

* Course Wide *

Week 1 - Notes

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* Course Wide *

Binary $10 = 2$ decimal (Number)

* Relay/Binary USED ON / current = 1
transistor OFF / No current = 0

* Petaflop = 10^{15} (10 to the power 15) Floating Point Operations Per Second

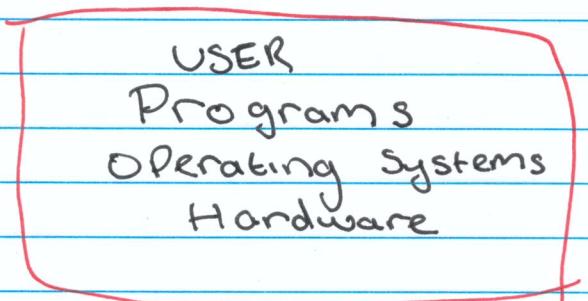
* ARM = Advanced RISC Machine - Side Note

↳ Reduced Instruction Set Computer

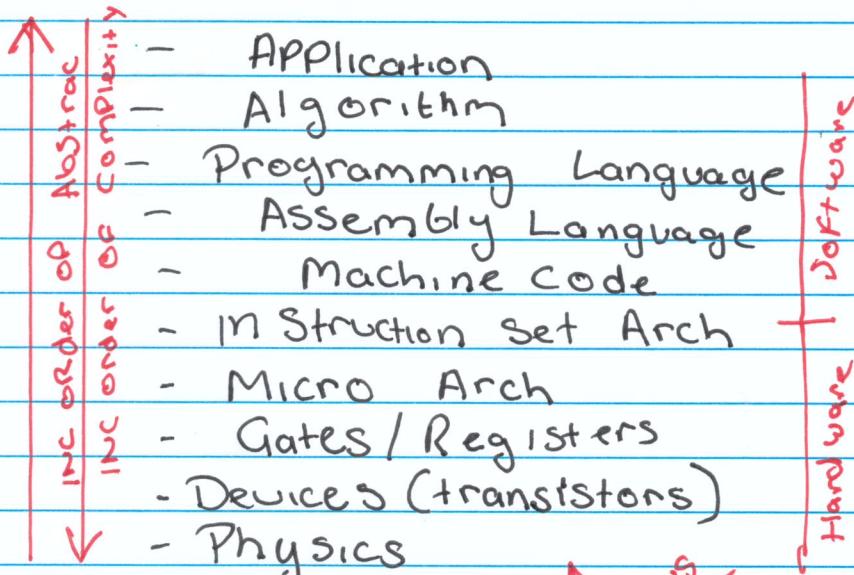
* CISC = Complex Instruction Set Computer

* Moore's Law = the number of transistors increase exponentially in every generation
Soon → * No Longer Really Applicable

* Computer Systems - Abstraction



Computer
Layered as a sys



↑
OUR focus

Week 1 - Cont (course wide) →

* 1's and 0's = Bits

→ at the lowest levels of digital computing hardware everything is either 0 or 1

$01001010 = J \rightarrow \text{ASCII (7 bit code) often Extended to 8}$

→ Humans don't like binary so we use
Octal, decimal & Hexadecimal
 ↓ ↓ ↓
 Base 8 Base 10 Base 16

→ Binary = Base 2 number system ←

Consider base 5 number: 410_5

$$410_5 = 4 \times 5^2 + 1 \times 5^1 + 0 \times 5^0$$

→ In Base 5, each place indicates a power of 5

→ 410_5 in Base 5 = 105 in base 10

Consider binary: 1101001:

$$\begin{array}{ccccccccc}
 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \\
 = 1 \times 2^6 & + 1 \times 2^5 & + 0 \times 2^4 & + 1 \times 2^3 & + 0 \times 2^2 & + 0 \times 2^1 & + 1 \times 2^0 \\
 \downarrow & & & \uparrow & & & \uparrow \\
 1 \times (2 \times 2 \times 2 \times 2 \times 2 \times 2) & & & 0_1 = 0 & & & = 1?
 \end{array}$$

$$= 64 + 32 + 0 + 8 + 0 + 0 + 1$$

$$= 105_{10} \leftarrow \text{As Decimal } \Downarrow$$

Binary to decimal

Week 1 - Course Wide - Cont 3 →

MSB = Most-Left = Most-Significant Bit 1001

LSB = Least-Right = Least " " Bit 1001

Convert Decimal to Binary

* Consider: 178_{10}

* Divide 178 By 2 until Result = 0

Results with decimal Place (IE) $1.1 = 1$

Whole number Results = 0 (work Backwards)

Quotient	Remainder	
$178/2$	89	0 + (LSB)
$89/2$	$44(44.4)$	1
$44/2$	22	0
$22/2$	11	0
$11/2$	$5(5.5)$	1
$5/2$	$2(2.5)$	1
$2/2$	1	0
$1/2$	$0(0.5)$ STOP	1

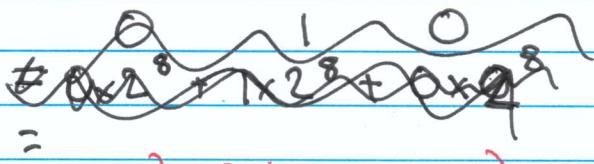
↑ Read ↓ ^{1 0 1 1 0 0 1 0} ₂ (MSB)

$$178_{10} = 10110010_2$$

* Binary to Octal Equivalent *

$$10110010_2 = 010/110/010_2$$

Split into groups of 3 starting at LSB
add 0's to MSB to gain group of 3



$$= \begin{array}{l} 1) 010 \\ 2) 110 \\ 3) 010 \end{array}$$

4 →

* Binary to Octal - CONT

1) 010

$$= 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 2$$

2) 110

$$= 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 6$$

3) 010

$$\begin{aligned} &= 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\ &\downarrow \quad \downarrow \quad \downarrow \\ &0 \times (2 \times 2) + 1 \times (2) + 0 \times (0) \\ &\quad 0 \quad 2 \quad 0 = 2 \end{aligned}$$

$$10110010_2 = 262_8$$

Binary Numbers

- With 4 bits we can represent:

- $0000_2 = 0_{10}$
- $0001_2 = 1_{10}$
- $0010_2 = 2_{10}$
- $0011_2 = 3_{10}$
- $0100_2 = 4_{10}$
- $0101_2 = 5_{10}$
- $0110_2 = 6_{10}$
- $0111_2 = 7_{10}$
- $1000_2 = 8_{10}$
- $1001_2 = 9_{10}$
- $1010_2 = 10_{10}$ A
- $1011_2 = 11_{10}$ B
- $1100_2 = 12_{10}$ C
- $1101_2 = 13_{10}$ D
- $1110_2 = 14_{10}$ E
- $1111_2 = 15_{10}$ F

Hexadecimal

5 ↴

6→

* Binary to Hexadecimal

1011 0010₂

* Divide it into groups of 4 called a nibble
Starting from Right (LSB). add extra zero's
in front of MSB as required

$$1011 \quad 0010_2 = B2_{16}$$

* Binary Addition

1) 0101 0101₂ + 0001 0010₂

CARRY |
+ 0101 0101 → = 2 so Carry 1, Mark AS 0
+ 0001 0010
Result 0110 0111 Valid to 8 Bits
~~overflow~~

2) 1111 0101₂ + 1001 0110₂

+ 1111 0101
+ 1001 0110
= 1000 1011

Carry Condition
INVALID to 8 Bits

+1 +1 +1 +1 +1
| | | | 0101
+ | 001 0110
= | 000 1011

Binary Addition

1

Carry Condition

- Computers can only allocate a finite number of bits to represent a number
- Assume only 8 bits are used for each integer

+1	+1	+1	+1	+1	+1	+1	+1
1	1	1	1	1	1	1	1
+	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0

This bit is lost, this error is known as a carry condition

Note that $1111\ 1111_2 = 255_{10}$

q →

- * Positive Binary is UNSIGNED
- * Negative Binary is SIGNED

- * There are other binary coding systems for signed integers such as

→ Two's Complement
→ One's Complement

- * There are other binary coding systems for representing floating point numbers

→ 1's Complement (only flipping bits)

$$+5_{10} = 0101_2$$

$$-5_{10} = \begin{matrix} \$ \\ 1010_2 \end{matrix}$$

$$+2_{10} = 0010_2$$

$$-2_{10} = \begin{matrix} \$ \\ 1101_2 \end{matrix}$$

* Problem with 1's complement is it has 2x zero's (0000_2 & 1111_2) so we always need to check for both which is inefficient

→ 2's complement

* To get 2's complement use 1's complement then add +1

* 4 Bits arithmetic

$$0101_2 (5_{10}) \Rightarrow \begin{matrix} 1's \text{ complement} \\ \oplus 1 \end{matrix} \begin{matrix} +1 \text{ (using binary add)} \\ 1010_2 \end{matrix} \Rightarrow 1011_2$$

$$1011_2$$

Tell us it's a negative in 2's complement

* Overflow in 2's complement is ignored

Negative Integers- 2's Complement

- 1011 (-5_{10})
- $0100 \Rightarrow 1\text{'s complement}$
+1 add 1
- 0101 We get back the original number= $\Rightarrow +5_{10}$
- Now consider $0 = 0000 \Rightarrow 2\text{'s complement}$

+1	+1	+1	+1	.	.	.
	1	1	1	1	1	1's complement
				+	1	Add 1
0	0	0	0		0	

In 2's complement you ignore the carry bit if you are using 4 bit arithmetic

- So there is only one representation of 0 in 2's complement

Characters- ASCII Table

- ASCII is a 7 bit code
 - Note: 1 is not 1 !!
(often extended to 8 bits)
 - Some ASCII characters:
00110000 = '0'
01000001 = 'A'
01000010 = 'B'
01000011 = 'C'
01011010 = 'Z'
...
0001000001 = ' ! '
 - 00100000 = ' '
 - 00110001 = '1'
 - 00110010 = '2'
 - 00110011 = '3'
 - 00100100 = '\$'
 - 00100111 = ring bell !!