

Assume the following properties of air and water unless otherwise specified:

**AIR:**  $\rho = 1.16 \text{ kg m}^{-3}$ ,  $\nu = 1.86 \times 10^{-5} \text{ m}^2 \text{ s}^{-1}$ ,  $C_p = 1.014 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ,  $Pr = 0.7$

**WATER:**  $\rho = 1000 \text{ kg m}^{-3}$ ,  $\nu = 1.0 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$ ,  $C_p = 4.186 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ,  $Pr = 7.0$

**Part I (10 marks)**

1. A flat heater surface, having emissivity of 0.8, runs parallel to a blackbody surface at a separation of 5 mm. The blackbody surface is maintained at 273 K by keeping it in contact with ice-bath. Under steady state,  $5 \text{ kW/m}^2$  heat is uniformly dissipated through the heater surface. If the gap between the plates is filled up by a heat transfer oil of thermal conductivity of  $1 \text{ W/mK}$ , what is the heater surface temperature? Heat transfer due to convection may be neglected. 10

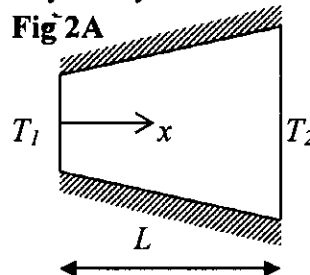
**OR**

A 1 cm diameter heated sphere ( $\rho_{\text{solid}} = 3000 \text{ kg/m}^3$ ,  $C_{\text{solid}} = 1000 \text{ J/kgK}$ ) at  $150^\circ\text{C}$  is dipped into an isothermal liquid ( $k_{\text{liquid}} = 1 \text{ W/mK}$ ) pool of  $50^\circ\text{C}$ . The liquid over the sphere does not have any relative velocity with respect to it. What is the rate of cooling of the sphere, right when it is dipped into the pool? How long does it take to cool the sphere to  $100^\circ\text{C}$ ? Assume that  $k_{\text{solid}} \gg k_{\text{liquid}}$ . Neglect radiation and free convection. 10

**Part II (Answer Q 2 and 3, total 30 marks)**

2. A conical cylinder is insulated along its tapered surface. The cylinder has a length  $L$  and its radii at the smaller and larger ends are  $R_1$  and  $R_2$ , respectively (see Fig 2A). The surfaces are maintained at temperatures  $T_1$  and  $T_2$  as shown in the figure. Considering 1-d steady heat conduction, find the expressions of temperature as a function of  $x$  and the overall thermal resistance offered by the cylinder. 20

Fig 2A



**OR**

The inner surface at  $r = a$  and the outer surface at  $r = b$  of a hollow sphere are maintained at uniform temperatures  $T_1$  and  $T_2$ , respectively. The thermal conductivity of the material is constant. (i) Develop an expression for the 1-dimensional steady-state temperature distribution  $T(r)$  in the sphere. Also evaluate the expressions of (ii) heat flow rate and (iii) thermal resistance offered by the hollow sphere. (iv) Using the last expression, show that the Nusselt number for a spherical solid in a quiescent fluid medium is 2.

10 + 3+3+4 = 20

Time: Three Hours

(Full Marks 100)

3. State the reciprocity and summation rules of view factors. Using them, derive an expressions of shape factors  $F_{12}$  and  $F_{13}$  of the following triangular prism of infinite length (See Fig 3A), and evaluate them where  $W_1: W_2: W_3 = 6: 4: 3$ : 10

OR

State Hottel's cross-string method, and deduce from it the view factors  $F_{11}$  and  $F_{12}$  for the pair of surfaces 1 and 2 of infinite length perpendicular to the plane of the paper, as shown in Fig 3B. 10

Fig 3A

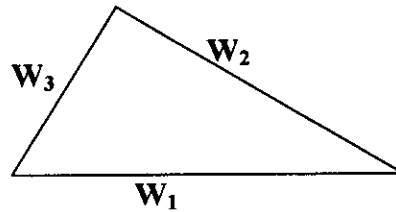
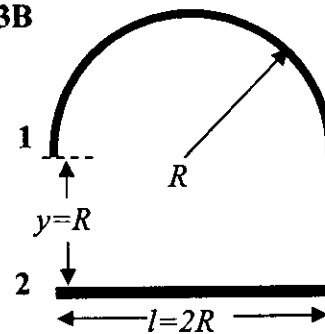


Fig 3B

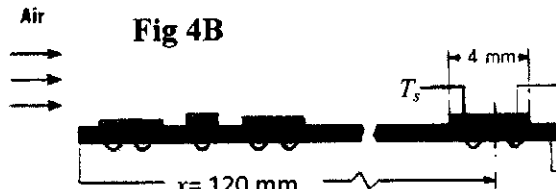


### Part III (Answer Q 4 and 5; $20 \times 2 = 40$ Marks)

4. Hot air at atmospheric pressure and  $80^\circ\text{C}$  enters an 8 m long un-insulated square duct of cross section  $0.2\text{m} \times 0.2\text{m}$  at a rate of  $0.15\text{ m}^3/\text{s}$ . The duct loses heat to the surroundings which is at  $15^\circ\text{C}$ . The heat transfer coefficient between the outer surface of duct and the outside ambient is  $20\text{ W/m}^2$  while the duct wall thickness is negligible. Consider the flow through the duct fully developed and neglect the effect of thermal radiation. Estimate the outlet temperature of air and the heat loss from the duct. 20

OR

Forced air at  $25^\circ\text{C}$  and  $10\text{ m/s}$  is used to cool electronic elements mounted on a circuit board (see Fig 4B). Consider a  $4\text{ mm} \times 4\text{ mm}$  chip located  $120\text{ mm}$  from the leading edge. Because the board has rough and irregular surface, the flow is disturbed, and the appropriate convection correlation is of the form  $Nu_x = 0.04 Re_x^{0.85} Pr^{0.33}$ . Estimate the average surface temperature  $T_s$  of the chip for a  $30\text{ mW}$  heat dissipation from it. 20



5. An incandescent spherical  $100\text{ W}$  lightbulb of  $8\text{ cm}$  diameter hung in a quiescent air of  $27^\circ\text{C}$  converts a fraction of its input to light energy and the remaining part is converted to heat, which is dissipated by radiation and free convection. If the surface temperature of the bulb is  $177^\circ\text{C}$ , find the fraction of the energy that is converted to light. Assume the walls of room where the bulb is housed are also at  $27^\circ\text{C}$  and the glass  $\epsilon = 0.9$ . Assume the correlation  $Nu_D = 2 + (0.589 Ra_D^{0.25}) / [1 + (0.469/Pr)^{9/16}]^{4/9}$  to hold good. 20

OR

Consider a cylindrical furnace of diameter  $D = 5$  m and height  $H = 5$  m with a flat base and a roof. The curved side wall and the roof of the furnace may be approximated as blackbody surface, and are maintained at 600 K. The spectral hemispherical emissivity of the base, which is maintained at 1000 K is approximated as  $\epsilon_1 = 0.1$  (for  $\lambda < 0.8 \mu\text{m}$ ),  $\epsilon_2 = 0.9$  (for  $0.8 < \lambda < 2 \mu\text{m}$ ), and  $\epsilon_3 = 0.2$  (for  $2 \mu\text{m} < \lambda$ ). Determine the net rate of radiation heat transfer emanating from the base to the side wall during steady operation. Consider the blackbody radiation fraction table provided at the end of the question paper. 20

**Part IV (20 Marks)**

6. A cylindrical pin fin of length  $L$  is to be mounted between two identical hot plates A and B, maintained at  $100^\circ\text{C}$ , as shown in Fig 6A. The fin metal has a thermal conductivity of  $100 \text{ W/mK}$ , while the intervening fluid has a convective heat transfer coefficient of  $10 \text{ W/m}^2\text{K}$  and a temperature of  $10^\circ\text{C}$ . What would be the highest practical length of the fin, and the total heat loss through the fin? 20

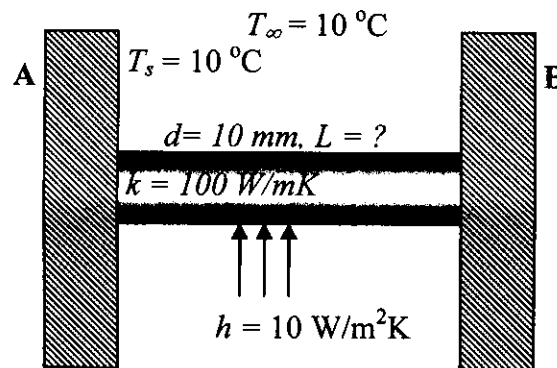


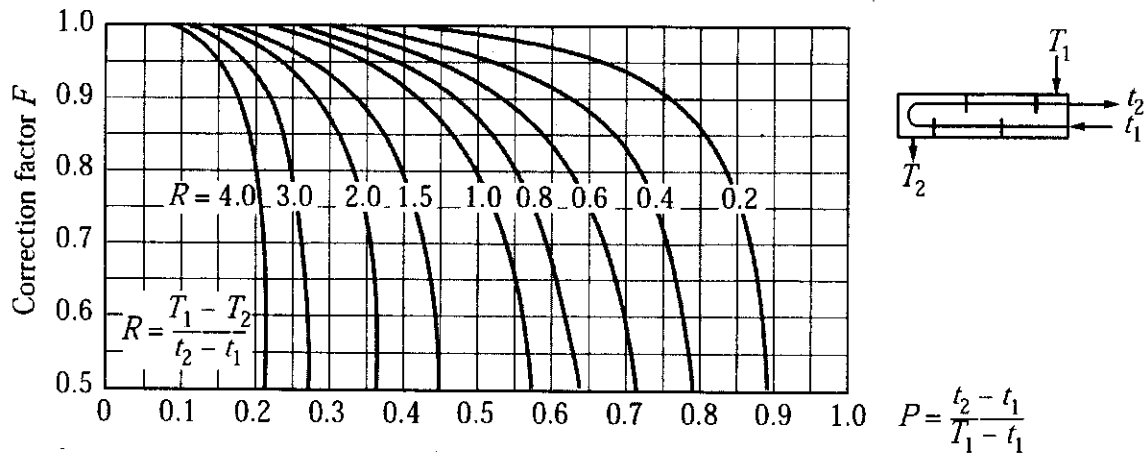
Fig 6A

OR

A shell-and-tube heat exchanger with 1-shell pass and 20-tube passes is used to heat glycerin ( $C_p = 2480 \text{ J/kgK}$ ) in the shell, with hot water in the tubes. The tubes are thin walled and have a diameter of  $1.5 \text{ cm}$  and length of  $2 \text{ m}$  per pass. The water enters the tubes at  $100^\circ\text{C}$  at a rate of  $5 \text{ kg/s}$  and leaves at  $55^\circ\text{C}$ . The glycerin enters the shell at  $15^\circ\text{C}$  and leaves at  $55^\circ\text{C}$ . Determine the mass flow rate of the glycerin and the overall heat transfer coefficient of the heat exchanger. Use the following Bowman chart provided at the end of the question paper. 20

Time: Three Hours

(Full Marks 100)

**Blackbody radiation functions  $f_\lambda$** 

| $\lambda T$ ,<br>$\mu\text{m} \cdot \text{K}$ | $f_\lambda$ |
|---|-------------|
| 200   | 0.000000    |
| 400   | 0.000000    |
| 600   | 0.000000    |
| 800   | 0.000016    |
| 1000  | 0.000321    |
| 1200  | 0.002134    |
| 1400  | 0.007790    |
| 1600  | 0.019718    |
| 1800  | 0.039341    |
| 2000  | 0.066728    |
| 2200  | 0.100888    |
| 2400  | 0.140256    |
| 2600  | 0.183120    |

