

## Ohm's Law

The ratio of potential difference ( $V$ ) between any two points on a conductor to the current ( $I$ ) flowing between them, is constant, provided the temperature of the conductor does not change.

$$\frac{V}{I} = \text{constant} \quad \text{or} \quad \frac{V}{I} = R.$$

ASSI

1. Derive the vector form of Ohm's law.

OR

Relation b/w current Density and electric field

$$\vec{J} = neV_d \quad V_d = \text{drift velocity}.$$

$$\vec{J} = ne \left( \frac{e \vec{E} \tau}{m} \right) \quad \tau = \text{Tao.}$$

$$\Rightarrow \vec{J} = \left( \frac{n e^2 \tau}{m} \right) \vec{E}$$

$$\text{Also, } \sigma = \frac{m}{n e^2 \tau}$$

$$\Rightarrow \vec{J} = \frac{\vec{E}}{\sigma} \quad \boxed{\sigma = \frac{1}{\rho}}$$

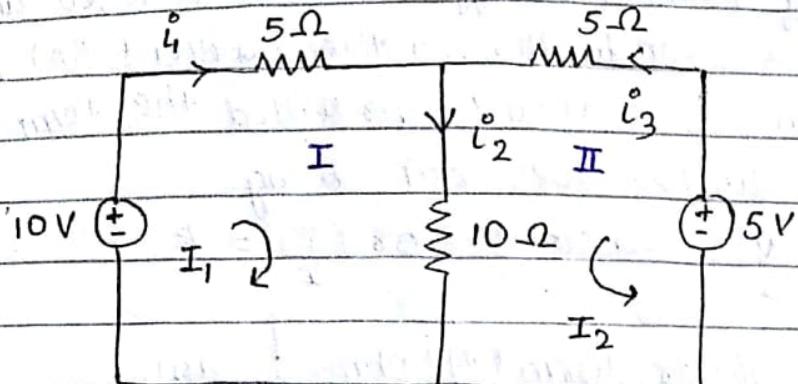
$$\Rightarrow \boxed{\vec{J} = \sigma \vec{E}}$$

KVL The sum of voltage rises = sum of voltage drop in closed loop.

KCL The sum of current entering through a junction is equal to the sum of current leaving through junction.

KVL

1. Find the ~~currents of all~~ Branch currents and loop currents in the circuit



Branch currents are:  $i_1$ ,  $i_2$  and  $i_3$

Loop currents are:  $I_1$  and  $I_2$

From loop I,

$$5i_1 + 10i_2 = 10 \quad \text{--- (1)}$$

From loop II,

$$5i_3 + 10i_2 = 5 \quad \text{--- (II)}$$

$$i_1 = I_1; i_2 = I_1 + I_2; i_3 = I_3$$

Replace it in (1) and (II),

$$5I_1 + 10I_1 + 10I_2 = 10$$

$$5I_2 + 10I_1 + 10I_2 = 5$$

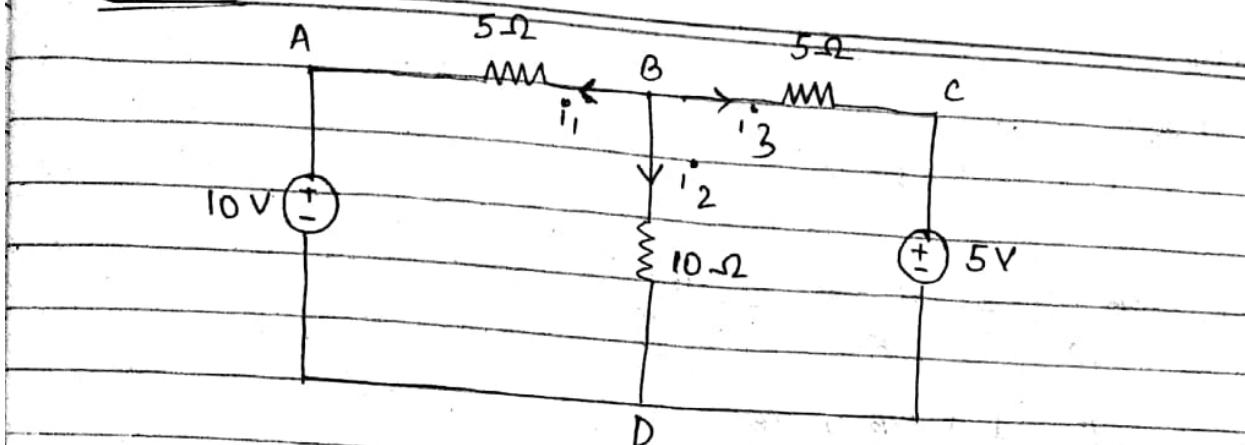
$$3I_1 + 2I_2 = 2$$

$$2I_1 + 3I_2 = 1$$

$$-5I_2 = 1$$

$$I_2 = -\frac{1}{5} \text{ A} \quad I_1 = \frac{4}{5} \text{ A}$$

KCL



From KCL,

$$i_1 + i_2 + i_3 = 0$$

$$\frac{V_B - 10}{5} + \frac{V_B - 0}{10} + \frac{V_B - 5}{5} = 0$$

$$\Rightarrow \frac{V_B}{5} - 2 + \frac{V_B}{10} + \frac{V_B}{5} - 1 = 0$$

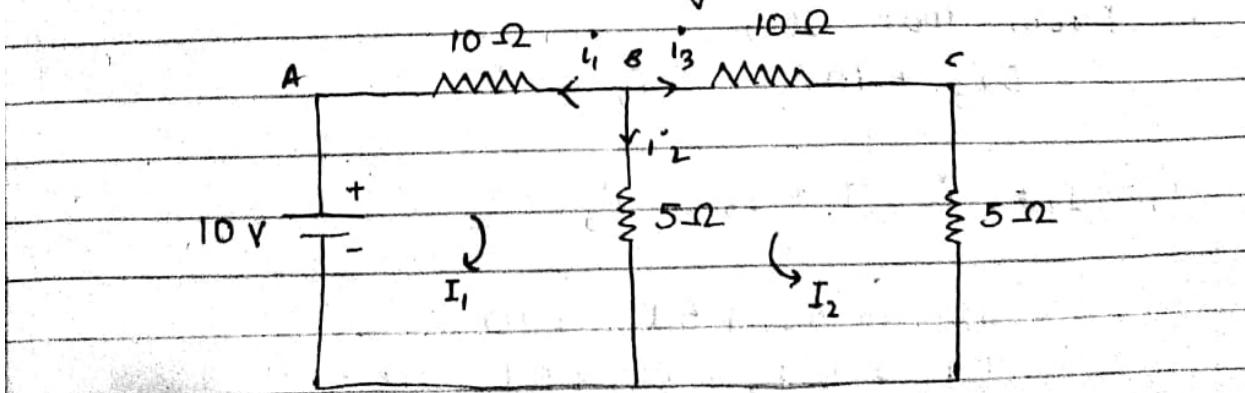
$$\Rightarrow \frac{2V_B}{5} + \frac{V_B}{10} = 3$$

$$\Rightarrow \frac{4V_B + V_B}{10} = 3 \Rightarrow \frac{5V_B}{10} = 3$$

$$\Rightarrow V_B = 6$$

$$i_1 = \frac{V_B - 10}{5} = -\frac{4}{5} \quad i_2 = \frac{3}{5} \quad i_3 = \frac{1}{5}$$

2. Find the branch currents using both KCL and KVL in the following circuit:



### i) KCL

From KCL,

$$i_1 + i_2 + i_3 = 0$$

$$\frac{V_B - 10}{10} + \frac{V_B - 0}{5} + \frac{V_B - 0}{15} = 0$$

$$\frac{V_B}{10} - 1 + \frac{V_B}{5} + \frac{V_B}{15} = 0$$

$$\cancel{\frac{2V_B}{10}} + \frac{V_B}{5} = 1 \Rightarrow \cancel{\frac{2V_B}{5}} = -1$$

$$V_B = \frac{5}{2}$$

$$\cancel{\frac{V_B}{5}} + \cancel{\frac{V_B}{2}} + V_B$$

$$\frac{V_B}{5} \left( \frac{1}{2} + 1 + \frac{1}{3} \right) = 1 \Rightarrow \frac{V_B}{5} \times \frac{11}{6} = 1$$

$$\Rightarrow V_B = \frac{30}{11}$$

$$i_1 = \frac{\frac{30}{11} - 10}{10} = 0.7272$$

$$\cancel{\frac{30 - 110}{11}} = \cancel{\frac{80 \times 10}{11}} = 0.7272$$

### ii) KVL

From loop I,

$$10i_1 + 5i_2 = 10$$

From loop II,

$$5i_3 + 10i_2 + 5i_1 = 0$$

$$i_1 = I_1; i_2 = I_1 + I_2 \quad i_3 = I_2$$

$$10I_1 + 5I_1 + 5I_2 = 10$$

$$5I_2 + 10I_2 + 5I_1 + 5I_2 = 0$$

$$\Rightarrow 15I_1 + 5I_2 = 10$$

$$50I_1 + 20I_2 = 0$$

$$\begin{array}{l} 3I_1 + I_2 = 0 \\ I_1 + 4I_2 = 0 \end{array} \quad \times 1 \quad \times 3$$

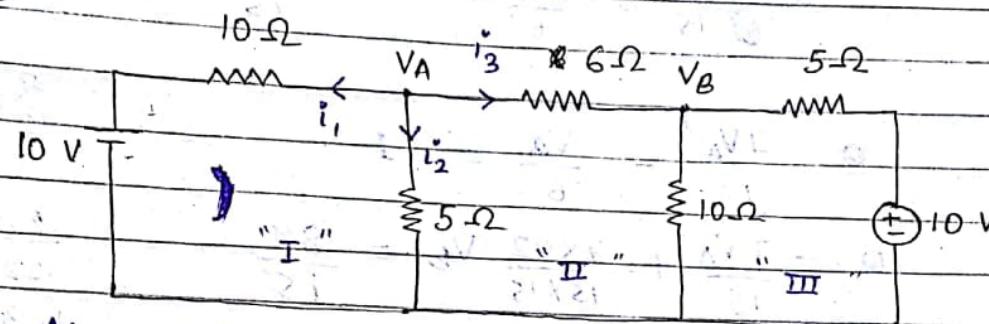
$$\begin{array}{l} 3I_1 + I_2 = 0 \\ 3I_1 + 12I_2 = 0 \end{array} \quad (-) \quad (-)$$

$$\begin{aligned} I_1 &= -4I_2 \\ &= \frac{4 \times 2}{11} = \frac{8}{11} \end{aligned}$$

$$i_1 = \frac{8}{11} = 0.727272$$

Assign

2.



At node A,

$$i_1 + i_2 + i_3 = 0$$

$$\frac{V_A - 10}{10} + \frac{V_A - 0}{5} + \frac{V_A - V_B}{6} = 0 \quad (1)$$

At node B,

$$\frac{V_B - V_A}{6} + \frac{V_B - 0}{10} + \frac{V_B - 10}{5} = 0 \quad (2)$$

From (1),

$$\frac{V_A}{10} - 1 + \frac{V_A}{5} + \frac{V_A}{6} - \frac{V_B}{6} = 0$$

$$\Rightarrow \frac{V_A}{5} \times \frac{3}{2} + \frac{V_A}{6} - \frac{V_B}{6} = 1$$

$$\Rightarrow \frac{3V_A}{10} + \frac{V_A}{6} - \frac{V_B}{6} = \frac{7V_A}{15} - \frac{V_B}{6} = 1$$

$$\Rightarrow \frac{7V_A}{15} - \frac{V_B}{6} = 1 \quad (3)$$

$$\frac{V_B}{6} - \frac{V_A}{6} + \frac{V_B}{10} + \frac{V_B}{5} - 2 = 0$$

$$\frac{7}{15} V_B - \frac{V_A}{6} = 2 \quad \text{--- (IV)}$$

$$\frac{7}{15} V_A - \frac{V_B}{6} = 1 \quad \times 1$$

$$\frac{7 \times 6}{15} \cancel{V_A}$$

~~$$\frac{7}{15} V_B - \frac{V_A}{6} = 2 \quad \times \frac{42}{15}$$~~

$$\frac{42}{15} \cancel{V_B}$$

~~$$\textcircled{a} \quad \frac{7}{15} V_A - \frac{V_B}{6} = 1$$~~

$$\frac{7}{15} \cancel{V_A} \frac{42}{15}$$

~~$$\textcircled{b} \quad -\frac{7}{15} V_A + \frac{7 \times 42}{15 \times 15} V_B = \frac{84}{15}$$~~

$$\frac{294}{225}$$

$$1.306$$

$$1.14 V_B = 6.6$$

$$0.166$$

$$V_B = 5.78$$

$$\frac{7}{15} \times 5.78 - 2 = \frac{V_A}{6}$$

$$V_A = 4.184$$

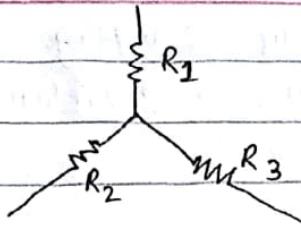
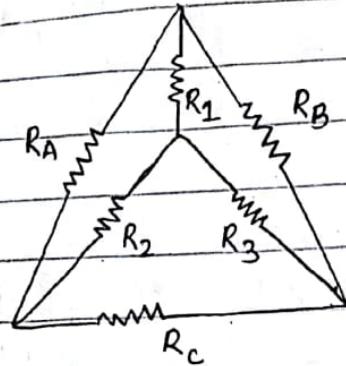
$$i_2 = \frac{V_A}{5} = 0.83$$

## Superposition

Active source : Voltage and current source.

Passive " : Resistance , inductance .

Star and Delta



Star

Delta

1. Delta  $\rightarrow$  Star

$R_A$ ,  $R_B$  and  $R_C$  are Known

$$R_1 = \frac{R_A \cdot R_B}{R_A + R_B + R_C}$$

$$R_2 = \frac{R_B \cdot R_C}{R_A + R_B + R_C}$$

$$R_3 = \frac{R_A \cdot R_C}{R_A + R_B + R_C}$$

2. Star  $\rightarrow$  Delta

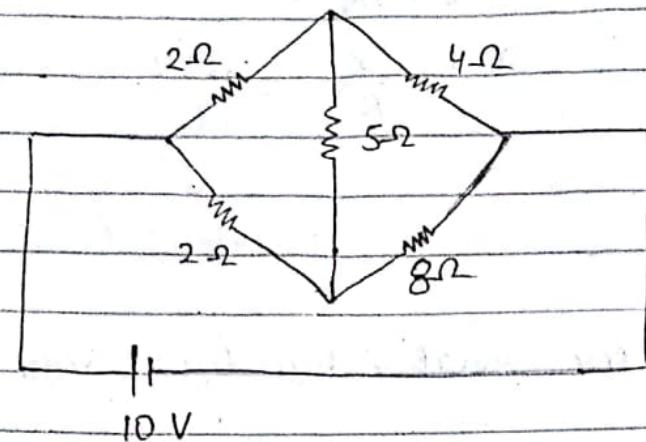
$R_1$ ,  $R_2$  and  $R_3$  are Known

$$R_A = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

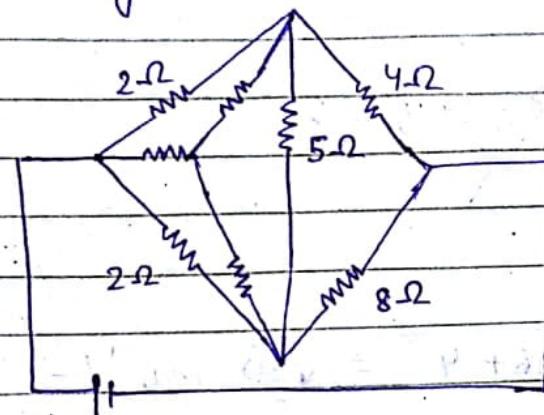
$$R_B = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

$$R_C = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

3. Find out the total current in the circuit

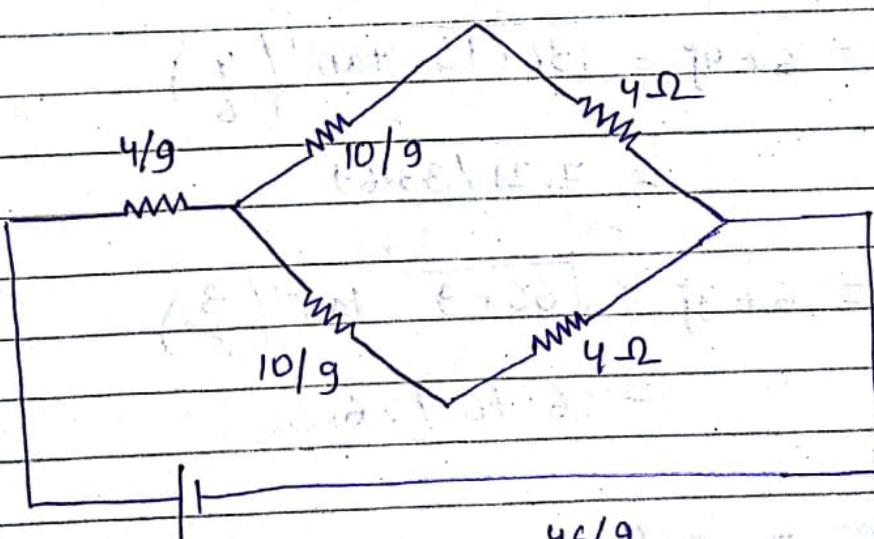


Assuming star,

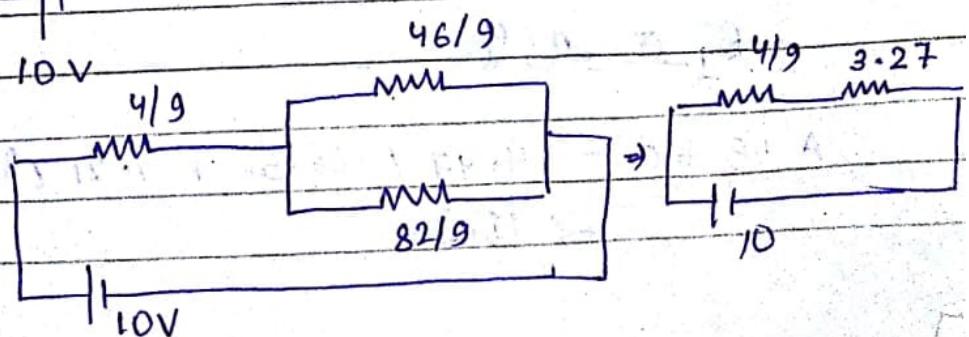


$$\frac{10}{9}$$

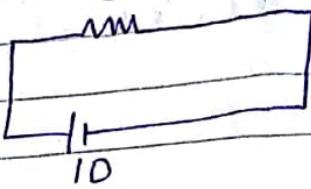
After rearranging it,



$$\frac{10 \times 4}{9} \\ \frac{10}{3} + 4 \\ = \frac{40}{9}$$



3.71



$$V = IR$$

$$\Rightarrow I = \frac{V}{R} = \frac{3.71}{10}$$

$$= 2.695$$

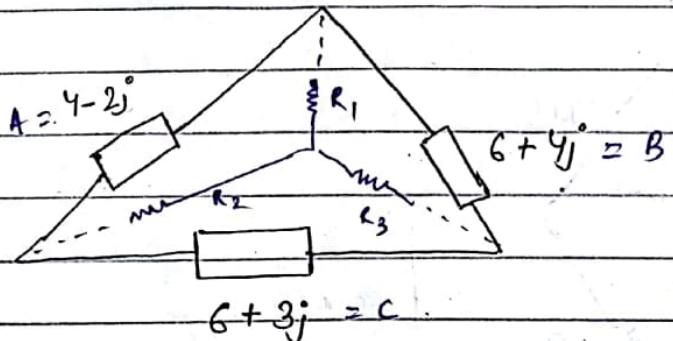
$$\approx 2.7$$

Assign

3. Derive the inter relationship b/w star and delta.

Assign

4.



$$A = 4 - 2j = \sqrt{16 + 4} = \sqrt{20} \tan^{-1}\left(\frac{-2}{4}\right)$$

$$= 4.47 \angle -26.56^\circ$$

$$B = 6 + 4j = \sqrt{36 + 16} \tan^{-1}\left(\frac{4}{6}\right)$$

$$= 7.21 \angle 33.69^\circ$$

$$C = 6 + 3j = \sqrt{36 + 9} \tan^{-1}\left(\frac{3}{6}\right)$$

$$= 6.70 \angle 26.56^\circ$$

RQ & QP

$$A + B + C = 4.47 \angle -26.56^\circ + 7.21 \angle 33.69^\circ + 6.70 \angle 26.56^\circ$$

~~50 = 18.88~~

$$a(\cos\theta + i \sin\theta)$$

~~(cosθ + i sinθ)~~

253.1281  
24.9001

$$= 4.47(0.89 - j0.44) + 7.21(0.83 + j0.55) \\ + 6.70(0.89 + j0.44)$$

$$= 3.97 - 1.96j + 5.98 + 3.96j + 5.96 + 2.99j$$

$$= 15.91 + 4.99j \approx 16 + 5j = 16.76 / 17.35$$

$$= \sqrt{278.0282} \tan^{-1}\left(\frac{4.99}{15.91}\right) = 16.67 / 17.41$$

~~R<sub>1</sub> = 16.67 / 17.41~~

$$R_1 = \frac{(4-2j)(6+4j)}{16.67 / 17.41} = \frac{24 + 16j - 12j + 8}{16.67 / 17.41}$$

$$= \frac{32 + 4j}{16.67 / 17.41}$$

$$= \frac{32.24}{16.76} / 17.12$$

$$= 1.92 / -10.23$$

$$= 1.88 + j(-0.33)$$

~~$$\frac{32 + 4j}{16.67 / 17.41}$$~~

~~$$= \frac{8.06}{16.67 / 17.41} / 17.12$$~~

~~$$= \frac{4 \times 8.06}{16.67 / 17.41} / 17.12$$~~

~~$$= 1.93 / -10.29$$~~

~~$$= 1.09 + j(-0.34)$$~~

$$R_2 = \frac{A \cdot C}{A + B + C} = \frac{(4-2j)(6+3j)}{16.76}$$

$$= \frac{24 + 12j - 12j + 6}{16.76}$$

$$= \frac{30}{16.76 / 17.35}$$

$$= 1.78 / 17.35$$

$$= 1.7 + j(-0.53)$$

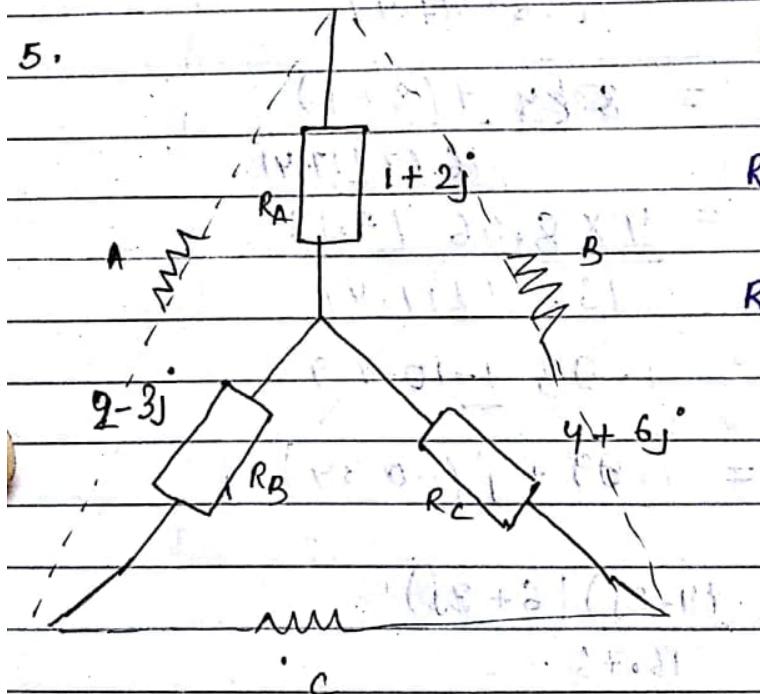
$$\begin{aligned}
 R_3 &= \frac{(6+4j)(6+3j)}{16 \cdot 76 \angle 17.35} \\
 &= \frac{36 + 18j + 24j - 12}{16 \cdot 76 \angle 17.35} \\
 &\approx \frac{24 + 42j}{16 \cdot 76 \angle 17.35} = \frac{48.37 \angle 60.25}{16 \cdot 76 \angle 17.35} \\
 &= 2.88 \angle 42.9^\circ \\
 &= 2.10 + j(1.96)
 \end{aligned}$$

$$R_1 = 1.88 + j(-0.33)$$

$$R_2 = 1.7 + j(-0.53)$$

$$R_3 = 2.10 + j(1.96)$$

5.



$$\begin{aligned}
 R_A &= 1+2j \\
 &= 2.23 \angle 63.43^\circ
 \end{aligned}$$

$$\begin{aligned}
 R_B &= 2-3j \\
 &= 3.6 \angle -56.30^\circ
 \end{aligned}$$

$$\begin{aligned}
 R_C &= 4+6j \\
 &= 7.21 \angle 56.30^\circ
 \end{aligned}$$

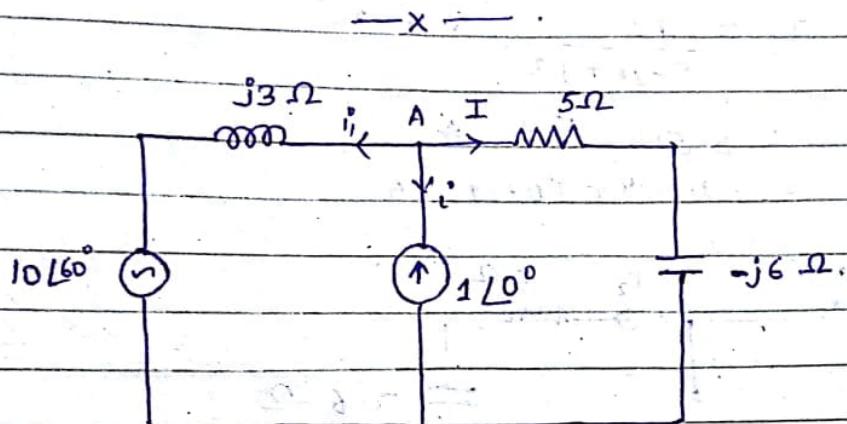
$$\begin{aligned}
 D &= R_A R_B + R_B R_C + R_C R_A \\
 &= (1+2j)(2-3j) + (2-3j)(4+6j) + (4+6j)(1+2j) \\
 &= 2-3j + 4j + 6 + 8 + 12j - 12j + 18 + 4 + 8j + 6j = 12 \\
 &= 26 + 15j \\
 &= 30.01 \angle 29.98^\circ = 30.01 \angle 30^\circ
 \end{aligned}$$

$$\begin{aligned}
 A &= \frac{D}{2-3j} = \frac{30.01 \angle 30^\circ}{3.6 \angle -56.30^\circ} = 8.33 \angle 86.3^\circ \\
 &= 0.53 + j(8.31)
 \end{aligned}$$

$$B = \frac{D}{4+6j} = \frac{30.01 \angle 30^\circ}{7.21 \angle 56.30^\circ} = 4.16 \angle -26.3^\circ$$

$$= 3.72 + j(-1.84)$$

$$C = \frac{30.01 \angle 30^\circ}{1+2j} = \frac{30.01 \angle 30^\circ}{2.23 \angle 63.43^\circ} = 13.45 \angle -33.43^\circ$$



$$X_L = j3 \quad \text{[REDACTED]} = 3 \angle 90^\circ$$

$$X_C = -j6 = 6 \angle -90^\circ$$

At Node A,

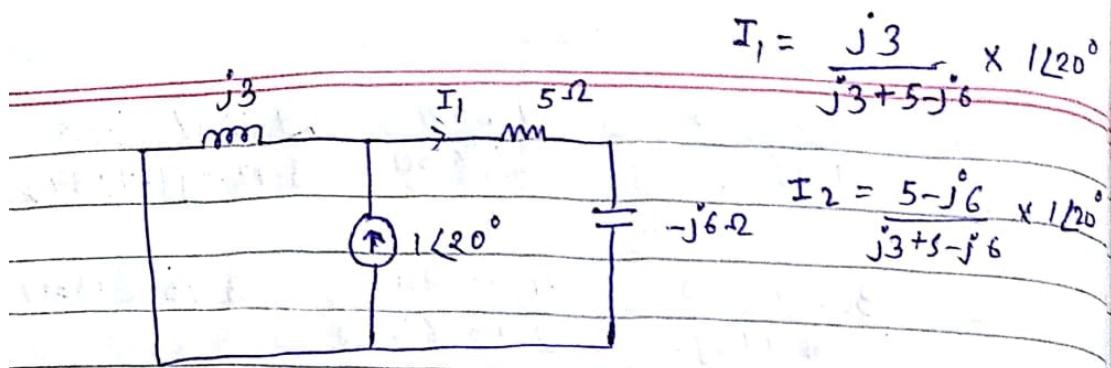
$$V_A - 10 \angle 60^\circ + \frac{V_A - 6 \angle 80.53^\circ}{5} + V_A = 0$$

$$i_j + I + i = 0$$

$$\frac{V_A - 10 \angle 60^\circ}{3 \angle 90^\circ}$$

$+ 2j$ )

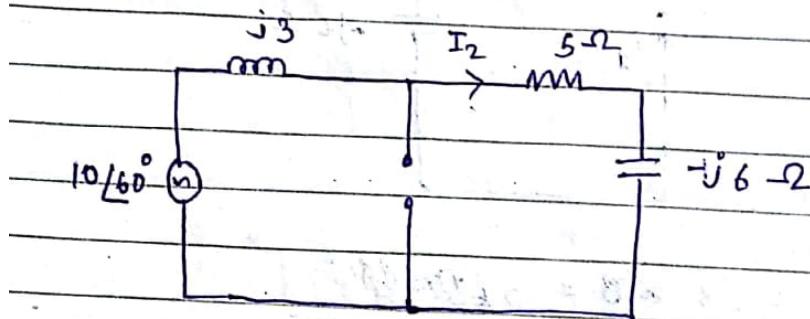
12



$$I_1 = \frac{j3}{5-j6+j3} \times 1 L20^\circ$$

$$= 0.515 L120^\circ A$$

$$= -0.264 + j0.442 A$$



$$I_2 = \frac{10 L60^\circ}{5-j3} = 1.71 L90.9^\circ$$

$$= -0.026 + j1.715 A$$

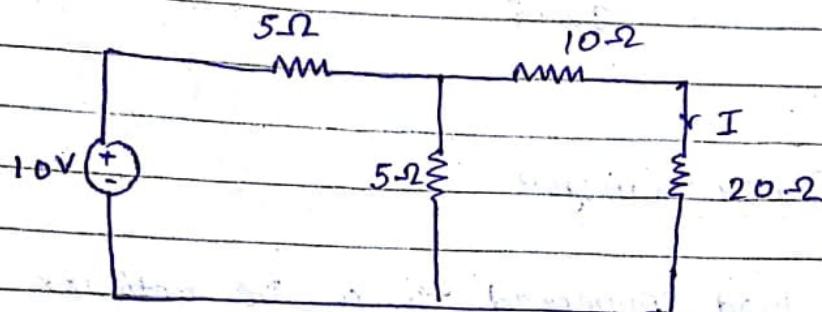
$$I = I_1 + I_2$$

$$= -0.29 + j2.157$$

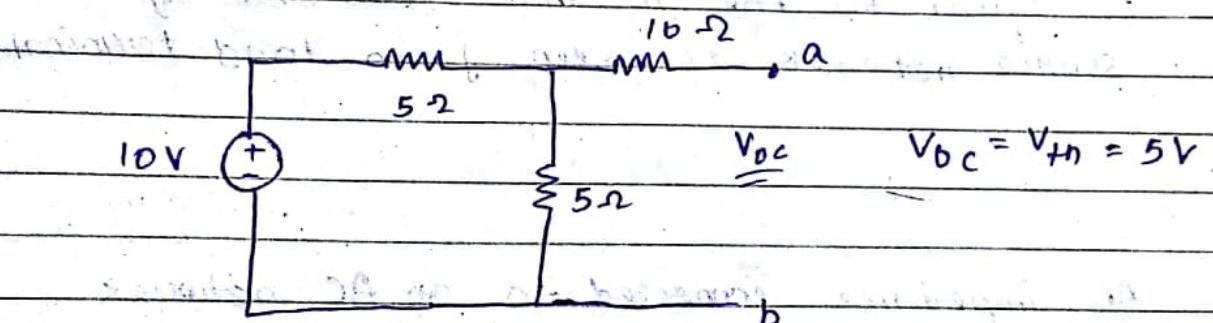
Thermin's th

Any linear active network consisting of dependent/independent sources and linear bilateral network elements (resistances, conductance, inductance) can be replaced by an equivalent circuit consisting of a voltage source in a series with a resistance. The voltage source being a open circuited across the open-circuited load resistance.

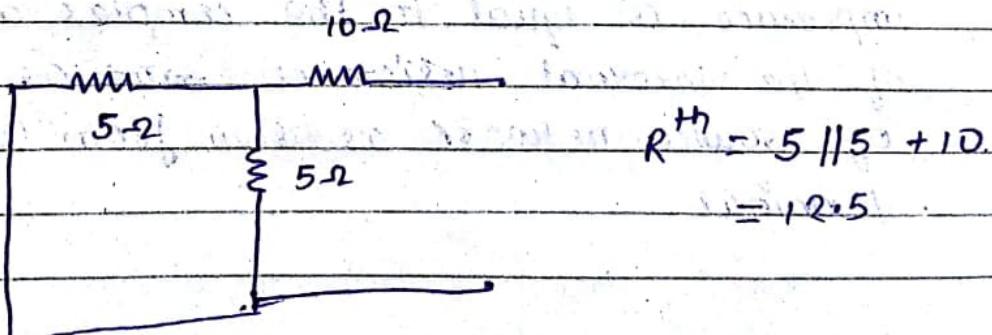
and the resistance being the internal resistance of load source ~~terminal~~ source network looking ~~through~~ through open circuited load terminal. with all the active sources either replaced by their internal resistances (if any) or short-circuited (in case of voltage source) or open circuited (in case of current source).



$$R_L = 20\Omega$$

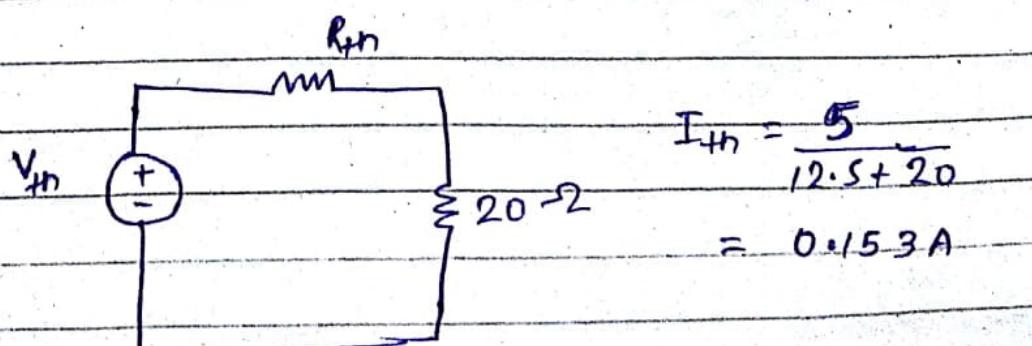


$$V_{oc} = V_{th} = 5V$$



$$R_{th} = 5 // 5 + 10$$

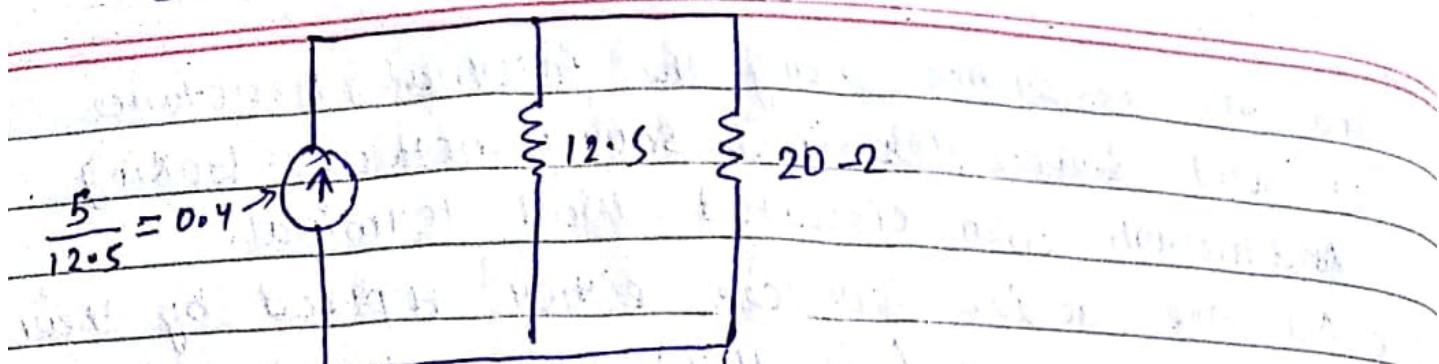
$$= 12.5$$



$$I_{th} = \frac{5}{12.5 + 20}$$

$$= 0.153A$$

## Norton.

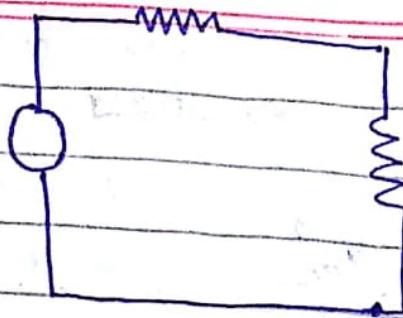


$$I_N = \frac{12.5}{32.5} \times 0.4$$

## Maximum Power transfer

A resistive load connected to a DC network receives maximum power when the load resistance is equal to the internal resistance of source network as seen from load terminal.

An impedance connected to an AC network receives maximum power when the load impedance is equal to the complex conjugate of the internal resistance ~~same as above~~ of source network as seen from load terminal.



$$P_L = I_L^2 R_L$$

$$= \left( \frac{V_m}{R_m + R_L} \right)^2 \cdot R_L$$

$\frac{dP_L}{dR_L} = 0$ , then power will be maximum.

~~$$V_m \left( \frac{2(R_m + R_L)}{(R_m + R_L)^2} \right)$$~~

$$\frac{V_m^2}{(R_m + R_L)^2} \cdot R_L$$

$$\Rightarrow V_m^2 \left[ \frac{2(R_m + R_L)}{(R_m + R_L)^2} \right] = (R_m + R_L)^2 \cdot \underline{2V_m}$$

$$\Rightarrow R_m = R_L$$

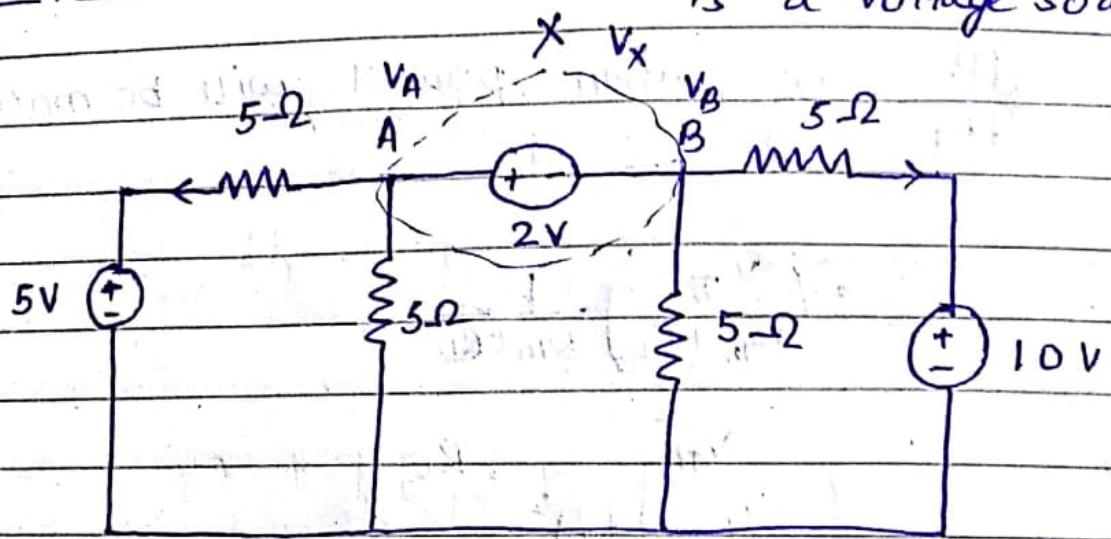
Proof the Maximum power transfer theorem  
for AC circuit.

$$P_L = \frac{2 V_m^2 \cdot R_L}{4 R_L^2} \rightarrow \text{Power consumed Load.}$$

$$= \frac{2 V_m^2}{4 R_L} = \frac{V_m^2}{2 R_L}$$

50% : Maximum Efficiency

Super Node Analysis (In b/w two Node there is a voltage source)



At Node X,

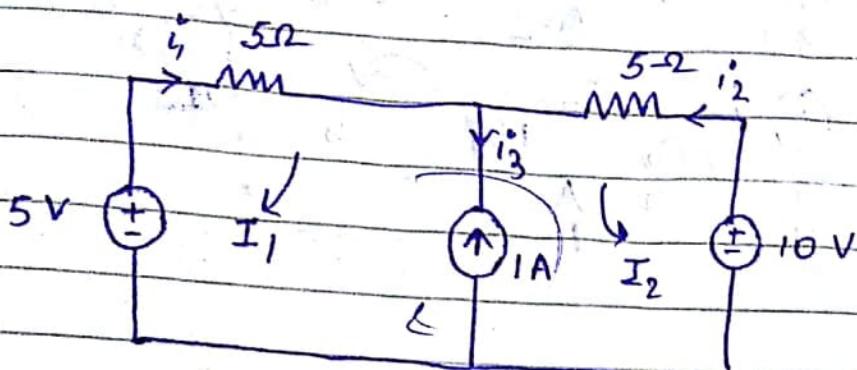
$$\frac{V_A - 5}{5} + \frac{V_A}{5} + \frac{V_B - 10}{5} + \frac{V_B}{5} = 0 \quad \textcircled{1}$$

$$V_A - V_B = 2 \quad \textcircled{2}$$

$$V_A =$$

$$V_B =$$

Super Mesh. (b/w two mesh a current source)



Considered as 1 mesh.

$$5I_2 + 5 = 5I_1 + 10 \quad \text{--- (1)}$$

Voltage rises = Voltage down drops

$$I_1 + I_2 = -1 \quad \text{--- (2)}$$

$$I_1 = -1 - I_2$$

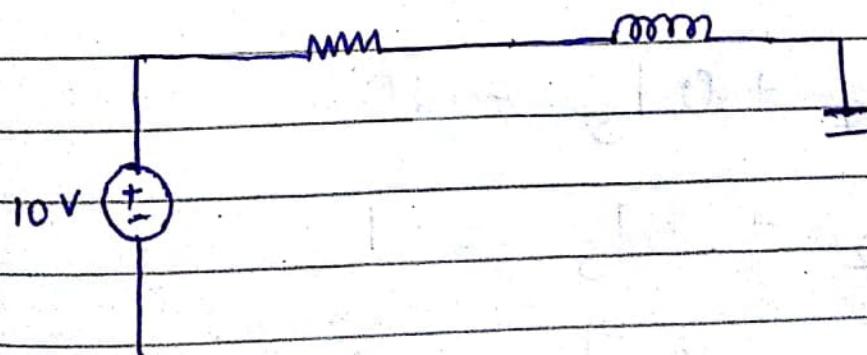
$$5I_2 + 5 = 5(-1 - I_2) + 10$$

$$\Rightarrow 5I_2 + 5 = -5 - 5I_2 + 10$$

$$\Rightarrow 10I_2 = 10$$

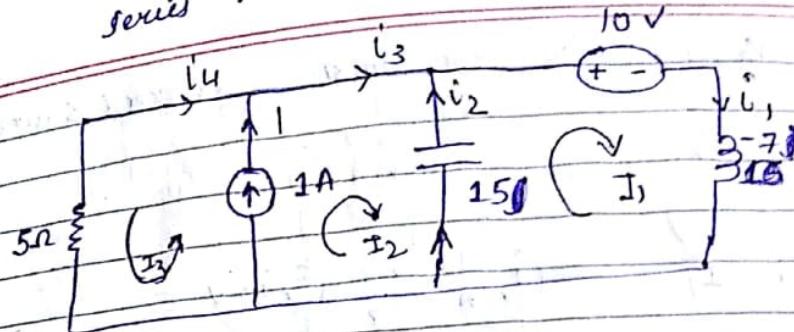
$$\Rightarrow I_2 = 1$$

$$I_1 = -1$$



Note

Parallel resistance + voltage source = super  
series resistance + current source = super  
res.



$$I_3 - I_2 = 1.$$

~~$$-10 + 7I_1 - 15(I_2 - I_2) = 0.$$~~

~~$$7I_1 = 15(1, - I_2) + 10$$~~

$$-10 + 7I_1 + 5I_3 = 0 \quad \dots \text{--- (1)}$$

$$7I_1 = 15(1, - I_2) + 10 \quad \dots \text{--- (2)}$$

$$I_3 - I_2 = 1.$$

$$7I_1 = 15I_1 - 15I_2 + 10.$$

$$-8I_1 + 15I_2 + 0I_3 = 10.$$

$$0I_1 - 1I_2 + I_3 = 1$$

$$7I_1 + 0I_2 + 5I_3 = 10.$$

$$I_1 = 0.1724 \text{ A}$$

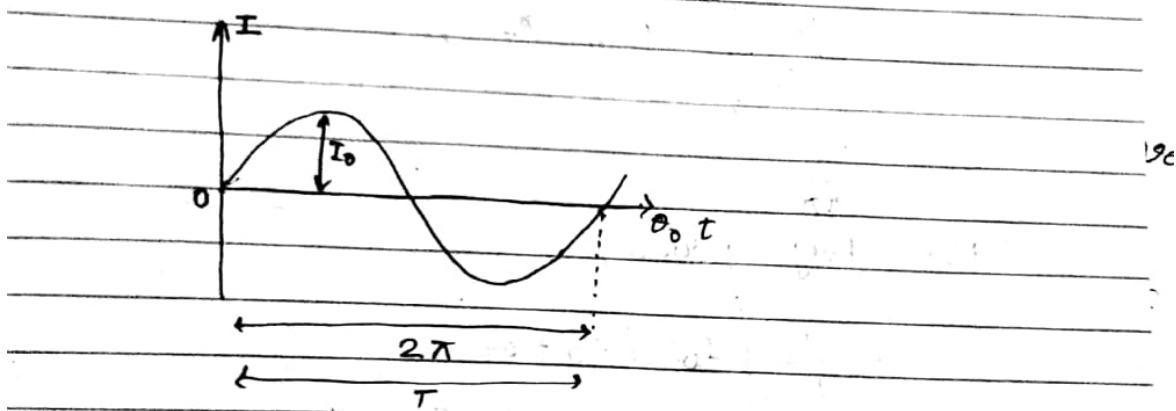
$$I_2 = 0.7586 \text{ A}$$

$$I_3 = 1.7586 \text{ A}$$

Rms : value of AC = value of DC ~~not~~ flowing in a circuit producing same amount of ~~heat~~ heat as of AC circuit

Avg value.

value of DC charge flowing in a circuit same amount of charge as of AC circuit.



Symmetrical electric signal :

In a symmetrical electrical signal : average value half of over a half period.

In a unsymmetrical electrical signal : average value over a complete period

$$I_{av} = \frac{1}{T/2} \int_0^{T/2} i dt = \frac{1}{\pi} \int_0^{\pi} i d\theta.$$

$$i = I_0 \sin \omega t$$

$$I_{avg} = \frac{1}{\pi} \int_0^{\pi} I_0 \sin \omega t \, dt$$

$$= \frac{I_0}{\pi} \left[ -\cos \omega t \right]_0^{\pi}$$

$$= \frac{I_0}{\pi} \cdot [-1 - 1]$$

$$= -\left( \frac{-2 I_0}{\pi} \right) = \frac{2 I_0}{\pi}$$

Formula

Peak fact

$$I_{rms}^2 = \frac{1}{2\pi} \int_0^{2\pi} i^2 d\theta \quad \text{mean} = 2\pi$$

$$= \frac{1}{2\pi} \int_0^{2\pi} I_0^2 \sin^2 \omega t \, dt$$

For half period,

$$= \frac{1}{\pi} \int_0^{\pi} I_0^2 \sin^2 \omega t \, dt$$

$$= \frac{I_0^2}{\pi} \left[ \sin^2 \omega t \, dt \right]_0^{\pi}$$

$$= \frac{I_0^2}{2\pi} \left[ \frac{1 - \cos 2\omega t}{2} \right]_0^{\pi}$$

$$= \frac{I_0^2}{4\pi} \left[ \theta - \frac{\sin 2\omega t}{2} \right]_0^{\pi}$$

$I_0$

Form factor : Ratio of rms value by avg

$$= \frac{I_{rms}}{I_{avg}}$$

$$= \frac{I_0}{\sqrt{2}} \times \frac{\pi}{2I_0}$$

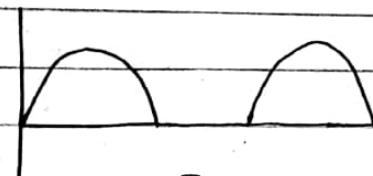
$$= \frac{\pi}{2\sqrt{2}} = 1.11.$$

Peak factor: Ratio of peak value by rms value

$$= \frac{I_{peak\ value}}{I_{rms}}$$

$$= \frac{I_0 \times \sqrt{2}}{I_0}$$

$$= \sqrt{2} = 1.414$$



FOM full ~~cycle~~  
period.

$$I_{avg} = \frac{1}{T} \int_0^T i dt$$

$$= \frac{1}{T} \left[ \int_0^{T/2} i dt + \frac{1}{T} \int_{T/2}^T i dt \right]$$

$$= \frac{1}{T} \int_0^{T/2} i dt$$

$$= \frac{1}{2\pi} \int_0^\pi i^2 dt$$

$$= \frac{I_0}{\pi} A$$

$$\begin{aligned} T/2 &= \pi \\ T &= 2\pi \end{aligned}$$

$$I_{rms}^2 = \frac{1}{2\pi} \int_0^{2\pi} i^2 d\theta = \frac{1}{2\pi} \int_0^\pi i^2 d\theta + \frac{1}{2\pi} \int_\pi^{2\pi} i^2 d\theta$$

$$= \frac{1}{2\pi} \int_0^\pi i^2 d\theta = \frac{I_0}{2} A$$

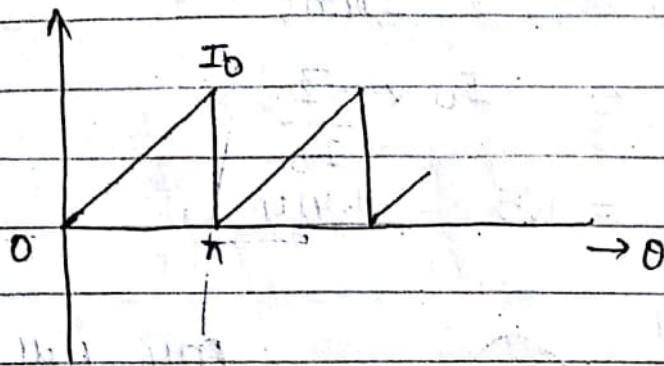
$$\text{Form factor} = \frac{I_0 \times \pi}{2 I_0}$$

$$= \frac{\pi}{2} = 1.57$$

$$\text{Peak factor} = I_0 \times \frac{2}{I_0}$$

$$= 2.$$

1. Find form factor and peak factor of :



$$y = m x + c$$

$$y = \frac{(y_1 - y_2)x}{(x_1 - x_2)}$$

$$I_{av} = \frac{1}{\pi/2} \int_0^{\pi/2} i dt$$

$$= \frac{1}{\pi} \int_0^{\pi} i d\theta \quad i = \frac{I_0}{\pi} \theta$$

$$= \frac{1}{\pi} \int_0^{\pi} \frac{I_0}{\pi} \theta d\theta$$

$$= \frac{I_0}{\pi^2} \left[ \frac{\theta^2}{2} \right]_0^{\pi}$$

$$= \frac{I_0}{2\pi^2} [\pi^2]$$

$$= \frac{I_0}{2}$$

$$\begin{aligned}
 I_{\text{rms}}^2 &= \frac{1}{2\pi} \int_0^{2\pi} i^2 d\theta \\
 &= \frac{1}{2\pi} \int_0^{2\pi} \frac{I_0^2}{2} t^2 dt = \cancel{\textcircled{1}} \\
 &= \frac{I_0^2}{2\pi^3} \left[ \frac{t^3}{3} \right]_0^{2\pi} \\
 &= \frac{I_0^2}{3\pi^3} \left[ t^3 \right]_0^{2\pi} \\
 &= \frac{I_0^2}{3\pi^3} [8\pi^3] = \frac{8I_0^2}{3} = \cancel{\frac{8}{3} I_0} \\
 &= \frac{I_0^2}{3} \cancel{I_{\text{rms}}} = \frac{I_0}{\sqrt{3}} = \cancel{0.63 I_0}
 \end{aligned}$$

~~peak factor~~

$$\begin{aligned}
 \text{Form factor} &= \frac{I_0 \times 2}{\sqrt{3} I_0} \\
 &= \boxed{1.15}
 \end{aligned}$$

$$\begin{aligned}
 \text{Peak factor} &= I_0 \times \frac{\sqrt{3}}{I_0} \cancel{\frac{I_0}{I_0}} \cancel{\frac{\sqrt{3}}{I_0}} \cancel{i = v \cdot t} \\
 &= \cancel{1.73} = 1.73
 \end{aligned}$$

2.

$$\begin{aligned}
 i &= \frac{I_0 - I_0}{\pi - 0} \theta \\
 i &= \frac{I_0}{2\pi} t = 0
 \end{aligned}$$

$$\begin{aligned}
 I_{\text{av}} &= \frac{1}{T} \int_0^T i dt \\
 &= \frac{1}{T} \int_0^{T/2} i dt + \frac{1}{T} \int_{T/2}^T 0 dt \\
 &= \frac{1}{T} \int_0^{T/2} i dt + \cancel{0} \cancel{+} \frac{1}{T} \int_0^{T/2} \frac{I_0}{2\pi} \theta dt
 \end{aligned}$$

$$I_{\text{av}} = \frac{1}{2\pi} \int_0^\pi I_0 dt = \frac{I_0 \times \pi}{2\pi} = \frac{I_0}{2}$$

Form factor  $> 1$  Always.  
 Minimum value form factor  
 have = 1.

$$\begin{aligned}
 &= \frac{1}{2\pi} \int_0^{2\pi} I_0 + dt \\
 &= \frac{I_0}{2\pi} \left[ t^2 \right]_0^{2\pi} = \frac{I_0}{2\pi} \times \pi^2 \\
 &= \frac{I_0}{8}
 \end{aligned}$$

$$I_{\text{rms}}^2 = \frac{1}{\pi} \int_0^{2\pi} i^2 d\theta$$

$$i = \frac{I_0 + dt}{2\pi}$$

$$= \frac{1}{\pi} \int_0^{2\pi} \frac{I_0^2}{4\pi^2} dt$$

$$= \frac{I_0^2}{4\pi^3} \left[ t^3 \right]_0^{2\pi} = \frac{I_0^2}{4\pi^3} \times 8\pi^3$$

$$= \frac{I_0^2 \times \pi}{\pi}$$

$$\sqrt{I_{\text{rms}}} = I_0$$

$$= \frac{I_0^2}{12\pi^3} \times 8\pi^3 = \frac{2I_0^2}{3}$$

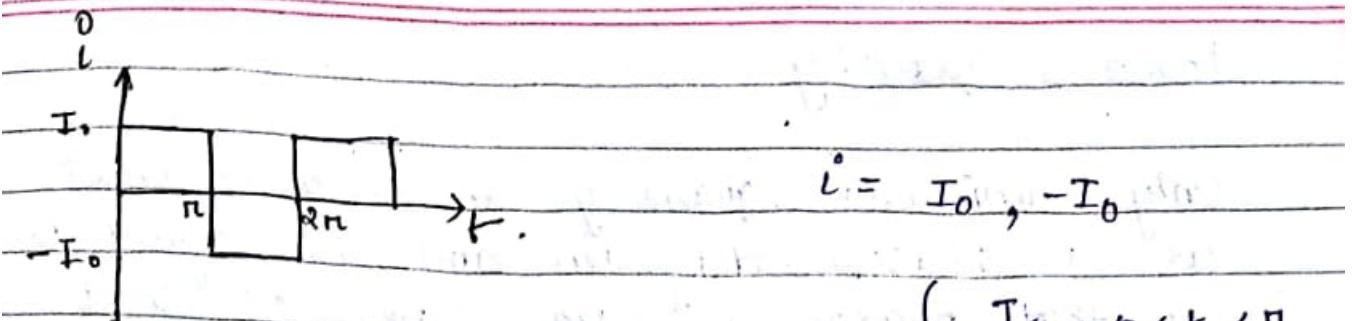
$$= 0.81 I_0$$

Form factor

$$\text{Form factor} = \frac{0.81 I_0 \times 2}{I_0}$$

$$= 0.81 \times 2$$

$$\text{Peak factor} = \frac{I_0 \times 2}{I_0} = 1.8$$



$$I_{\text{rms}}^2 = \frac{1}{T} \int_0^{T/2} i^2 dt$$

$$i = \begin{cases} I_0 & 0 < t < \pi \\ -I_0 & \pi < t < 2\pi \end{cases}$$

$$\begin{aligned} &= \frac{1}{T} \left[ \int_0^{\pi} I_0^2 dt + \int_{\pi}^{2\pi} (-I_0)^2 dt \right] \\ &= \frac{1}{2\pi} \left[ I_0^2 (t) \Big|_0^\pi + I_0^2 (t) \Big|_\pi^{2\pi} \right] \end{aligned}$$

$$= \frac{I_0^2}{2\pi} (\pi + \pi) = \frac{I_0^2 \times 2\pi}{2\pi} = I_0^2$$

$$I_{\text{rms}} = I_0$$

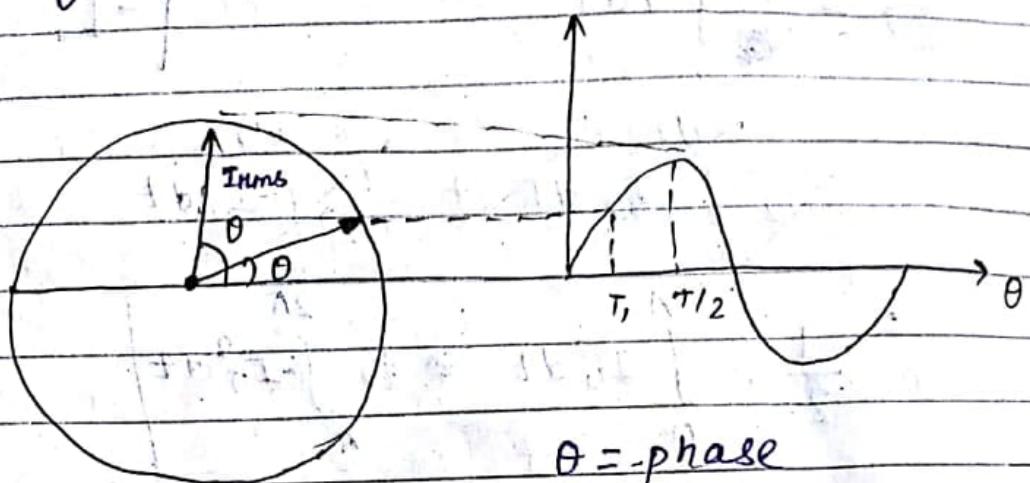
$$\begin{aligned} I_{\text{avg}} &= \frac{1}{T/2} \int_0^{T/2} i dt = \frac{1}{\pi} \int_0^{\pi} I_0 dt \\ &= \frac{I_0 \times \pi}{\pi} = I_0. \end{aligned}$$

$$\text{Form factor} = \sqrt{2}$$

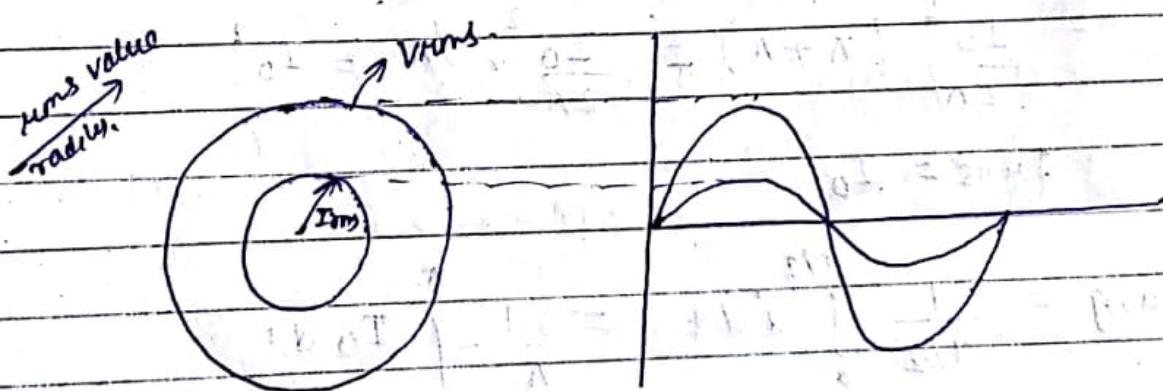
$$\text{Peak factor} = \frac{I_0}{I_0} = 1$$

## Phasor quantity

Only sinusoidal quantity can be represented as a phasor diagram and the magnitude of that phasor is rms. value of that quantity.



$$V = IR$$



In a resistive ckt, current and voltage are in same phase.

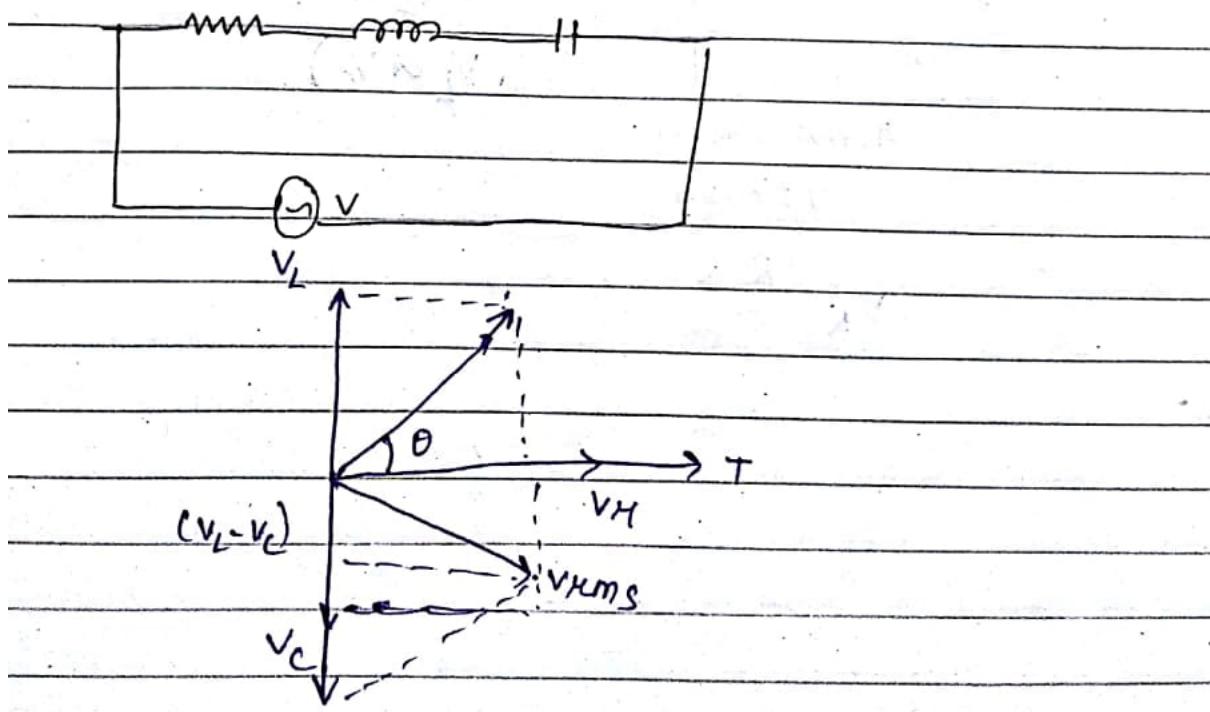
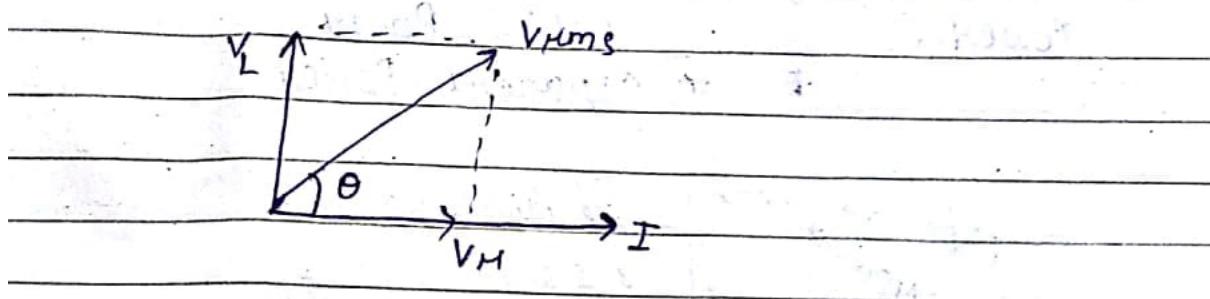
$$E = E_0 \sin \omega t$$

$$I = E_0 \sin \omega t$$

$$= I_0 \sin \omega t$$

$V = V_0 \sin \omega t$   
 $I_L = \frac{V}{jX_L} = \frac{V}{j\omega L} \sin(\omega t - 90^\circ)$

$V_{rms}$  is reference.  
 $I_L$



## Power factor angle

$$P = V_{\text{rms}} I_{\text{rms}}$$

$P = \text{apparent Power}$

$$\text{Unit of } P = \text{VA} = \text{Volt-Ampere}$$

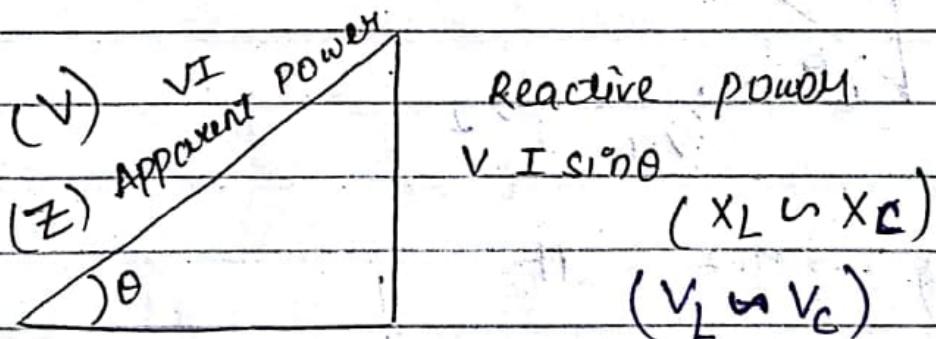
$$\text{Active / Available Power} = V_{\text{rms}} \cdot I_{\text{rms}} \cos \theta$$

$$\text{Reactive Power} = V_{\text{rms}} \cdot I_{\text{rms}} \sin \theta$$

## Power factor

The ratio of active power to the apparent power.

$$\text{Power Factor} = \frac{\text{Active Power}}{\text{Apparent Power}}$$

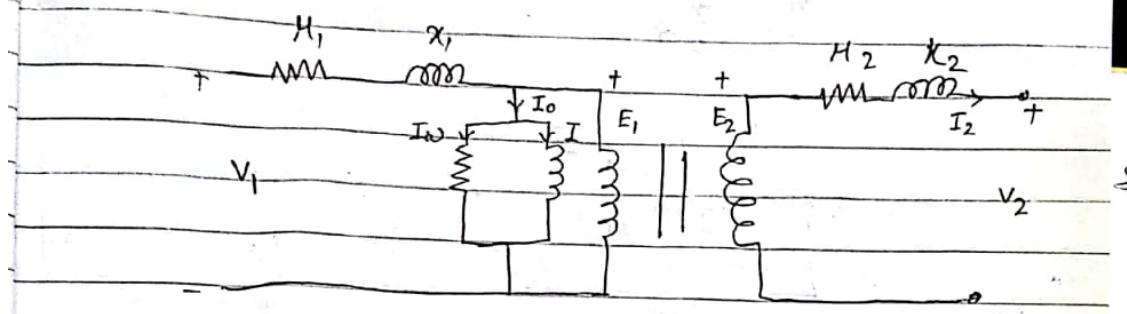
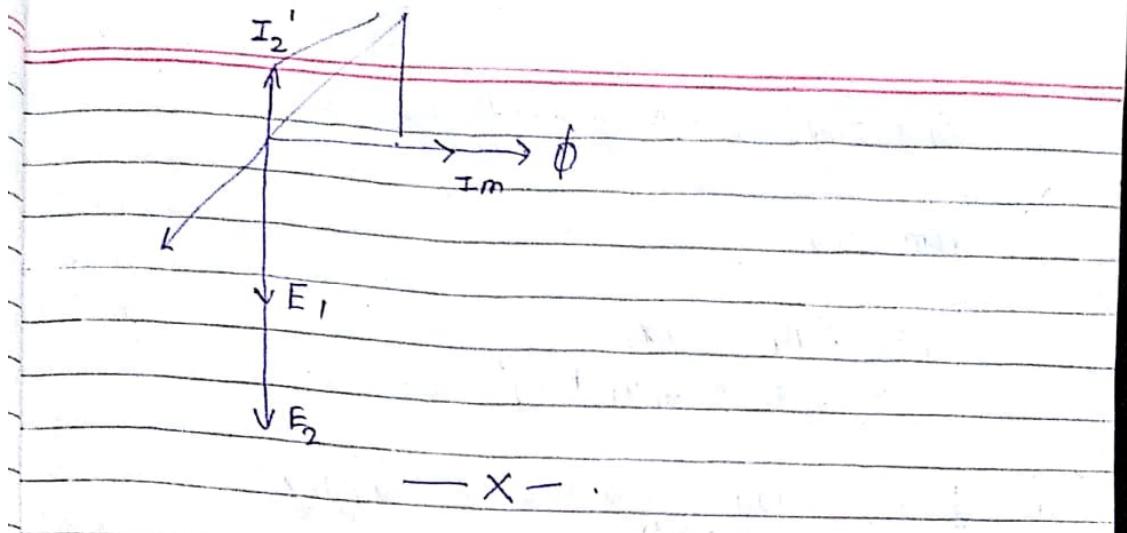


Active Power

$$VI \cos \theta$$

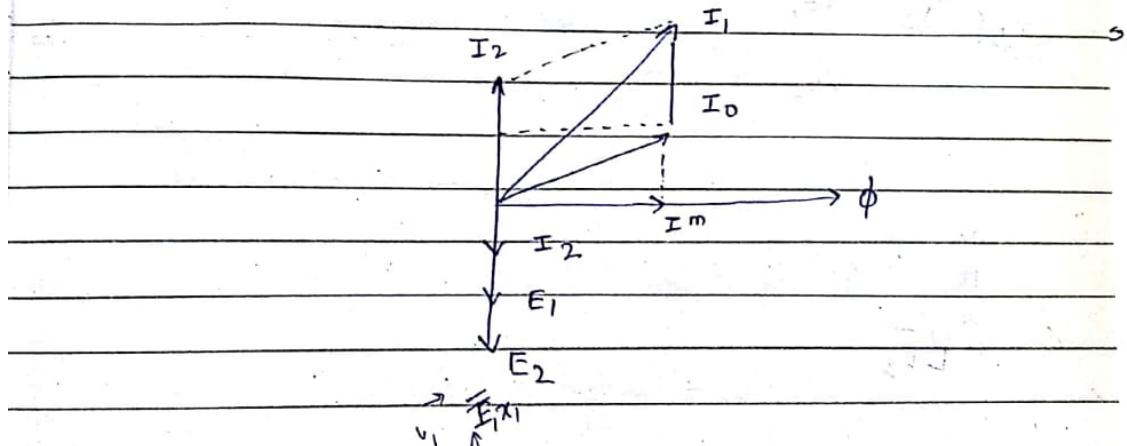
$$(R)$$

$$V_R$$

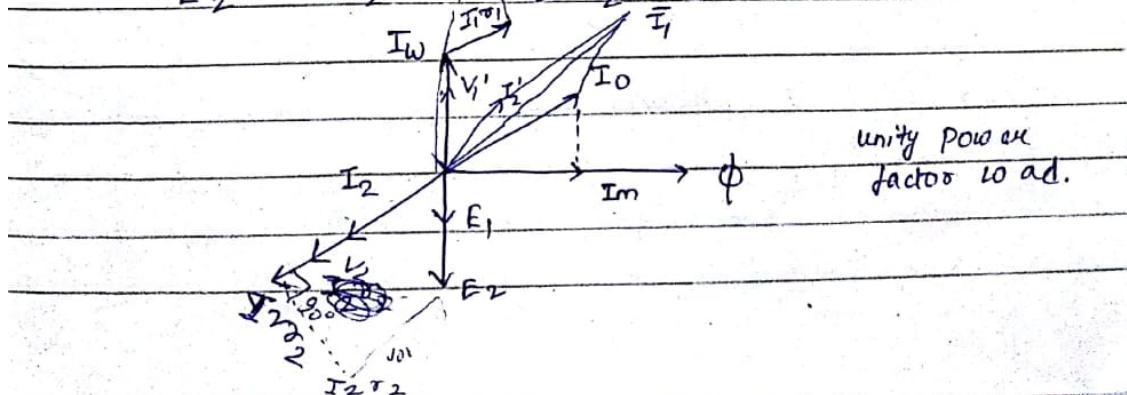


Applying KVL at Primary, phasor eq<sup>n</sup>

$$v_1 = \bar{I}_1 x_1 + \bar{I}_1 x_1 + \bar{E}_1 \quad \text{(1)}$$



$$E_2 = \bar{I}_2 x_2 + \bar{I}_2 x_2 + v_2$$

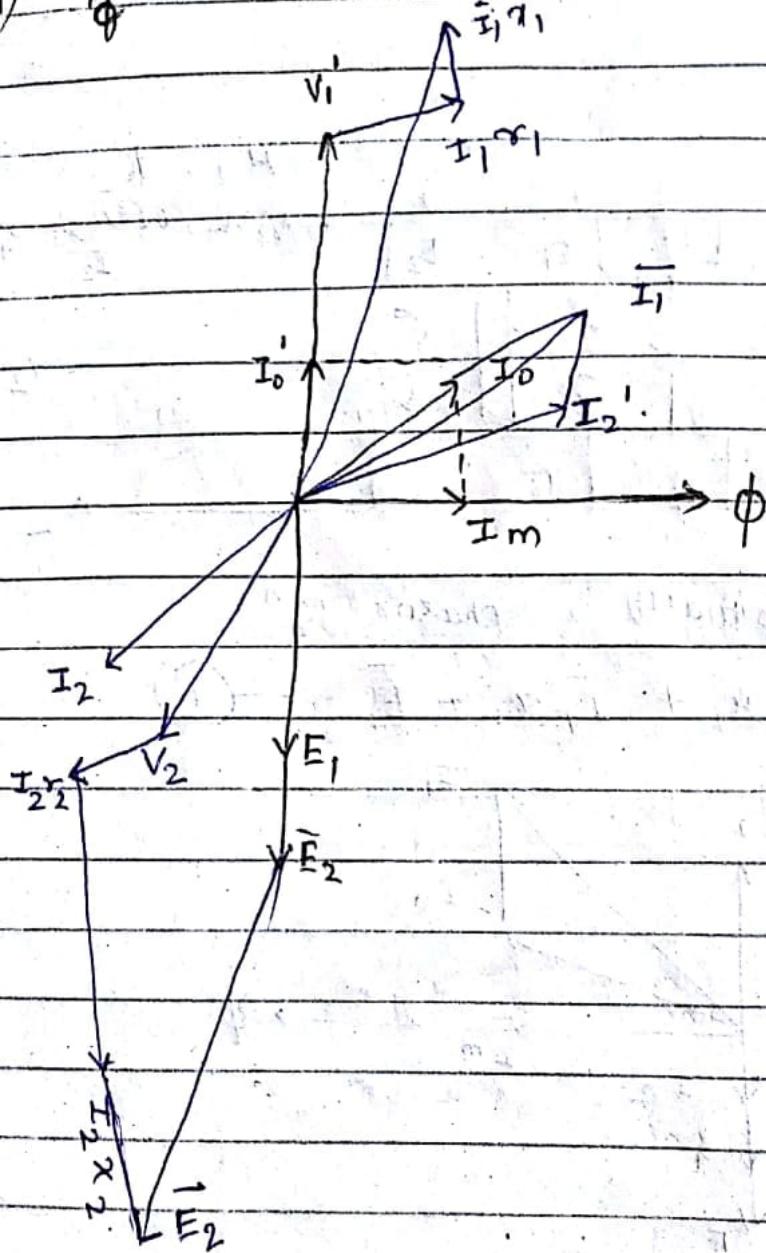


$$E_1 = -\bar{V}_1' \quad [(-) \text{ to indicate direction, not magnitude.}]$$

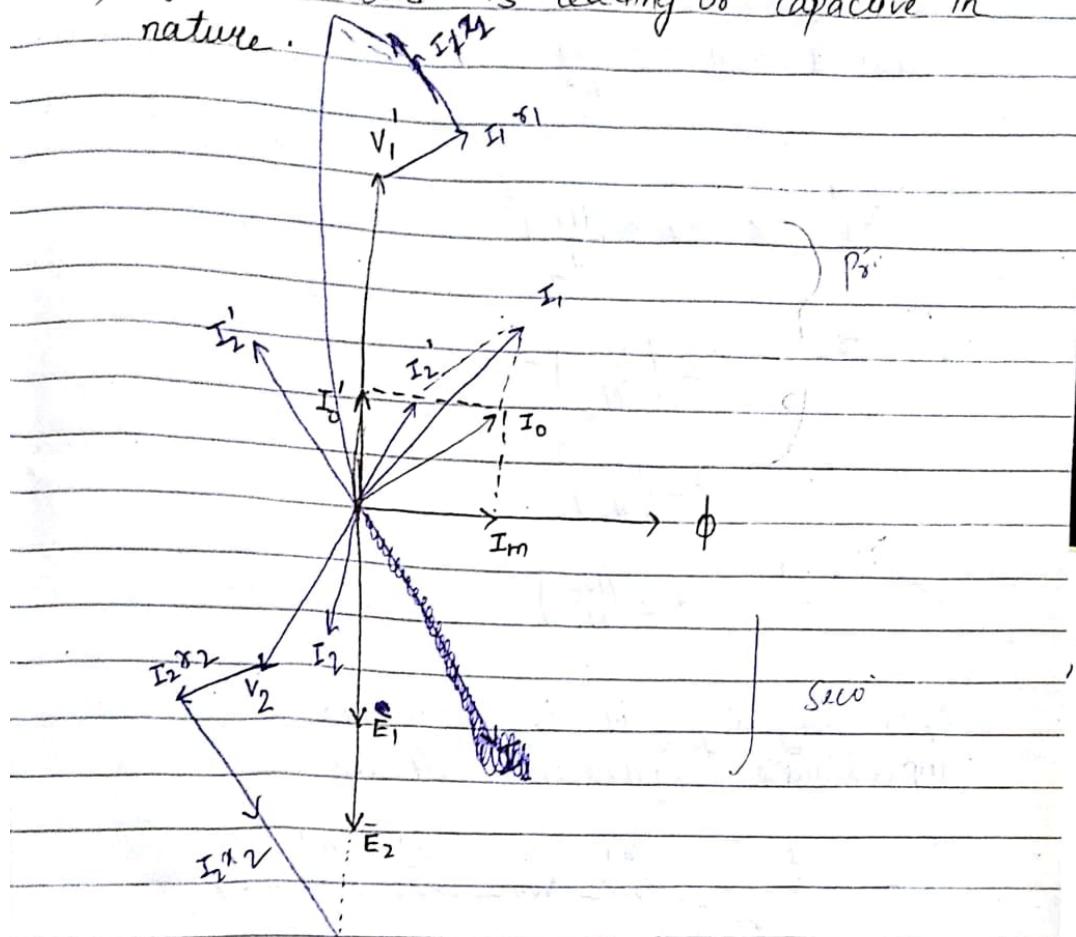
From ①,

$$\begin{aligned} \bar{V}_1 &= \bar{I}_1 H_1 + \bar{I}_1 X_1 + \bar{E}_1 \\ &= \bar{I}_1 x_1 + \bar{I}_1 x_1 + v_1' \end{aligned}$$

ii) If the Load connected is lagging

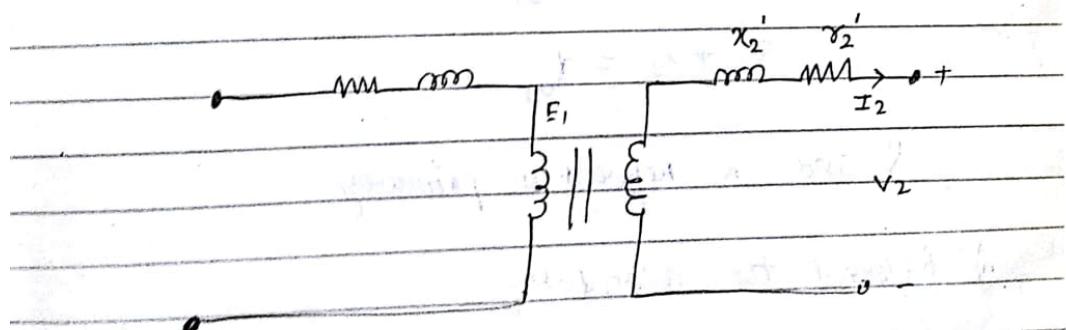


iii) If the Load is leading or capacitive in nature.



i) Referred to primary

$$\frac{E_1}{N_1} = \frac{E_2}{N_2} \Rightarrow E_2 = \frac{N_2}{N_1} E_1$$



Value of  $E_2$  is referred to primary  $= E_2'$

$$\frac{E_2'}{E_2} = \frac{N_1}{N_2}$$

$$\frac{N_2}{N_1} \rightarrow \frac{\tau_2}{\tau_1} \quad 2 \\ \frac{N_2}{N_1} \rightarrow \frac{\tau_2}{\tau_1} \left( \frac{N_1}{N_2} \right)$$

$$E_2' = \frac{N_1}{N_2} E_2$$

$$N_2 \rightarrow \tau_2 \\ \text{For 1 turn} \rightarrow \frac{\tau_2}{N_2^2}$$

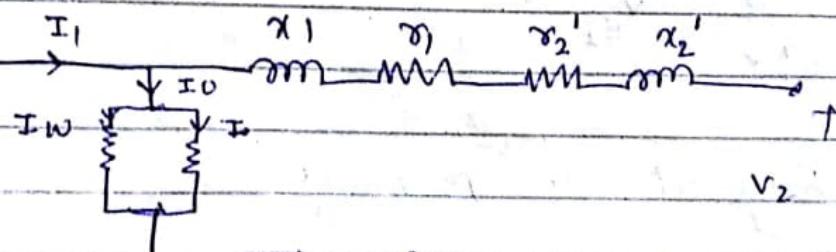
$$N_1' \rightarrow \tau_2 \times \left(\frac{N_1}{N_2}\right)^2$$

$$\tau_2' = \tau_2 \left(\frac{N_1}{N_2}\right)^2$$

$$x_2' = x_2 \left(\frac{N_1}{N_2}\right)^2$$

$$I_2' = \mp_2 \left(\frac{N_2}{N_1}\right)$$

After Meffering, it is known as approximate equivalent circuit.



$I_0$  is very small

$$\tau_1 + \tau_2' = R_{01}$$

$$x_1 + x_2' = X_{01}$$

R and X referred to primary.

i) Referred to secondary

value of  $E_1'$  is referred to secondary =  $E_1'$

$$\frac{E_1'}{E_1} = \frac{N_2}{N_1}$$

$$E_1' = \left(\frac{N_2}{N_1}\right) E_1 \quad x_1' = \left(\frac{N_2}{N_1}\right)^2 x_1$$

$$\gamma_1' = \left(\frac{N_2}{N_1}\right)^2 \gamma_1 \quad I_1' = \frac{N_1}{N_2} I_1$$

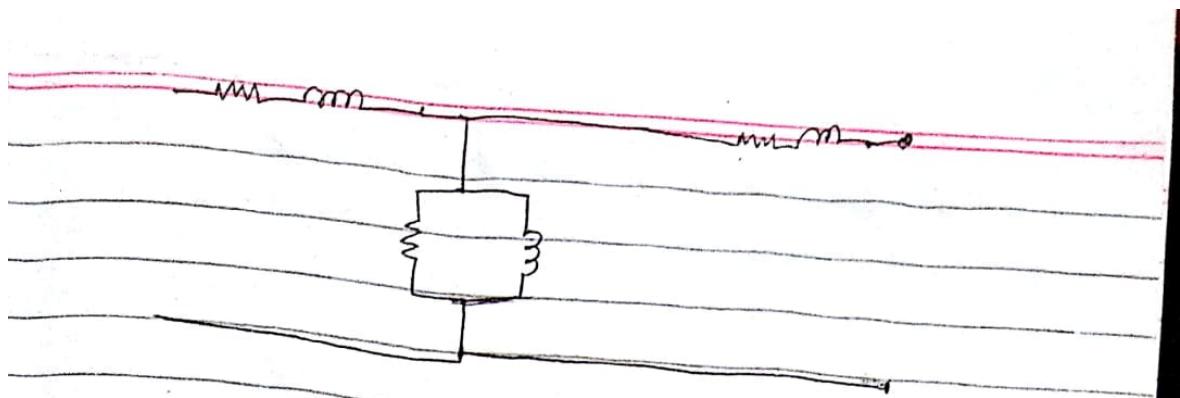
$$I_W' = \frac{N_1}{N_2} I_W \quad I_m' = \frac{N_1}{N_2} I_m$$

$$R_W' = \left(\frac{N_2}{N_1}\right)^2 R_W \quad X_m' = \left(\frac{N_2}{N_1}\right)^2 X_m$$

$$\gamma_1' + \gamma_2 = R_{02}$$

$$x_1' + x_2 = X_{02}$$

$R_{02}$  and  $X_{02}$  are referred to secondary



$$E_2' = \frac{N_1}{N_2} E_2 \quad x_2' = \left(\frac{N_1}{N_2}\right)^2 x_2$$

$$x_2' = \left(\frac{N_1}{N_2}\right)^2 x_2 \quad V_2' = \frac{N_1}{N_2} V_2$$

$$I_2' = \frac{N_2}{N_1} I_2$$

Exact equivalent ckt referred to primary.

$$x_1 + x_2' = R_{01}$$

$$x_1 + x_2' = x_{01}$$

$$E_1' = \frac{N_2}{N_1} E_1 \quad I_W' = \frac{N_1}{N_2} I_W \quad x_m' = \left(\frac{N_2}{N_1}\right)^2 x_m$$

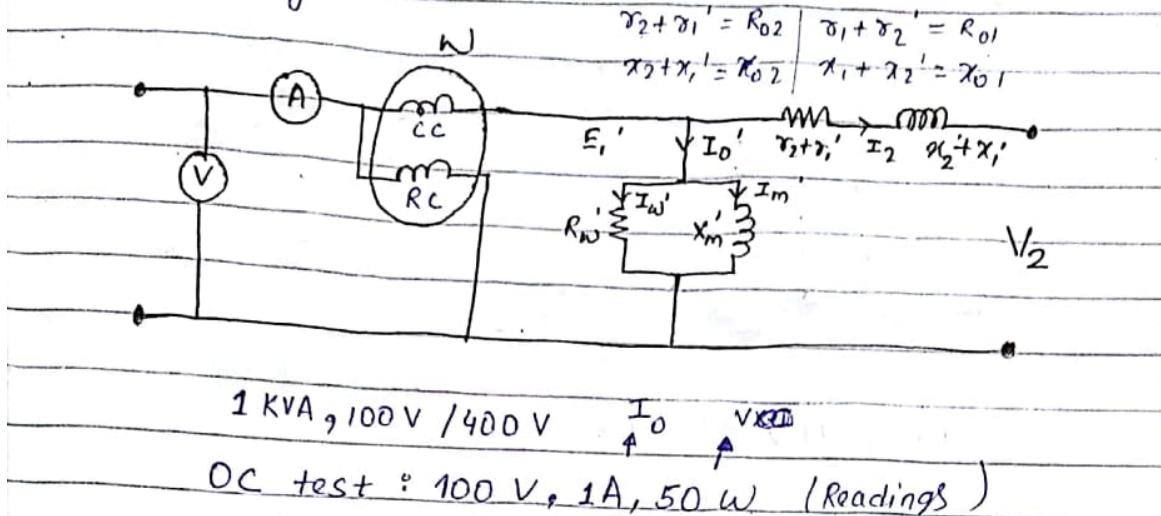
$$V_1' = \frac{N_2}{N_1} V_1 \quad I_m' = \frac{N_1}{N_2} I_m \quad I_0' = \frac{N_1}{N_2} I_0$$

$$I_1' = \frac{N_1}{N_2} I_1 \quad R_W' = \left(\frac{N_2}{N_1}\right)^2 R_W \quad x_1' = \left(\frac{N_2}{N_1}\right)^2 x_1$$

$$x_1' = \left(\frac{N_2}{N_1}\right)^2 x_1$$

( core made of grain oriented steel)  
 CRGO, Silicon, with bit of  
 Hysteresis loss reduce  
 laminated sheet : Reduce Eddy current  
Open - CKT test  
 wattmeter :  
 No-load losses are fixed  
 losses in TXH i.e. they  
 remain const  $\rightarrow$  Hysteresis  
 $\rightarrow$  Eddy current loss

As the name suggest, we will open the circuit  
 Apply rated voltage. Open-CKT test perform on  
 low voltage side



OC test : 100 V, 1A, 50 W (Readings)

$$I_m = I_0 \sin \phi$$

$$I_w = I_0 \cos \phi$$

$$VI_0 \cos \phi = 50$$

$$\cos \phi = \frac{50}{1 \times 100}$$

$$= \frac{1}{2}$$

$$\cos \phi = 0.5$$

$$\sin \phi = 0.867$$

$$I_m = 0.867 \text{ A}$$

$$I_w = 0.5$$

$$X_m = \frac{100}{0.867}$$

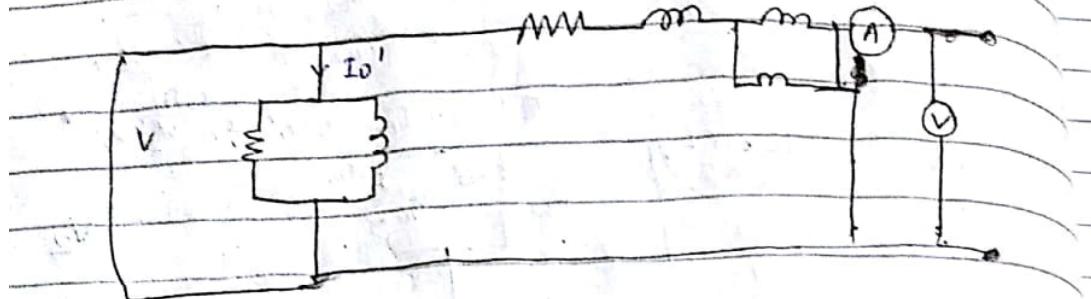
$$R_w = \frac{100}{0.5} - 200 \Omega$$

$$= 115.34 \Omega$$

why low voltage not high voltage.

- 1) very high voltage needed i.e. 400 V.
- 2) Dangerous

SC perform on high voltage side. LV side is short circuited.



1 kVA, 1000 V / 400 V

DC test : 100V, 1A, 50W

SC test : 40V, 2.3A, 80W → ohmic or varia. loss  
or  
 $I^2R$  loss

$$I^2 R_{02} = 80$$

$$R_{02} = \frac{80}{(2.3)^2} \therefore R_{02} = 12.8 \Omega$$

$$Z_{02} = \frac{40}{2.3} = 16 \Omega$$

$$X_{02} = \sqrt{Z_{02}^2 - R_{02}^2}$$

$$= \sqrt{16^2 - (12.8)^2} = \sqrt{256 - 163.84}$$

$$= 9.6 \Omega$$

$$R_{01} = 12.8 \times \left(\frac{100}{400}\right)^2$$

$$= \frac{12.8}{16}$$

$$X_{01} = 9.6 \times \left(\frac{100}{400}\right)^2 \Omega$$

$$X_m' = X_m \times \left(\frac{100}{400}\right)^2$$

$$R_w' = R_w \times \left(\frac{100}{400}\right)^2$$

~~Primary~~

OC test

→ Low voltage side

Convert high voltage side parameters  
to low voltage side.

~~secondary~~

SC test

→ high voltage side

convert low voltage side parameters  
to high voltage side.

Find parameters for primary and secondary re

5 kVA, 500 V / 200 V  $I_0$   $V I_0 \cos \phi$

DC test :  $\frac{\text{Rated voltage}}{200 \text{ V}}, 1.5 \text{ A}, 80 \text{ W} \rightarrow \text{No load lossy}$

SC test : 50 V, 10 A, 200 W.

Primary :

$$I_m = I_0 \sin \phi$$

$$I_w = I_0 \cos \phi$$

$$\phi = 0^\circ$$

$$V I_0 \cos \phi = 80$$

$$V = 200$$

$$\cos \phi = \frac{80}{200 \times 25}$$

$$I_0 = \frac{5000}{3200} = 1.5$$

$$= \frac{8}{25 \times 20} + \frac{8}{500} = 0.016$$

$$CO = \sqrt{1 - 0.016^2} = 0.996$$

$$\cos \phi = 0.996$$

$$\cos \phi = \frac{80}{200 \times 1.5} = 0.26$$

$$\sin \phi = 0.965$$

$$I_m = 1.5 \times 0.965 = 1.44$$

$$I_w = 1.5 \times 0.26 = 0.4$$

$$X_m = \frac{200}{1.44} = 138.88 \quad R_w = \frac{200}{0.4} = 500$$

$R_{01} \rightarrow$  when perform in primary  
 $R_{02} \rightarrow$  when perform in secondary

Secondary :

$$I^2 R_{01} = 200$$

$$R_{01} = \frac{200}{10 \times 10} = 2$$

$$Z_{01} = \frac{50}{10} = 5$$

$$X_{01} = \sqrt{25 - 4} = \sqrt{21} = 4.58$$

$$R_{02} = R_{01} \times \left(\frac{200}{500}\right)^2$$

$$= \frac{2 \times 2 \times 2}{5 \times 5} = \frac{8}{25} = 0.32$$

$$X_{02} = X_{01} \times \left(\frac{200}{500}\right)^2$$

$$X_m = X_m \times \left(\frac{500}{200}\right)^2$$

$$R_w' = R_w \times \left(\frac{500}{200}\right)^2$$

$\therefore 10 \text{ kVA}, 1000 \text{ V}/500 \text{ V}$

OC test  $\rightarrow 500 \text{ V}, 2 \text{ A}, 1100 \text{ W}$   
 SC test  $\rightarrow 50 \text{ V}, 10 \text{ A}, 300 \text{ W}$

Find the eq. ckt parameters  
 i) OC  
 ii) SC.

Voltage regulation.

Fractional change of  $\text{txr}$  from No load to Full load.

$$V_{NL} = \text{No load Voltage} = E_2$$

$$\text{Full load voltage} = V_2$$

$$\text{Voltage regulation} = \frac{E_2 - V_2}{E_2}$$

## DC Machine

Mechanical part → Rotating Machine

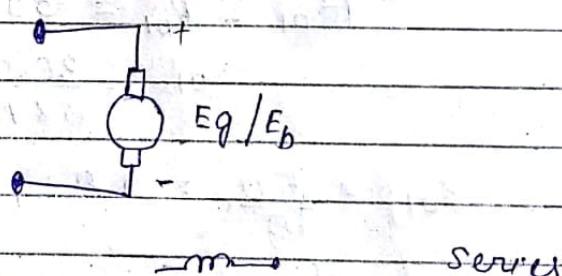
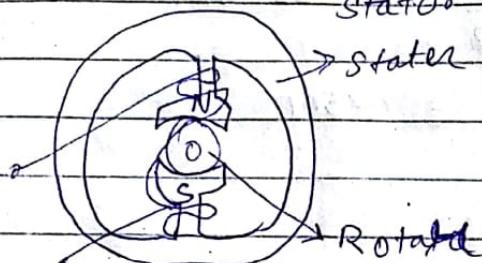
→ Stator : stationary part

→ Rotator : Rotating part

→ Electrical part : Field and Armature.

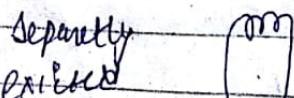
→ Field placed on ~~Armature~~ and Rotator in Stator

~~Field~~ Armature



Parallel

Separately excited



compound

