

# Take Home Assignment 1

## 1. Algo implementation of :

Display all paths in a directed acyclic graph and count the number of them.

- Initialize an empty list to store paths
- For  $v \in V$  {unexplored set of vertices} :
  - Add the path traversed till now to list
  - Recursively, move to the child of  $v$ ,  
 $v = \text{child}(v)$ , add child to path and path to list

Note : Since, it's an acyclic graph, the recursive function should terminate

**Time Complexity :  $O(V \cdot E)$**  , where  $E$  = no. of edges and  $V$  = no. of vertices

**Efficient Approach** : Memoization of paths starting from already visited nodes in a map has been implemented too. **Time complexity :  $O(V + E)$** .

- Initialize another empty list to store all the paths related to a single current node
- Add the list to a map and mark the node visited.
- Repeat the step 2 of the above algo but this time if ( $\text{child}(v)$  is visited) then  
Add all paths corresponding to the  $\text{child}(v)$  stored in map to  $v$
- Add all in the global list.

## 2. Algo implementation of :

Topological Sort -

- Insert all vertices with indegree 0 in a Queue
- While Queue is not empty
  - $U = \text{Queue.Poll}()$
  - Print( $U$ )
  - For  $v \in \text{child}(U)$
  - If indegree of  $v$  reducing by 1 is 0
  - Add  $v$  to Queue

**Time Complexity** : same as BFS -  **$O(E + V)$** , where  $E$  = no. of edges and  $V$  = no. of vertices