

Design and modular self-assembly of nanostructures

Joakim Bohlin

Balliol College
University of Oxford

*A thesis submitted for the degree of
Doctor of Philosophy*

Michaelmas 2021

Abstract

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Acknowledgements

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Abstract

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Contents

List of Figures	xi
List of Tables	xv
Glossary	xvii
1 Introduction	1
1.1 Scope of the thesis	1
1.2 Background	1
1.2.1 Deoxyribonucleic acid (DNA)	2
1.2.2 Ribonucleic acid (RNA)	2
1.2.3 DNA origami	2
1.2.4 RNA origami	3
2 An introduction to high-level modular assembly	5
2.1 Experimental applications	6
2.1.1 DNA tiles and bricks	6
2.1.2 RNA tiles	6
2.1.3 DNA origami arrays	7
2.1.4 Shape-complementary origami	7
2.1.5 DNA origami nanochambers	8
2.1.6 Octahedral DNA origami frames	8
2.2 Tile assembly models	8
2.2.1 Wang tiles	8
2.2.2 The algorithmic tile assembly model	9
2.2.3 The polyomino model	10
2.3 Algorithmic Information Theory and input-output maps	12
2.4 Patchy particle simulation	14
3 Modular self-assembly of polycubes	15
3.1 The polycube model	15
3.2 Sampling the space of assembly rules	18
3.3 Complexity bias	19
3.4 Robustness	20

4 Designing polycube assembly rules	21
4.1 Satisfiability solving	21
4.2 Finding the minimal assembly rule	22
4.3 Example solves	24
5 An introduction to tools for the design and simulation of nucleic acid structures	25
5.1 Design tools	26
5.1.1 Lattice-based design tools	26
5.1.2 Top-down shape converters	26
5.1.3 Free-form or hybrid tools	27
5.2 Simulation tools	29
5.2.1 All-atom simulation	29
5.2.2 oxDNA/RNA	30
5.2.3 mrDNA	30
5.2.4 Cando	31
6 Structure design and analysis in oxView	35
6.1 Importing designs	36
6.1.1 Basic import	37
6.1.2 Multi-component designs	38
6.1.3 Far-from-physical caDNAno designs	38
6.2 Rigid-body manipulation and dynamics	39
6.3 Editing designs	39
6.4 Example conversions	39
6.5 Visualization options	43
6.6 Exporting designs	43
6.6.1 Exporting oxDNA simulation files	43
6.6.2 Exporting other 3D formats	44
6.6.3 Exporting sequence files	44
6.6.4 Saving image files	44
6.6.5 Creating videos	44
6.7 Converting RNA origami designs	44
7 Conclusion	47
7.1 Individual module design	47
7.2 Modular assembly	47
7.3 Future work	47

Appendices

A Possible appendix chapter	51
References	53

x

List of Figures

1.1	Conceptual DNA Robotics design. The nanorobots are assembled from standardised cubic modules that functions as sensor, actuators, processors, or structural components. Image adapted from https://dna-robotics.eu/about/	2
1.2	Illustration of DNA origami self-assembly of a tetrahedron. A long scaffold strand (purple), obtained from a virus, is folded into the desired shape by multiple short staple strands binding to complementary domains of the scaffold. Tetrahedron design obtained from https://cando-dna-origami.org/examples/ and melted using oxDNA simulation [4].	3
2.1	DX tiles forming 2D lattices, adapted from [9]. a) Lattices made from two units and four units respectively. b) Examples of DAO and DAE tile designs.	6
2.2	3D bricks from [10]	7
2.3	2D RNA tiles from [7]	8
2.4	Adapted from [11]	9
2.5	Adapted from [12]	9
2.6	DNA nanochambers, adapted from [14]	10
2.7	Octahedral DNA origami frames, adapted from [15]	11
2.8	Wang tiles	11
2.9	Algorithmic self-assembly model	12
2.10	Illustration of the polyomino assembly model used by Johnston. A <i>genotype</i> , in the form of a ruleset of possible tiles, encodes for a polyomino <i>phenotype</i> , grown stochastically from an initial seed tile. Image adapted from [19].	13

3.1	Illustration of the polycube assembly model. Compare to the polyomino model in Figure 2.10. The top of the figure shows the genotype, in the form of a rule with two species one colour. The rule is visualised in three different ways. The first is a hexadecimal representations, with each two digits coding for a patch and a total of 12 digits describing a species. The second representation is of the two species shown as 3D cubes. The first species has colour=1 on all patches while the second has a single patch with colour=-1. Since the polycube is symmetric the patch rotations do not matter and are all kept at 0.	17
3.2	Polycube versions of the conceptual DNA Robotics designs. Compare to Figure 1.1. From left to right, the size of the rule required to specify each polyomino is: <u>4</u> , <u>2</u> , <u>5</u> and <u>11</u> . Note how the third polyomino (L-shaped) requires a larger rule than the first (double cross), although it is smaller in size. This is because each cube in the L-shaped nanobot needs to be unique, while the double-cross-shaped first nanobot consists of two identical parts. If we only wished to reproduce the polycube shape, the rulesets could be minimised further.	18
3.3	Heat map of rule size vs polycube size, for a simulation with a maximum of 8 species and a limit of 8 colours, evaluating 2.5 million random rules. Note that the frequency scale is logarithmic.	19
3.4	Example of polycubes grown from 1, 2 and 3 species. Although any polycube can be encoded into a rule, the larger polycubes that have small rules tend to be symmetrical. This agrees with Johnston’s polyomino model in that they have low complexity	19
4.1	Algorithm for finding the minimal solution using SAT. Even if a solution is found to be satisfiable it might not assemble correctly every time. Additional solutions for a given N_c and N_t are found by explicitly forbidding the current solution. Alternatively, it is possible to use a solver like relsat to obtain multiple solutions.	23
4.2	Examples of undefined assemblies. a) Unbounded assembly that tiles the plane using two species 05050a08000085858a880000, b) An undeterministic assembly of a “giraffe duck” with a neck that can have a new length each time it is assembled	23
5.1	The caDNAo design interface, adapted from figure 1.(a) in [24]	27
5.2	BSCOR	28
5.3	daedalus	29
5.4	Tiamat	29
5.5	vHelix	30

5.6	Adenita	31
5.7	All-atom simulation	32
5.8	The oxDNA model	33
5.9	MrDNA	33
5.10	Cando	34
6.1	Rigid-body dynamics of clusters. Snapshots from the automatic rigid-body relaxation of an icosahedron, starting with the configuration converted from caDNAno a), through the intermediate b) where the dynamics are applied, and c) the final resulting relaxed state.	40
6.2	Designing the DNA tetrahedron from [45] using the oxView editing tools. a) The initial helix created. b) Duplicated helices being translated into place. c) Strands ligated together. d) The resulting 3D tetrahedron shape, as seen after applying rigid-body dynamics.	40
6.3	Relaxation results for various DNA designs. Each row depicts a new design, with the left-hand side showing the structure as it was drawn in caDNAno (and parsed by mrdna), while the right-hand side is the relaxed structure in oxDNA. Intermediate images are edits done in mrdna. While the switch design[46] in a) and the small DNA origami box[47] in b) relaxed without any required editing, the tensegrity kite structure [48] in c) and the Möbius strip[49] in d) benefited greatly from moving selected helices to a position off the lattice before starting the simulation.	41
6.4	Screenshot of the online oxView tool, exporting a video of a slider on a rail from a simulated trajectory.	44
6.5	Conversion and simulation of various RNA designs. Each row, from left to right, shows the ASCII blueprint design, the PDB model (visualised using ChimeraX), and a frame from the simulated structure (visualised using oxView). a) Is a simple hairpin loop. b) is a two-helix bundle tile used in [7]. c) is two helices connected by a double crossover, analysing the flexibility of such a motif. d) is a possible design for a tensegrity triangle. e) is a siz-helix bundle.	46

List of Tables

4.1	SAT variables and descriptions	22
4.2	SAT clauses. (i) Each colour is compatible with <i>exactly one</i> colour. (ii) Each patch has <i>exactly one</i> colour. (iii) Each lattice position contains a single cube type with an assigned rotation. (iv) Adjacent patches in the lattice must have compatible colours. (v) Patches at a lattice position are coloured according to the (rotated) occupying cube type. (vi) All N_t cube types are required in the solution. (vii) All N_c patch colours are required in the solution. (iix) Each patch is assigned <i>exactly one</i> orientation. (ix) Adjacent patches in the target lattice must have the same orientation. (v) Patches at a lattice position are oriented according to the (rotated) occupying cube type.	22
6.1	Editing tools available in oxView	42

Glossary

- 2D, 3D** Two- or three-dimensional, referring in this thesis to spatial dimensions of a self-assembly structure.
- DNA** Deoxyribonucleic acid.
- RNA** Ribonucleic acid.
- PDB** The Protein Data Bank. Used in this thesis to refer to the file format used to save atomic structures.
- Species** Used in this thesis to denote a type of cube allowed by the polycube rule.
- Polycube** A structure consisting of multiple cubes connected by their sides.

Far out in the uncharted backwaters of the unfashionable end of the western spiral arm of the Galaxy lies a small unregarded yellow sun. Orbiting this at a distance of roughly ninety-two million miles is an utterly insignificant little blue green planet whose ape-descended life forms are so amazingly primitive that they still think digital watches are a pretty neat idea.

— D. Adams, The Hitchhiker’s Guide to the Galaxy

1

Introduction

Contents

1.1	Scope of the thesis	1
1.2	Background	1
1.2.1	Deoxyribonucleic acid (DNA)	2
1.2.2	Ribonucleic acid (RNA)	2
1.2.3	DNA origami	2
1.2.4	RNA origami	3

This chapter explains the background and motivation for my project and introduces the two sub-projects I have been working on for the last year.

1.1 Scope of the thesis

1.2 Background

I am pursuing my graduate studies in Condensed Matter Physics as an Early-Stage Researcher, part of a Marie Skłodowska-Curie Innovative Training Network called *DNA-Robotics*¹. The network consists of the leading European DNA nanotechnology research groups and was formed with the goal of creating a unified framework for integrated biomolecular robotics[1].

¹<https://dna-robotics.eu/>, grant agreement number 765703

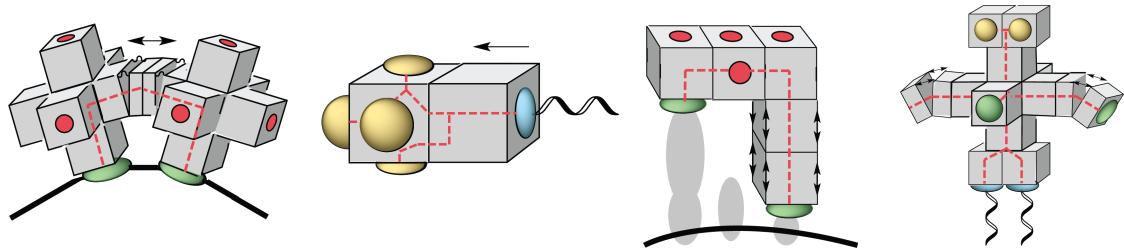


Figure 1.1: Conceptual DNA Robotics design. The nanorobots are assembled from standardised cubic modules that functions as sensor, actuators, processors, or structural components. Image adapted from <https://dna-robotics.eu/about/>

My position, in particular, is assigned to develop standardised techniques for the design and self-assembly of the nanorobotic modules[2]. The original design proposed for the robotic modules was to use cubic DNA origami modules, as shown in Figure 1.1, but the the goals have since broadened to include additional module types. Other Early-Stage Researchers within the network are tasked with developing such modules with either sensing, actuating or signal processing capabilities. The motivation for developing standardised modules is that they, when proven to work, can be reused in new designs, saving development time and resources.

As such, my contribution to the network and the field will be a step further in the ongoing effort to find methods for organising matter on the nanoscale.

1.2.1 Deoxyribonucleic acid (DNA)

Deoxyribonucleic acid (DNA)

1.2.2 Ribonucleic acid (RNA)

Ribonucleic acid (RNA) is a molecule

1.2.3 DNA origami

DNA origami[3] is a popular and proven method for creating larger irregular structures using DNA. The principle behind it, as illustrated in Figure 1.2, is to use short staple strands to fold one long viral scaffold strand into the desired structure.

Using design tools such as caDNAno[5], it has become relatively easy to design structures of any given form. However, the size of the origami is limited by the

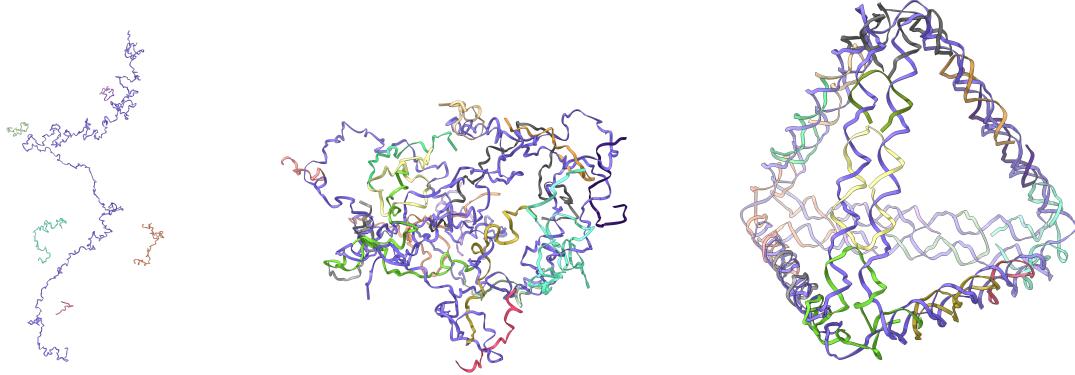


Figure 1.2: Illustration of DNA origami self-assembly of a tetrahedron. A long scaffold strand (purple), obtained from a virus, is folded into the desired shape by multiple short staple strands binding to complementary domains of the scaffold. Tetrahedron design obtained from <https://cando-dna-origami.org/examples/> and melted using oxDNA simulation [4].

length of the scaffold, which one of the motivations for researchers to investigate modular approaches, as described in Section 2.1.

1.2.4 RNA origami

Another possible building material investigated by the DNA robotics network is RNA. While DNA folding is easier to predict, the fact that RNA is more reactive also offers the possibility of a more useful structure; for example by incorporating aptamers, enzymes and other such functionalities[6]. Geary, et al., from the Andersen lab in Aarhus, demonstrated a method[7, 8] for co-transcriptionally folded RNA origami in 2014, which also enables folding *in vivo*. Using RNA origami, they were able to develop RNA tile modules, connecting through kissing-loop interactions. The Andersen lab is one of the network partners and I have spent a two-months secondment there working with their RNA origami method.

In order achieve my goal of improving the design of modular robotic structures, simulation tools are needed to analyse the assembly of both the complete structures and of each module. During the past year, I have been working with two related sub-projects to solve both those needs, each described in the following two sections.

Simplicity is prerequisite for reliability.

— Edsger W. Dijkstra

2

An introduction to high-level modular assembly

Contents

2.1	Experimental applications	6
2.1.1	DNA tiles and bricks	6
2.1.2	RNA tiles	6
2.1.3	DNA origami arrays	7
2.1.4	Shape-complementary origami	7
2.1.5	DNA origami nanochambers	8
2.1.6	Octahedral DNA origami frames	8
2.2	Tile assembly models	8
2.2.1	Wang tiles	8
2.2.2	The algorithmic tile assembly model	9
2.2.3	The polyomino model	10
2.3	Algorithmic Information Theory and input-output maps	12
2.4	Patchy particle simulation	14

Already from the start, the field of structural DNA nanotechnology has been interested in modular assemblies, although then mostly in the form of infinite chrystral structures. Allegedly, Ned Seeman was inspired to pioneer the field after seeing the artwork *Depth* by M.C. Escher.

This chapter will provide an overview on the background of self-assembled multi-component structures, starting with experimental results of ever-increasing

size and followed by a selection of theoretical models.

2.1 Experimental applications

From small tiles made from a handful of strands to megadalton-scale structures made from multiple origamis, modular assembly has seen a lot of experimental research. This section will detail some results of particular interest to the polycube model presented in Chapter 3.

2.1.1 DNA tiles and bricks

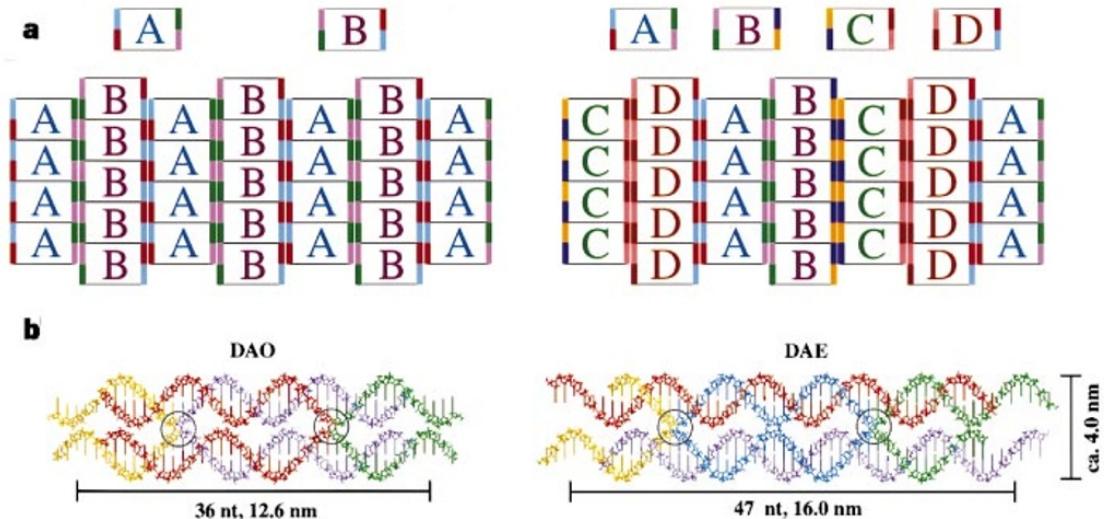


Figure 2.1: DX tiles forming 2D lattices, adapted from [9]. a) Lattices made from two units and four units respectively. b) Examples of DAO and DAE tile designs.

2.1.2 RNA tiles

In 2014, Cody Geary published a method of folding RNA tiles co-transcriptionally [7]. The design used a set of tertiary RNA motifs, such as kissing hairpins and double crossovers, to fold the RNA strand into the desired tile structure. The tiles then assembled connected by complementary 120-degree kissing loop interactions. The design method was later described in depth in the *Methods in Molecular Biology* book series [8].

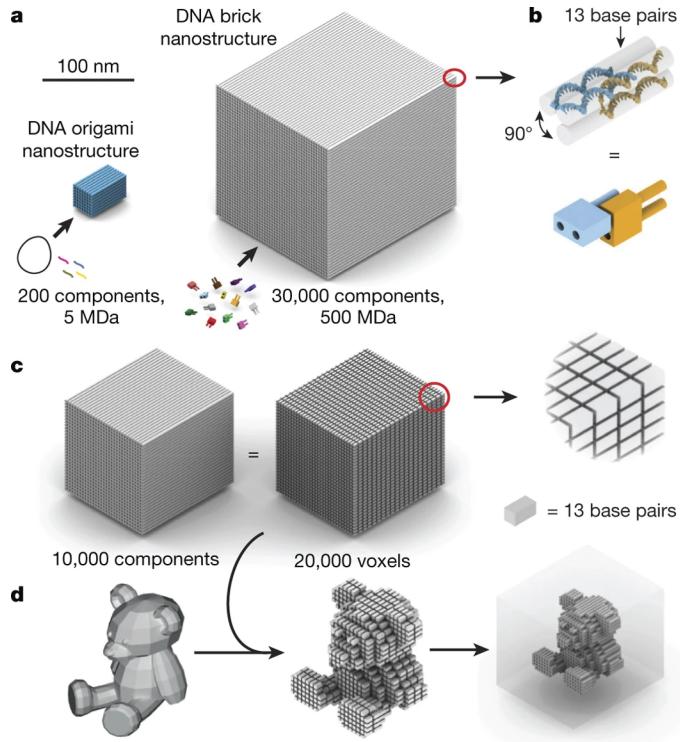


Figure 2.2: 3D bricks from [10]

2.1.3 DNA origami arrays

In 2017, Tikhomirov, et al.[11] demonstrated two-dimensional patterns assembled on the micrometre-scale using square origami tiles connecting through their complementary edges. helices

2.1.4 Shape-complementary origami

Also in 2017, Wagenbauer, et al. [12] used shape-complementarity to assemble origami tiles into three-dimensional polyhedral shapes up to 450 nanometers in diameter.

[13]

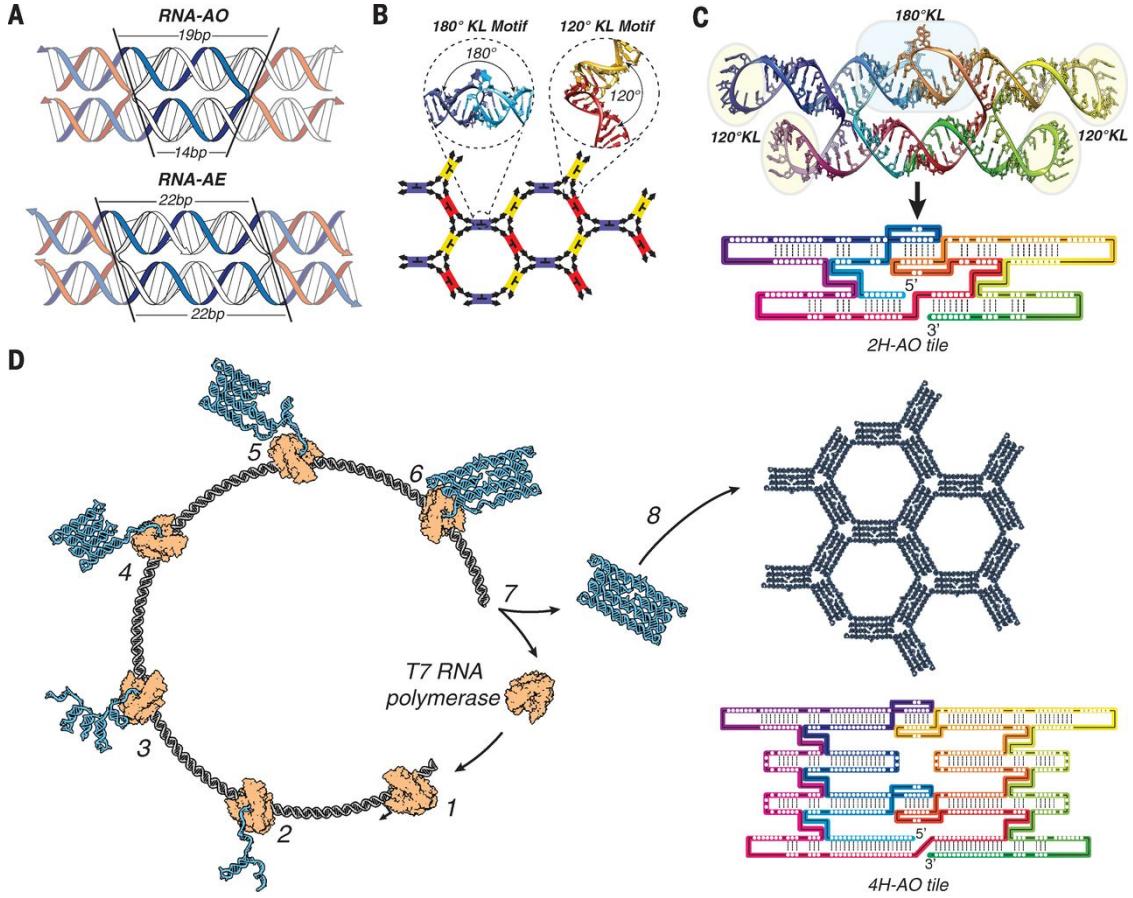


Figure 2.3: 2D RNA tiles from [7]

2.1.5 DNA origami nanochambers

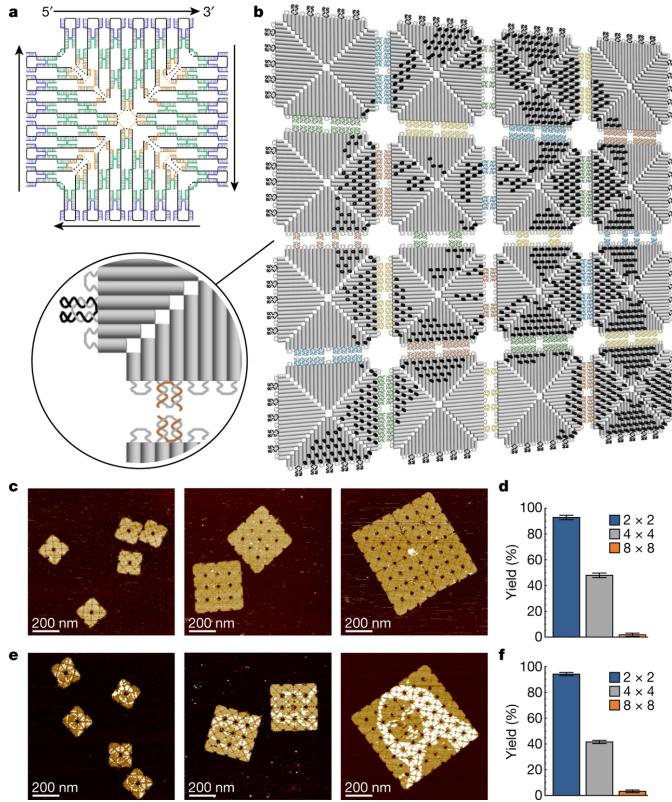
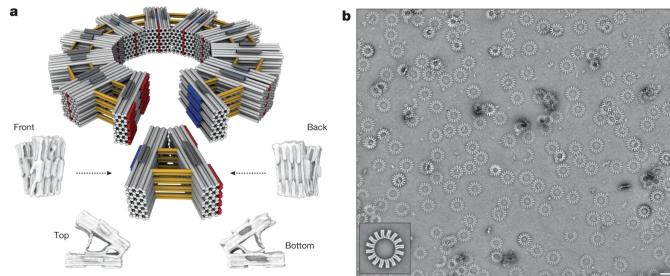
2.1.6 Octahedral DNA origami frames

2.2 Tile assembly models

It would be computationally unreasonable to simulate module assembly at the level of individual nucleotides. A better approach is instead to use an abstract model to predict the assembly process with the modules treated as rigid bodies. This section will present earlier such models as a background to my own model described in Chapter 3.

2.2.1 Wang tiles

Introduced by Hao Wang in 1961 [16], so called *Wang tiles* are

**Figure 2.4:** Adapted from [11]**Figure 2.5:** Adapted from [12]

2.2.2 The algorithmic tile assembly model

In his 1998 thesis Erik Winfree showed the usage of the double-crossover (DX) motif to create regular arrays [9]. These tiles behave like Wang tiles[16] and do not allow rotations or reflections. Winfree also investigated the possibility of using such tiles for computation [17].

Co-operative binding

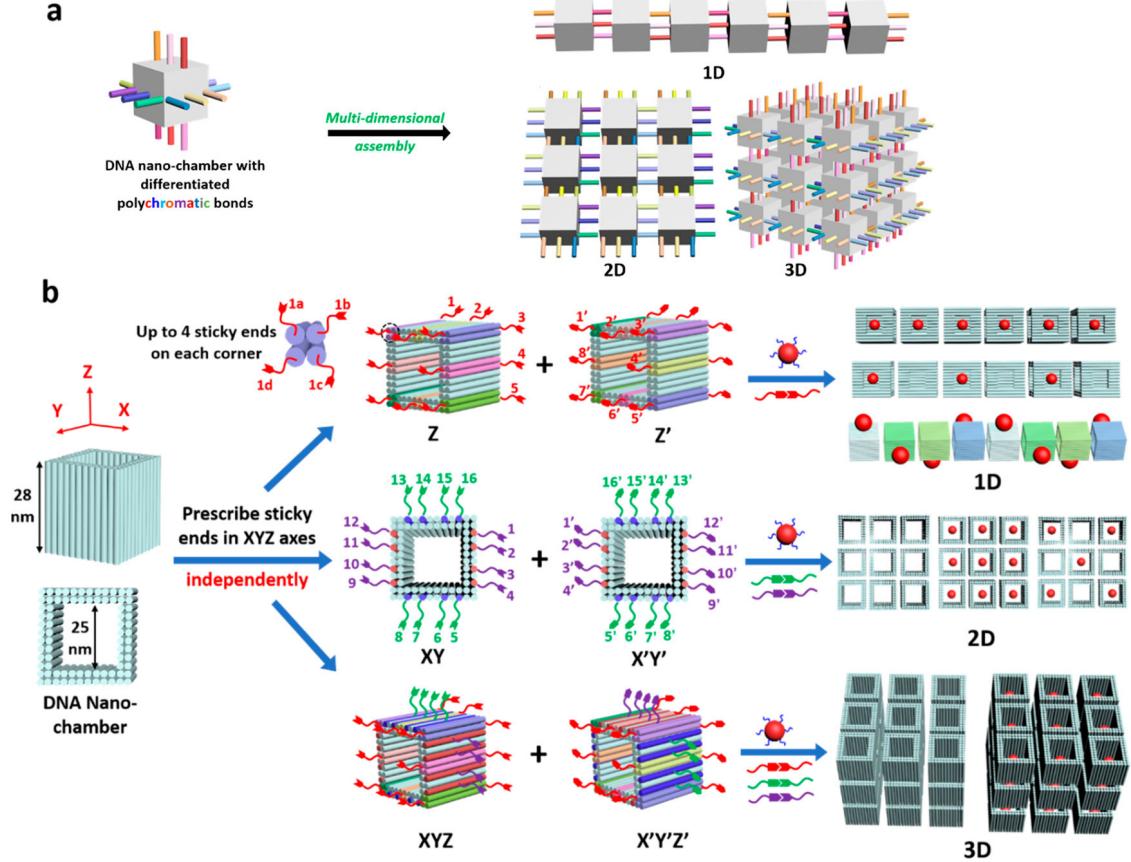


Figure 2.6: DNA nanochambers, adapted from [14]

2.2.3 The polyomino model

The main inspiration for the polycube model presented in Chapter 3 is the polyomino model [18][19]. The main difference to aTAM is that polyomino tiles are allowed to rotate. They also have a constant binding strength (in other words, it is a temperature-1 model).

Polyominoes are abstract structures composed of one or more squares, connected by their edges. The polyomino assembly model developed is similar in assembly to the later experimental micro-meter scale tile designs by Tikhomirov [11] described in Section 2.1.3. Compared to Wang tiles[16], the edge binding does not need to be between edges of the same colour, but can be specified by a more complex interaction matrix. Furthermore, the tiles can be rotated to bind, creating further possibilities for symmetries.

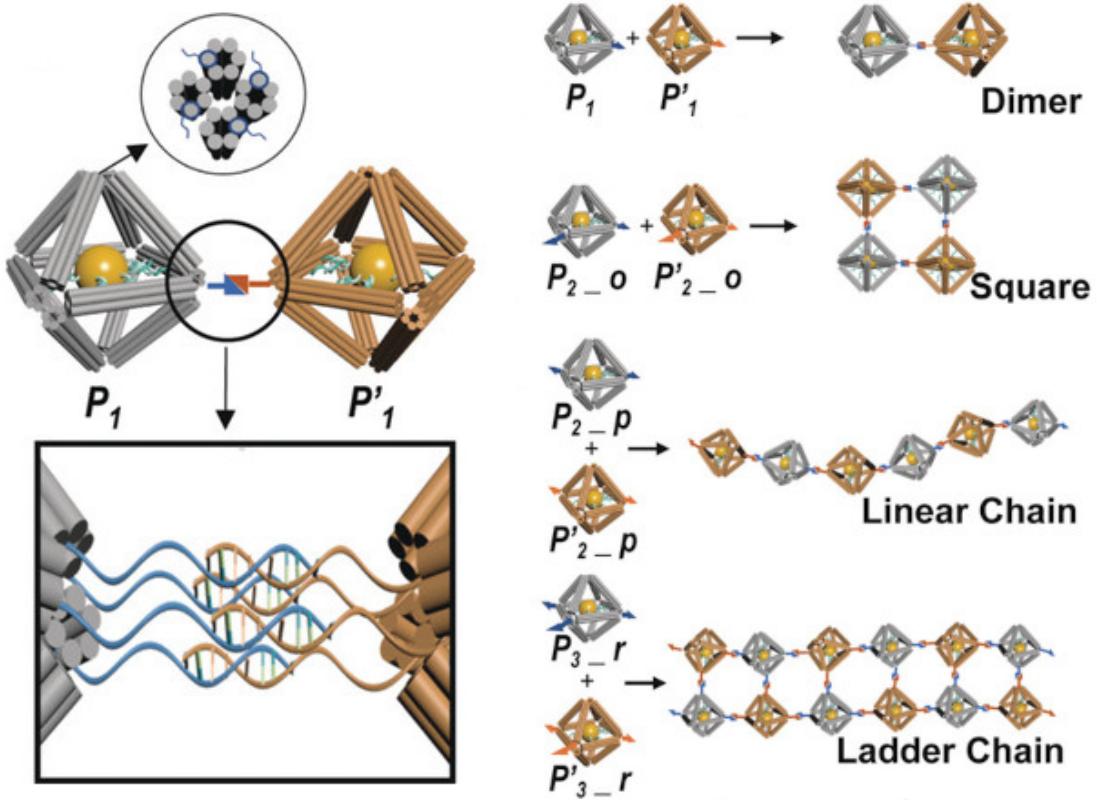


Figure 2.7: Octahedral DNA origami frames, adapted from [15]

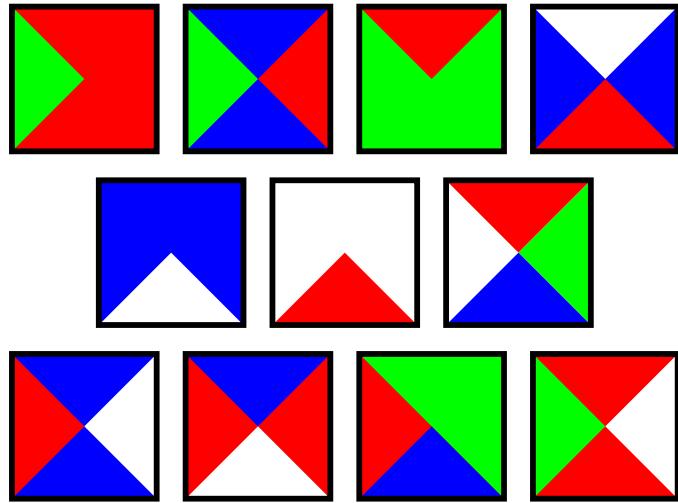


Figure 2.8: Wang tiles

I aim to build on Johnston's work on polyominoes to explore the properties of such self-assembling systems in three dimensions; the self-assembly of *polycubes*. With such a model in place, it should be possible to design, through shape complementary in DNA origami [12], kissing interactions in RNA origami [7], or other methods,

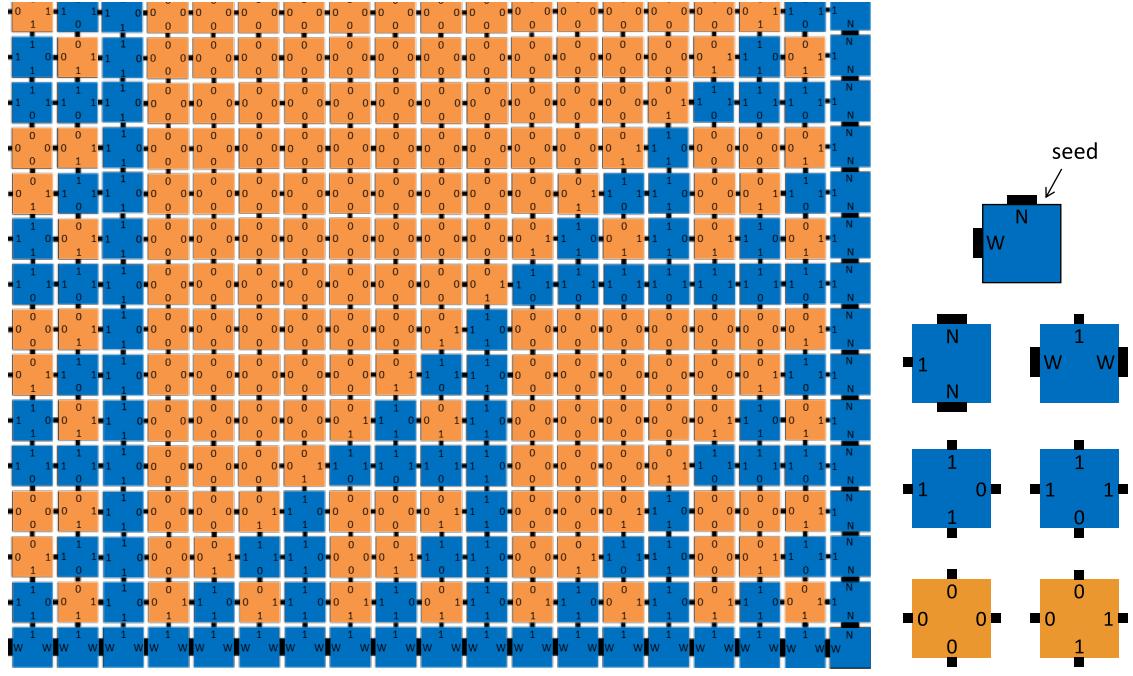


Figure 2.9: Algorithmic self-assembly model

robotic modules with the interfaces necessary to assemble into the desired polycube shape. My current progress within this project is covered in Chapter 3.

2.3 Algorithmic Information Theory and input-output maps

If you have a monkey pressing random keys on a typewriter, you would expect it to produce every string of length N with equal probability (assuming the keystrokes were indeed truly random). With k keys on the keyboard, the probability for any string of length N is then k^{-N} . For example, the title of this thesis, while unlikely to appear randomly, would be equally as probable as any other 50-character string, see the three example strings below:

1 DESIGN AND MODULAR SELF-ASSEMBLY OF NANOSTRUCTURES
 2 SHWDRVWKFORWJD0EXOZLSBNREKC Z VSDJJF ROKFYRVMUI
 3 AAAAAAAA.....AAAAA.....AAAAA.....AAAAA.....AAAAA

However, some strings can have a description shorter than a full listing of the letters it contains. For example, string number three above could be described simply as “Print A, 50 times”, or if we use the C programming language:

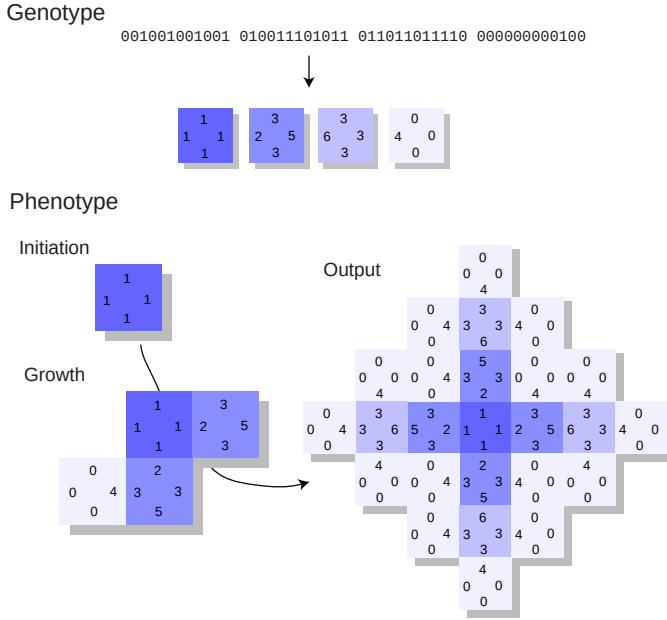


Figure 2.10: Illustration of the polyomino assembly model used by Johnston. A *genotype*, in the form of a ruleset of possible tiles, encodes for a polyomino *phenotype*, grown stochastically from an initial seed tile. Image adapted from [19].

```
for (int i=50; i--;) printf("A");
```

There are also a number of possible valid variations of the code above, with different variable names and coding conventions, all producing the same output. In other words, not only is the description shorter than writing out the full string, but there are also multiple inputs that map to the same output, increasing the probability further.

The concept of using the shortest possible computer program that can describe an object (for example, a binary string) to determine its complexity is central within the field of Algorithmic Information Theory (AIT) and is called Kolmogorov complexity (or Solomonoff–Kolmogorov–Chaitin to give full credit) [20]. More specifically, the Kolmogorov complexity $K(x)$ of an output x is the length of the shortest program that generates x on a Universal Turing Machine (UTM). However, finding the shortest program for an output is far from trivial (in general, it is in fact *uncomputable*, due to the *halting problem*).

AIT includes the *coding theorem*, introducing lower and upper bounds for the probability $P(x)$ of generating a binary string x as $2^{-K(x)} \leq P(x) \leq 2^{-K(x)+\mathcal{O}(1)}$. In other words, low-complexity outputs are exponentially more likely to be generated by random input. This could be compared to how, intuitively, there are likely more programs generating the “simple” string number 3 above compared to the seemingly random number 2.

This was later applied by Dingle at all

2.4 Patchy particle simulation

3

Modular self-assembly of polycubes

Contents

3.1	The polycube model	15
3.2	Sampling the space of assembly rules	18
3.3	Complexity bias	19
3.4	Robustness	20

As introduced in the previous chapter, there is an increasing interest within the field of DNA nanotechnology to create finite-sized multi-component objects. While some coarse-grained tile models exists, there still remains a need for methods to quickly explore the assembly of multi-component 3D structures. This chapter describes my polycube model and details how it can be used to sample a large amount of assembly rules, showing that some polycube shapes are significantly more common than others. The following chapter will show how to obtain the simplest assembly rule for any given polycube shape.

3.1 The polycube model

A polycube consists of a number of equally-sized cubes, connected by their neighbouring faces; a three-dimensional analogue to how polyominoes are squares connected by their neighbouring edges. In the model presented here, a polycube is stochastically

self-assembled according to a specified rule, where a rule is a set of available species. Each cube species describes a type of cube that can be present in the polycube; cubes belonging to the same species are always identical.

Each species has six patches; one on each face of the cube, and each patch has a "colour" and an orientation. The colour is indicated by a signed integer and the orientation is one of four possible rotations: (0), ($\frac{\pi}{2}$), (π) or ($\frac{3\pi}{2}$). A patch can bind to another patch if and only if they have the opposite colour and the same orientation. If the patch color is zero, the patch is considered empty and will not bind to anything. The model can also be expanded to more complicated colour interaction matrices or changed to pair odd integers with each subsequent integer as in the polyomino model[18][19] described in Section 2.2.3.

The stochastic self-assembly of a polycube starts by placing a cube from one of the available species as a seed at the origin. If the assembly mode is set to be seeded, it will always use first species in of rule. If the assembly mode is stochastic, the species of the seed is chosen at random.

Each possible neighbour to the placed cube, given the cube's patches, is then added to a list of possible moves. For the next step, a possible move is chosen at random and the rule is searched in a random order for a species fitting the move. Cubes can be rotated to fit and if a fitting species is found, the corresponding cube is added. If there is no fit, the move is discarded. Moves are processed until the list of moves is empty or the polycube grows beyond a specified size, at which point it is considered unbounded.

To determine if the rule is deterministic, the assembly is repeated n_{times} times (default 10) and the outputs compared for equality (allowing rotation).

ADD FIGURE ABOUT DETERMINISTIC AND UNBOUNDED ASSEMBLIES!!

It could be argued, instead of first picking a random move and then randomly trying all available species to find a fit, that one should pick both a move and a species at random until a fit is found. While this would take longer time, it would avoid biasing the assembly toward unlikely assembly results, where a move is

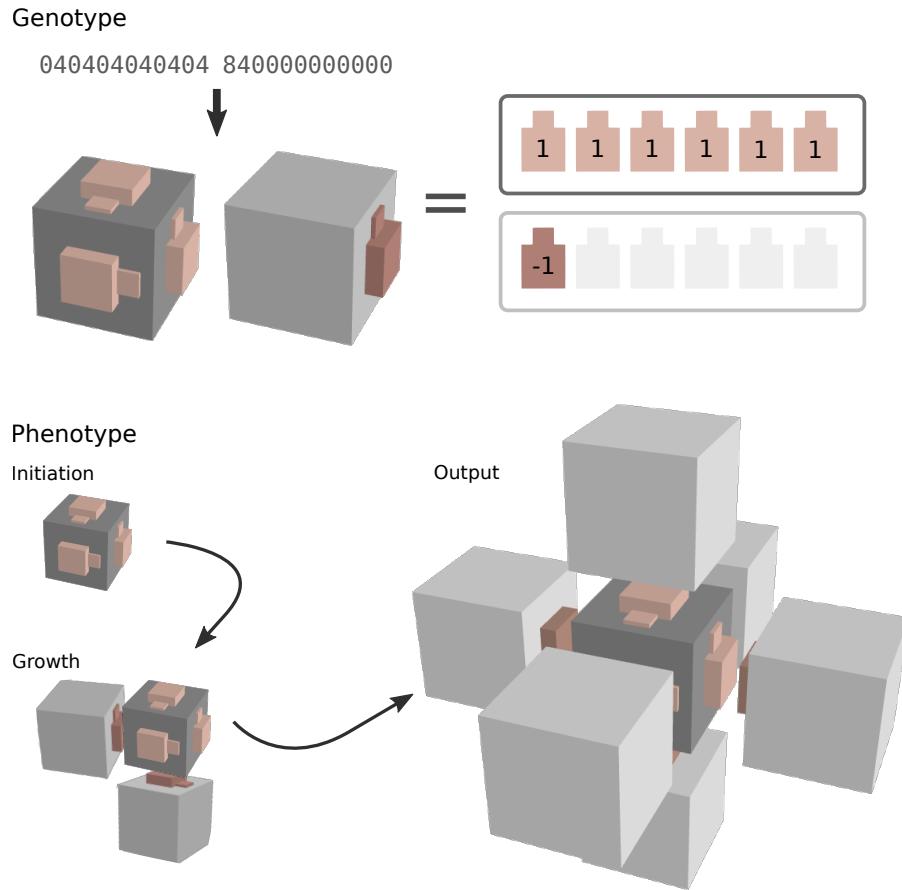


Figure 3.1: Illustration of the polycube assembly model. Compare to the polyomino model in Figure 2.10. The top of the figure shows the genotype, in the form of a rule with two species one colour. The rule is visualised in three different ways. The first is a hexadecimal representation, with each two digits coding for a patch and a total of 12 digits describing a species. The second representation is of the two species shown as 3D cubes. The first species has colour=1 on all patches while the second has a single patch with colour=-1. Since the polycube is symmetric the patch rotations do not matter and are all kept at 0.

picked that would otherwise usually be blocked by more likely surrounding cubes. However, since only deterministic and bounded rules are of interest, this would only affect the end result in the cases where the bias is strong enough and n_{times} is low enough to falsely make the rule seem deterministic.

For an illustration of the model, see Figure 3.1. The example in the figure is a three-dimensional "cross" structure created from a rule of size 2. The initial seeding cube belongs to the first species, enabling six additional cubes, all belonging to the second species, to bind at each patch. They bounds are made since the patch colours 1 and -1 are opposites. After all six outer cubes have bound, there are no remaining

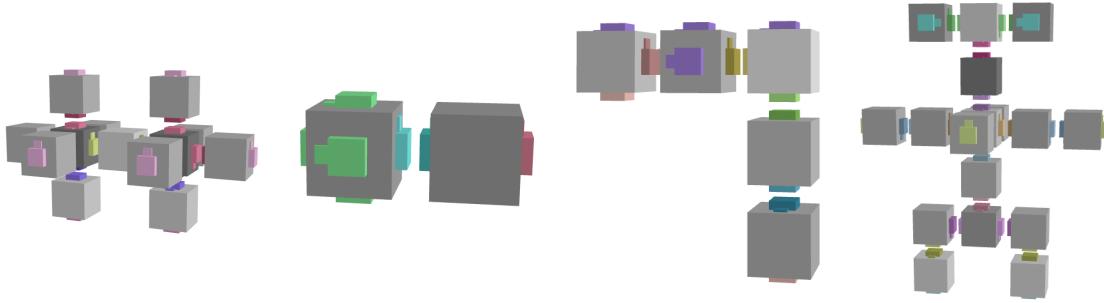


Figure 3.2: Polycube versions of the conceptual DNA Robotics designs. Compare to Figure 1.1. From left to right, the size of the rule required to specify each polyomino is: 4, 2, 5 and 11. Note how the third polyomino (L-shaped) requires a larger rule than the first (double cross), although it is smaller in size. This is because each cube in the L-shaped nanobot needs to be unique, while the double-cross-shaped first nanobot consists of two identical parts. If we only wished to reproduce the polycube shape, the rulesets could be minimised further.

possible moves and thus the polycube stops growing. Since the growth stops, this particular polycube is bounded, at a size of seven cubes. Furthermore, since the rule gives the same polycube every time it is evaluated, the polycube is deterministic.

The polycube assembly model has been implemented in two versions: one browser implementation for outreach activities and accessible visualisation, and one C++ implementation for fast rule evaluation. Using the C++ implementation, large sets of random rules have been evaluated and the resulting polycubes examined and categorised. This has also been repeated for different values of rule size and colour limits.

See figure 3.3 for a heat map of the frequency of rules of a certain size creating polycubes of a certain size. Notice how only three different polycube sizes were found for one species. This is understandable when inspecting the first column in Figure 3.4; using only one species, you cannot create a bounded structure of any other size.

For larger rule sizes, polycubes can have any form, as shown in Figure 3.2, but upon inspection of the larger polycube sizes (and small rule sizes) from Figure 3.3, the polycubes all seem to be highly symmetrical, as shown in 3.4.

3.2 Sampling the space of assembly rules

$$I_{n_c, n_t} = (4(1 + 2n_c))^{6n_t}$$

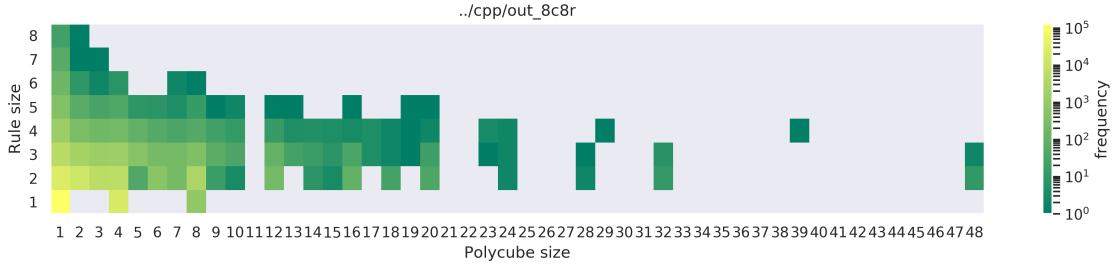


Figure 3.3: Heat map of rule size vs polycube size, for a simulation with a maximum of 8 species and a limit of 8 colours, evaluating 2.5 million random rules. Note that the frequency scale is logarithmic.

Figure 3.4: Example of polycubes grown from 1, 2 and 3 species. Although any polycube can be encoded into a rule, the larger polycubes that have small rules tend to be symmetrical. This agrees with Johnston’s polyomino model in that they have low complexity

Trying all inputs in a brute-force approach is impossible. Even if we limit both the amount of allowed colours n_c and the amount of species n_t to eight, the space of possible inputs, with four patch orientations and six patches per cube, is $I_{8,8} \approx 9 * 10^{87}$. But, while this is too large to sample fully, we can still get an idea of how likely it is for an input to map to a certain output by taking samples of the space of possible input rules.

This was done by uniformly sampling and assembling one billion random rules from $I_{8,8}$. Rules growing larger than 100 cubes were discarded as unbounded, while those remaining bounded were re-assembled 15 times to ensure they assembled deterministically. Deterministic and bounded output was then grouped by their shapes, counting the number of times each given phenotype occurs. For each rule found to produce a given phenotype, the number of colours is multiplied with the number of species in the rule, producing a measure of the rule size. The smallest such rule size is then used as a proxy for the phenotype complexity.

3.3 Complexity bias

As can be seen in Figure ??, there is a clear log-linear relationship between the probability of finding a rule that assembles into a particular structure, and the

information needed to specify the structure, as predicted in [21, 22].

3.4 Robustness

4

Designing polycube assembly rules

Contents

4.1	Satisfiability solving	21
4.2	Finding the minimal assembly rule	22
4.3	Example solves	24

Fully addressable is the easy solution

Could also sample the whole input space as in previous chapter

But is there a better way?

4.1 Satisfiability solving

Building upon a method for determining patchy particle interactions for unbounded structures [23] it is possible to also formulate and solve satisfiability problems for the bounded polycube structures.

Clauses (i)-(vii) are the same as in [23], while the remaining clauses have been added, together with variables x^D , x^A and x^O , to include torsional restrictions.

Interaction matrix is fixed (compared to [23]).

Figure of topology graph. Figure of particle schematic

Add giraffe-duck-like example of when SAT solver gives UND solution

Variable	Description
$x_{l,p,o}^A$	Patch p at position l has orientation o
x_{c_i,c_j}^B	Colour c_i is compatible with colour c_j
$x_{s,p,c}^C$	Patch p on cube type s has colour c
x_{p_1,o_1,p_2,o_2}^D	Patch p_1 , orientation o_1 binds to patch p_2 , orientation o_2
$x_{l,p,c}^F$	Patch p at position l has colour c
$x_{s,p,o}^O$	Patch p on cube type s has orientation o
$x_{l,s,r}^P$	Position l is occupied by cube type s rotated by r

Table 4.1: SAT variables and descriptions

Id	Clause	Boolean expression
(i)	C_{c_i,c_j,c_k}^B	$\neg x_{c_i,c_j}^B \vee \neg x_{c_j,c_k}^B$
(ii)	C_{s,p,c_k,c_l}^C	$\neg x_{s,p,c_k}^C \vee \neg x_{s,p,c_l}^C$
(iii)	C_{l,s_i,r_i,s_j,r_j}^P	$\neg x_{l,s_i,r_i}^P \vee \neg x_{l,s_j,r_j}^P$
(iv)	$C_{l_i,p_i,c_i,l_j,p_j,c_j}^{BF}$	$(x_{l_i,p_i,c_i}^F \wedge x_{l_j,p_j,c_j}^F) \Rightarrow x_{c_i,c_j}^B$
(v)	$C_{l,s,r,p,c}^{rotC}$	$x_{l,s,r}^P \Rightarrow (x_{l,p,c}^F \Leftrightarrow x_{s,\phi_r(p),c}^C)$
(vi)	C_s^{alls}	$\bigvee_{\forall l,r} x_{l,s,r}^P$
(vii)	C_c^{allc}	$\bigvee_{\forall s,p} x_{s,p,c}^C$
(iix)	C_{s,p,o_k,o_l}^O	$\neg x_{s,p,o_k}^O \vee \neg x_{s,p,o_l}^O$
(ix)	$C_{l_i,p_i,c_i,l_j,p_j,c_j}^{DA}$	$(x_{l_i,p_i,c_i}^A \wedge x_{l_j,p_j,c_j}^A) \Rightarrow x_{p_i,c_i,p_j,c_j}^D$
(x)	$C_{l,s,r,p,o}^{rotO}$	$x_{l,s,r}^P \Rightarrow (x_{l,p,o}^A \Leftrightarrow x_{s,\phi_r(p),o}^O)$

Table 4.2: SAT clauses. (i) Each colour is compatible with *exactly one* colour. (ii) Each patch has *exactly one* colour. (iii) Each lattice position contains a single cube type with an assigned rotation. (iv) Adjacent patches in the lattice must have compatible colours. (v) Patches at a lattice position are coloured according to the (rotated) occupying cube type. (vi) All N_t cube types are required in the solution. (vii) All N_c patch colours are required in the solution. (iix) Each patch is assigned *exactly one* orientation. (ix) Adjacent patches in the target lattice must have the same orientation. (v) Patches at a lattice position are oriented according to the (rotated) occupying cube type.

4.2 Finding the minimal assembly rule

The method presented here uses a SAT solver to determine if a provided polycube shape is satisfiable for a given number of cube types N_t and colours N_c . By iteratively ruling out lower values of N_t and N_c , a minimal solution can be found, as detailed in Figure 4.2. It is also possible to generate and compare alternative solutions of varying complexity.

ADD FIGURE ABOUT UNDETERMINISTIC AND UNBOUNDED ASSEMBLIES!!

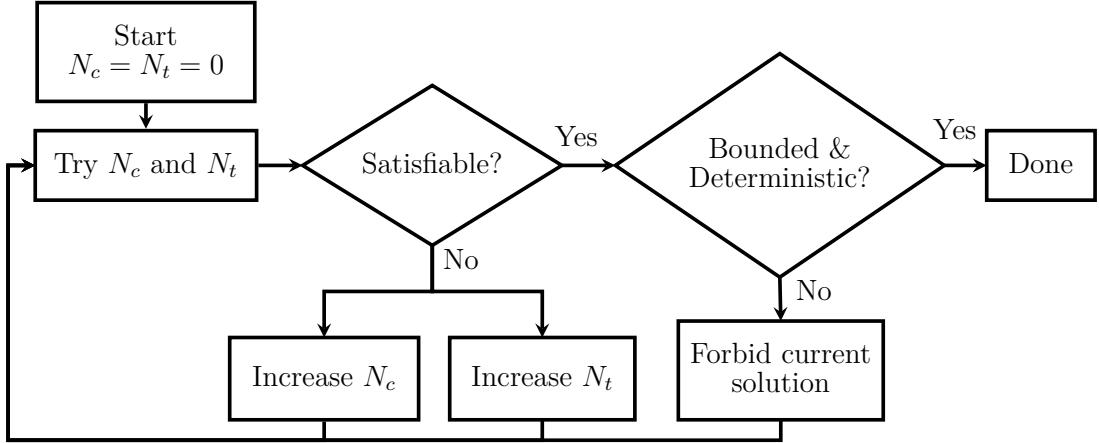


Figure 4.1: Algorithm for finding the minimal solution using SAT. Even if a solution is found to be satisfiable it might not assemble correctly every time. Additional solutions for a given N_c and N_t are found by explicitly forbidding the current solution. Alternatively, it is possible to use a solver like relsat to obtain multiple solutions.

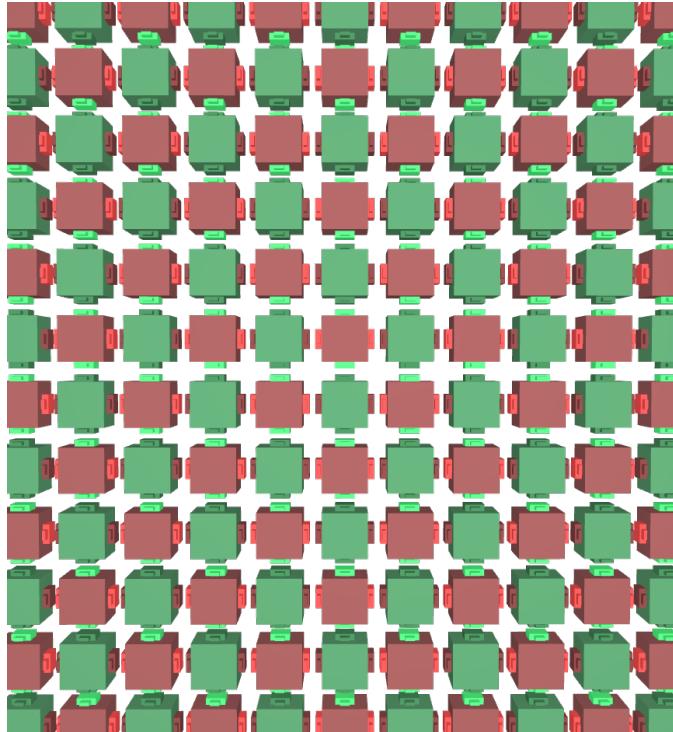


Figure 4.2: Examples of undefined assemblies. a) Unbounded assembly that tiles the plane using two species 05050a08000085858a880000, b) An undeterministic assembly of a “giraffe duck” with a neck that can have a new length each time it is assembled

4.3 Example solves

*A process cannot be understood by stopping it.
Understanding must move with the flow of the process,
must join it and flow with it. (First Law of Mentat)*

— Frank Herbert, Dune

5

An introduction to tools for the design and simulation of nucleic acid structures

Contents

5.1	Design tools	26
5.1.1	Lattice-based design tools	26
5.1.2	Top-down shape converters	26
5.1.3	Free-form or hybrid tools	27
5.2	Simulation tools	29
5.2.1	All-atom simulation	29
5.2.2	oxDNA/RNA	30
5.2.3	mrDNA	30
5.2.4	Cando	31

While previous chapters have covered modular self-assembly on a very abstract level, approximating the modules as simple cubes or patchy particles, this chapter will introduce tools and methods for designing and simulating individual structures or modules folded using DNA (or RNA).

The following sections will cover a selection of useful design and simulation tools that have been developed over the years, providing context for the presentation of my contributions to the *oxView* tool in Chapter 6.

5.1 Design tools

Designing a DNA origami structure by hand would be a very labourious task for anything but the most simple design. As such, a host of computer-aided design tools have been introduced over the years to make things easier. This section will cover some of the more popular examples.

5.1.1 Lattice-based design tools

The caDNAno design tool [24] and the web-based scadnano[25] it inspired, allows the user to design DNA origami on a lattice of parallel helices.

caDNAno

CaDNAno [24] was introduced in 2009 as a way to simplify 2D and 3D DNA origami designs. It has a graphical user interface, seen in Figure 5.1, where the designer can place virtual helices on an either hexagonal or square lattice in a slice panel (the leftmost panel in the figure). The helices can then be filled in with strands and connected using crossovers in a path panel, seen in the middle of the figure.

Finally, caDNAno is also available as a plugin to the Autodesk Maya software, which enables a 3D visualisation of the design as seen in the render panel to the right in Figure 5.1. However, caDNAno doesn't support Maya versions after 2015 [26].

Scadnano

Scadnano [25] (scriptable caDNAno) is a relatively new design tool, independent from but inspired by caDNAno version 2. The main difference is that Scadnano is completely web-based (not requiring any installation). The python code base is also designed to make it easier to write scripts generating DNA designs.

5.1.2 Top-down shape converters

While tools like caDNAno simplifies bottoms-up design, where the user builds structures from individual strands and nucleotides, a top-down tool can take a target polyhedral shape as input and provide a suitable origami design as output.

5. An introduction to tools for the design and simulation of nucleic acid structures

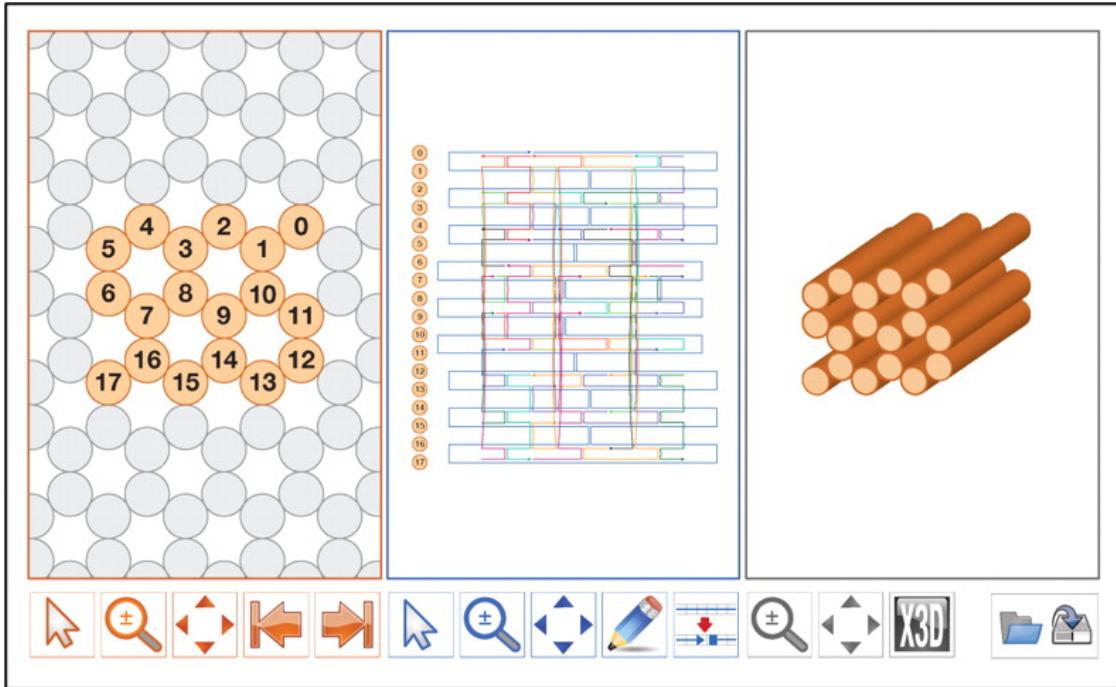


Figure 5.1: The caDNAno design interface, adapted from figure 1.(a) in [24]

BSCOR

DAEDAULS/PERDIX

ATHENA?

Triangulated truss structures

5.1.3 Free-form or hybrid tools

Tiamat

Tiamat is an early free-form design tool introduced in 2009

vHelix

Adenita

A final option for structure editing is Adenita [27]. So far, a version has only been released for beta testers and unfortunately, they do not yet support Linux. Still, after talking to Haichao Miao at the Nantech2019 conference, Adenita sounds like it could become a valuable off-lattice tool for designing and editing DNA nanostructures, with import options from caDNAno and export to oxDNA.

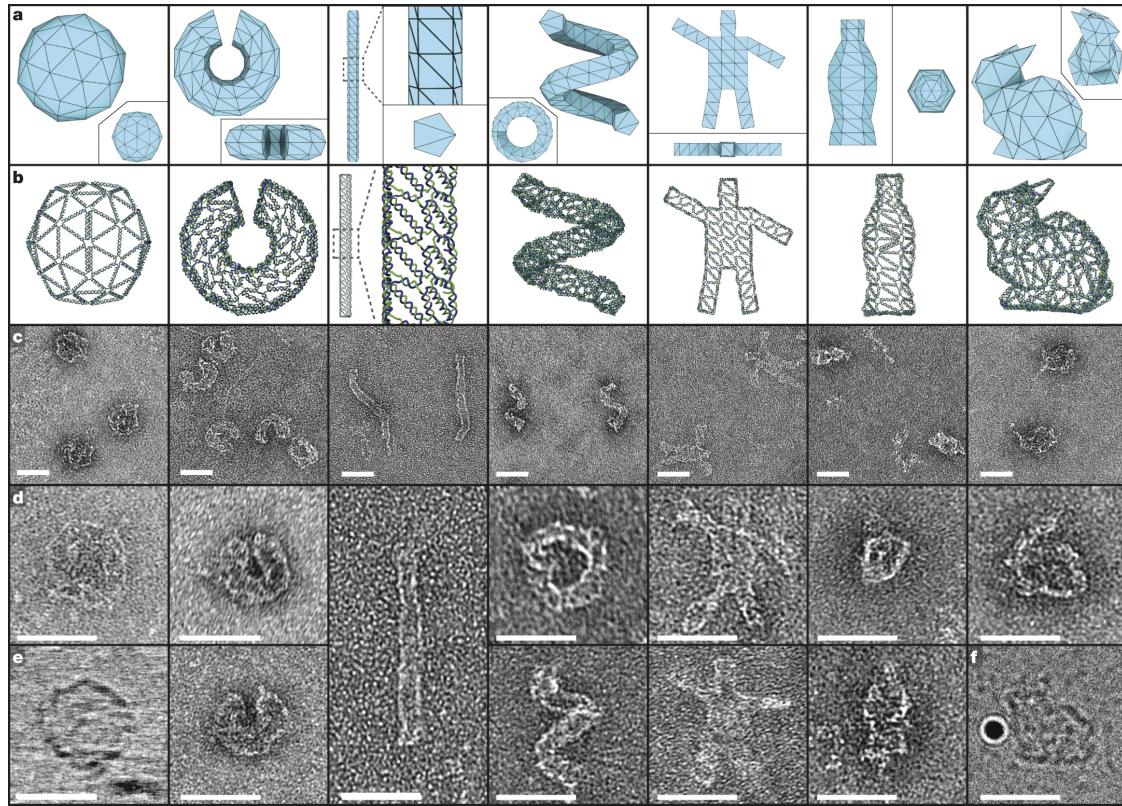


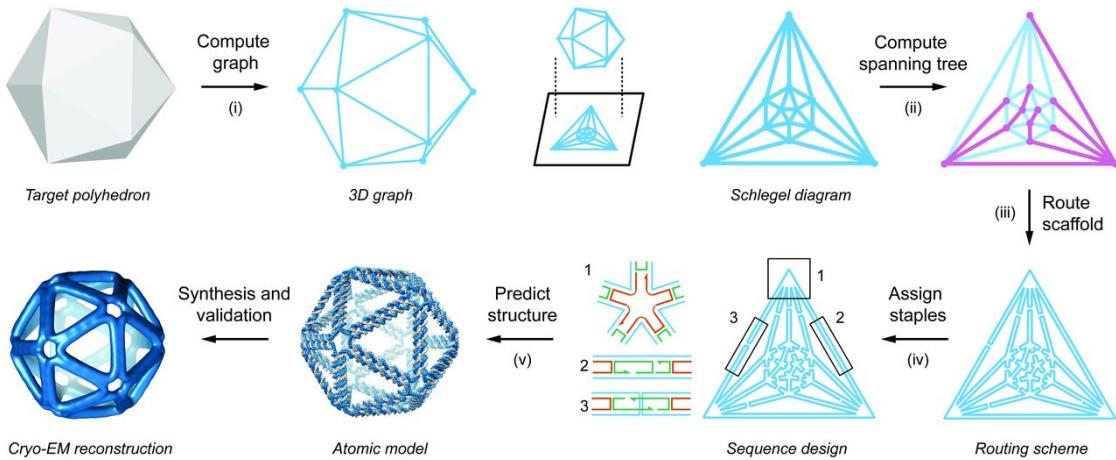
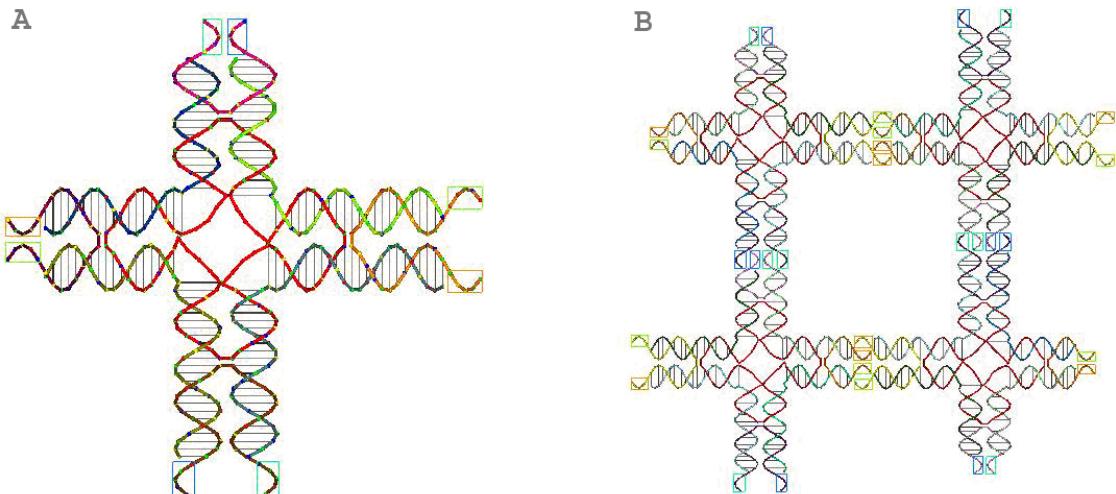
Figure 5.2: BSCOR

MagicDNA

Another method of solving topological issues through rigid-body manipulation was used by Chao-Min Huang [28]. The tool used is not public, so I have not been able to examine it, but the supplementary material of the article shows them using a Matlab script to interactively move and rotate the helix bundles (treated as rigid bodies) into a desired configuration with less stretched bonds.

oxView

The oxView application was developed as part of this thesis project and will be described more in Chapter 6.

**Figure 5.3:** daedalus**Figure 5.4:** Tiamat

5.2 Simulation tools

Simulating a structure can provide insight to understand experimental results, but can also guide decisions at the design stage. Different models

5.2.1 All-atom simulation

Simulation tools such as NAMD[29], use force fields such as AMBER[30] and CHARMM [31] that model interactions between individual atoms. While it is possible to perform atomistic simulations of large DNA origami structures[32],

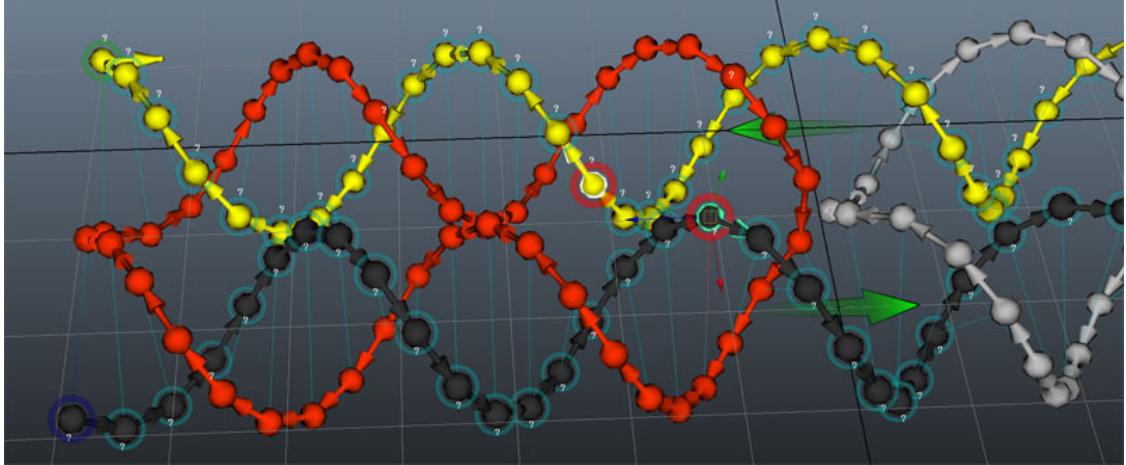


Figure 5.5: vHelix

the simulations take a long time to run and it is unknown how well the models represent DNA thermodynamics [33].

5.2.2 oxDNA/RNA

In 2010, a the coarse-grained simulation software called oxDNA was introduced by Thomas Ouldridge [4]. It simulates DNA on the level of nucleotides and has been shown to model complex origami devices with a generally good agreement with experimental data [34]. In 2014, the DNA model was extended to include RNA by Petr Šulc [35], showing its ability to model a set of common RNA motifs.

Molecular Dynamics (MD) and Monte Carlo (MC) simulation techniques.

OxDNA was joined by cogli1 for trajectory visualisation.

While oxDNA can be very useful for modelling a structure, it has traditionally not been very accessible for experimentalists.

5.2.3 mrDNA

Another promising feature of mrdna is that it has a spline-based helix representation and is implemented in python. This enables users to easily script edits to the structure, translating and rotating parts of it before starting the simulation. Thus, topological issues or over-stretched bonds can, with some skill, be resolved even before starting

5. An introduction to tools for the design and simulation of nucleic acid structures

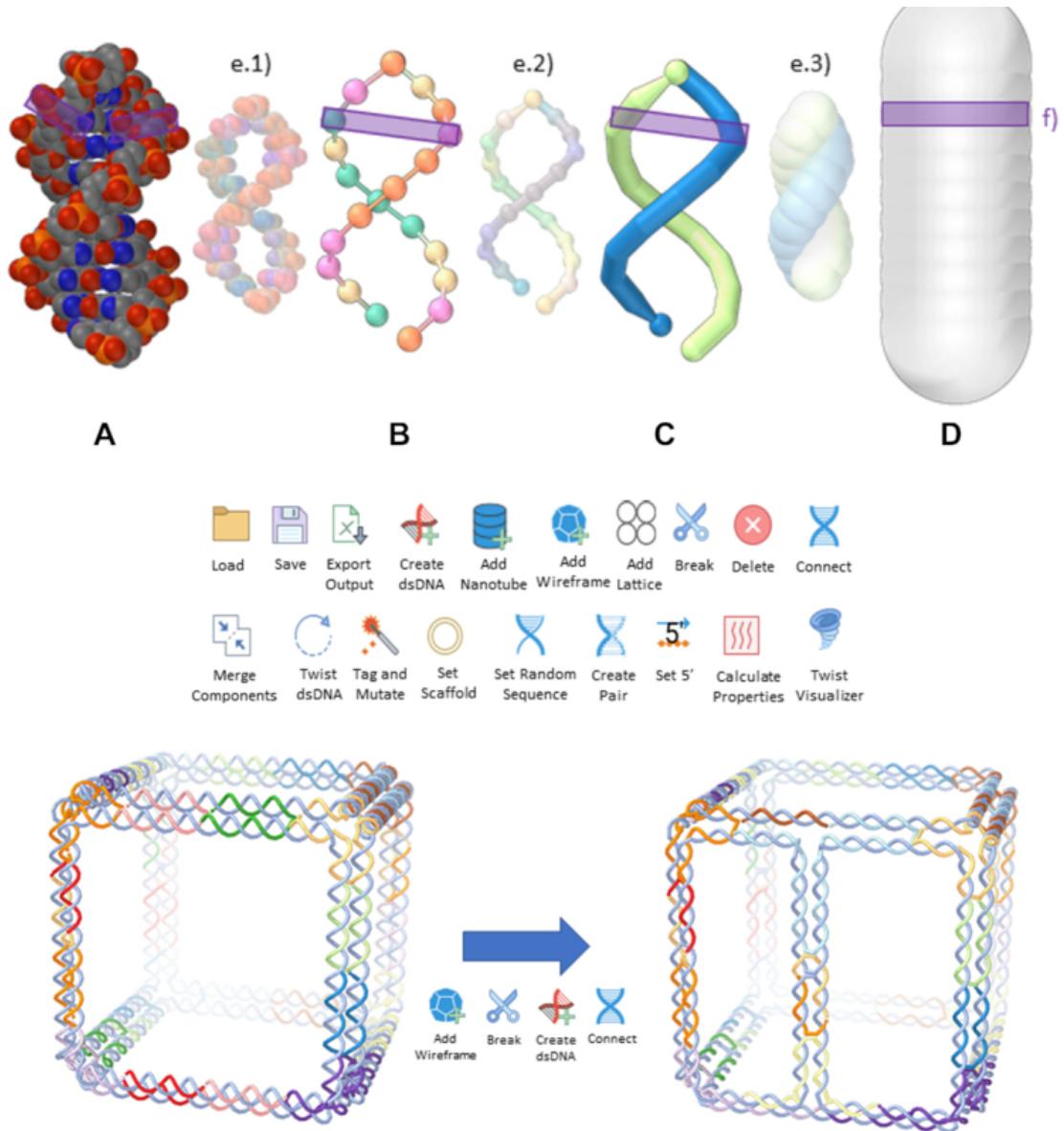


Figure 5.6: Adenita

to simulate. I did, based on this, also create a rudimentary interactive editor interface to mrdna, but it would need a lot of refinement to be externally usable.

5.2.4 Cando

Cando is a finite element modelling framework[36] available through a web server at <https://cando-dna-origami.org>. DNA double helices are modelled as elastic rods (connected by rigid crossovers) that stretch, twist and bend in line with

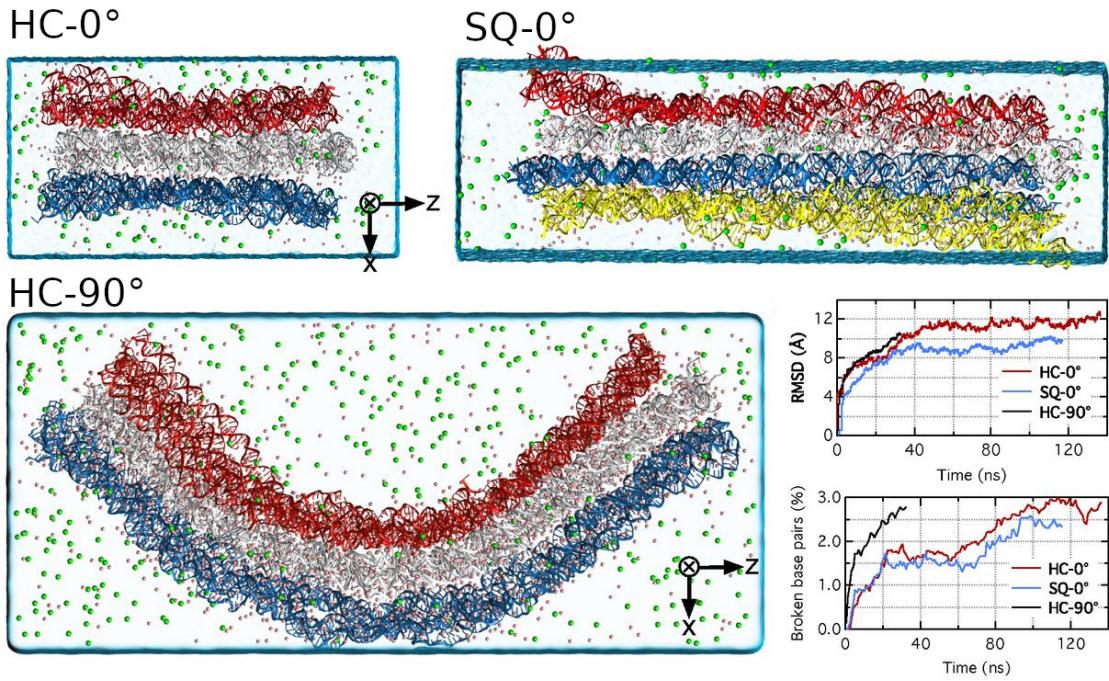


Figure 5.7: All-atom simulation

experimental measurements.

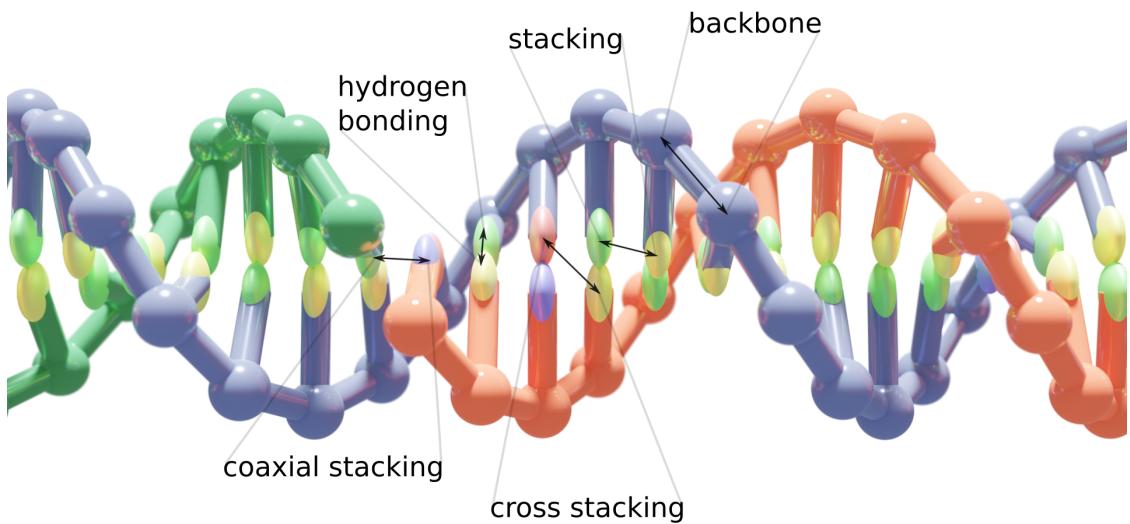


Figure 5.8: The oxDNA model

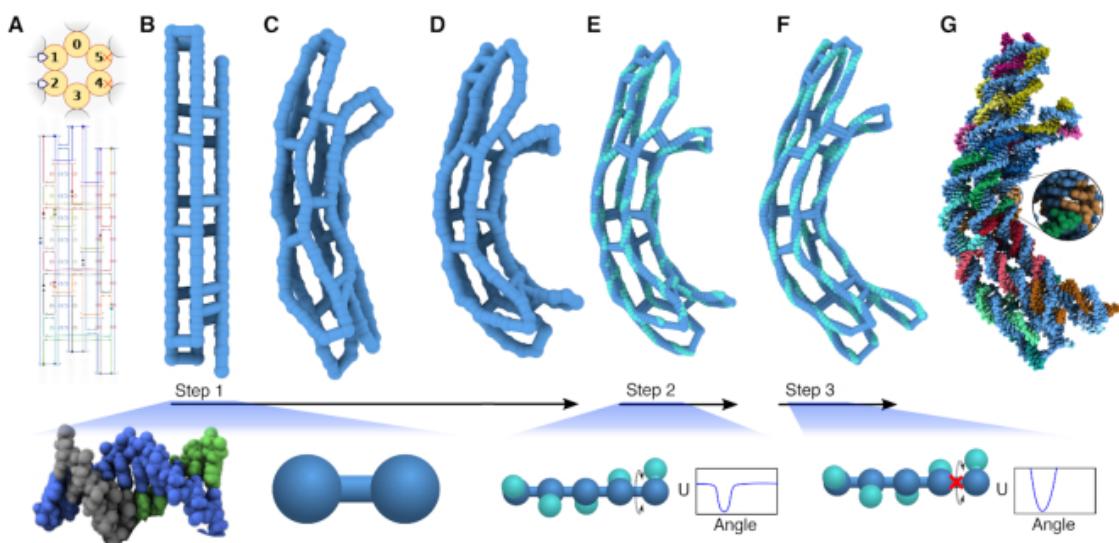


Figure 5.9: MrDNA

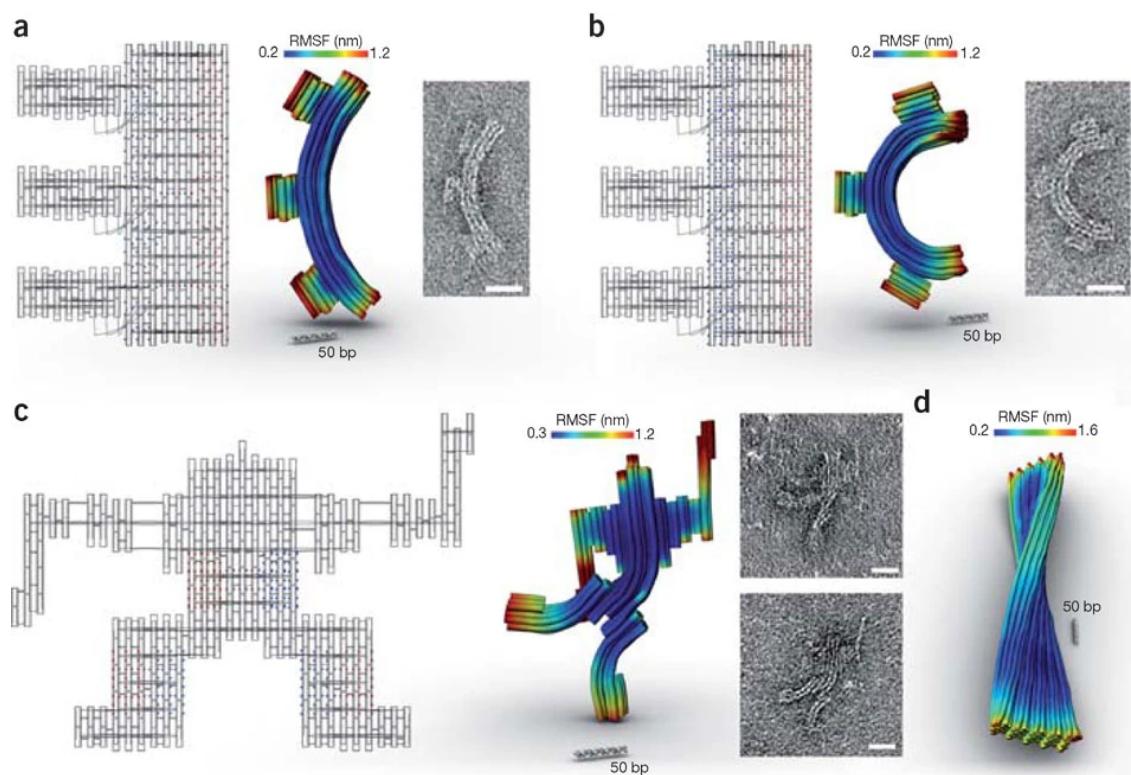


Figure 5.10: Cando

6

Structure design and analysis in oxView

Contents

6.1	Importing designs	36
6.1.1	Basic import	37
6.1.2	Multi-component designs	38
6.1.3	Far-from-physical caDNAno designs	38
6.2	Rigid-body manipulation and dynamics	39
6.3	Editing designs	39
6.4	Example conversions	39
6.5	Visualization options	43
6.6	Exporting designs	43
6.6.1	Exporting oxDNA simulation files	43
6.6.2	Exporting other 3D formats	44
6.6.3	Exporting sequence files	44
6.6.4	Saving image files	44
6.6.5	Creating videos	44
6.7	Converting RNA origami designs	44

This chapter contains my results on how to design, simulate and analyse DNA and RNA nanostructures. It starts with an introductory description of earlier approaches to this problem and will then describe how my contributions to the oxView tool have improved the previous methods and enabled new results.

As I started this DPhil, I was tasked with the issue of converting origami designs created in caDNAno so that they can be correctly simulated in oxDNA.

I soon started collaborating with Hannah Fowler from the Doye group at Theoretical Chemistry. She was simulating a large collection of old DNA designs, so it was a good opportunity to convert and relax problematic structures, investigating why some structures are more problematic than others.

At this time, there was a python script included in the UTILS directory of the oxDNA repository, but it was difficult to use and it failed for many structures. At the end of 2018, the taxoxDNA webserver [37] was launched, updating the conversion script and making it more accessible. Still, since caDNAo structures are drawn on a lattice, the resulting oxDNA configurations often had unnaturally extended backbone bonds, requiring time-consuming relaxation.

During a secondment within the Šulc group at Arizona State University in 2019, I contributed to the development of a web-based oxDNA viewer called oxView[38]. Among the main features I added to oxView was a cluster-level rigid-body dynamics option (detailed in Section 6.2) that in many cases speed up the relaxation with orders of magnitude compared to oxDNA relaxation alone. Since then I have been collaborating with the Šulc group to add more features and to make the tool more accessible as a visualiser and editor. For our second oxView publication I rewrote the main parts of the taxoxDNA codebase into typescript, resulting in the *taxodna.js* library (<https://github.com/Akodiat/tacoxdna.js>) which oxView uses to import various common design formats automatically.

This section will present my own contributions to oxView, unless otherwise stated, but also I want to acknowledge the work done by Erik Poppleton and Michael Matthies; without them this tool would not exist. Michael was the original oxView developer and has done a great work in enabling live oxDNA relaxations through the *ox-serve* webserver. Erik made oxView able to smoothly render and analyse systems with over a million nucleotides and has created a large set of handy analysis scripts.

6.1 Importing designs

There are a lot of different formats available for DNA origami design; some of the main design tools are covered in Section 5.1. This section will describe how

to use oxView to import different designs.

6.1.1 Basic import

Thanks to the *tacoxdna.js* library I created, the conversion is now straightforward for many designs. The formats listed below can all be imported by simply clicking the *Import* button in oxview. Some additional formats still require the use of the external TacoxDNA webserver[39] however.

Importing caDNAno files

Select the caDNAno JSON file to import, making sure that *caDNAno* is selected as file format. Next, select the correct lattice type; either *Square* or *Hexagonal*. Optionally, input a sequence to assign to the origami scaffold (which will otherwise be random).

Importing rpoly files

Rpoly files are the output from the BSCOR[40] tool (described in Section 5.1.2) for converting polyhedral meshes into DNA origami. Select the rpoly file to import, making sure that *rpoly* is selected as file format. Optionally, input a sequence to assign to the origami scaffold (which will otherwise be random).

Importing Tiamat files

Select the tiamat *.dnajson* file to import, making sure that *tiamat* is selected as file format. Binary *.dna* Tiamat files need to be reopened in Tiamat and saved to the text-based *.dnajson*. Select Tiamat version (1 or 2), then select nucleic acid type (DNA or RNA).

By default, nucleotides without assigned base types will be given a random type. However, it is also possible to select a fixed default base.

Importing PDB files

While I did create include the DNA PDB to oxDNA converter from TacoxDNA in *tacoxdna.js*, a more versatile PDB import was created by Jonah Procyk to support his ANM-oxDNA model [41]. Simply drag and drop (or load) a PDB file into an oxView window and the DNA, RNA and/or protein it contains will be automatically converted and loaded.

6.1.2 Multi-component designs

Designs spread across multiple files (or even multiple design tools) can be easily combined in oxView by simply importing them all and using the editing tools to arrange and connect them properly.

6.1.3 Far-from-physical caDNAno designs

Some structures, while converted without failure to the oxDNA format, will have a very far-from-physical configuration due to the way they are drawn in caDNAno. As mentioned above, since it is only possible to draw all helices parallel to each other, on a lattice, backbone bonds may be very elongated, creating high energies and/or topological problems.

The oxDNA software already includes relaxation procedures for such structures, bringing them together in a slow and controlled manner using a specified maximum backbone force. However, for large structures, this can take a very long time, even while using GPU simulation.

In such cases, another software I have investigated, called mrdna (Multi-resolution DNA nanotechnology), proves very useful[42]. It is a python package using ARBD (Atomic Resolution Brownian Dynamics), both being developed by Chris Maffeo, to simulate double- and single-stranded DNA structures at multiple levels of coarse-graining. Since these simulations are more coarse-grained than oxDNA, they run significantly faster. Furthermore, after I have been in contact with Chris, mrdna can now also be configured to output and simulate oxDNA

configurations as the final simulation step. Because of this, mrdna can also be useful for converting simple structures, if tacoxDNA fails to parse the caDNAno file.

6.2 Rigid-body manipulation and dynamics

Rapid relaxation of converted cadnano designs

Rigid-body manipulation [28]. The translation and rotation tools in oxView allow users to select and rearrange blocks of nucleotides as rigid bodies.

Dynamics [43]

Manually, on import or through DBSCAN algorithm [44].

Clusters held together with spring forces at each shared backbone bond, with a magnitude of

$$f_{\text{spr}} = c_{\text{spr}}(l - l_r),$$

where c_{spr} is a spring constant, l is the current bond length and l_r is the relaxed bond length. To avoid overlaps, a simple linear repulsive force, of magnitude

$$f_{\text{rep}} = \max \left(c_{\text{rep}} \left(1 - \frac{d}{r_a + r_b} \right), 0 \right)$$

is added between the centre of each group, where c_{rep} is a repulsion constant, d is the distance between the two centres of mass, and $r_a + r_b$ is the sum of the group radii (the greatest distance they can be while still overlapping).

6.3 Editing designs

6.4 Example conversions

A selection of the DNA designs I have relaxed are shown in Figure 6.3. The first two examples, adopted from [46] and [47] and illustrated in Figure 6.3.a and 6.3.b, are both quite straightforward to relax in oxDNA, although the relaxation is much faster using mrdna.

The tensegrity kite structure, adopted from [48] is harder to relax since, as seen in the first image in Figure 6.3.c, the two helix bundles are drawn parallel

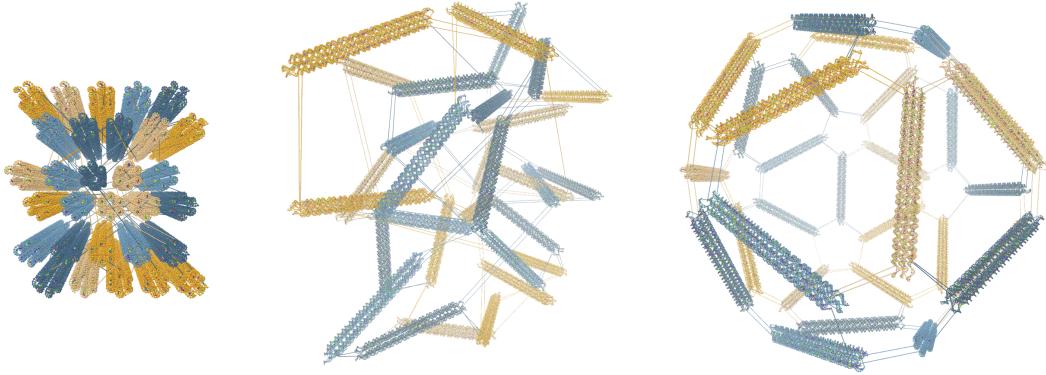


Figure 6.1: Rigid-body dynamics of clusters. Snapshots from the automatic rigid-body relaxation of an icosahedron, starting with the configuration converted from caDNAno **a)**, through the intermediate **b)** where the dynamics are applied, and **c)** the final resulting relaxed state.

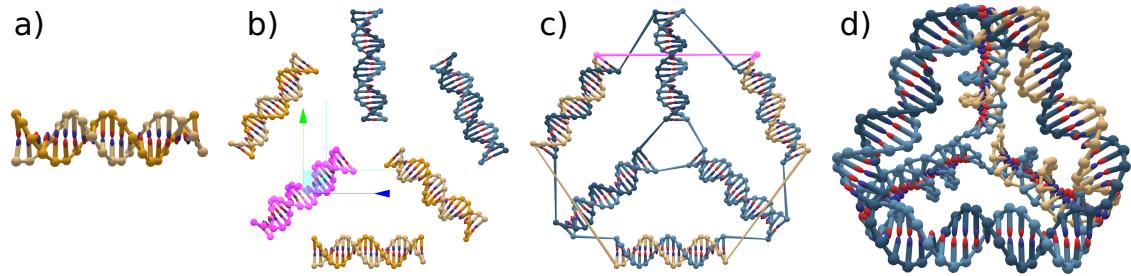


Figure 6.2: Designing the DNA tetrahedron from [45] using the oxView editing tools. a) The initial helix created. b) Duplicated helices being translated into place. c) Strands ligated together. d) The resulting 3D tetrahedron shape, as seen after applying rigid-body dynamics.

to each other in caDNAno. Given enough time to relax, they should still become orthogonal, but a much more efficient way is to write a mrdna script to rotate one helix bundle so that it is orthogonal from the start, as seen in the middle image of 6.3.c. The remaining overstretched bonds are then quickly relaxed using mrdna.

Finally, the Möbius strip, adopted from [49], is particularly tricky to relax, since the caDNAno design have all helices drawn in the same plane, with bonds from each end stretching through the whole structure and intersecting at a single point, as can be seen in the first image of Figure 6.3.d. With some help from Chris Maffeo, however, I was able to use a mrdna script to edit the structure into a configuration much easier to relax, as seen in the second image of Figure 6.3.d. Since the caDNAno design does not make it clear if the Möbius strip should be left-handed or right-

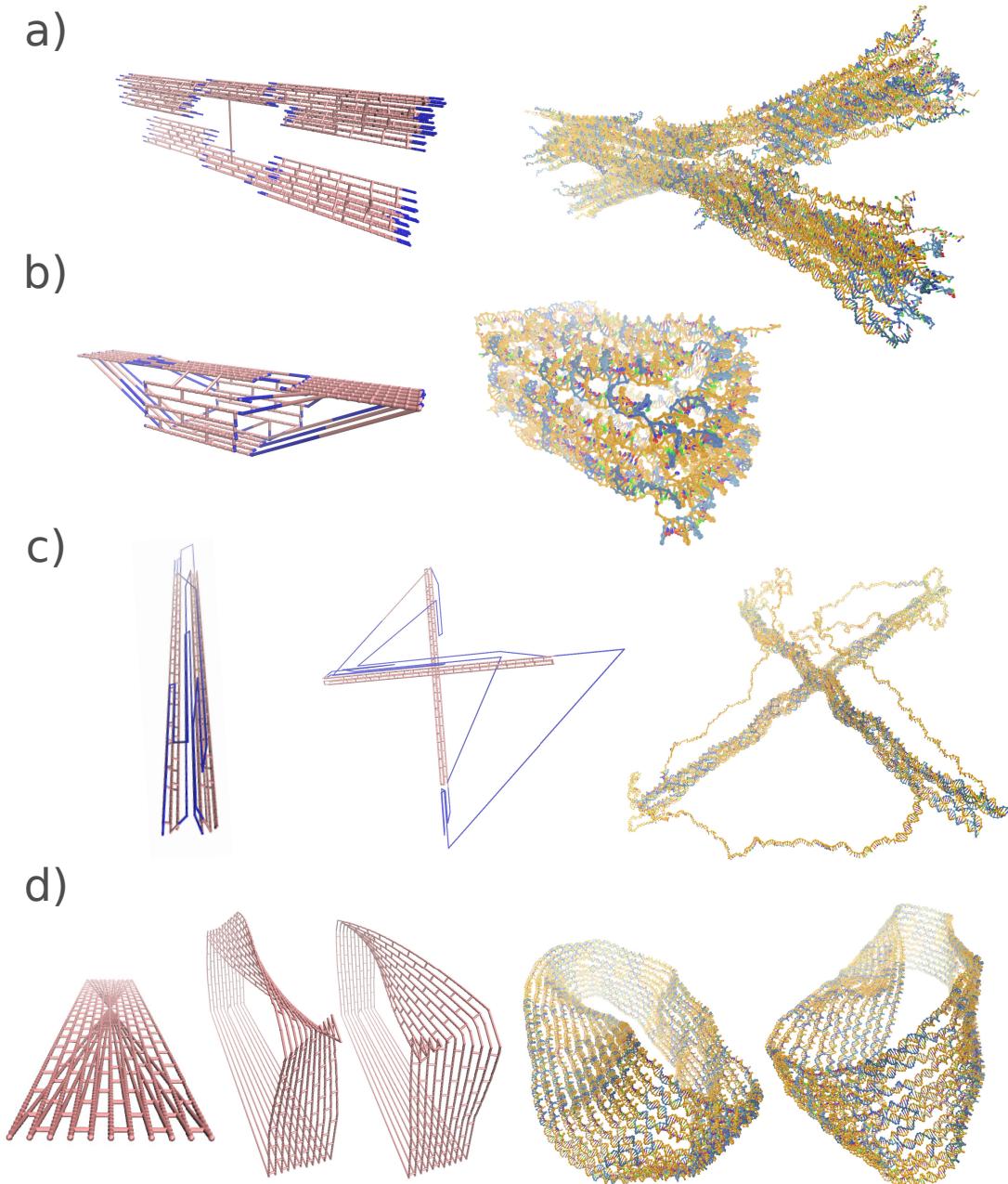


Figure 6.3: Relaxation results for various DNA designs. Each row depicts a new design, with the left-hand side showing the structure as it was drawn in caDNAno (and parsed by mrdna), while the right-hand side is the relaxed structure in oxDNA. Intermediate images are edits done in mrdna. While the switch design[46] in **a)** and the small DNA origami box[47] in **b)** relaxed without any required editing, the tensegrity kite structure [48] in **c)** and the Möbius strip[49] in **d)** benefited greatly from moving selected helices to a position off the lattice before starting the simulation.

Tool	Description
	Create a new strand from a given sequence. Select <i>duplex mode</i> to instead create a helix.
	Copy the selected elements (Ctrl+C).
	Cut the selected elements (Ctrl+X).
	Paste elements from clipboard (Ctrl+V to paste in original position, or Ctrl+Shift+V to paste in front of camera).
	Delete all currently selected elements. (delete)
	Ligate two strands by selecting the 3' and 5' endpoint elements to connect (L)
	Nick a strand at the selected element (N)
	Extend strand from the selected element with the given sequence. Select <i>duplex mode</i> to also extend the complementary strand.
	Insert (add) elements within a strand after the selected element
	Skip (remove) selected elements within a strand.
	Rotate selected elements around their center of mass (R).
	Translate currently selected elements (T).
	Move to. Move other selected elements to the position of the most recently selected element.
	Connect 3' duplex. Connects the 3' ends of two selected staple strands with a duplex, generated from the sequence input.
	Connect 5' duplex. Connects the 5' ends of two selected staple strands with a duplex, generated from the sequence input.
	Set the sequence of currently selected elements. Select duplex mode to also set the complementary sequence on paired elements.
	Get. Assigns the sequence of selected bases to the sequence input.
	Reverse complement. Generates the reverse complement of a provided sequence.
	Search. Highlights the position the provided sequence in each strand, if present.

Table 6.1: Editing tools available in oxView

handed, this is also decided in the script; changing the rotational direction will produce a mirrored version of the structure, as seen in the third image of Figure 6.3.d.

6.5 Visualization options

Depending on the design, a user of oxView might want to modify the visualization settings to make certain features of the structure more or less visible.

Centring with periodic boundary conditions. A useful utility when visualising an oxDNA trajectory is to keep the structure centered at the origin, stopping it from drifting out of view. The method described in [50] was used to achieve centering while taking periodic boundary conditions into account.

In essence, for each coordinate $p_j = (p_x^j, p_y^j, p_z^j)$ in the centring set of size n , each dimension $i \in \{x, y, z\}$ gets averaged in its own variable α_i , representing its 1D interval as a 2D circle (where the circumference b_i is the bounding box side length):

$$c_i = \frac{1}{n} \sum_{j=1}^n [\cos(\alpha_i^j), \sin(\alpha_i^j)]$$

Where $\alpha_i^j = \frac{2\pi}{b_i} p_i^j$ is the angle on the unit circle and c_i is the average 2D position representing dimension i . Finally, the averages are converted back to cartesian coordinates:

$$cm_i = \pi + \frac{b_i}{2\pi} \text{atan2}(-c_{i,y}, -c_{i,x})$$

Change component sizes , change colours, fog, virtual reality.

6.6 Exporting designs

Once a structure has been created in or loaded into oxView, it can be exported in a variety of formats.

6.6.1 Exporting oxDNA simulation files

Also force files

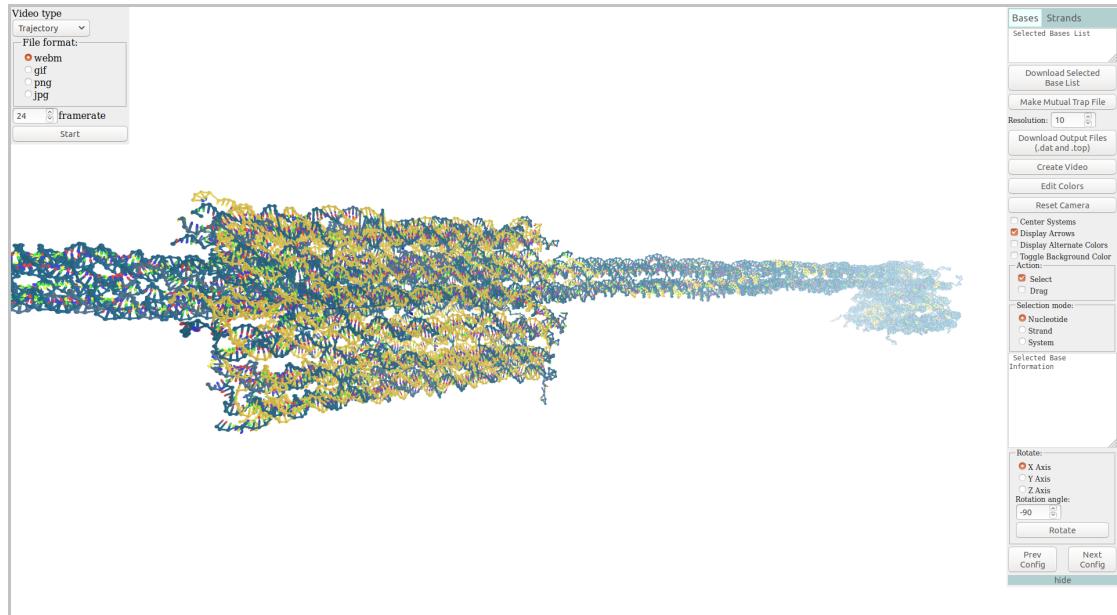


Figure 6.4: Screenshot of the online oxView tool, exporting a video of a slider on a rail from a simulated trajectory.

6.6.2 Exporting other 3D formats

6.6.3 Exporting sequence files

6.6.4 Saving image files

6.6.5 Creating videos

Trajectory

Leminiscate

6.7 Converting RNA origami designs

During my secondment at the Andersen lab in Aarhus, I worked with converting RNA structures designed using their ASCII-based blueprint format into oxRNA simulation files. Examples of converted structures are shown in Figure 6.5. The Andersen lab already has scripts, soon to be published, for parsing their blueprint files and building the corresponding PDB structures (the first two columns of Figure 6.5). However, the resulting PDB files are not relaxed and would take a long time to relax using all-atom simulation. As such, I modified the tacoxDNA [37] PDB parser to enable PDB-to-oxRNA conversion. I have contacted Lorenzo to let him

know about these additions and hopefully, they will be included in a future version of tacoxDNA. One issue I noticed with the conversion was that the asterisk (*) and prime (') characters were used interchangeably in the RNA motif library to name atoms of the sugar group, causing problems with the tacoxDNA script, which only recognises the prime. This has already been fixed in tacoxDNA. The third column of Figure 6.5 shows the structures relaxed and simulated in oxRNA, some significantly different from the previously available PDB models in the second column.

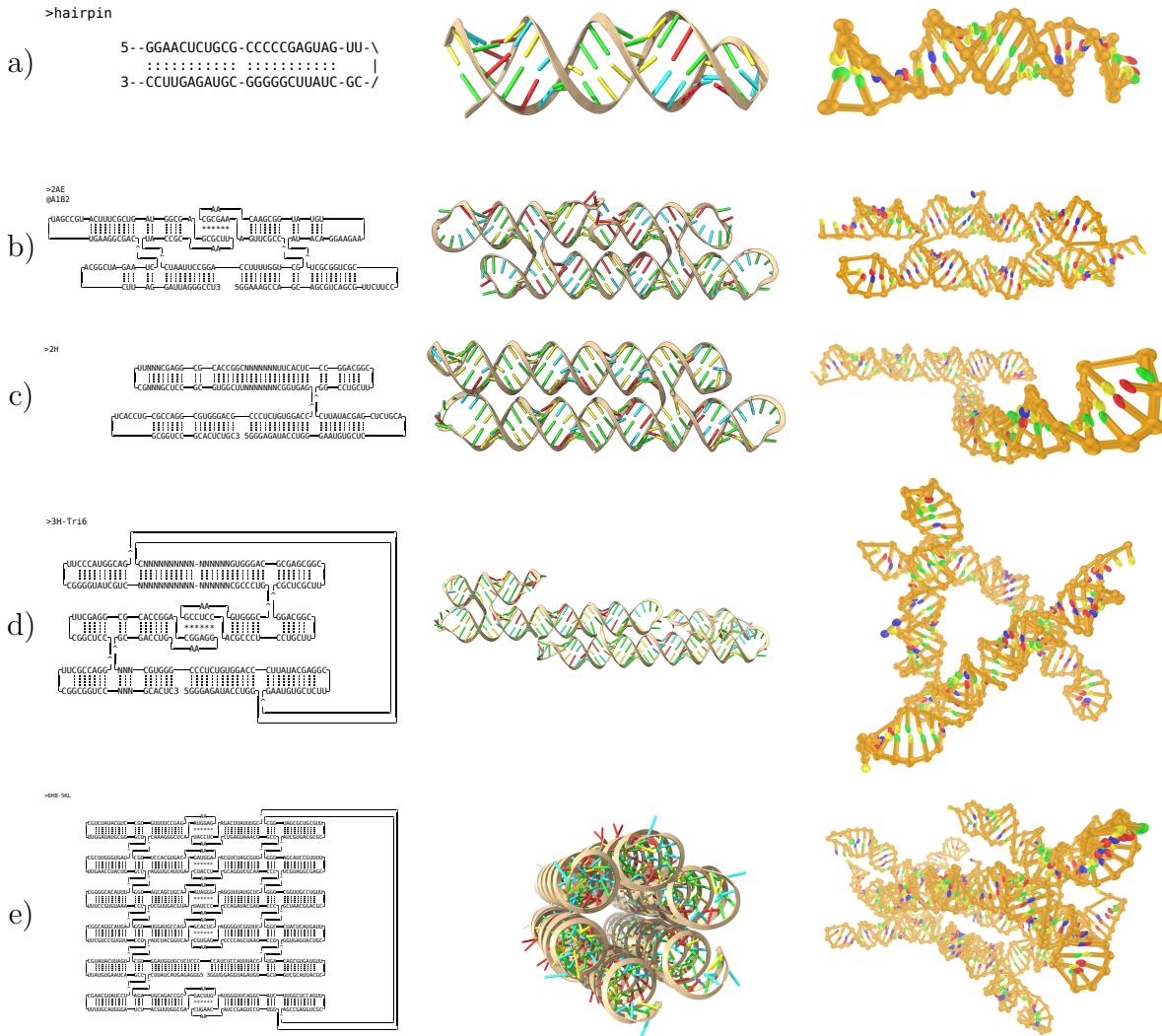


Figure 6.5: Conversion and simulation of various RNA designs. Each row, from left to right, shows the ASCII blueprint design, the PDB model (visualised using ChimeraX), and a frame from the simulated structure (visualised using oxView). **a)** Is a simple hairpin loop. **b)** is a two-helix bundle tile used in [7]. **c)** is two helices connected by a double crossover, analysing the flexibility of such a motif. **d)** is a possible design for a tensegrity triangle. **e)** is a siz-helix bundle.

You live and learn. At any rate, you live.

— Douglas Adams, *Mostly Harmless*

7

Conclusion

7.1 Individual module design

7.2 Modular assembly

7.3 Future work

Appendices

A

Possible appendix chapter

Appendices are just like chapters. Their sections and subsections get numbered and included in the table of contents; figures and equations and tables added up, etc. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Sed et dui sem. Aliquam dictum et ante ut semper. Donec sollicitudin sed quam at aliquet. Sed maximus diam elementum justo auctor, eget volutpat elit eleifend. Curabitur hendrerit ligula in erat feugiat, at rutrum risus suscipit. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Integer risus nulla, facilisis eget lacinia a, pretium mattis metus. Vestibulum aliquam varius ligula nec consectetur. Maecenas ac ipsum odio. Cras ac elit consequat, eleifend ipsum sodales, euismod nunc. Nam vitae tempor enim, sit amet eleifend nisi. Etiam at erat vel neque consequat.

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