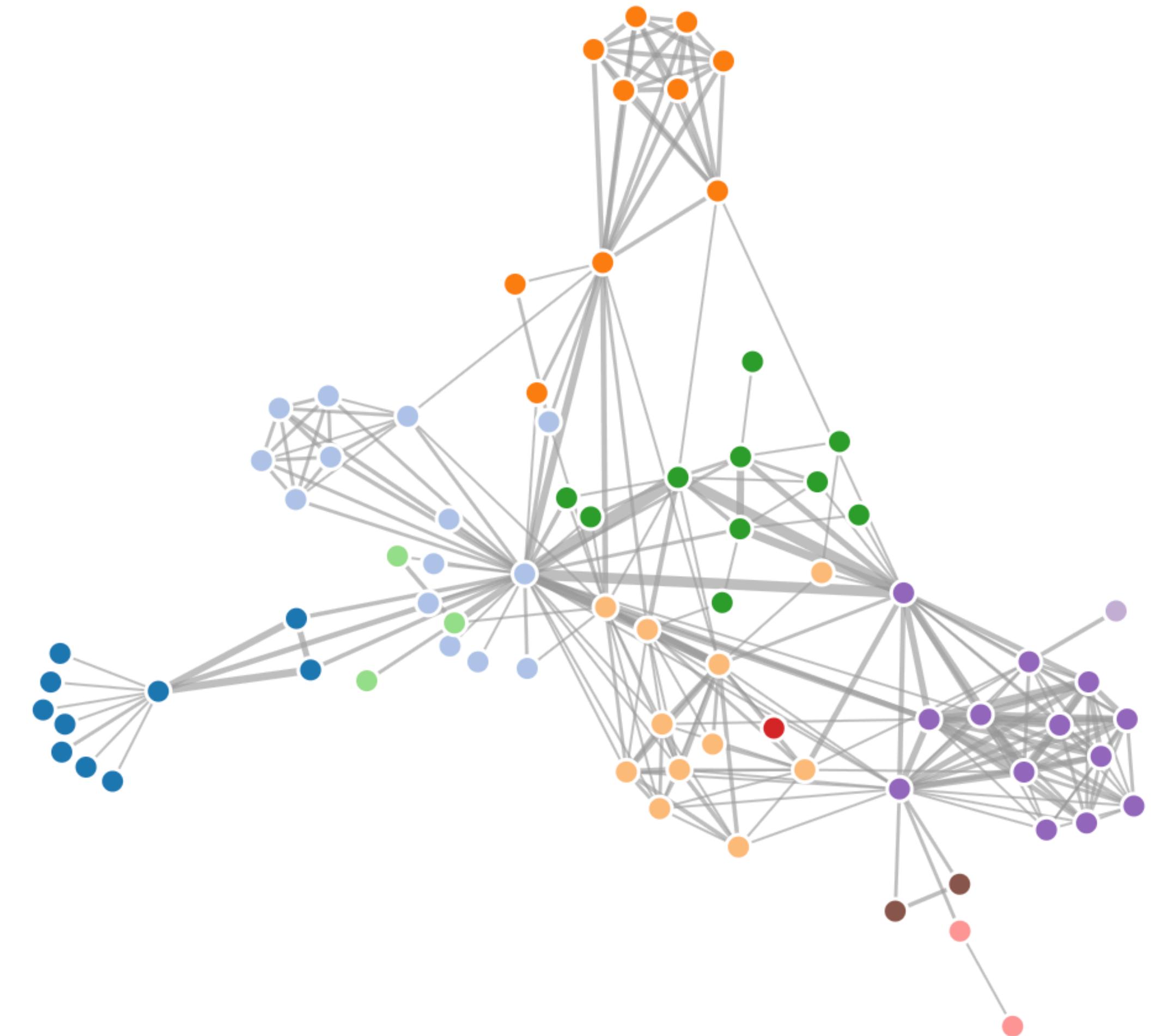
Force-directed layouts

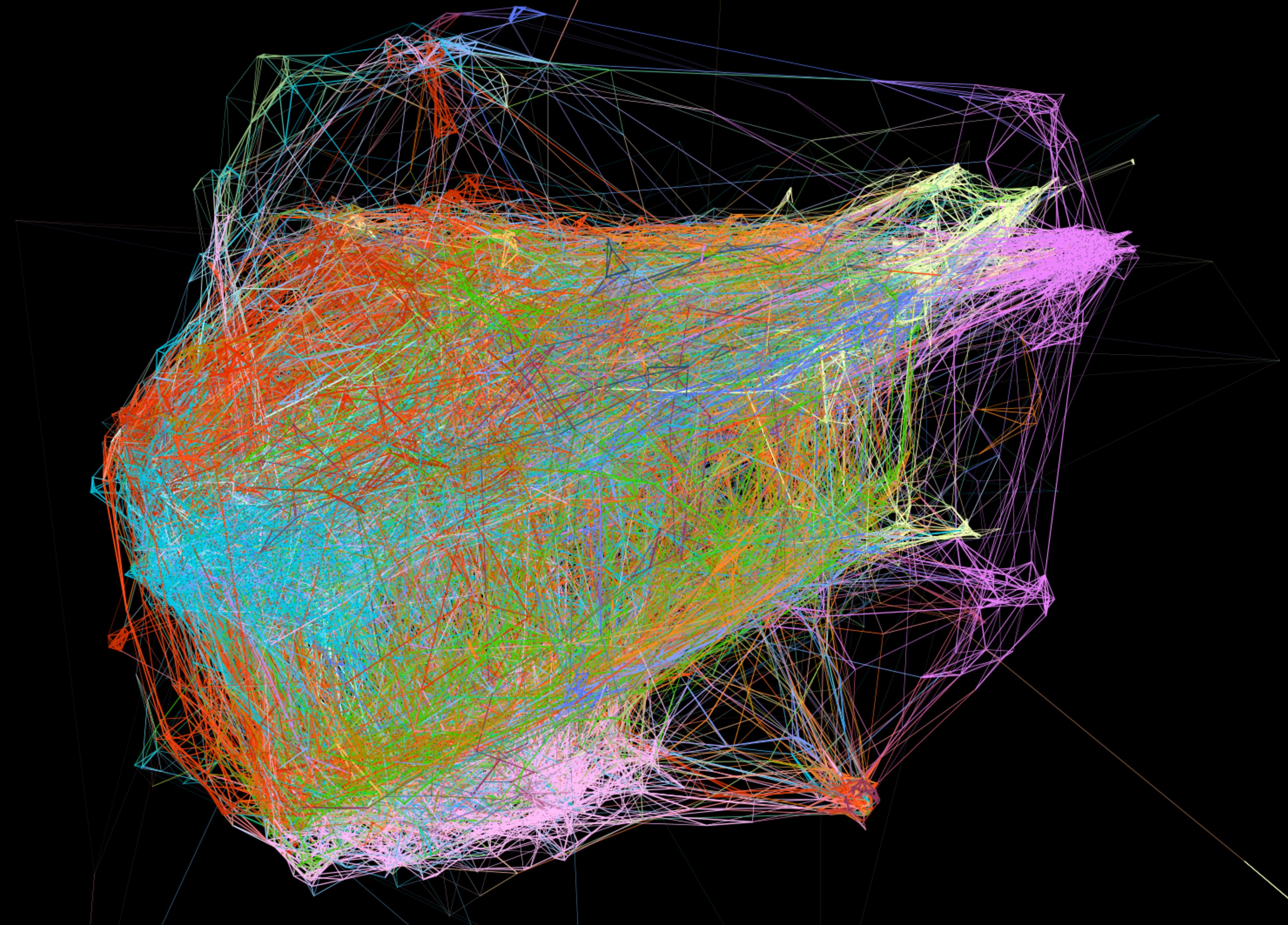
Most common layouts

Adapted from Physics, with vertices as repulsive magnets and edges as springs

Computationally expensive: $O(n^3)$

Hard to scale for interactivity





Force-directed issues

Giant hairball depending on the topology of the graph

Computing an optimal layout lies in NP

Try to solve as an optimization problem, not necessarily convex

Complexity is still high $O(n^2)$

In each optimization step, all vertices are compared to all others

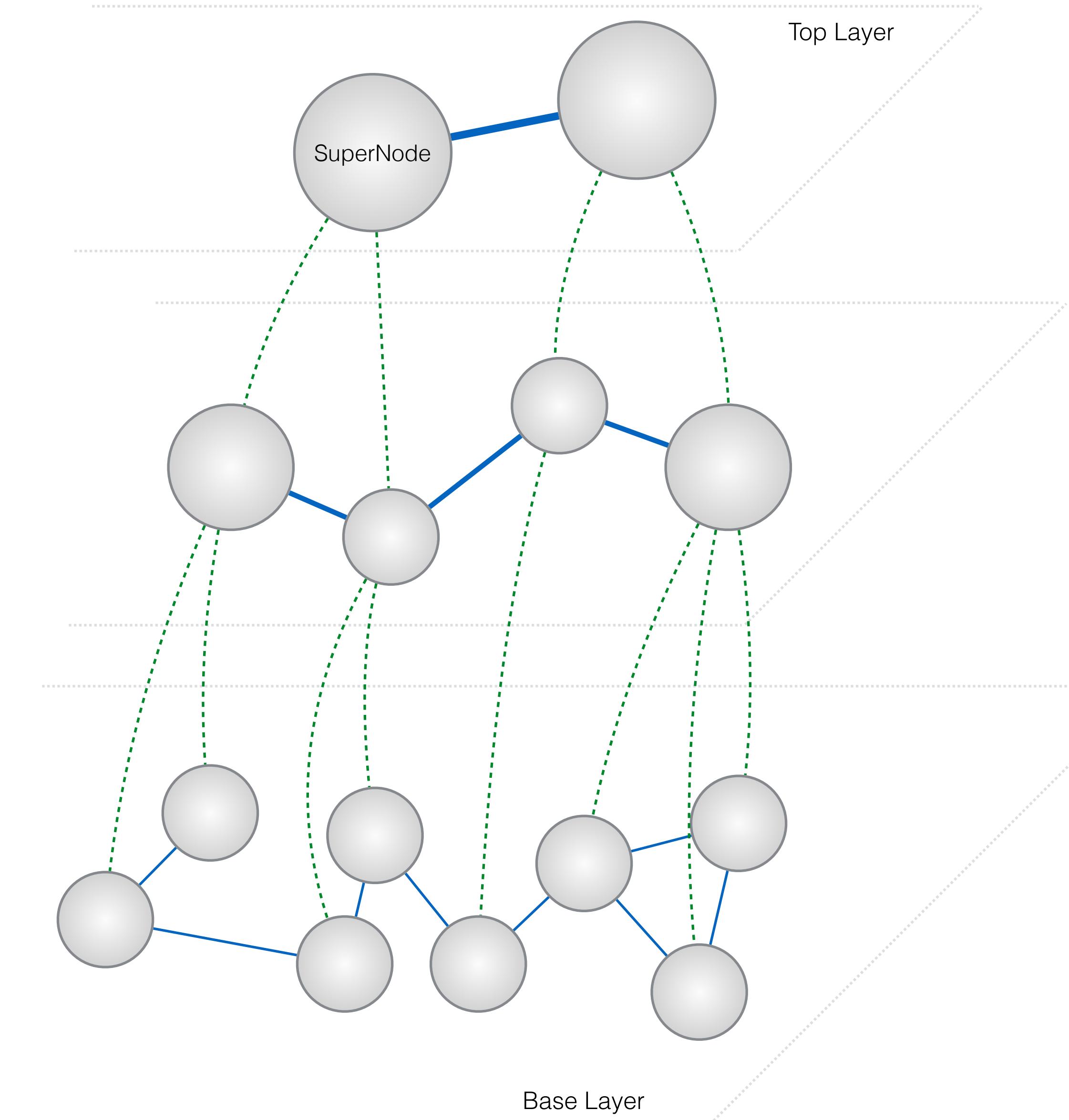
Multilevel approaches

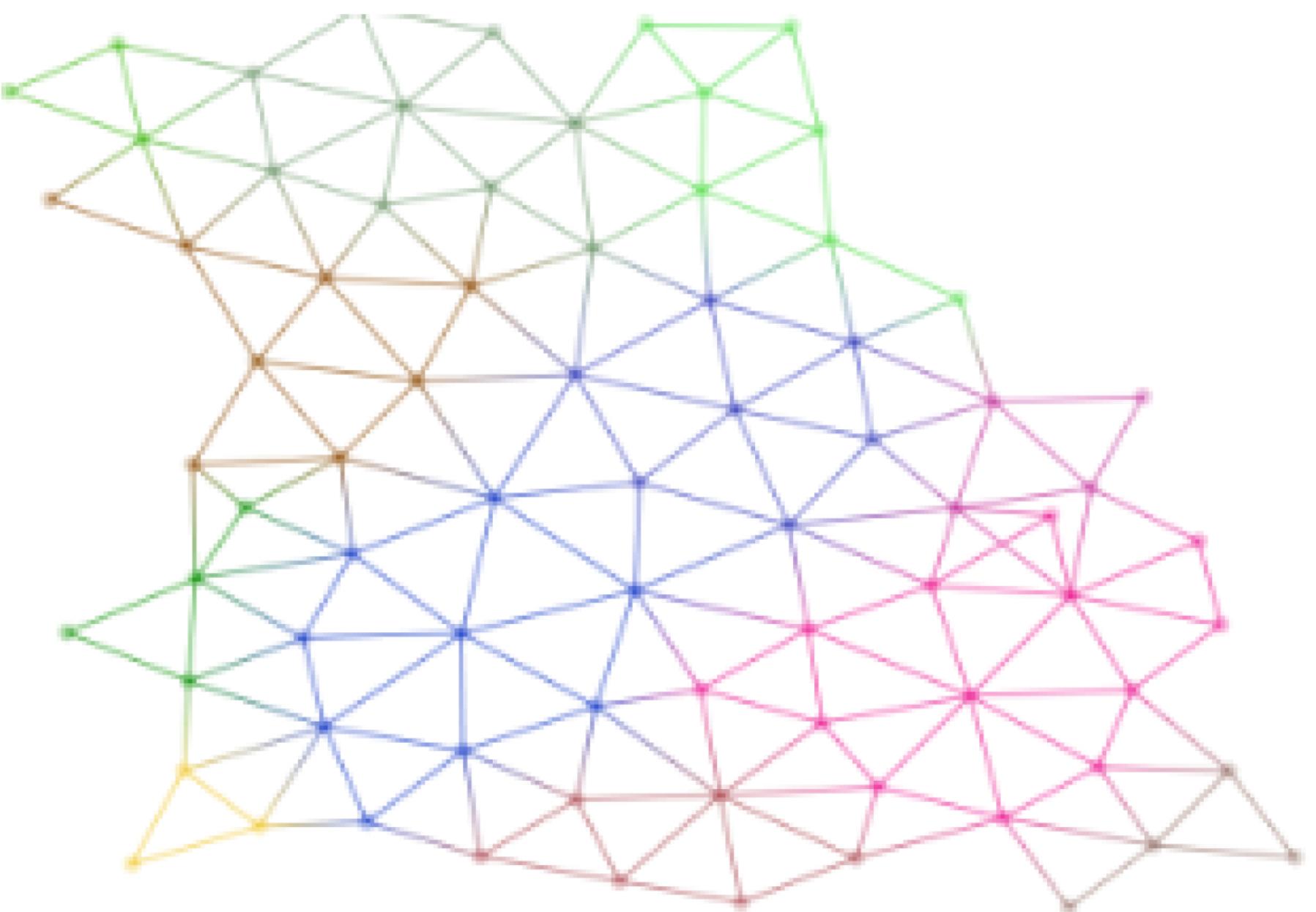
Also known as graph coarsening

Different strategies to collapse node or edges

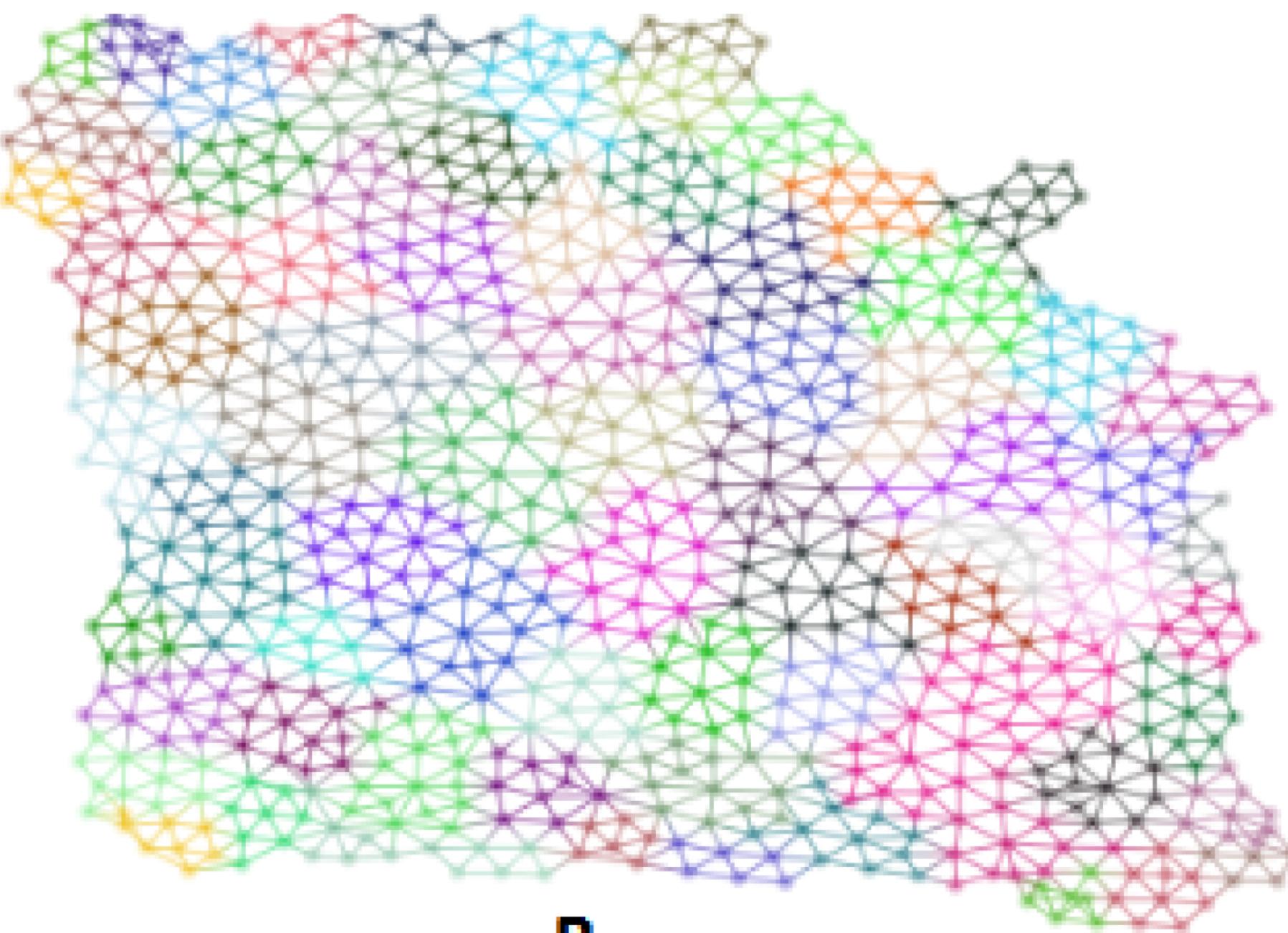
Recursive graph layout from top to bottom

Used also in graph partitioning, shortest path, etc.

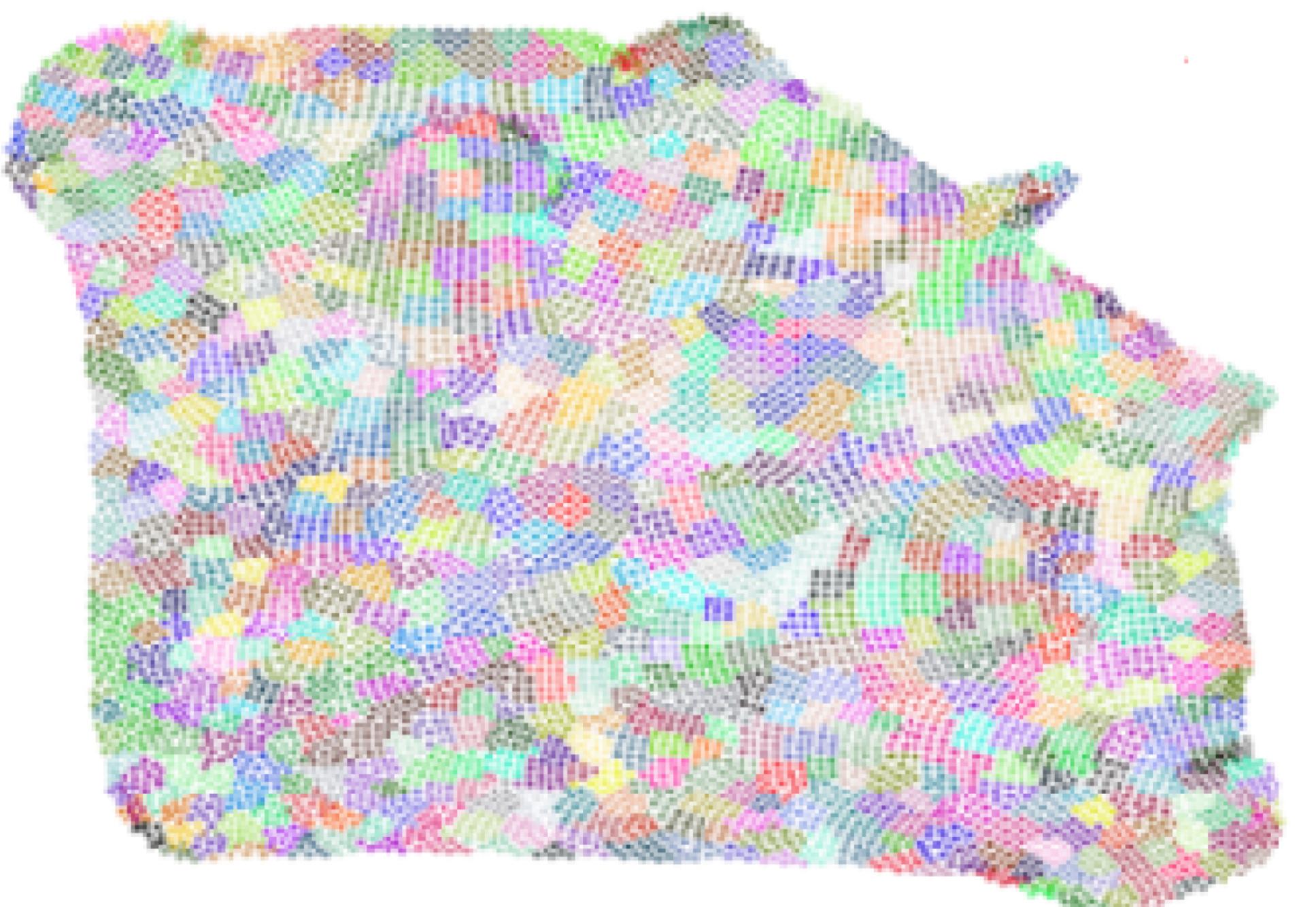




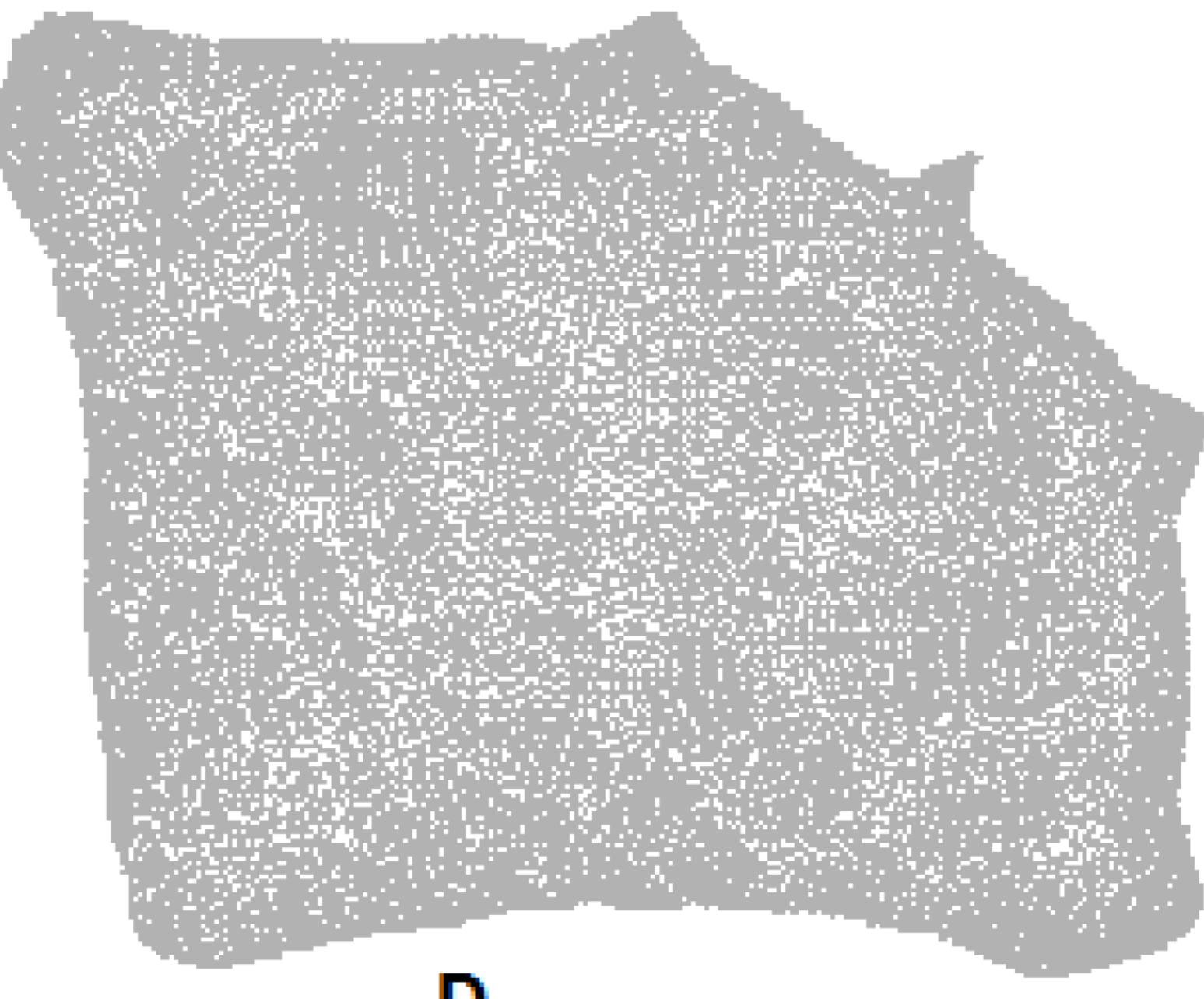
A



B



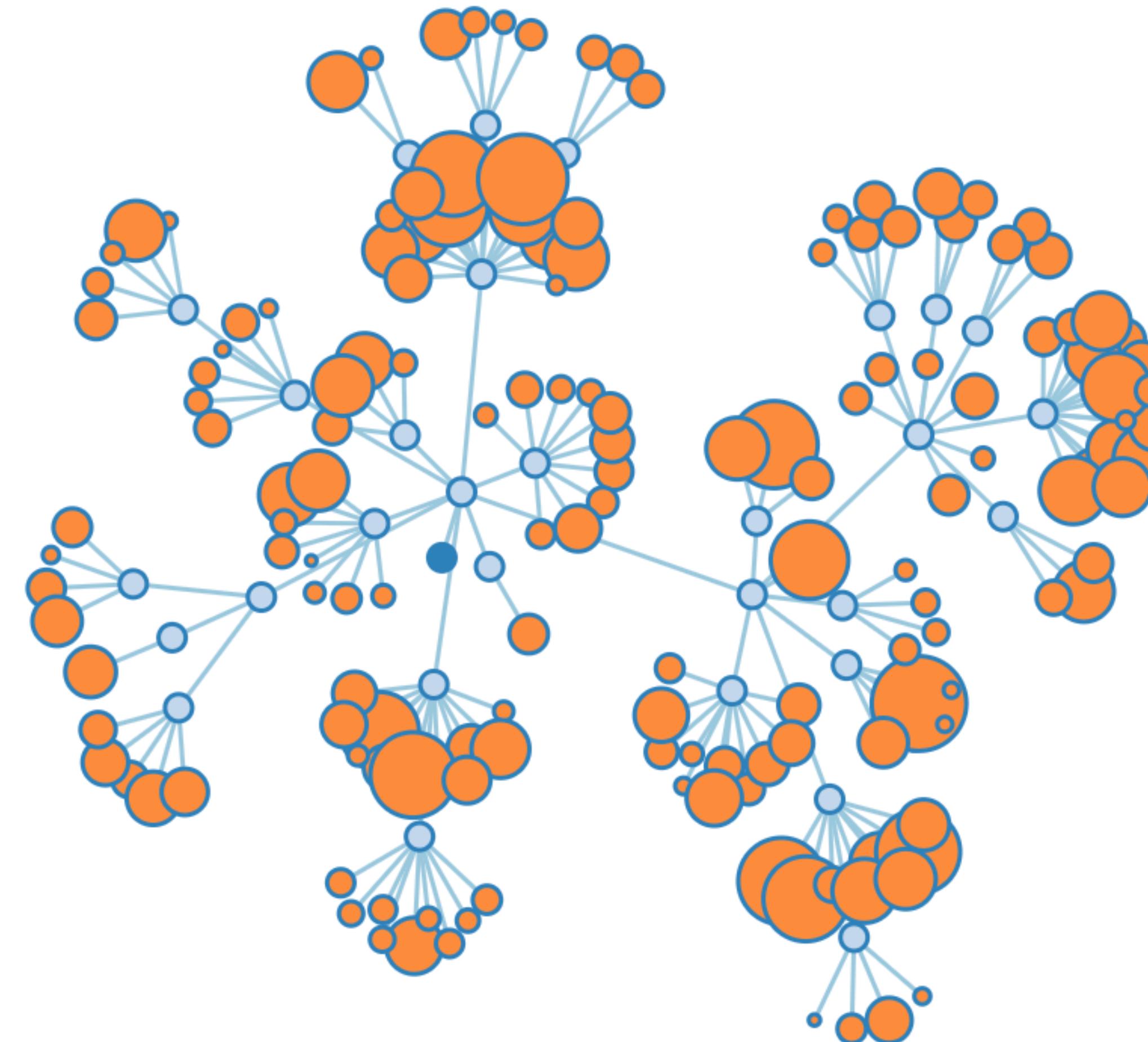
C



D

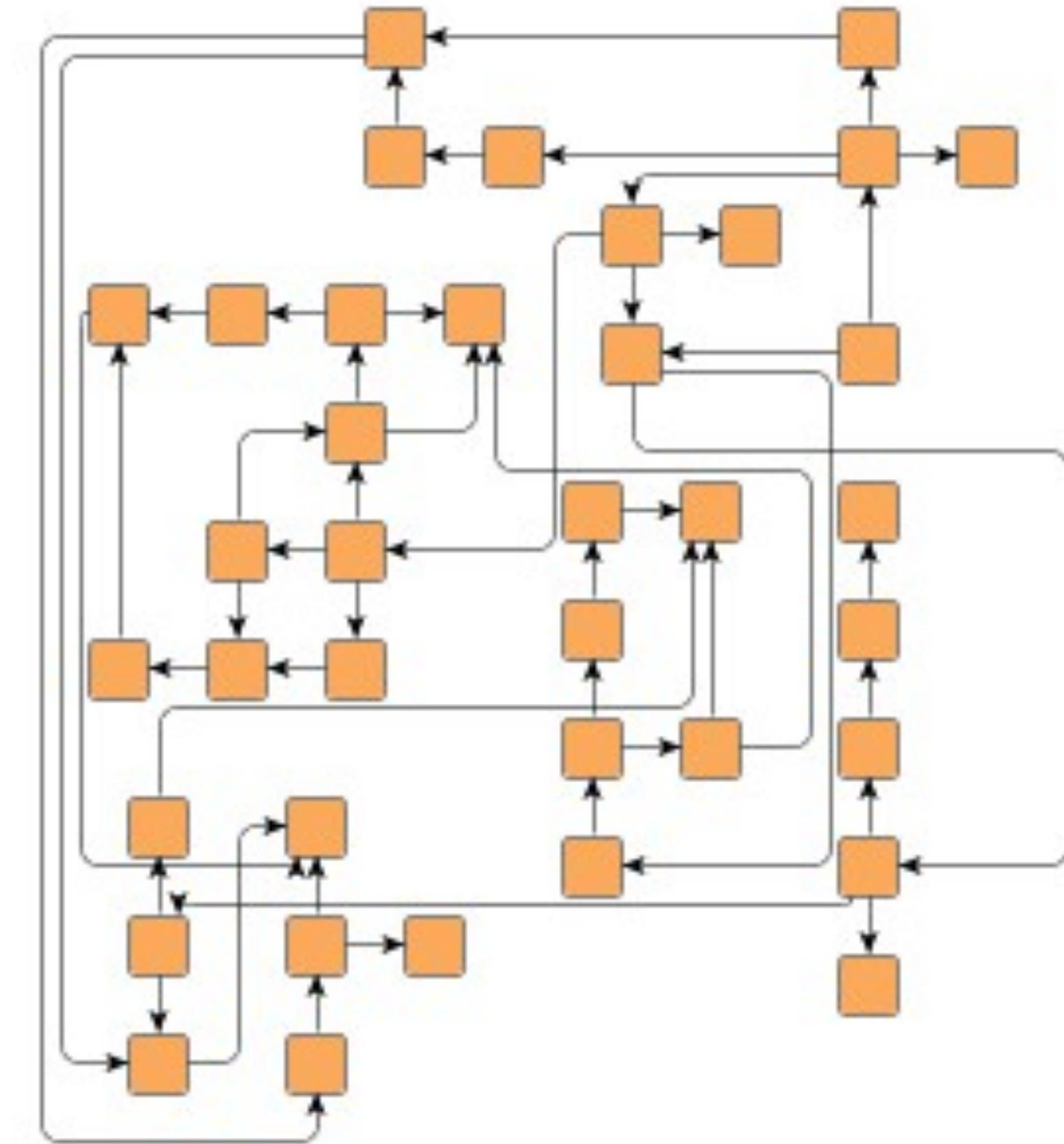
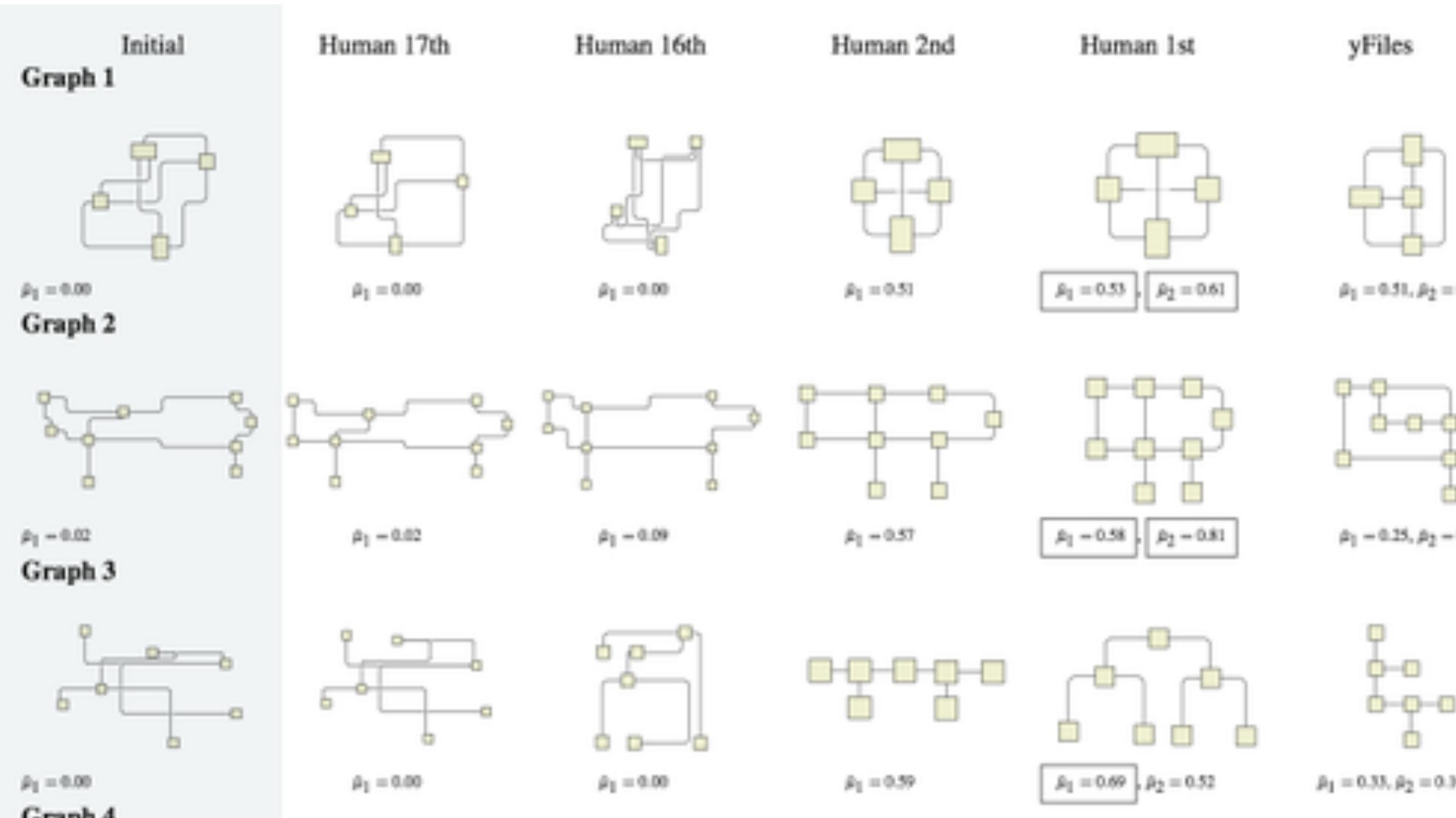
[Mi et al.]

Collapsible Force Layout



Orthogonal layout

Used primarily in electrical engineering and software dev

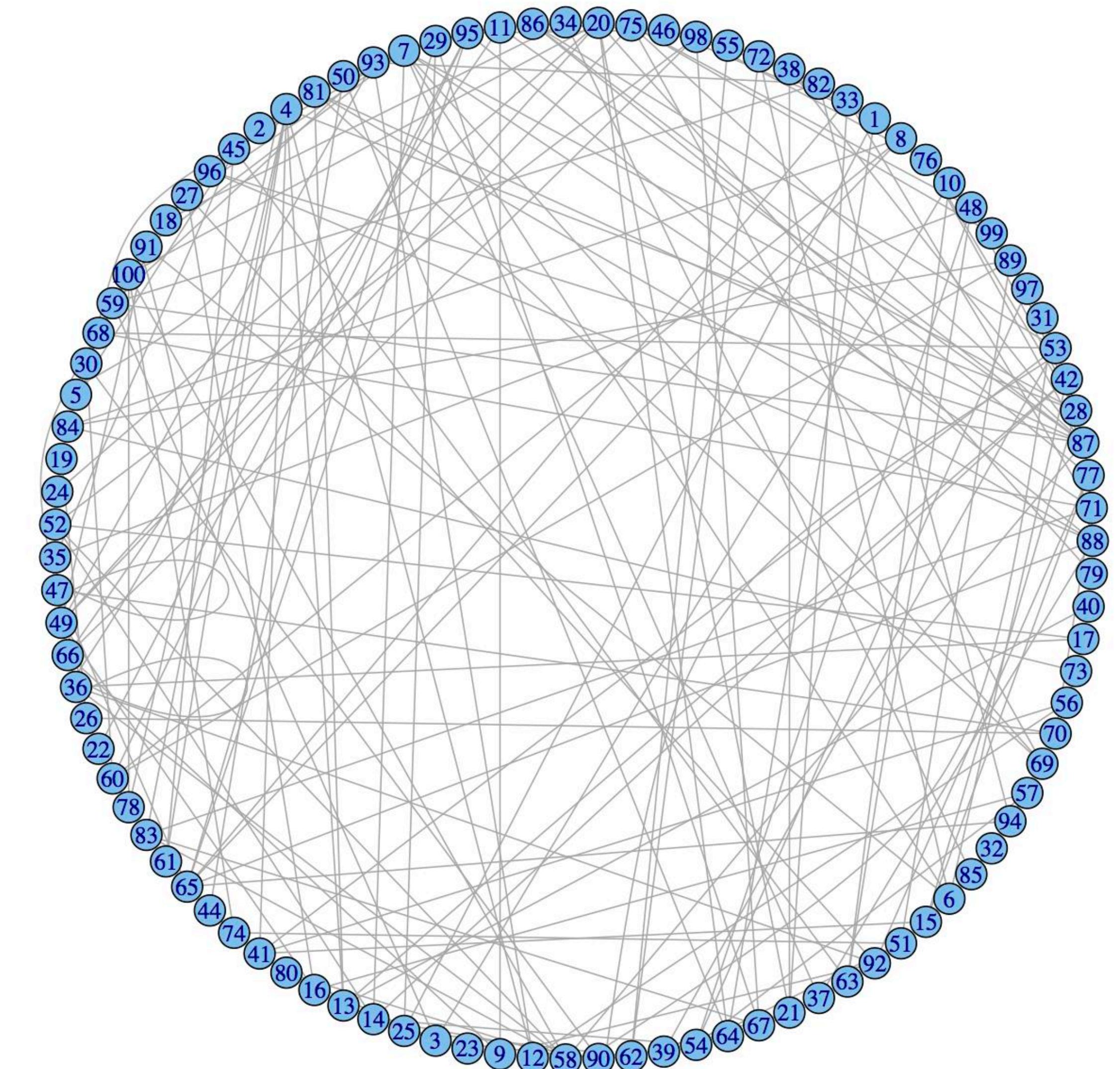
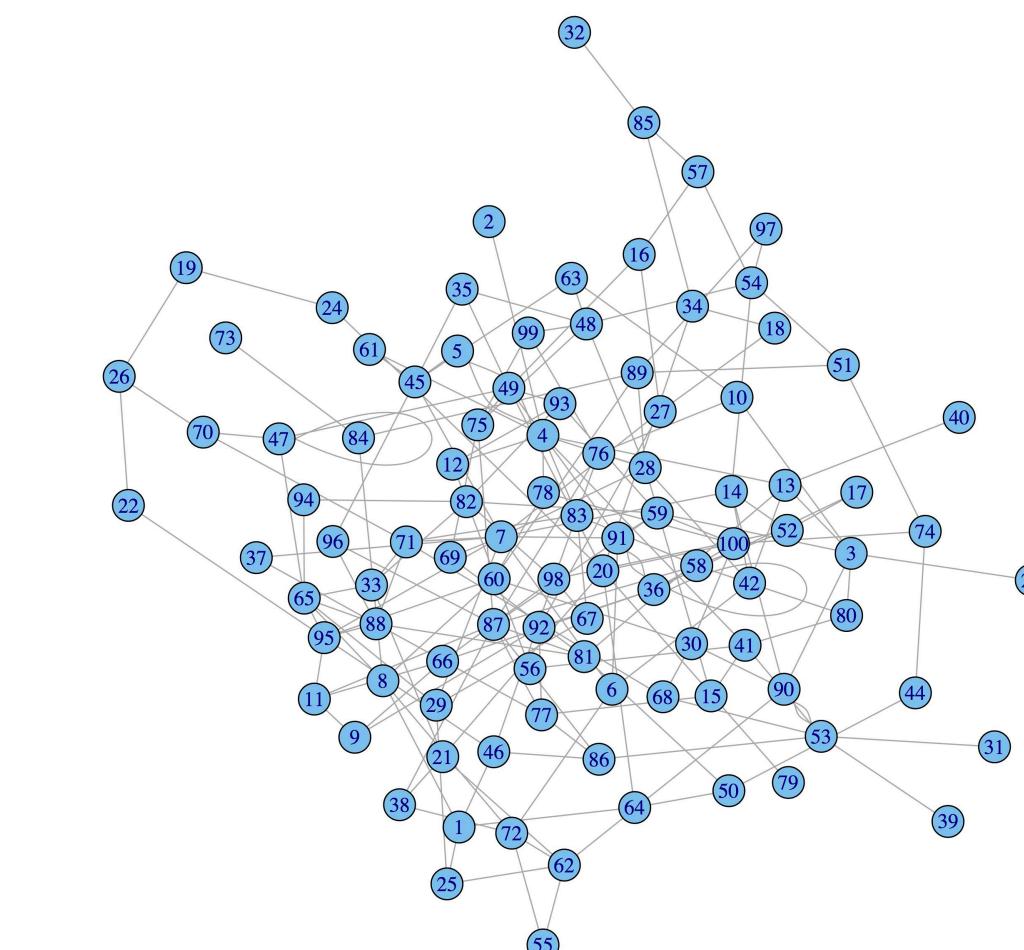


Circle layout

Node positions are constrained
on the edge of the circle

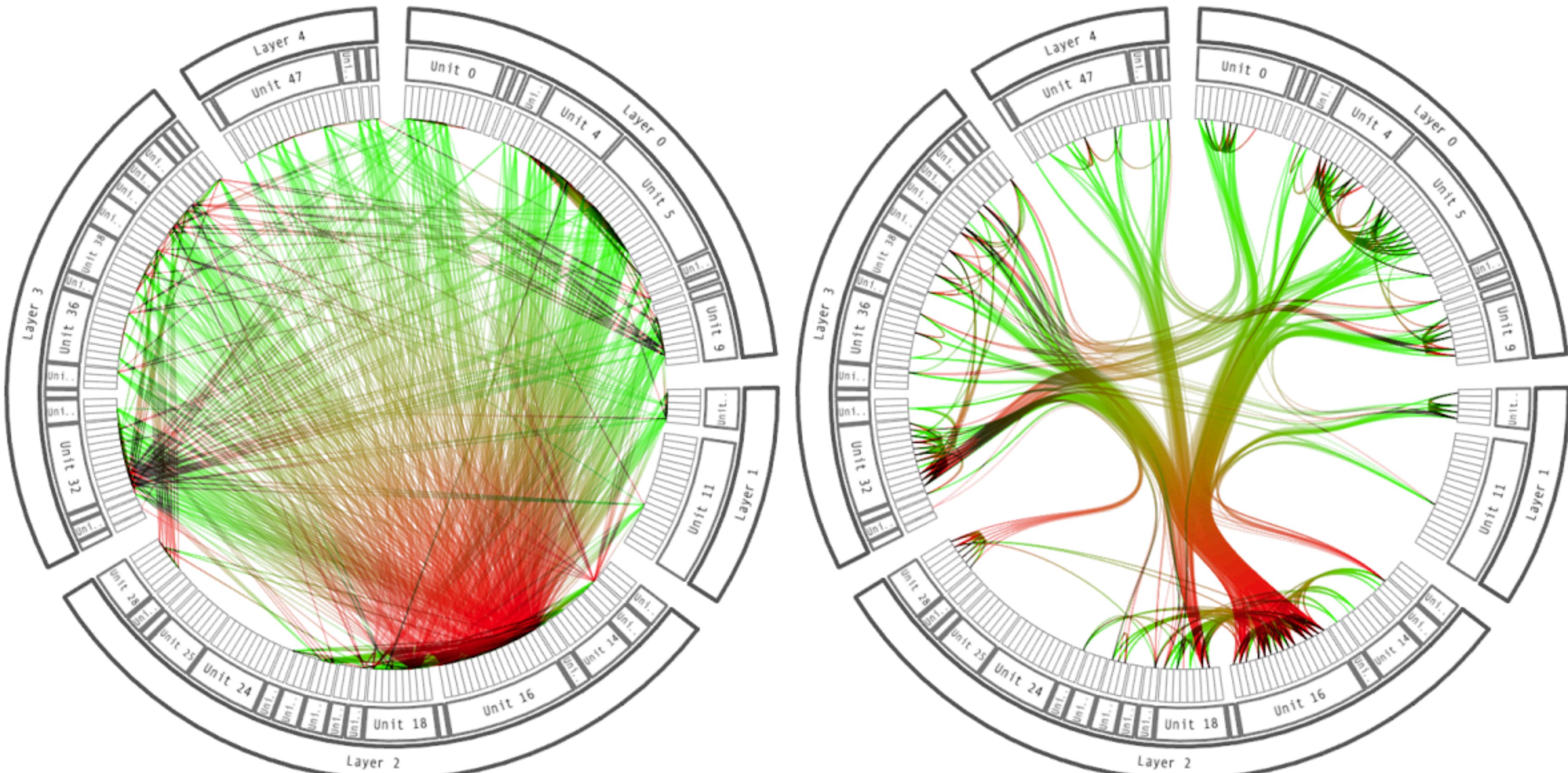
Clutter is important

Node ordering is paramount

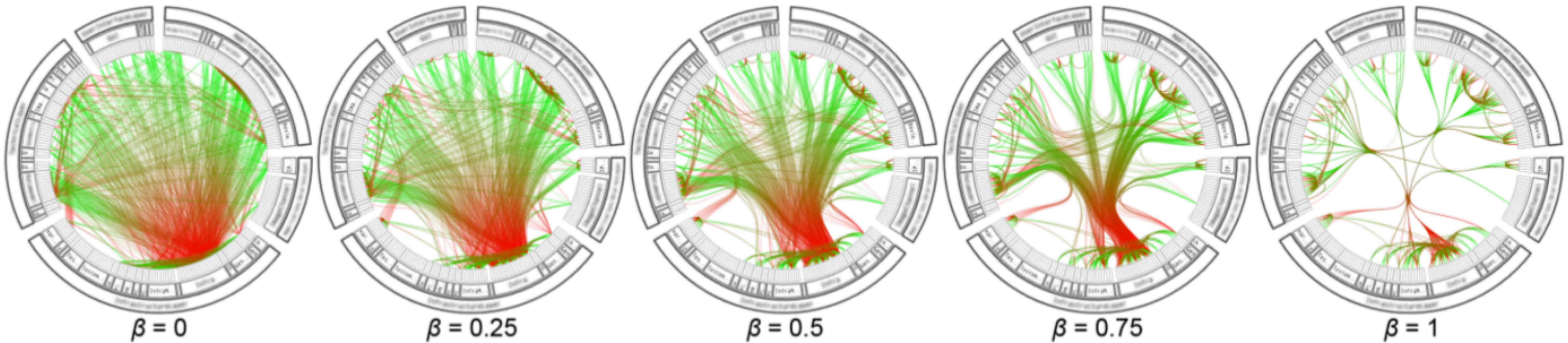
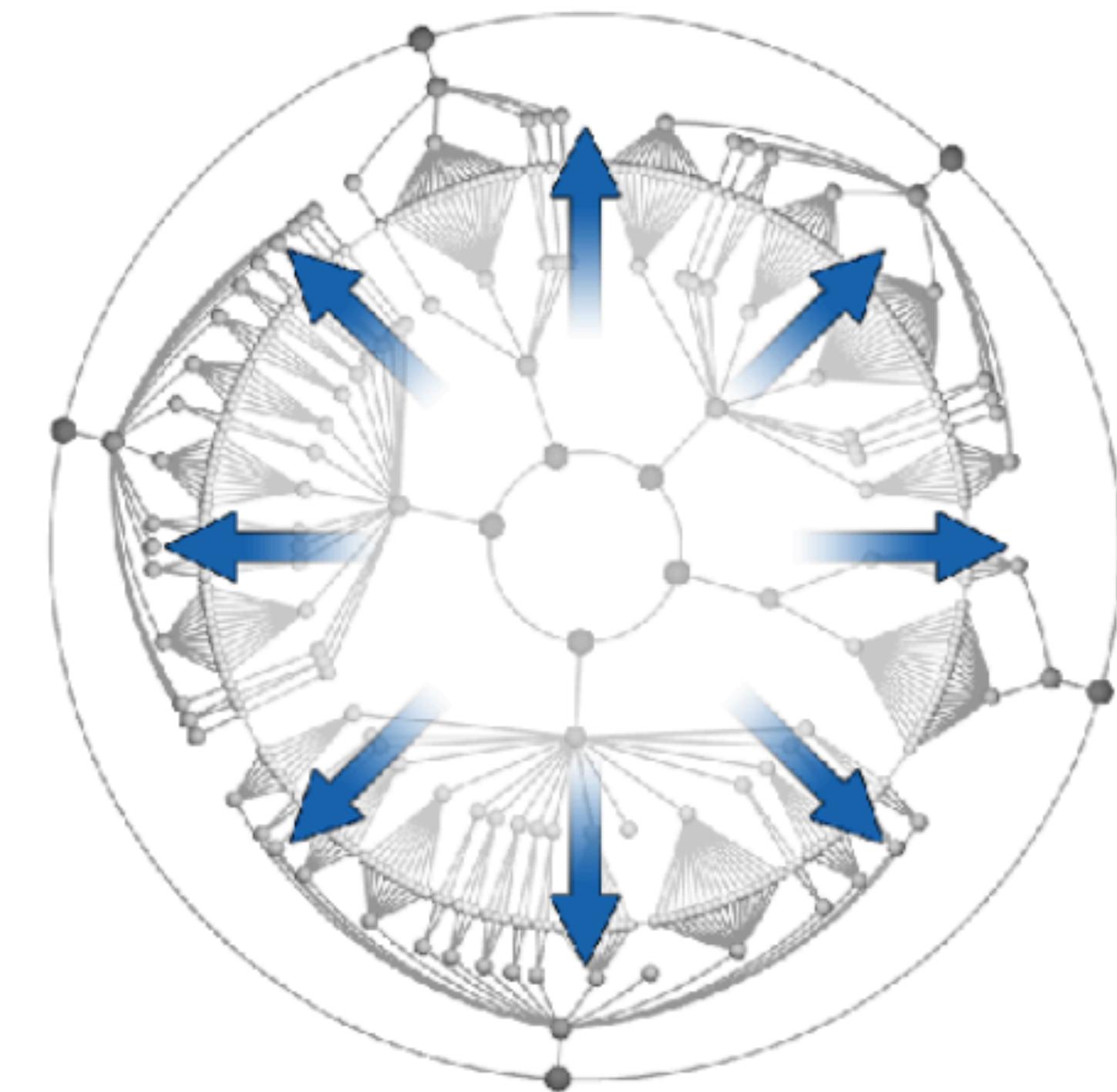
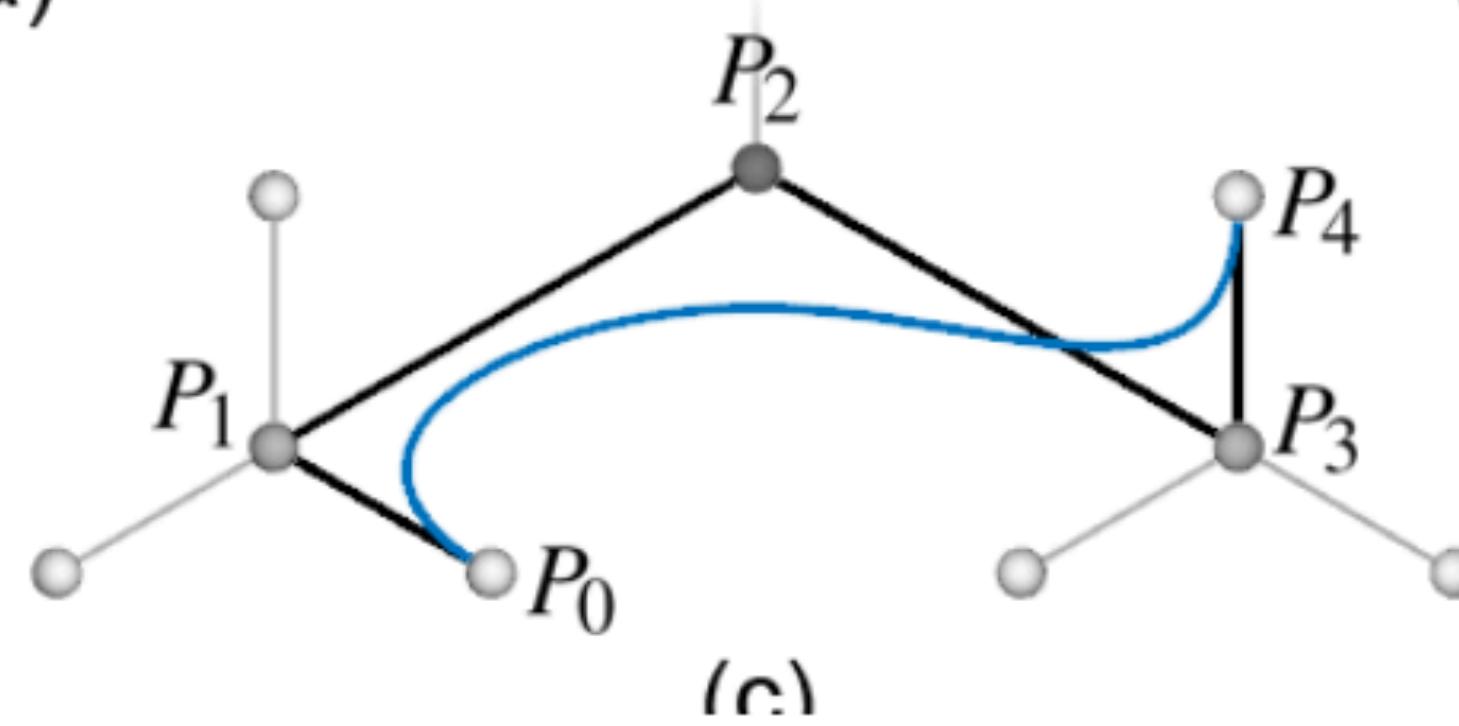
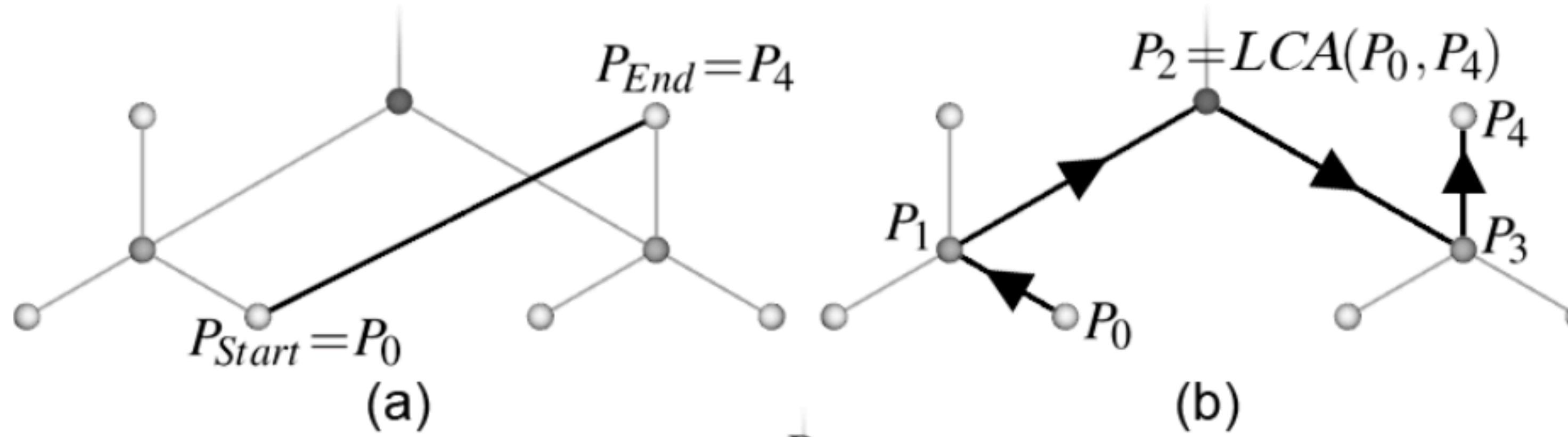


Edge bundling

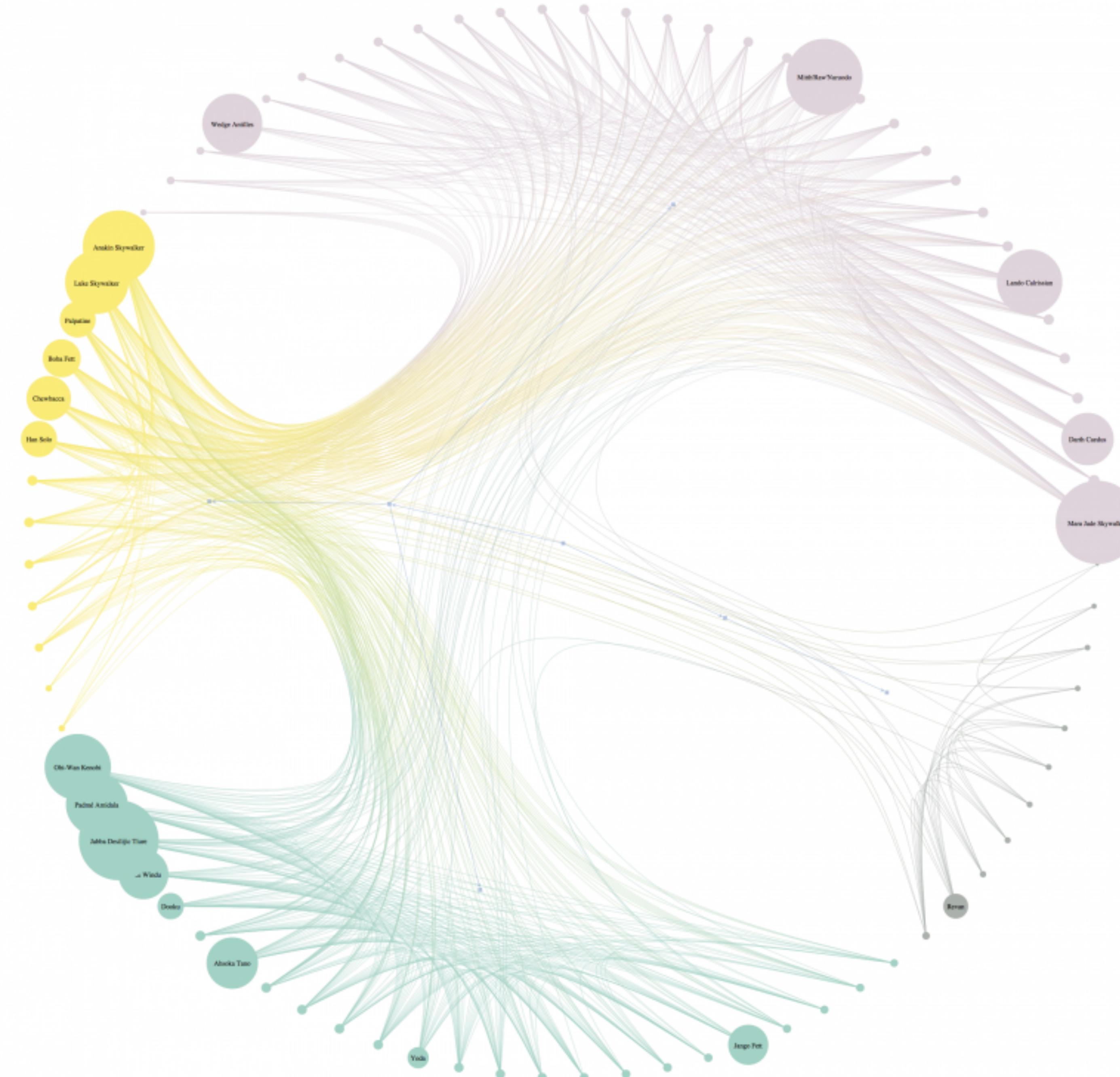
Reduce clutter by visually grouping edges

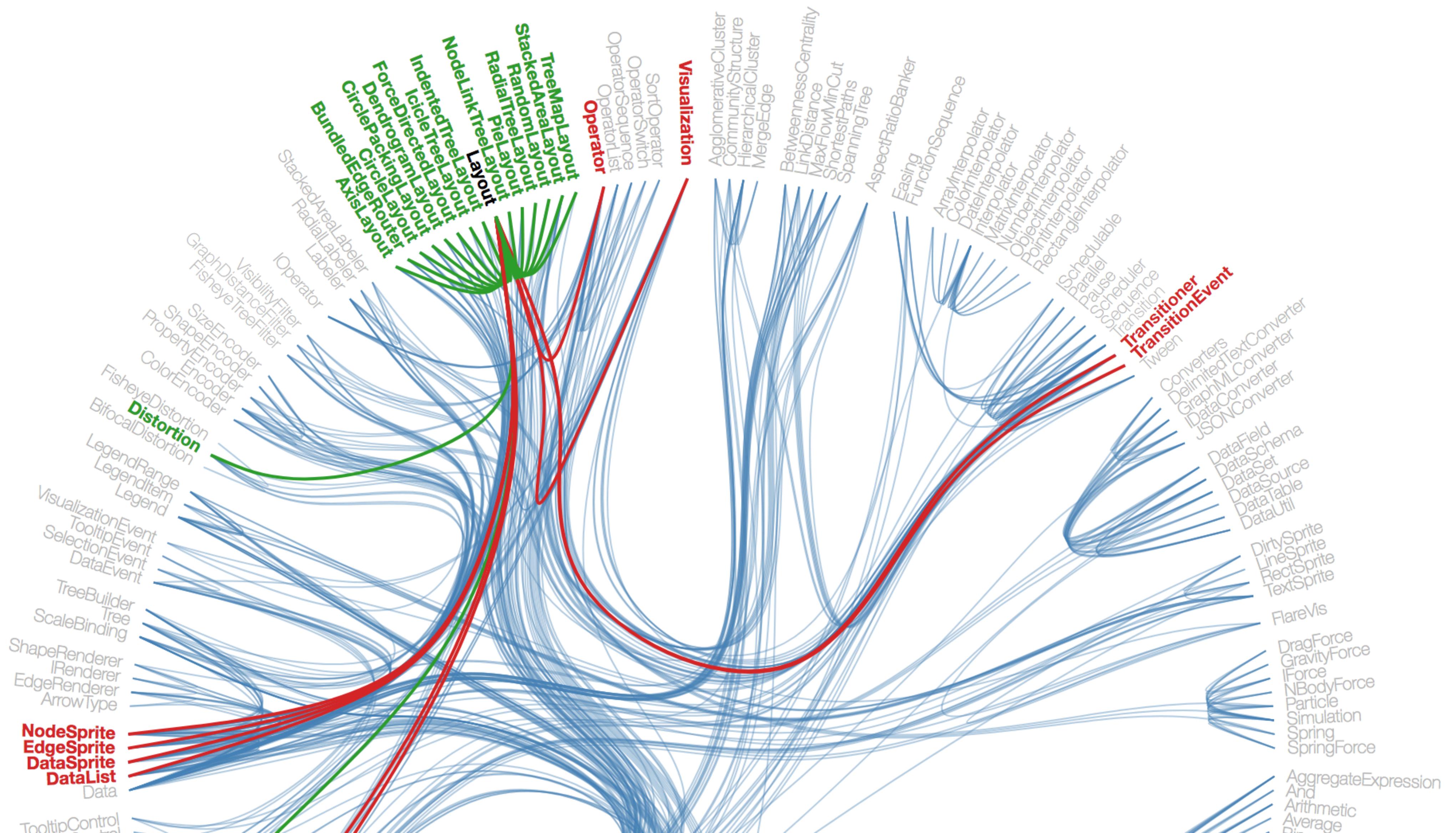


[Holten]

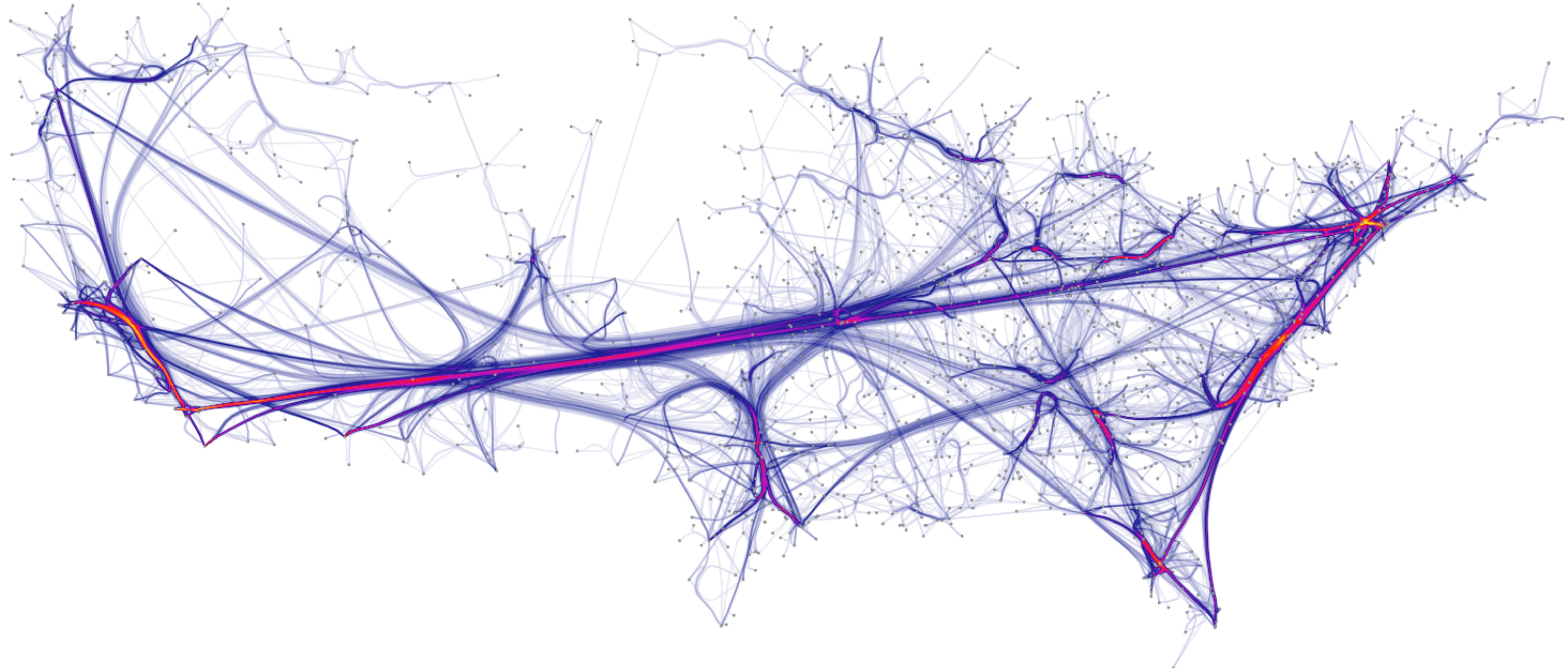


[Taken from Lex]





Fixed layout





facebook

December 2010

Node-link diagrams

Pros

Visualize all graph classes

Very flexible in the layout

Good for topology related queries (if good layout)

Cons

Tendency to clutter

Hard to find a good layout (lies in NP)

Even heuristics are still slow/complex to run

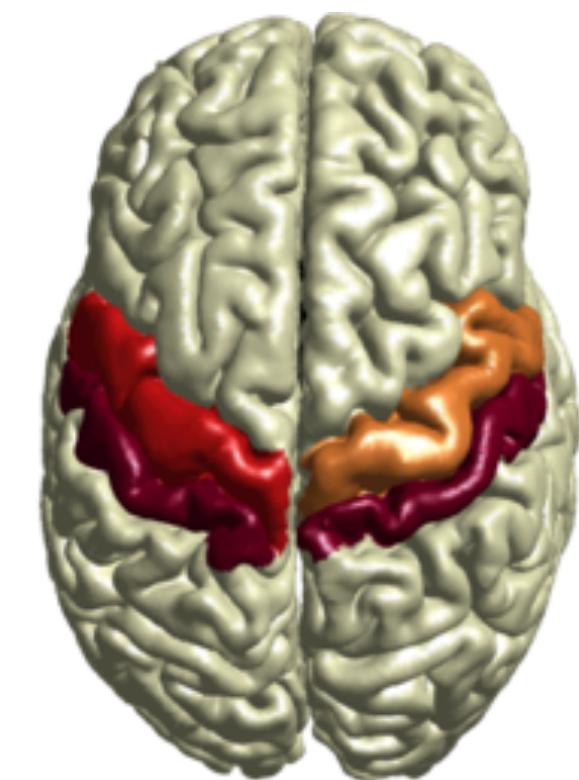
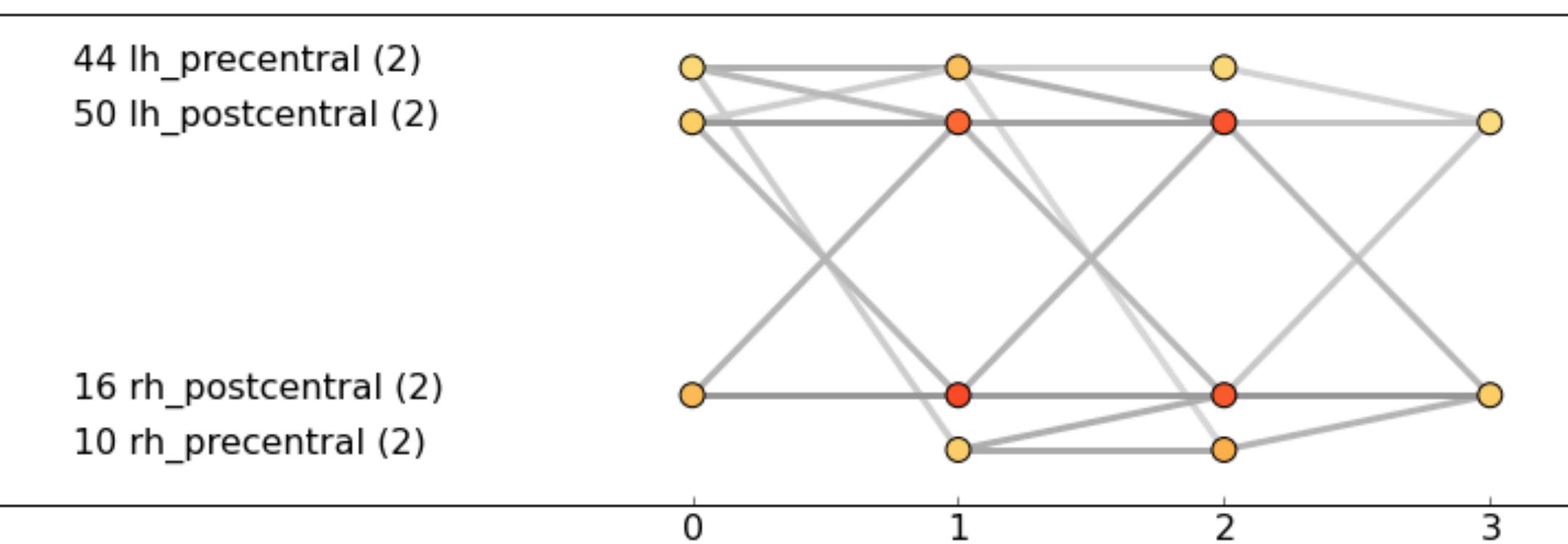
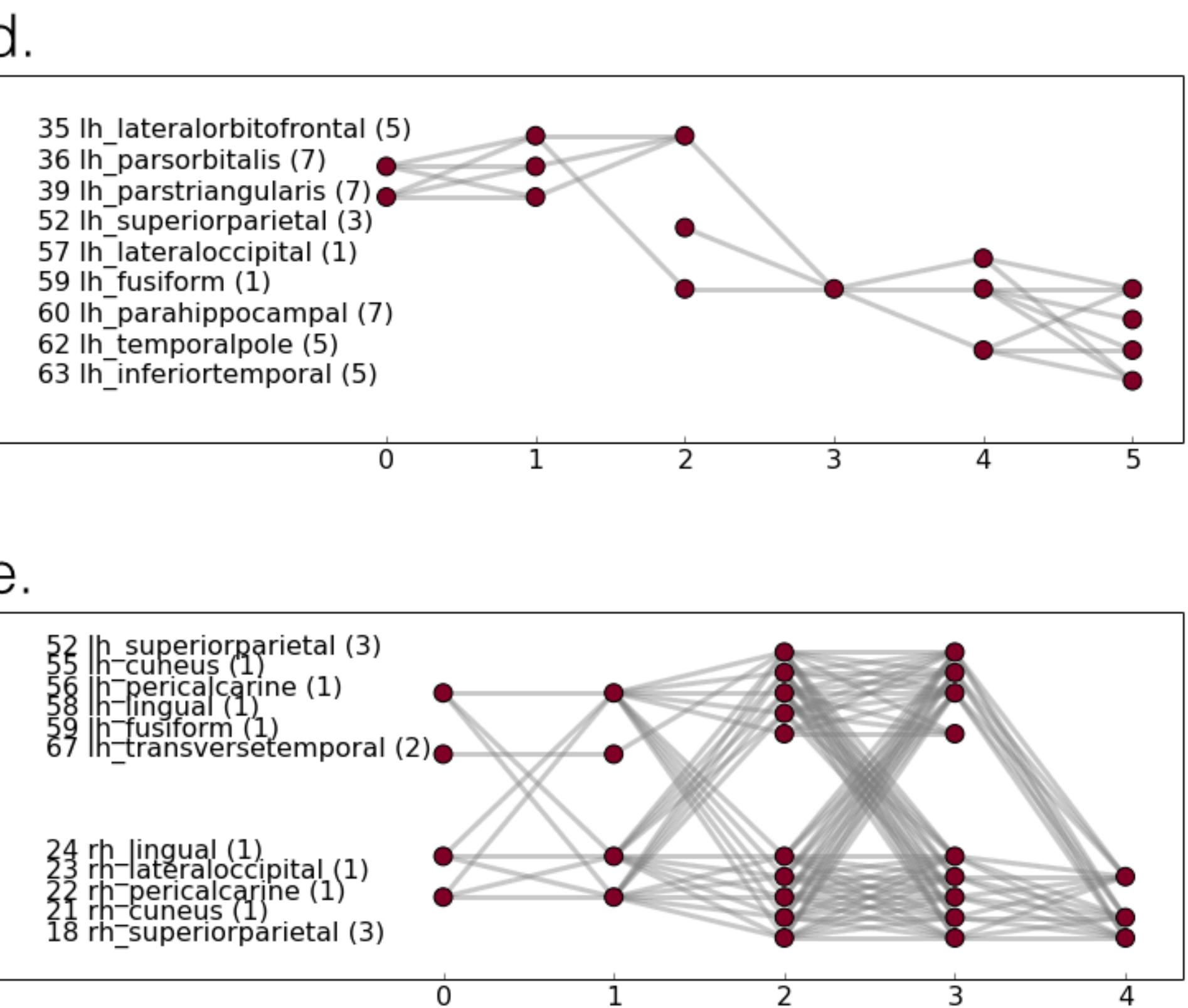
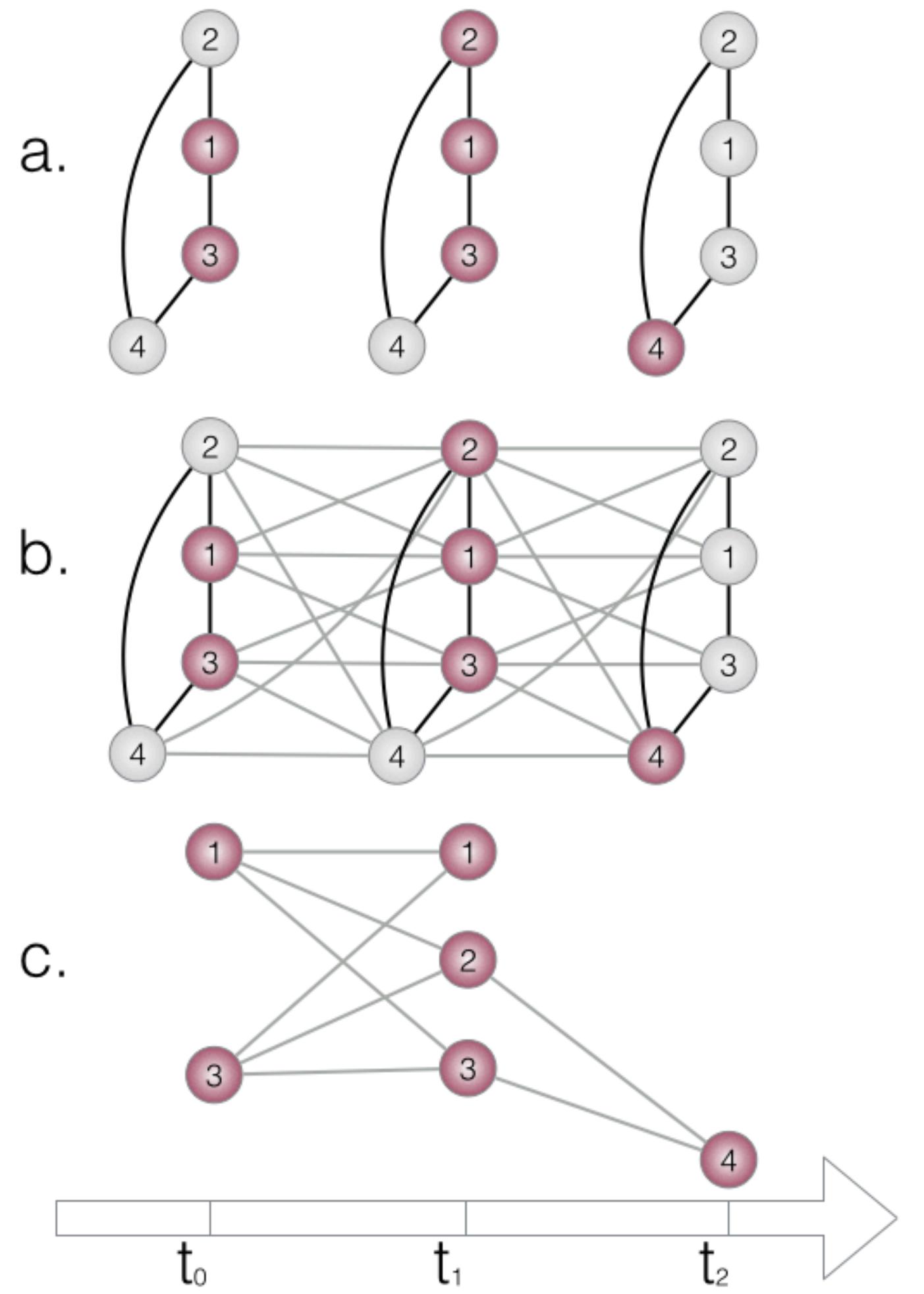
Multivariate graphs

Multivariate Graphs

How to represent both the topology and attributes on the graph?

Attributes can also influence topology

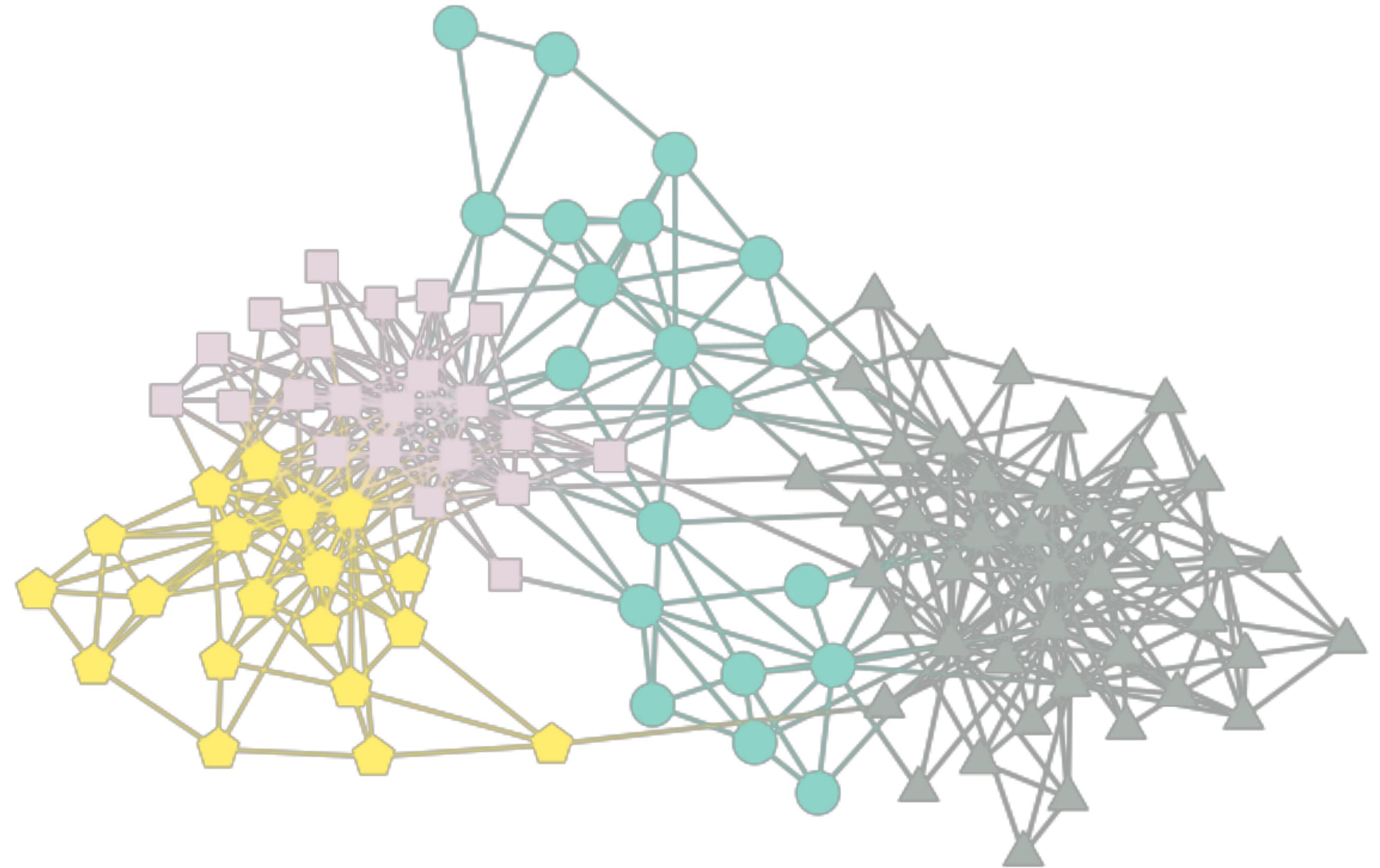
Show/hide edges or paths



Node attributes

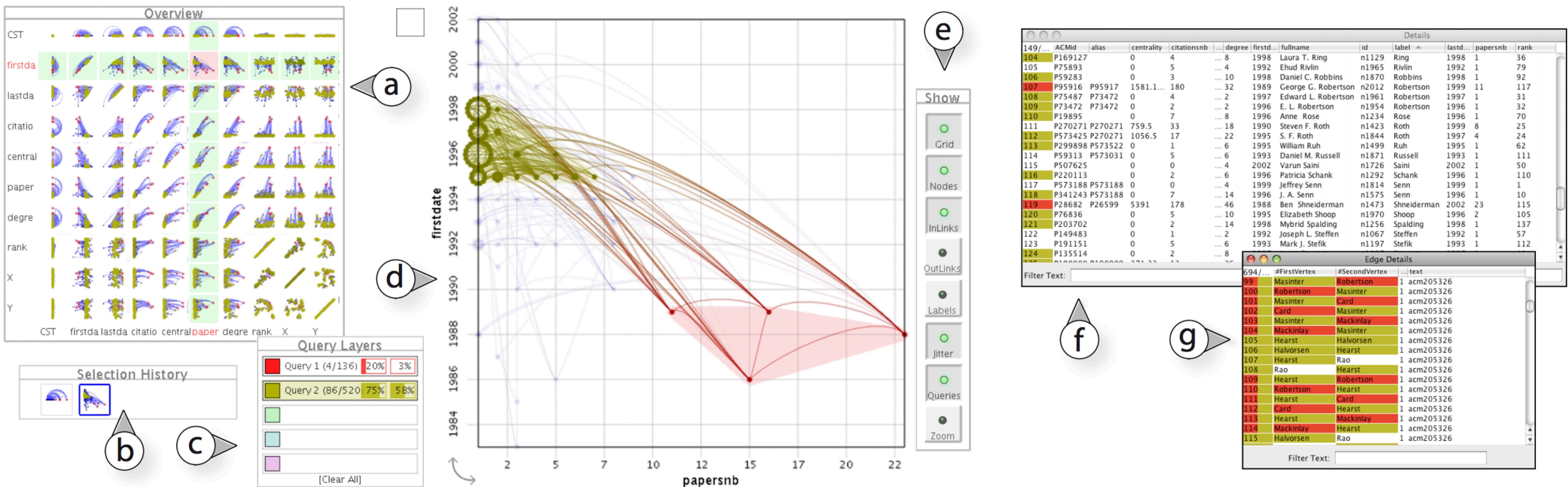
Natural choice is color or glyphs

Limited in scalability



GraphDice

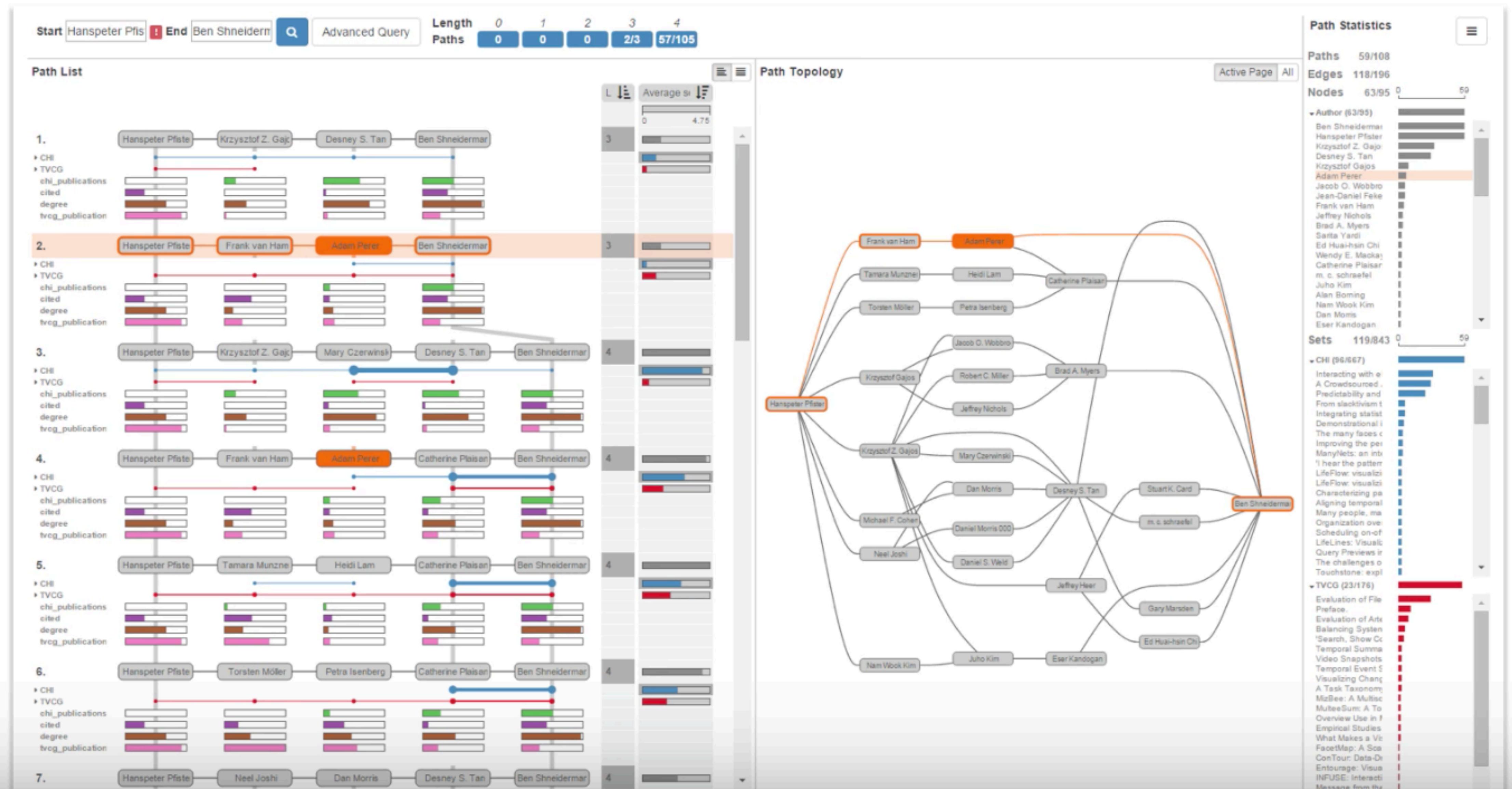
Nodes are positionned in space according to attribute values



[Bezerianos et al, 2010]

PathFinder

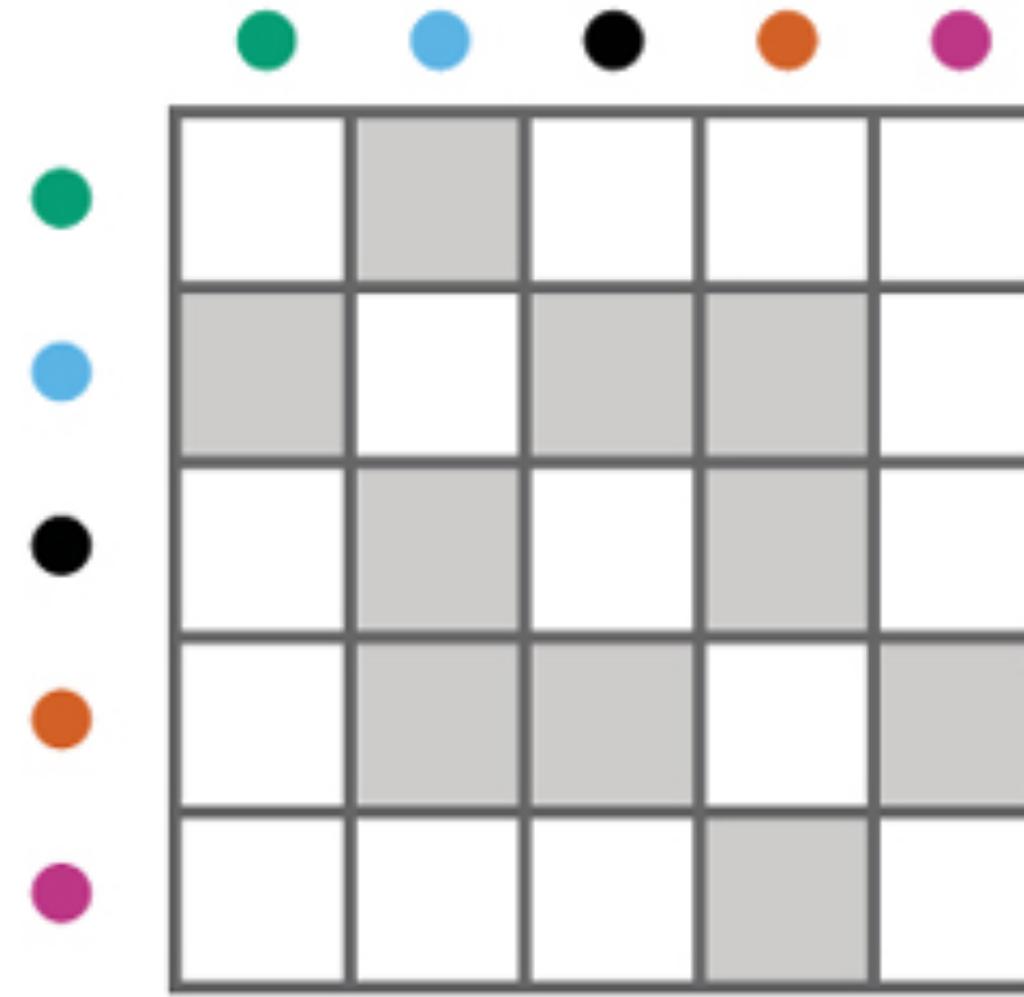
[Partl et al.]



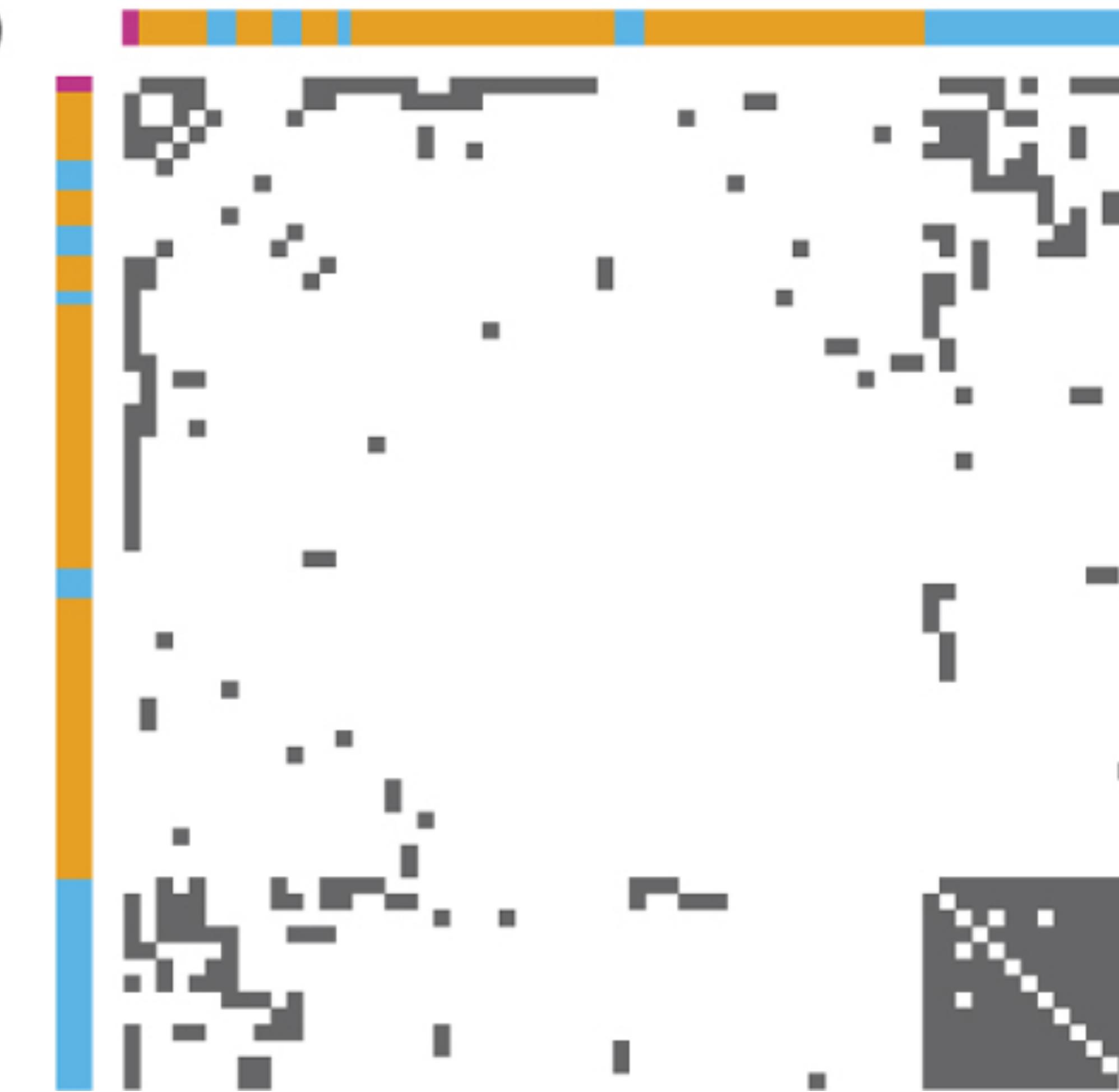
Matrix representation

Matrix representation

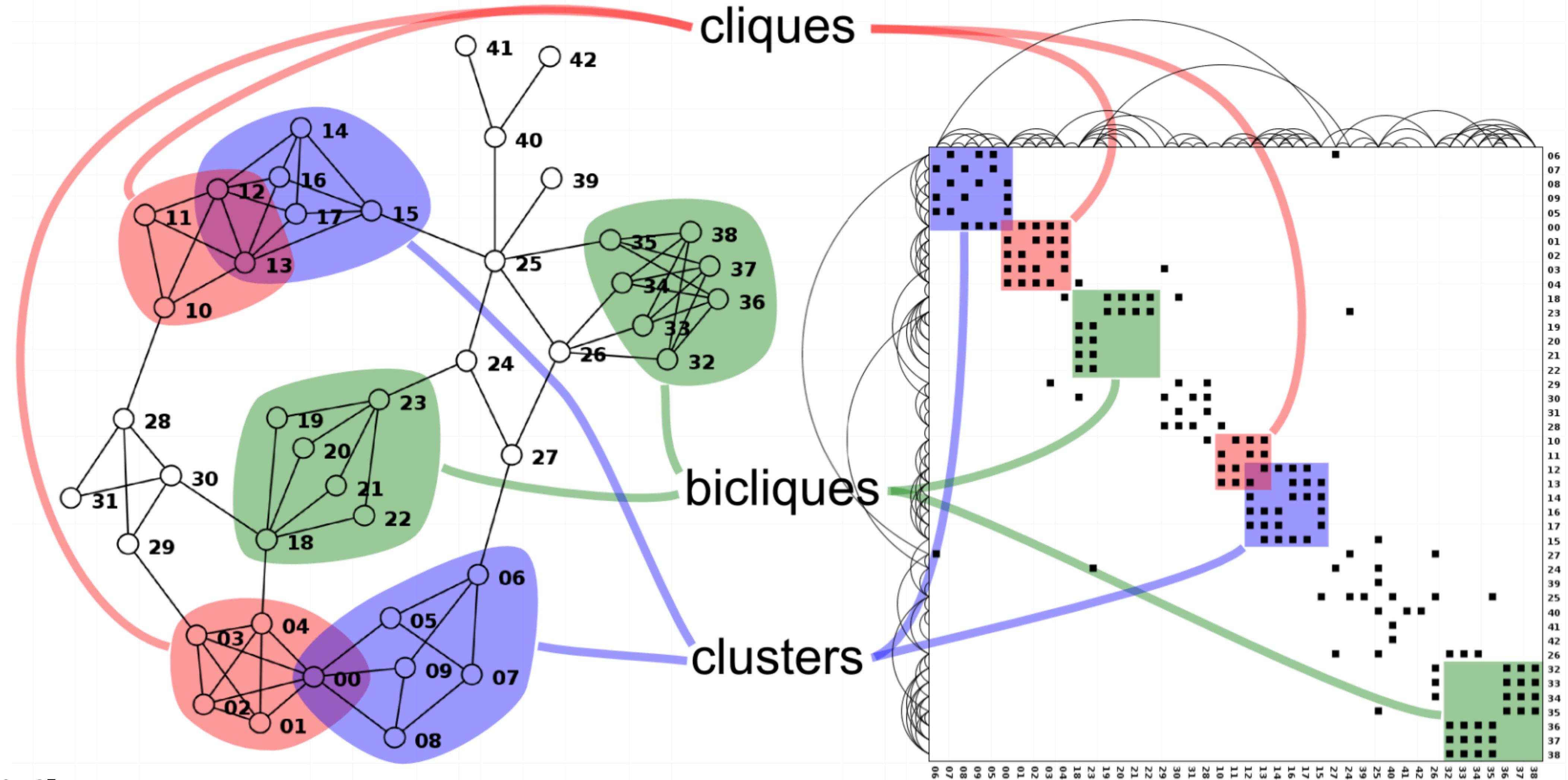
a



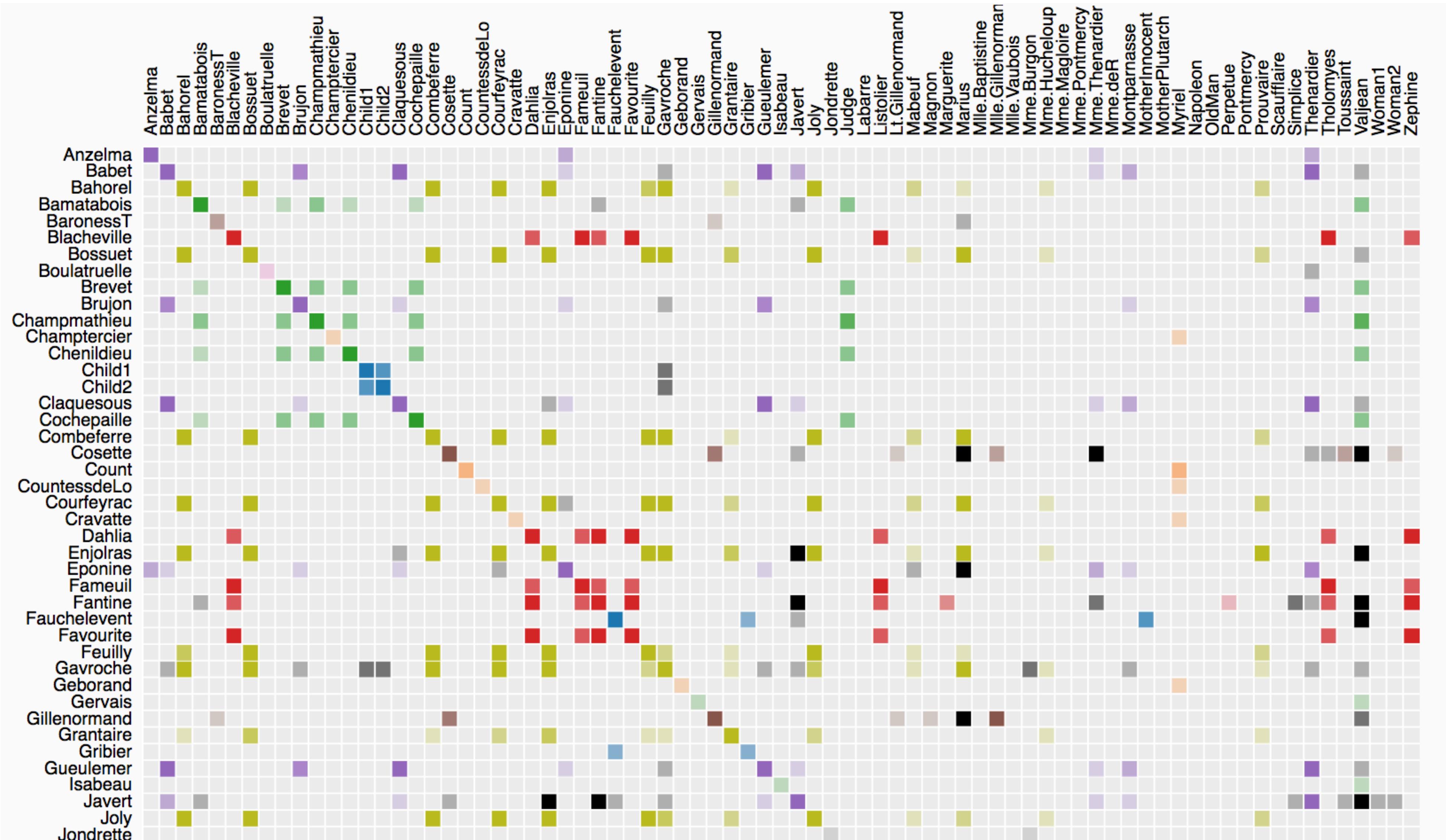
b



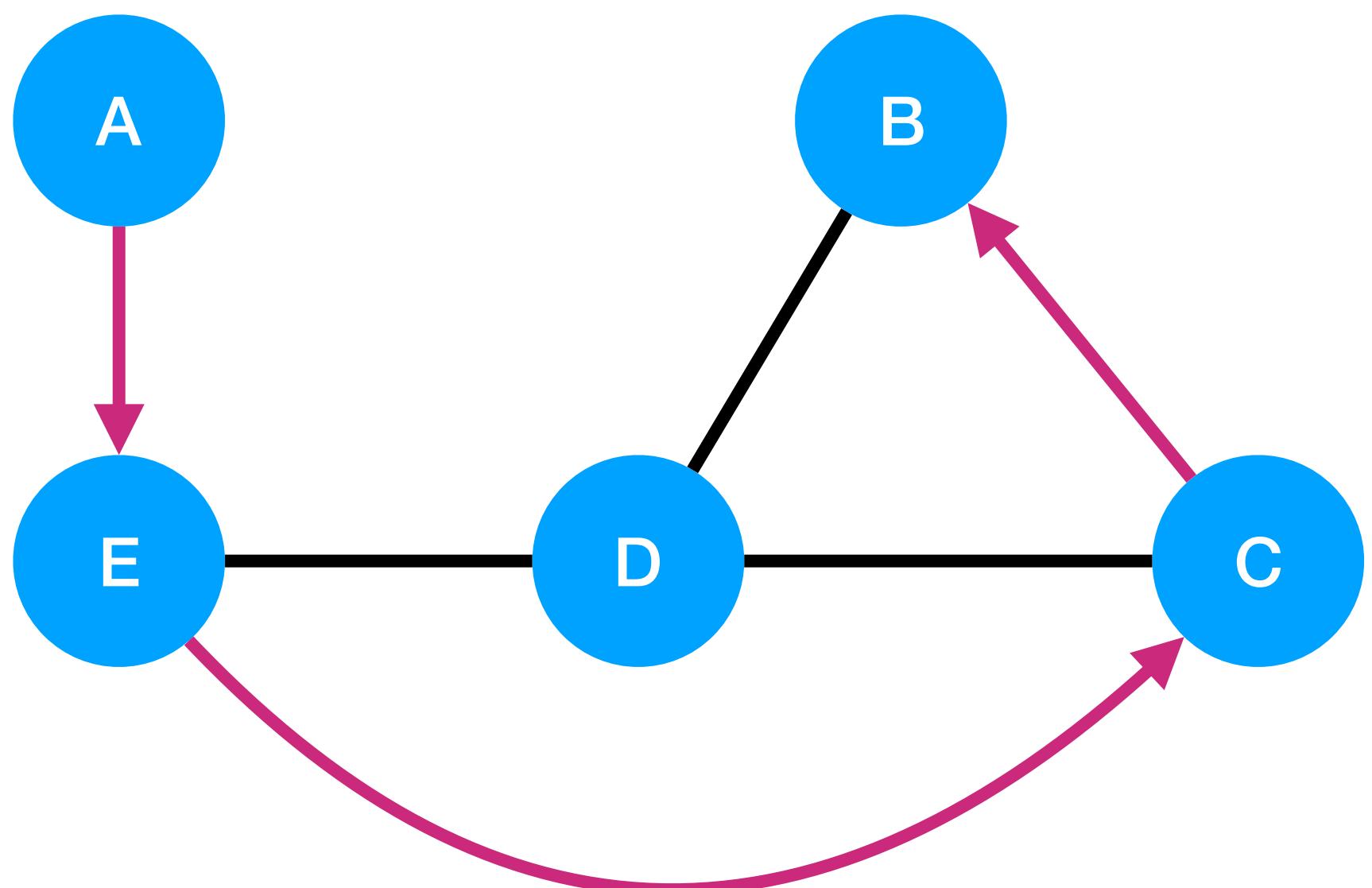
Good for neighborhood tasks



Node ordering is paramount!



Don't use for paths!



	A	B	C	D	E
A					1
B					
C			3		
D					
E	2				

Matrix-based representations

+

- No node overlapping
- No edge crossing
- Readable for dense graphs
- Fast navigation
- Fast manipulation
- More readable for some tasks

-

- Less intuitive
- Use more space
- Weak for path following tasks

Node-link diagrams

- Intuitive
- Compact
- More readable for path following
- More effective for small graphs
- More effective for sparse graphs

- Useless without layout
- Node overlapping
- Edge crossing
- Not readable for dense graphs
- Manipulation requires layout computation

Tree visualization

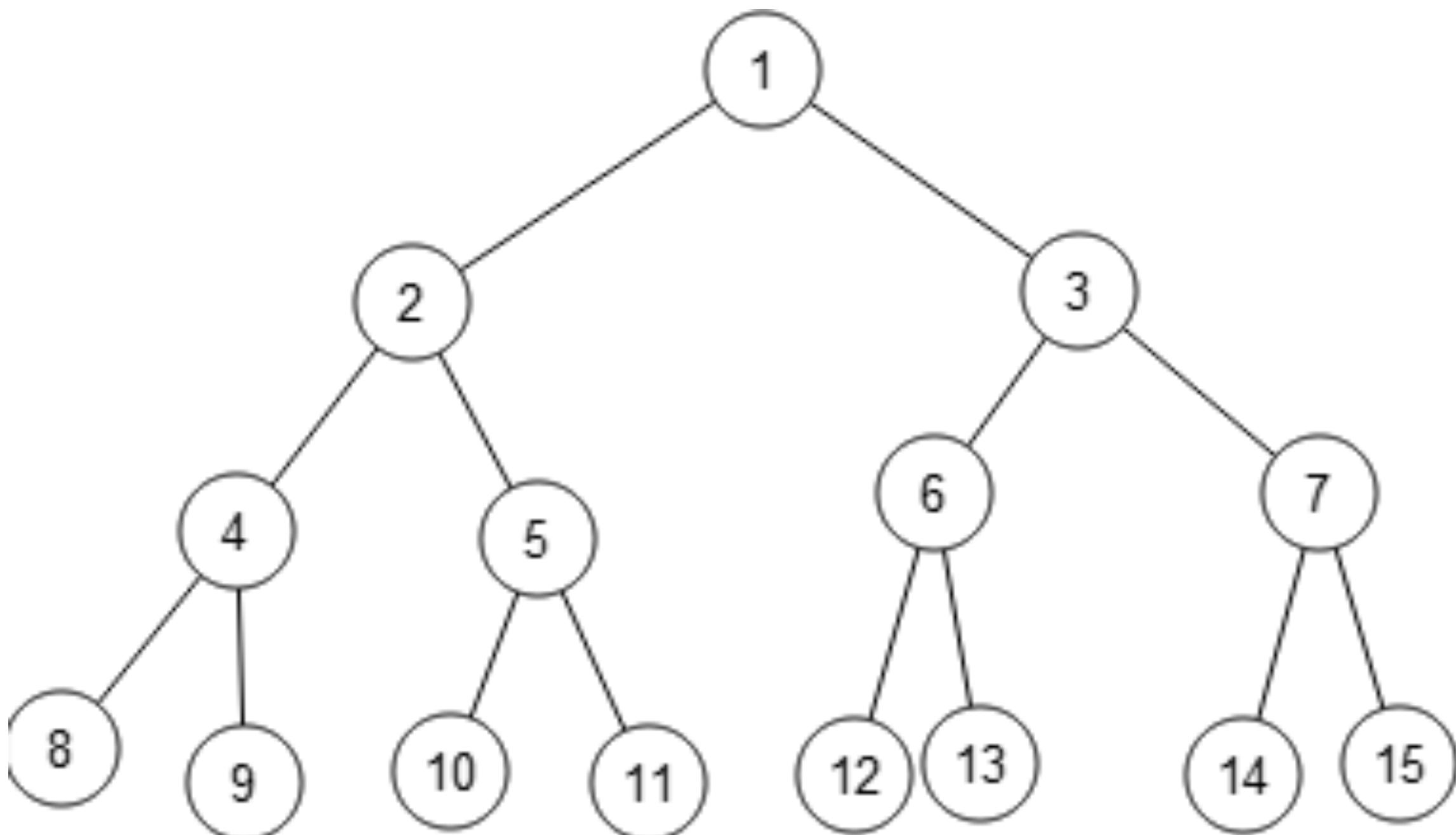
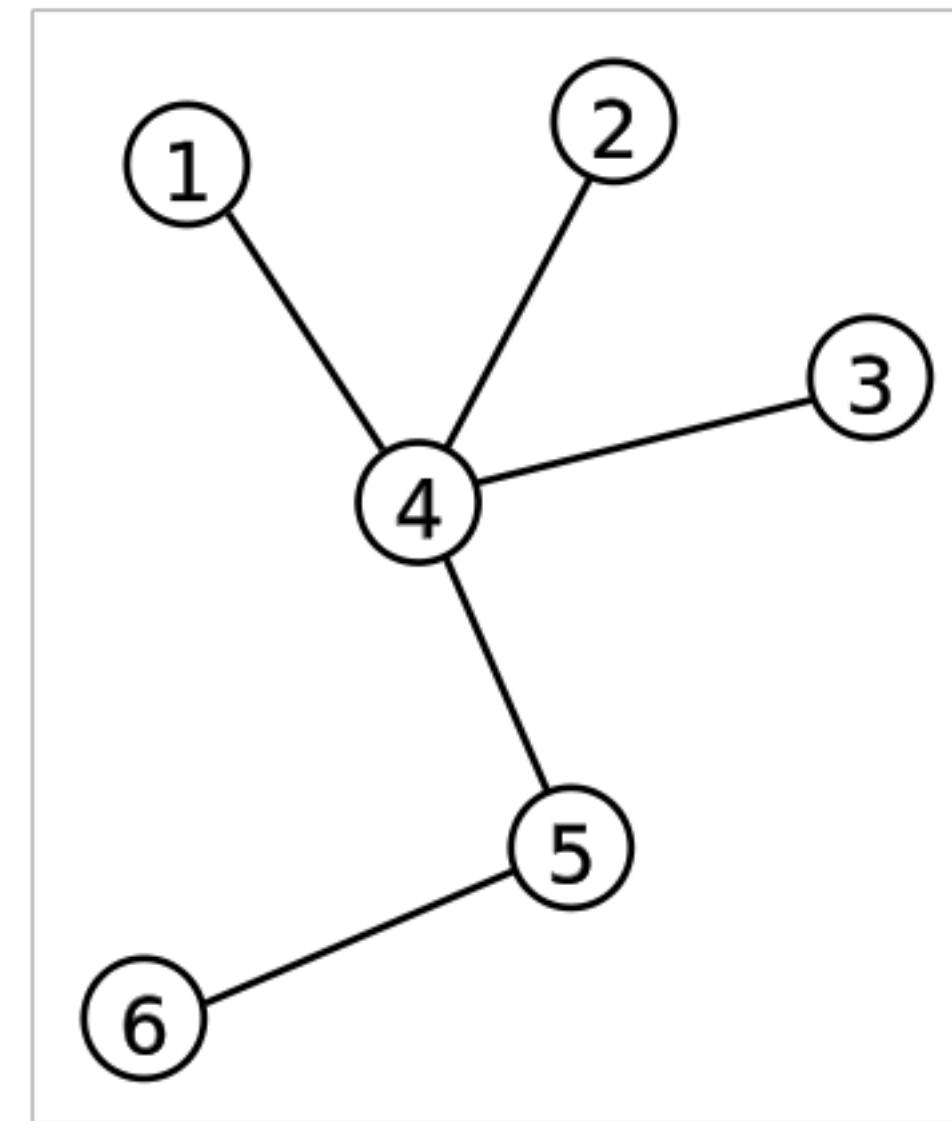
Trees

A tree is a graph with constraints:

no cycles

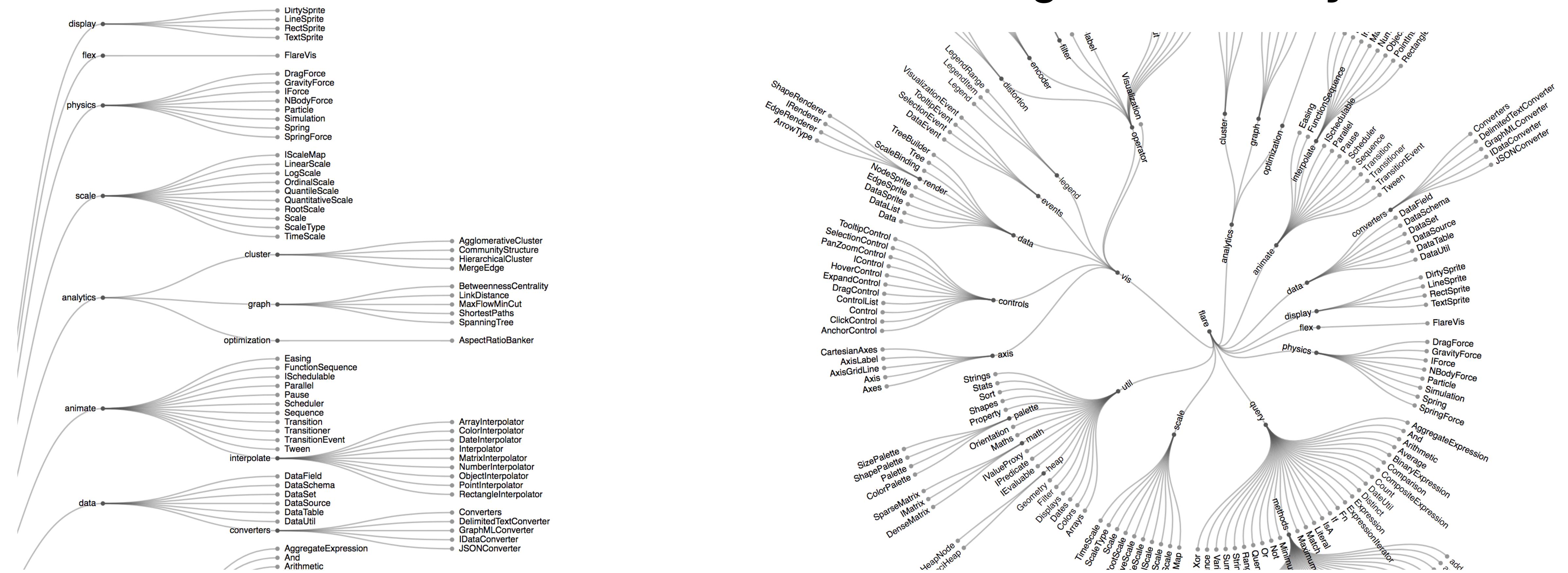
can have a root node and subtrees

can be ordered

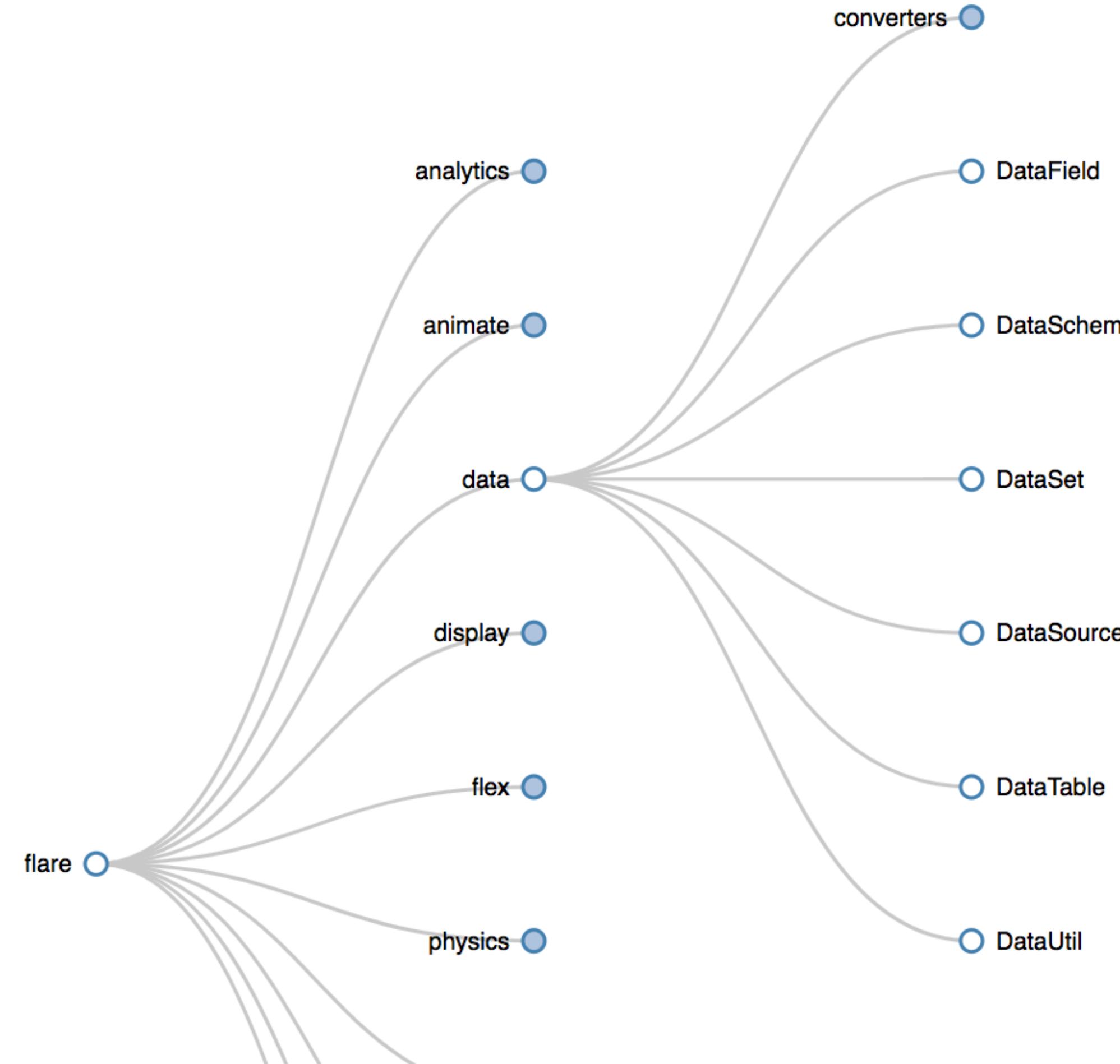


Node-link diagram

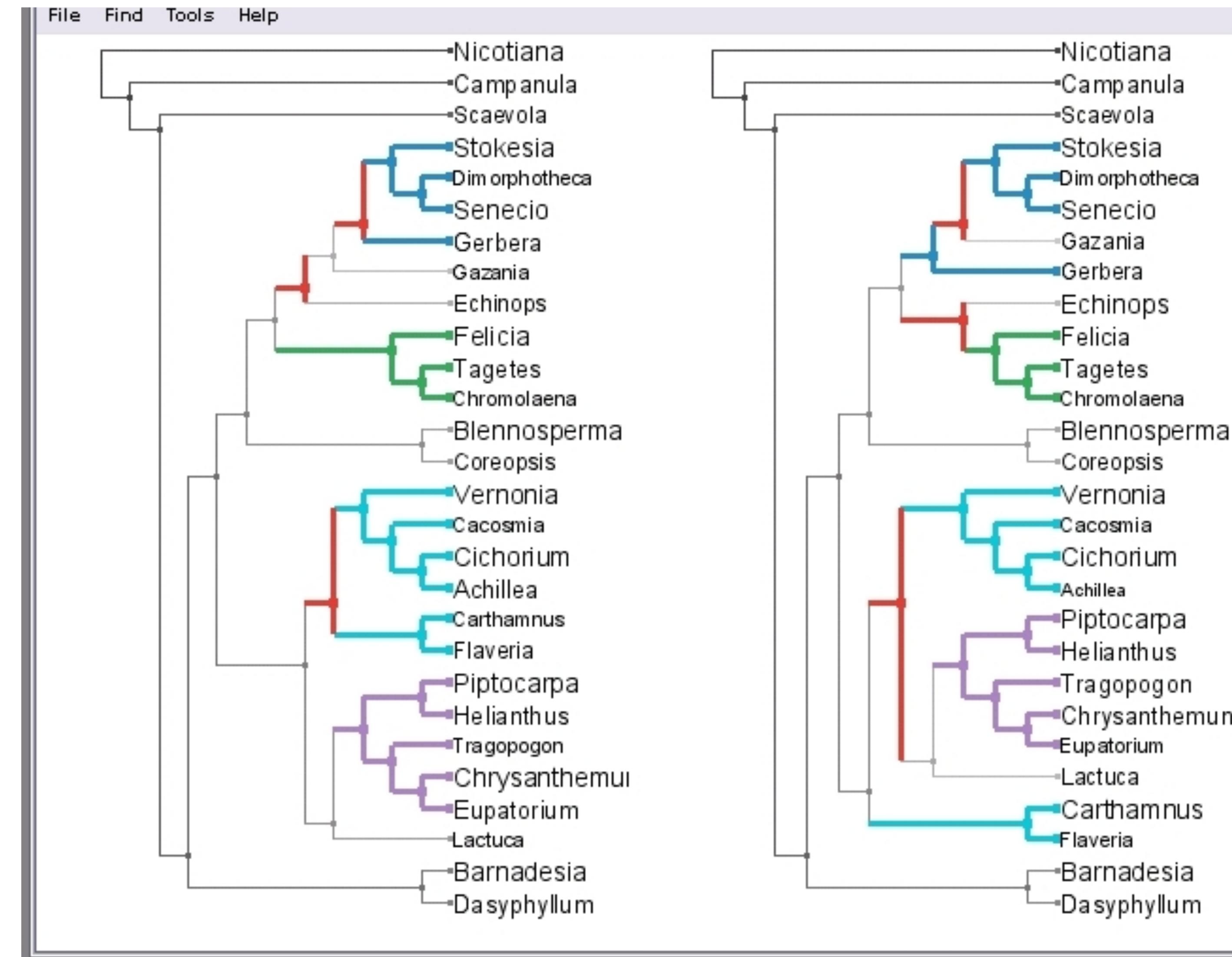
Reingold-Tilford layout



Collapsible Tree

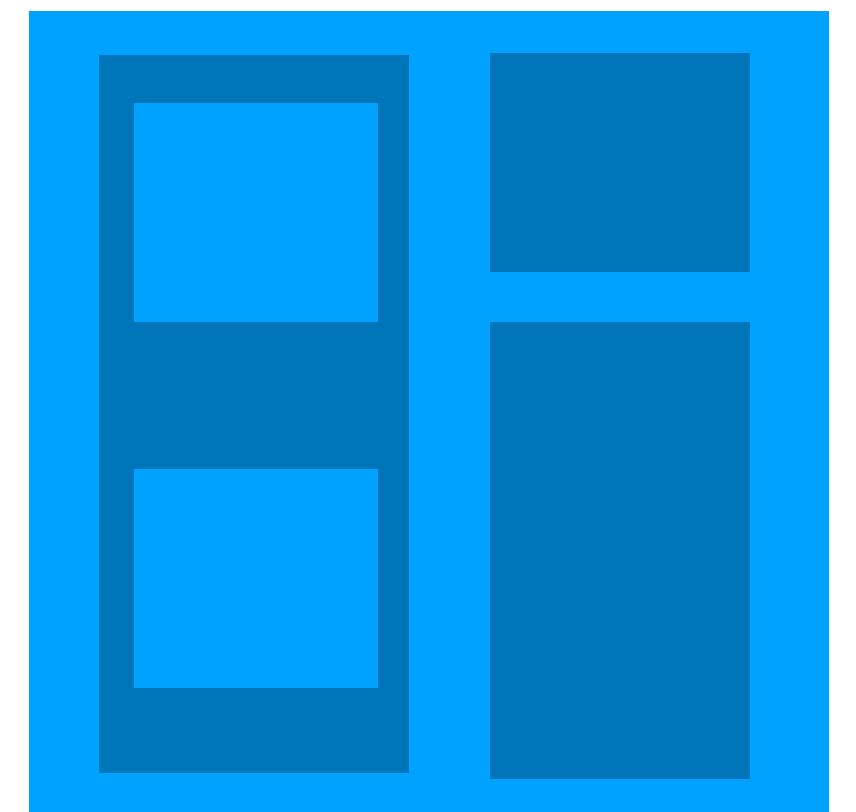


TreeJuxtaposer



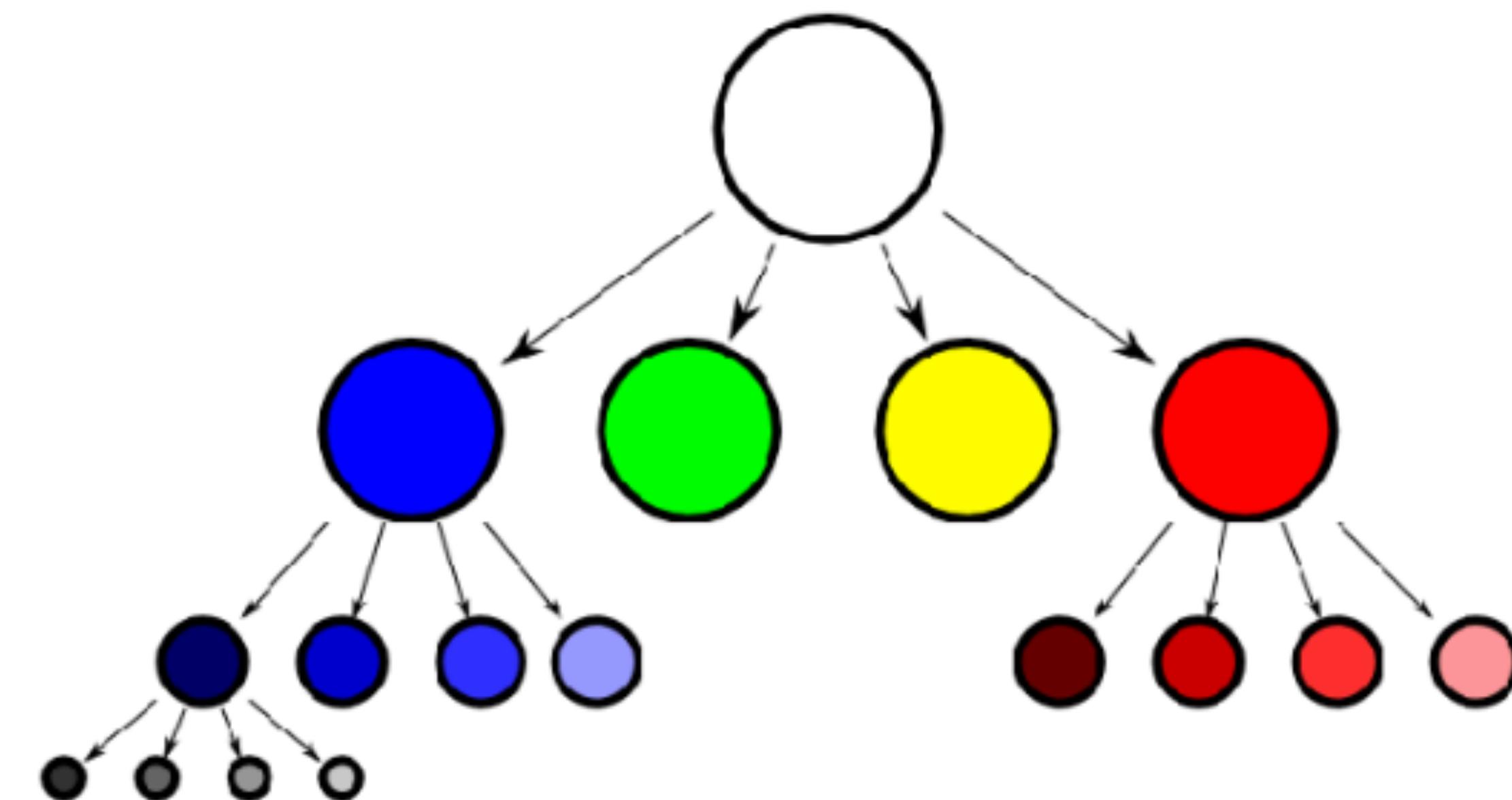
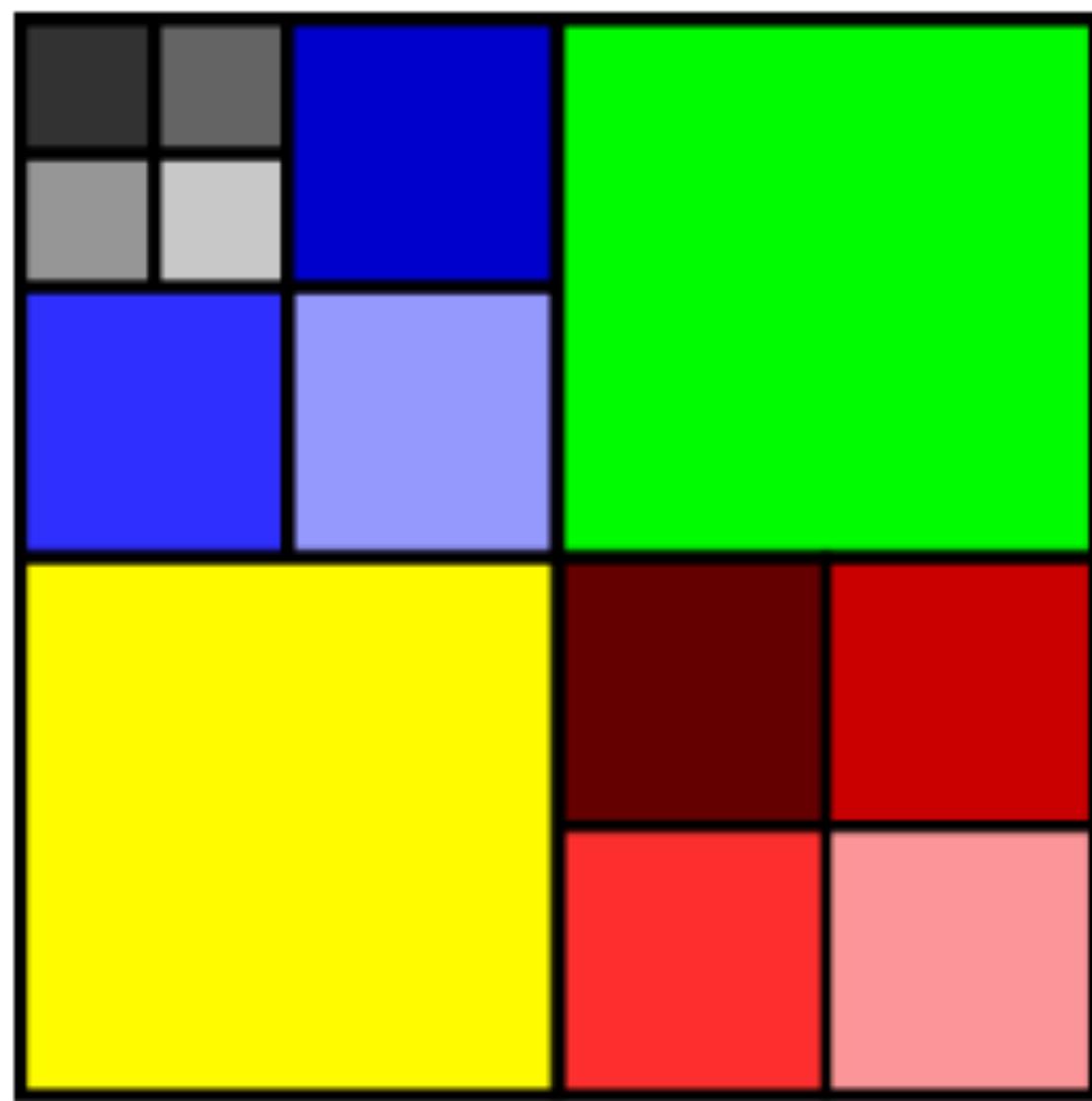
TreeMap

Implicit layout for tree



Display hierarchical (tree-structured) data as a set of nested rectangles

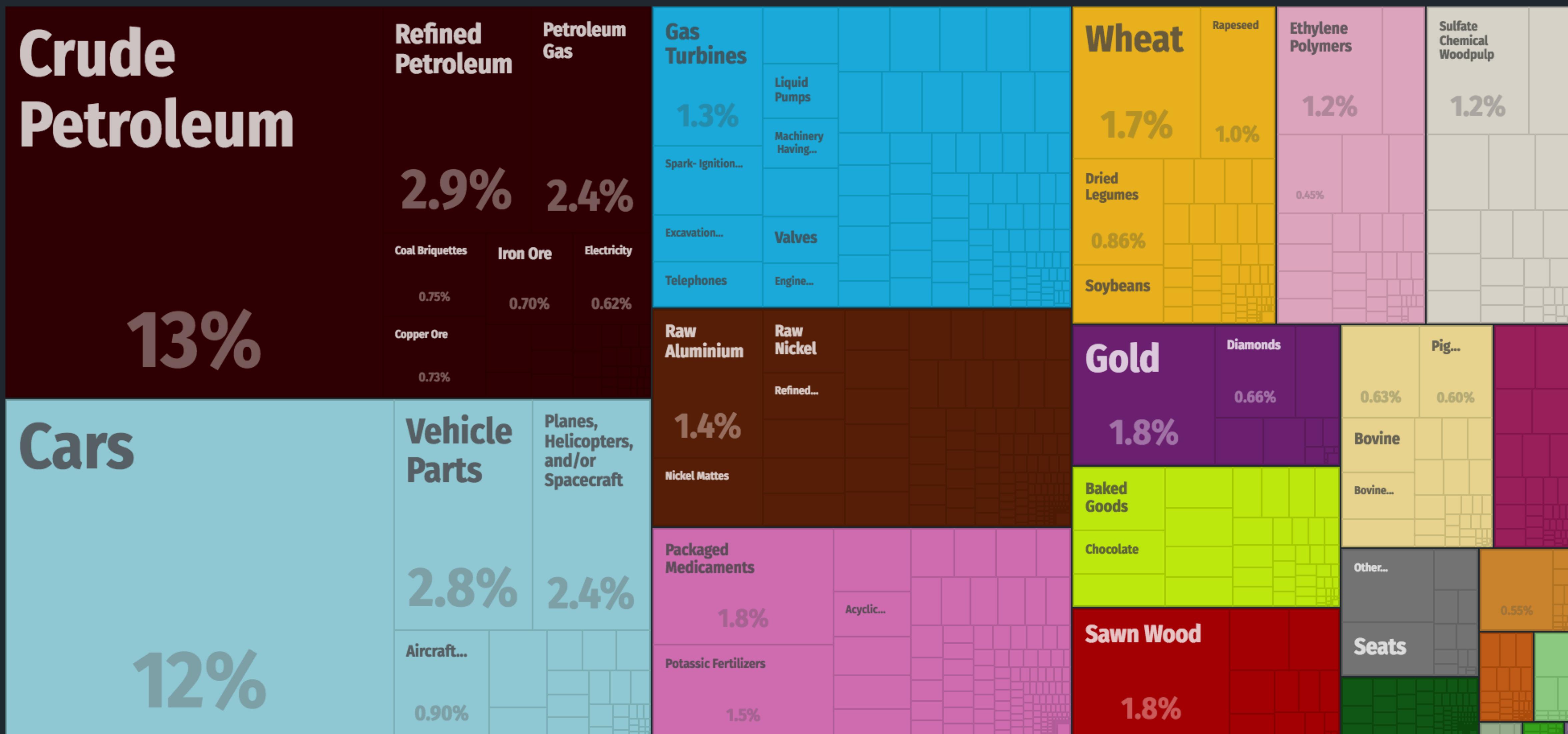
Efficient use of space

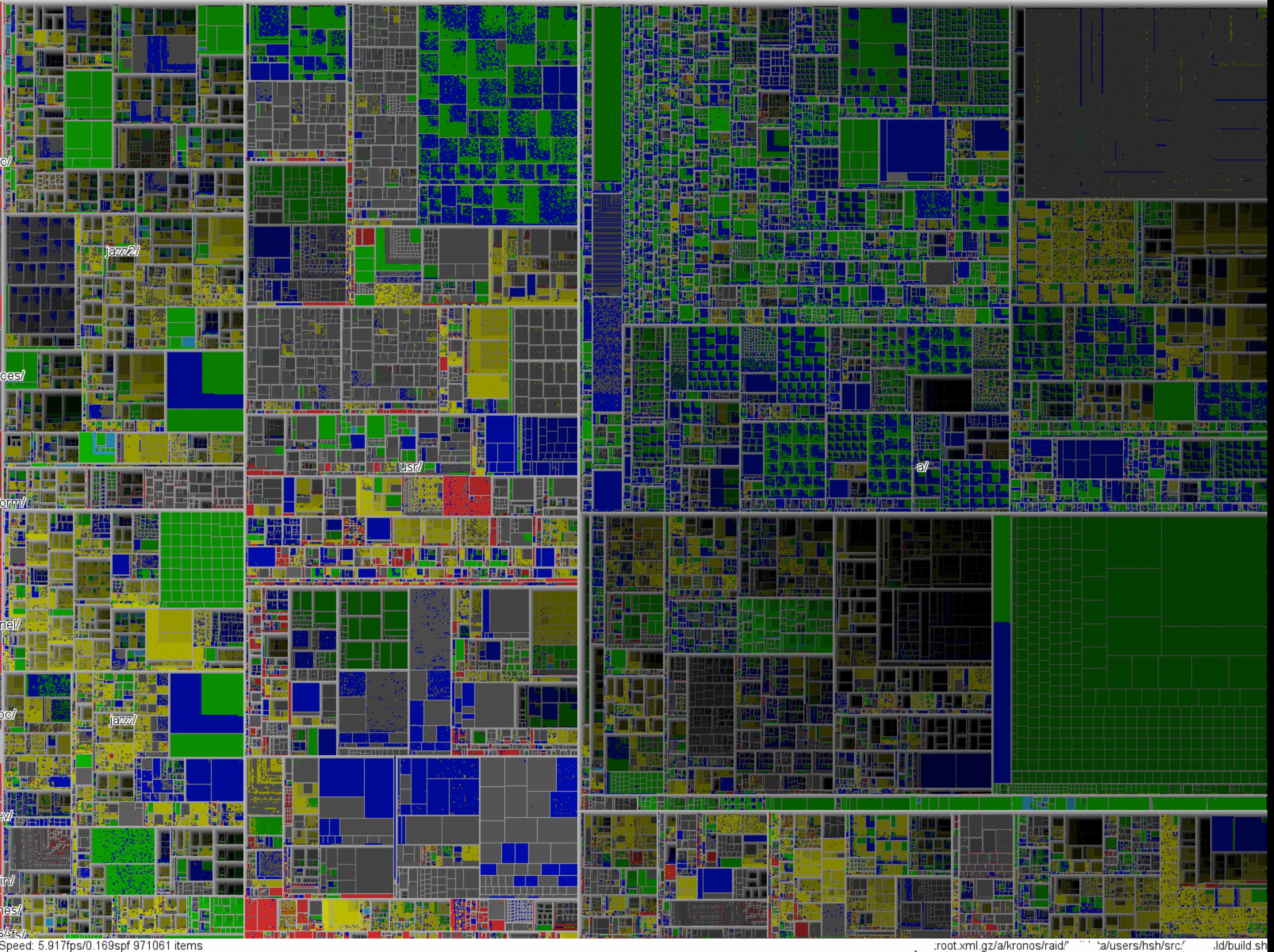


<2014

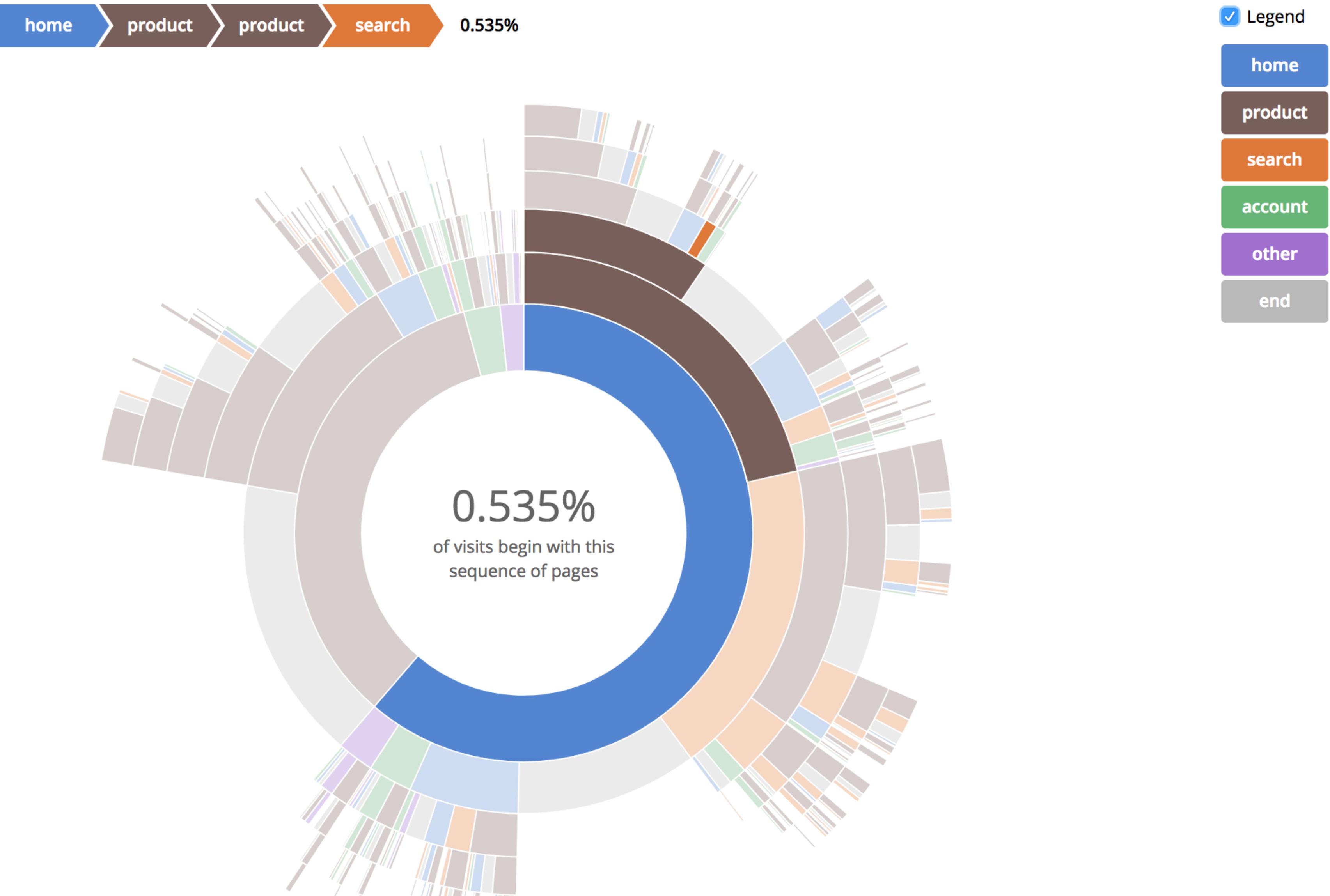
What does Canada export? (2015)

TOTAL: \$390B





Radial layout



Implicit visualization

Pros

Space-efficient because there is no need to draw the edges

Scale well up to large graphs

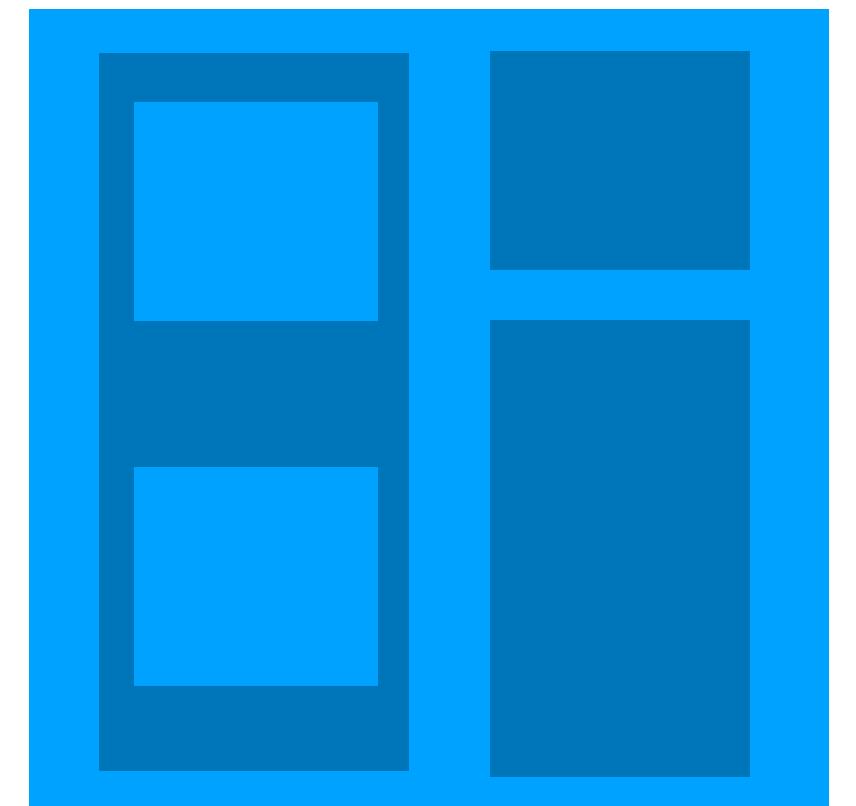
Useful for Attribute based tasks on nodes, also useful for simple paths related tasks

Cons

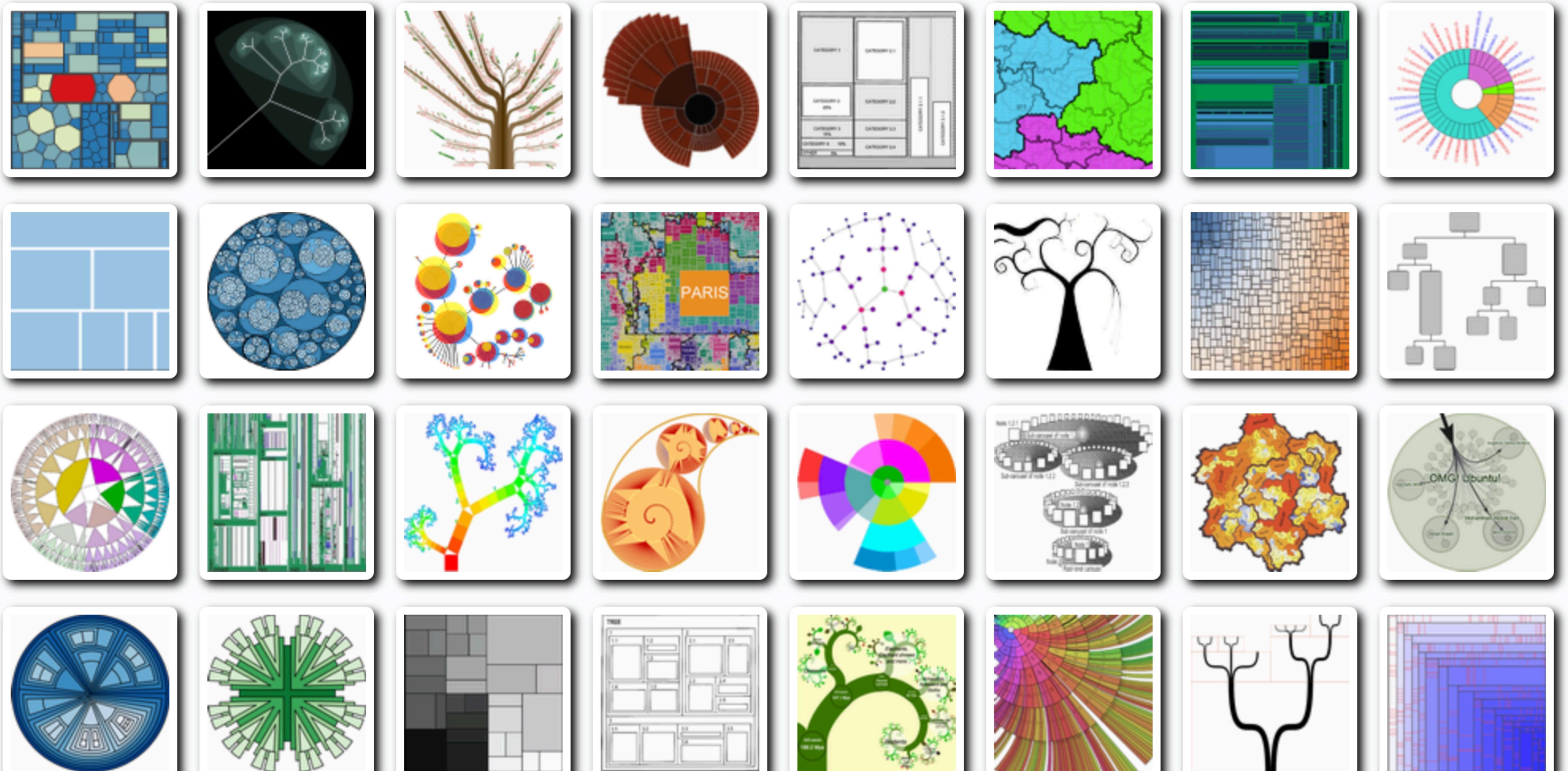
Only works for trees

Nodes cannot be freely arranged in space, no edges

Spatial relations such as overlap or inclusion lead to occlusion



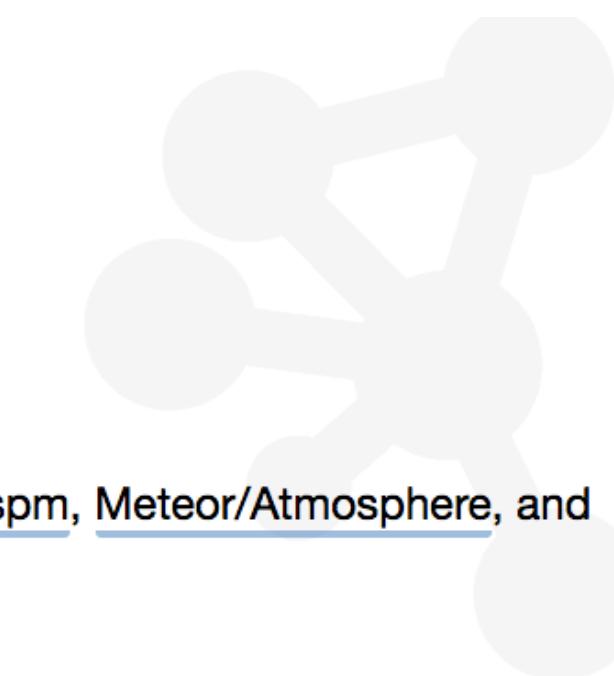
More on tree viz



Tools, libraries

Cytoscape.js

Graph theory / network library for analysis and visualisation



Supports [CommonJS](#)/[Node.js](#)/[Browserify](#)/[Webpack](#), [AMD](#)/[Require.js](#), [jQuery](#), [npm](#), [CDNJS](#), [Bower](#), [jspm](#), [Meteor/Atmosphere](#), and plain JS/JavaScript



[Extensions](#) [News & tutorials](#) [Twitter](#) [Gitter](#) [File a GitHub issue](#)

[Contribute](#) [Search previous questions via Stack Overflow \(or ask a different question\)](#)

Like Cytoscape.js?



[Star it on GitHub](#)

[Share it on Twitter](#)

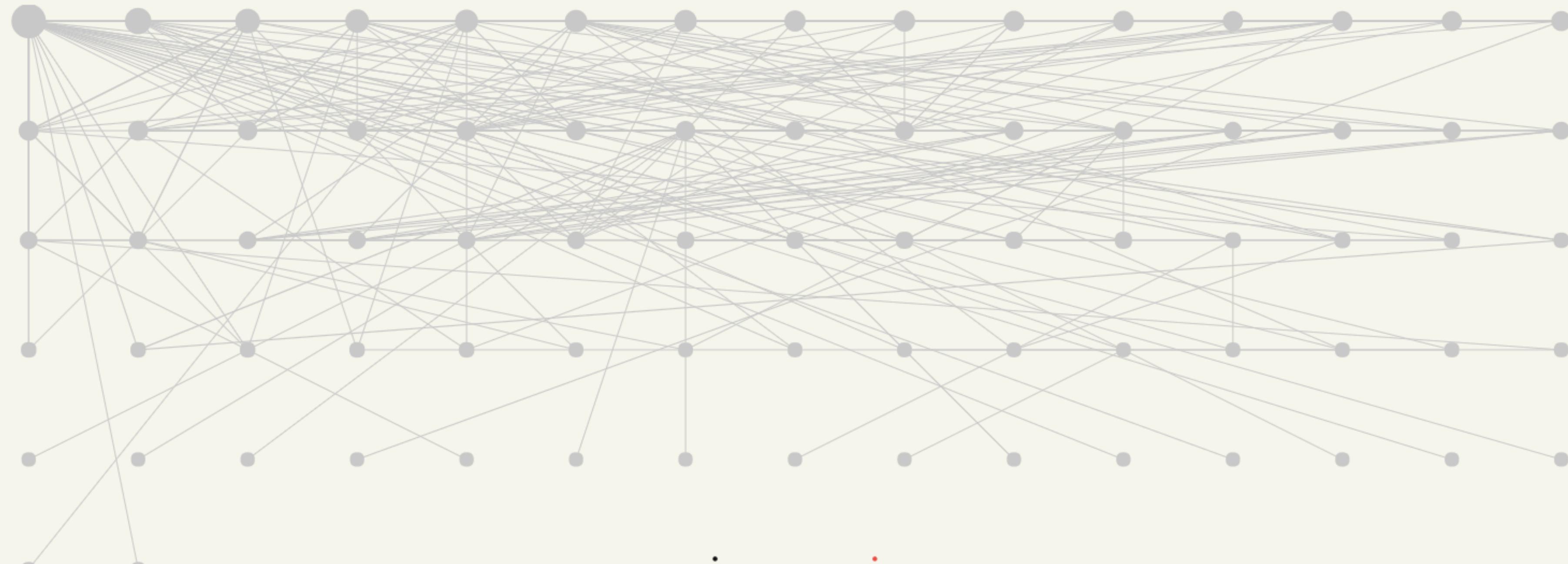
[Share it on Google+](#)

Donations are tax deductible to a 501(c)(3) nonprofit organization, The Cytoscape Consortium, Tax ID: 20-4909879.

Use Cytoscape.js? [Let us know](#)

Demos





sigmajs

 TUTORIAL

v1.2.0

DOWNLOAD 

The Open Graph Viz Platform

Gephi is the leading visualization and exploration software for all kinds of graphs and networks. Gephi is open-source and free.

Runs on Windows, Mac OS X and Linux.

[Learn More on Gephi Platform »](#)

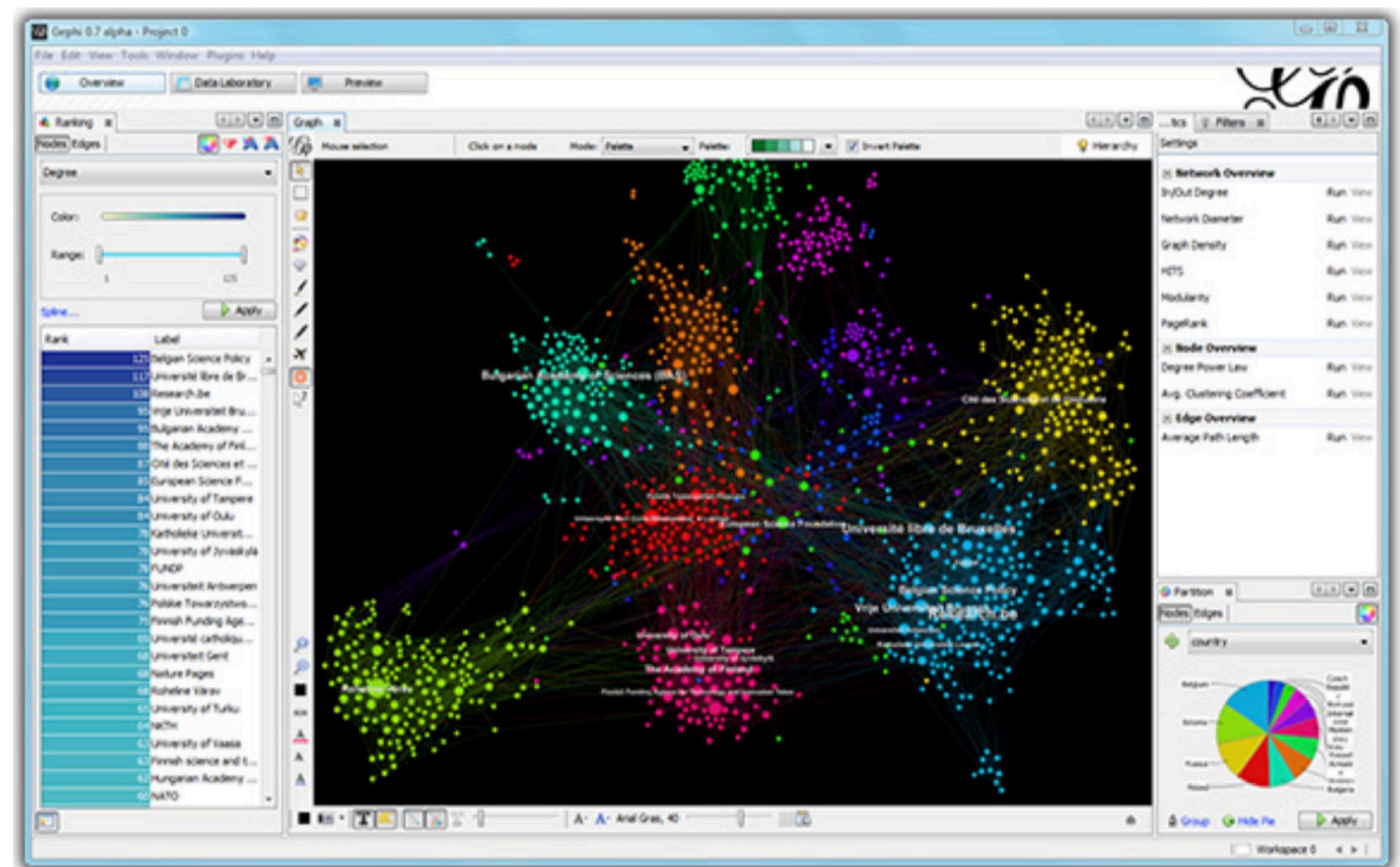


**Download FREE
Gephi 0.9.1**

[Release Notes](#) | [System Requirements](#)

► [Features](#)
► [Quick start](#)

► [Screenshots](#)
► [Videos](#)





graph-tool

Efficient network analysis

[Download](#)[Documentation](#)[Mailing List](#)[Git](#)[Issues](#)

What is graph-tool?

Graph-tool is an efficient [Python](#) module for manipulation and statistical analysis of [graphs](#) (a.k.a. [networks](#)). Contrary to most other python modules with similar functionality, the core data structures and algorithms are implemented in [C++](#), making extensive use of template [metaprogramming](#), based heavily on the [Boost Graph Library](#). This confers it a level of [performance](#) that is comparable (both in memory usage and computation time) to that of a pure C/C++ library.

[Download version 2.22 ↓](#)[See Instructions](#) | [See Changelog](#)

► It is *Fast!*

☕ Extensive Features

👁 Powerful Visualization

NetworkX

Stable (notes)

1.11 – January 2016
[download](#) | [doc](#) | [pdf](#)

Latest (notes)

2.0 development
[github](#) | [doc](#) | [pdf](#)

Archive

Contact

[Mailing list](#)

[Issue tracker](#)



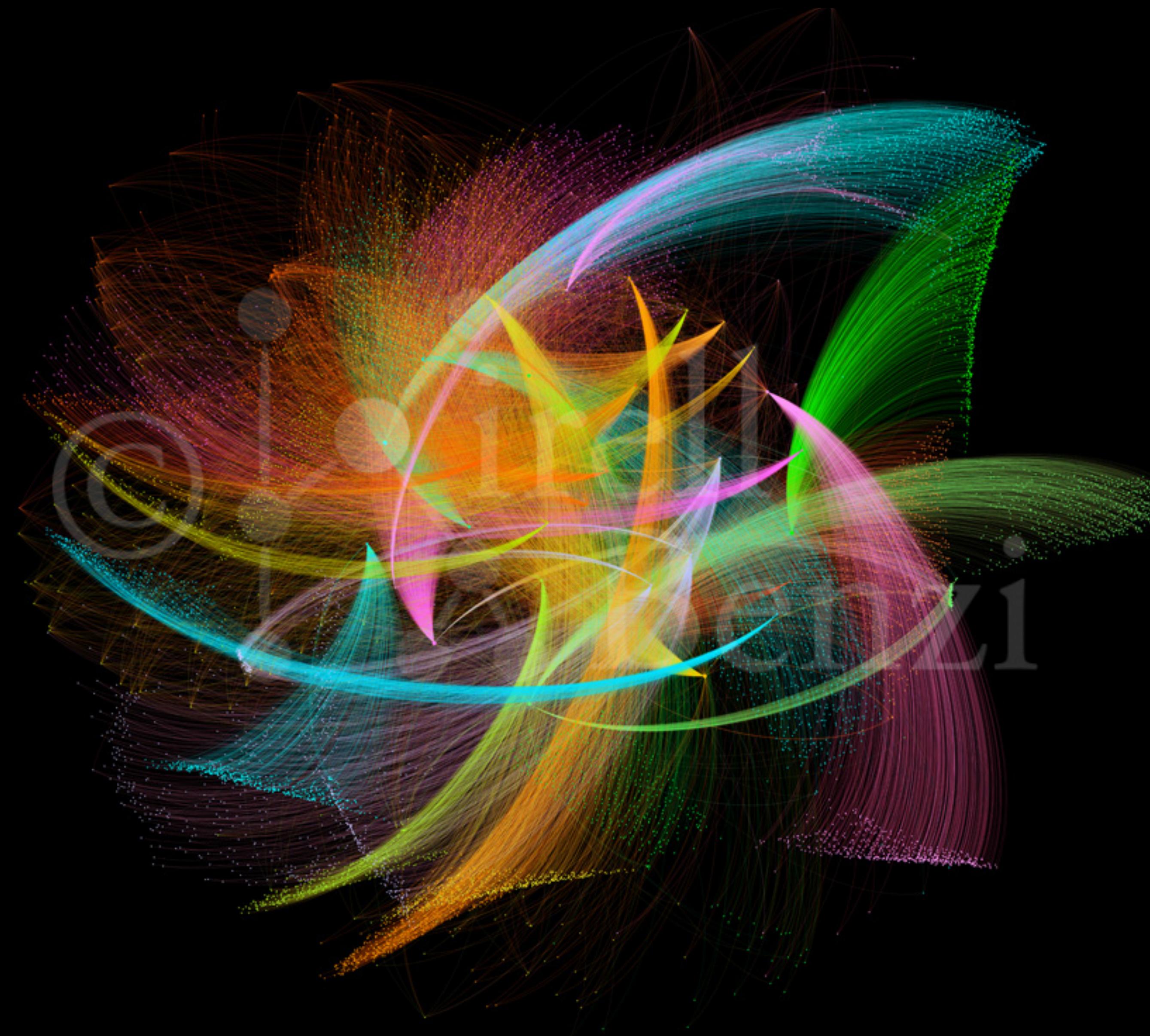
Software for complex networks

NetworkX is a Python package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.



Features

- Data structures for graphs, digraphs, and multigraphs
- Many standard graph algorithms
- Network structure and analysis measures
- Generators for classic graphs, random graphs, and synthetic networks
- Nodes can be "anything" (e.g., text, images, XML records)
- Edges can hold arbitrary data (e.g., weights, time-series)
- Open source [3-clause BSD license](#)
- Well tested with over 90% code coverage
- Additional benefits from Python include fast prototyping, easy to teach, and multi-platform



Kirell Benzi

kirellbenzi.com

"ART UPSETS, SCIENCE REASSURES" GEORGES BRAQUE