

1.

a) False,

Naive Bayes classifier assumes that each feature x_i is conditionally independent of each other feature x_j for $j \neq i$

b) ~~False~~, True

The success of pattern classification scheme using decision function depends on two factors :-

- i) The form of the decision function $d(x)$
- ii) ~~The~~ One's ability to determine the coefficients.

The first factor is governed by the geometrical properties of the classes under consideration.

c) ~~False, True, False~~

~~The~~ In syntactic pattern recognition the set of ~~input~~ pattern primitives & ~~the~~ the grammar is required for the classification. Training phase is not an essential step.

d) False, ~~The~~ points that are ~~also~~ within the margin of the hyperplane can only be the support vectors.

e) True,

Density-based clustering algorithms groups points together under one cluster when they occur in a high density region.

Outliers generally occur in low ~~as~~ density regions, hence are not classified.

4). True,

Naive Bayes classifier assumes that the classes are conditionally independent.

For example consider a naive-bayes classifier to classify spam & important emails. The classifier will only consider the occurrence of certain keywords in the mails in order to classify the mail. The ordering of the keywords ~~is not~~ words ~~are~~ in not in paid importance, which is not true in real life.

g) False,

~~the~~ Syntactic Pattern Recognition attempts to classify ~~problems~~ patterns based on a set of extracted features called pattern primitives and their geometrical model ~~repres~~ represented through the grammar.

h) False,

Hierarchical clustering methods help in exploring data at different levels of ~~gr~~ granularity.

i) False,

A Hopfield net is mainly used for optimization.

j) False,

for a supervised pattern classification problem having M -classes ~~sets~~, where the classes are pairwise separable, the classifier needs to compute $[M(M-1)]/2$ number of decision surfaces.

k). false,

Data processing is required to ensure

- accuracy, consistency, completeness, timeliness, believability &
- interpretability.

2.

M-patterns.

prototypes: Z_1, Z_2, \dots, Z_M classes: $\omega_1, \omega_2, \omega_3, \dots, \omega_M$

~~We can determine the~~

we use euclidean distance of a point from any given prototype as a measure of similarity of that point to a particular the particular class belonging to the prototype.

$$D_i = \|X - Z_i\| = \sqrt{(X - Z_i)'(X - Z_i)}$$

Minimum-distance classification is used here, i.e. a given point X is assigned to the class that has the minimum euclidean distance from it.

X is assigned to class ω_i if $D_i < D_j \forall j \neq i$.

(Ties are resolved arbitrarily)

$$\begin{aligned} D_i^2 &= \|X - Z_i\|^2 = (X - Z_i)'(X - Z_i) \\ &= X'X - X'Z_i - Z_i'X + Z_i'Z_i \\ &= X'X - 2(X'Z_i - \frac{1}{2}Z_i'Z_i) \end{aligned}$$

we need to choose i such that D_i^2 is minimum

$\Rightarrow D_i^2$ is minimum (as D_i is always a +ve value)

\Rightarrow choosing i such that $(X'Z_i - \frac{1}{2}Z_i'Z_i)$ is maximum.
as $X'X$ is independent of i .

∴

∴ we can define decision function as follows: | Md. Sahid, 001710501019 (4)

$$d_i(x) = X'Z_i - \frac{1}{2} Z_i'Z_i, i=1,2,\dots, H$$

when X is assigned to the class w_i

$$\text{when } d_i(x) > d_j(x) \quad \forall i \neq j$$

We can see that $d_i(x)$ is a linear decision function.

3.

Bayes's theorem describes the probability of an event, based on prior knowledge of conditions that might be related to the event.

Mathematically :-

Let X be a data sample

Let H be a hypothesis that X belongs to a class C .

$P(H) \rightarrow$ initial probability.

$P(X) \rightarrow$ (evidence) probability that sample data is observed

$P(X|H) \rightarrow$ (likelihood) the probability of observing X given that the hypothesis holds.

$$P(H|X) = \frac{P(X|H) P(H)}{P(X)}$$

Let D be a set of N tuples $\{x_1, x_2, \dots, x_N\}$

when $x_i \in \mathbb{R}^n$.

→ ~~class~~ K -classes C_1, C_2, \dots, C_K .

∴ From Bayes's theorem

$$P(C_k|X) = \frac{P(X|C_k) P(C_k)}{P(X)} \quad P(C_i|X) = \frac{P(X|C_i) P(C_i)}{P(X)}$$

Since the denominator is not dependent on C_i and all values of the ~~fact~~ features are known, \therefore The denominator is effectively constant.

\therefore Only numerator is significant, which is equivalent to the joint

probability model $P(C_k, x_1, \dots, x_n)$

$$P(C_i) P(X|C_i) = P(C_k, X)$$

$$\text{or } P(C_i) P(x_1, x_2, \dots, x_n | C_k) = P(C_k, x_1, x_2, \dots, x_n)$$

$$\text{Let } [X = \{x_1, x_2, x_3, \dots, x_n\}]$$

using chain rule for repeated application of definition of conditional probability:

$$\begin{aligned} P(C_i, x_1, x_2, \dots, x_n) &= P(x_1, x_2, \dots, x_n, C_i) \\ &= P(x_1 | x_2, \dots, x_n, C_i) P(x_2, x_3, \dots, x_n, C_i) \\ &\vdots \\ &= P(x_1 | x_2, \dots, x_n, C_i) P(x_2 | x_3, \dots, x_n, C_i) \dots P(x_{j-1} | x_j, \dots, x_n, C_i) \\ &\quad \dots P(x_{n-1} | x_n, C_i) P(x_n | C_i) P(C_i) \end{aligned}$$

Naive Bayes assumes that each feature x_i is conditionally independent of every other feature x_j for $i \neq j$.

$$\Rightarrow P(x_j | x_{j+1}, \dots, x_n, C_i) = P(x_j | C_i)$$

Then the joint model can be expressed as :-

$$\begin{aligned} &\cancel{P(C_i, x_1, \dots, x_n)} \propto \cancel{P(C_k, x_1, \dots, x_n)} \\ &= P(C_k) P(x_1 | C_k) P(x_2 | C_k) \dots P(x_n | C_k) \end{aligned}$$

$$\begin{aligned} P(C_i, x_1, x_2, \dots, x_n) &= P(C_i) \cdot P(x_1 | C_i) P(x_2 | C_i) \dots P(x_n | C_i) \\ &= P(C_i) \prod_{j=1}^n P(x_j | C_i) \end{aligned}$$

In order to classify X , we pick the hypothesis that is most probable, i.e.

∴ The corresponding classifier, a Bayes classifier, is the function that assigns a class label $\hat{y} = c_i$ for some i as follows:

$$\hat{y} = \underset{i \in \{1, \dots, k\}}{\operatorname{argmax}} P(c_i) \prod_{j=1}^n P(x_j | c_i)$$

Let A_j denote the j th feature of a given data sample X .

Now A_j can be either categorical or continuous valued.

$P(x_j | c_i)$ has to be computed ~~differential~~ differently for the above mentioned two cases.

If A_j is categorical, $P(x_j | c_i)$ is the number of tuples in c_i having value x_j of A_j divided by $|c_i|$ (number of tuples of c_i in D).

If A_j is continuous-valued, $P(x_j | c_i)$ is usually computed based on the Gaussian distribution with a mean μ and SD σ .

$$g(x, \mu, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$$\text{so, } P(x_j | c_i) = g(x_j, \mu_{c_i}, \sigma_{c_i})$$

5.



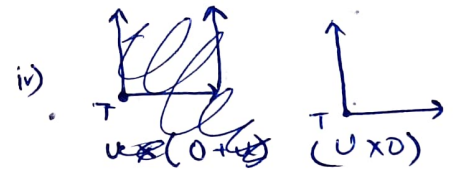
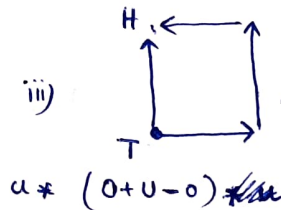
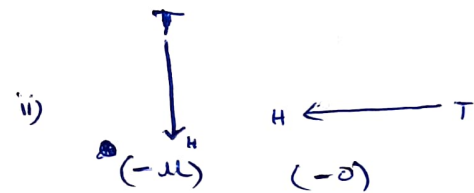
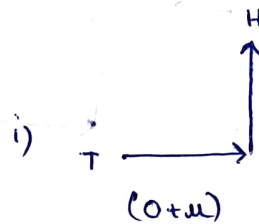
Primitives required :-
 $\{0, u\}$

$$T \xrightarrow{0} H$$



Operation allowed on primitives :-

$\{*, -, +, \times\}$



$*$ \longrightarrow represents head-head & tail-tail attachment.

$+$ \longrightarrow represents head to tail concatenation

$-$ \longrightarrow represents head-tail reversal

\times \longrightarrow represents tail-tail attachment.

The grammar consists of :

1. Start symbol S

2. Set of terminals $\{u, 0, *, -, +, \times, |, (,)\}$

(where "|" is or-operator, "(" & ")" are opening & closing parentheses)

3. Set of non-terminals $\{S, A, C, P, F\}$

4. Set of production rules $P = \{$

$$S \rightarrow A | C | P | F,$$

$$A \rightarrow u + ((0u + 0 + -u) \times 0) + -u,$$

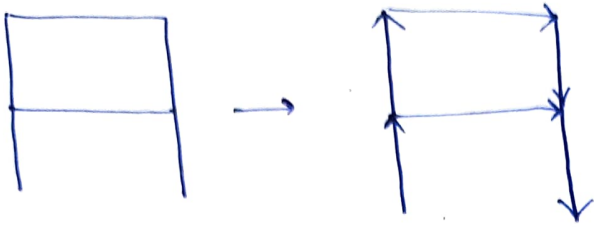
$$C \rightarrow -0 + u + u + 0,$$

$$P \rightarrow u + ((u + 0 + -u) \times 0),$$

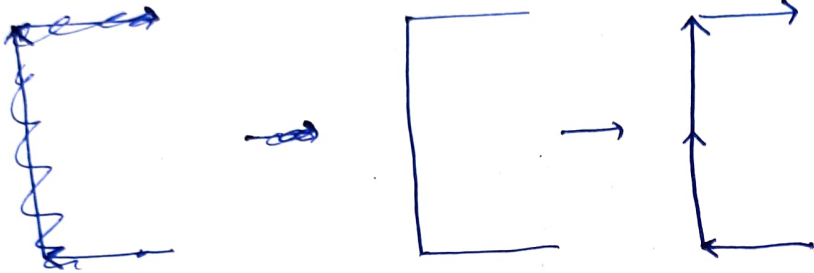
$$F \rightarrow u + (0 \times u) + 0$$

}

Primitive representation & interconnections :-



$$A = u + ((u + 0 + -u) * 0) + -u$$



$$C = -0 + u + u + 0$$



$$P = u + ((u + 0 + -u) * 0)$$



$$F = u + (0 * u) + 0$$

6. Pattern recognition is the automated recognition of patterns and regularities in data.

It can be divided into two use cases.

i) Recognizing concrete items.

Ex- pictures.

ii) Recognizing abstract items.

Ex- voical audio.

Most conventional approaches of pattern recognition are based on direct computation through machines which are math-related techniques. These conventional approaches include :- feature extraction, classification, clustering etc.

We can also use application of biological concepts of neurons ~~inside~~ in humans for computing. This lead to the development of neural networks.

ANN (Artificial Neural Networks):-

An Artificial Neural Network is a paralleled distributed information processing structures in the form of a directed graph.

It consists of a larger number of simple processing units (perceptions) ~~with~~ a high degree of ~~data~~ arranged into ~~layers~~ one or more layers with a high degree of interconnection between each layer of units.

The processing units works parallelly and in coordination with each other.

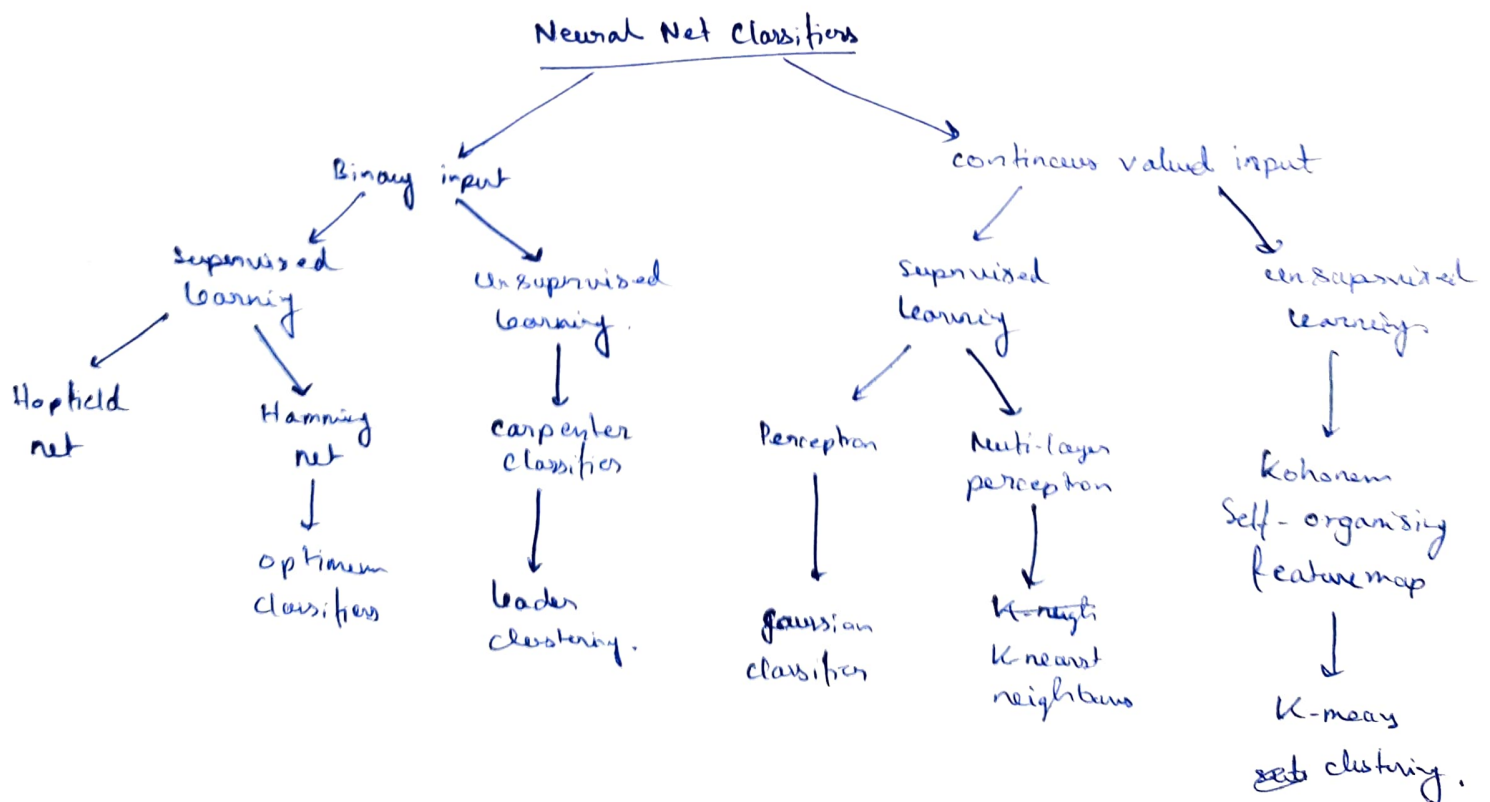
The design & function of neural networks simulate some functionality of biological brains and neural system.

Pattern recognition can be done using both conventional computers and neural networks.

- Neural networks require simple processors as opposed to general computers which use few complex processors.
- Neural networks use fewer processing steps.
- Neural networks use the concept of distributed processing making them faster.
- Neural nets are trained by example helping them to achieve far better results even for unknown data.
- Neural nets are tolerable to noisy patterns.

Due to the adaptive-learning, self-organizing and fault tolerance capabilities of neural nets, ANNs are used for various pattern recognition applications.

Neural networks as classifiers:-



We can see the importance of ANN in Pattern Recognition by looking at the diversity of applications that ANN's have in Pattern Recognition problems.

Algorithms	Type	usage
Hopfield	recursive	optimization
Multi-layer perceptron	feedforward	classification
Kohonen	self-organising	data-coding
Temporal differences	predictive	forecasting.

∴ Neural networks provides the following advantages:-

- Can work with incomplete information once trained
- Fault tolerance (robust to outliers)
- Distributed
- Parallel
- Can learn non-linear and complex relationships
- ~~are~~ trained by example
- Generalizability & i.e. can infer unseen relationships once trained.