

# Package ‘GA’

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**Type** Package

**Title** On Multivariate Feature Selection with Genetic Algorithms

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**Description** This package provides a genetic algorithm to identify optimal features for linear regression under R's LM and GLM models. Users are able to set multiple parameters for the genetic algorithm and request optimization via R2, AIC, BIC, AICc or a user defined function. The algorithm can process these score functions in parallel on a single machine with the parallel = TRUE argument.

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## R topics documented:

apply_elitism . . . . .	2
breed_next_gen . . . . .	3
create_initial_generation . . . . .	5
generate_data . . . . .	6
score_fitness2 . . . . .	6
see_if_terminate . . . . .	7
select . . . . .	9
select_parent . . . . .	13
test_user_function . . . . .	14

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apply_elitism	<i>Processes the Highest Fitness Creatures to ensure that they Make it into the Next Generation</i>
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### Description

Since the primary selection mechanisms of the genetic algorithm are probabilistic, there is a chance that a high performing gene goes extinct causing the gene pool to become less fit. This function counteracts this by ensuring that the best performing creatures survive into future generations. This function selects a number of most fit creatures equal to the ceiling(pop \* elite\_prop) and guarantees that they make it to the next generation. Additionally, this function makes a copy of each most-fit creature and conducts one gene mutation randomly on each creature. If the copy is more fit than the original, it is returned instead of the original so that the final returned matrix of elite creatures are at least as fit as the incoming elite creatures.

### Usage

```
apply_elitism(
  data,
  gene,
  score_vec,
  elite_prop = 0.1,
  mutate = 0.1,
  metric = "AIC",
  family = "gaussian",
  custom_function = NULL,
  fittest
)
```

### Arguments

data	a matrix or dataframe with ncol = gene_length plus 1
gene	matrix with all 0s and 1s with ncol = gene_length and nrow = pop
score_vec	a positive, numeric vector with length equal to the total population
elite_prop	a numeric, the percentage of the population that is selected for elitism
mutate	percentage mutation rate
metric	a character, a user specified statistic such as R2, AIC, BIC, or AICc
family	model family corresponding to GLM. Defaults to 'gaussian'
custom_function	defaults to NULL, if defined takes a single row from a generation_matrix and returns a numeric value
fittest	whether a custom function has the highest value corresponding to the fittest or the lowest value

### Value

a matrix containing all 1s and 0s representing the genes of the elite population

**Examples**

```
data <- matrix(rnorm(11*3),nc=11)
gene <- matrix(rbinom(10*10,1,.5),nc=10)
score_vec <- rnorm(10)
elite_prop <- .05

elite_gen <- apply_elitism(score_vec = score_vec, gene = gene, data = data, elite_prop = elite_prop)
```

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breed_next_gen	<i>Breeds Next Generation</i>
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**Description**

The purpose of this function is to take a vector of new parents, their corresponding fitness score vector and their corresponding genes to output the next generation in the genetic algorithm. It does this via 'several crossover methods including uniform, k-point, fitness-uniform along with their corresponding parameters. After Crossover is complete mutation is applied in two different methods either adaptive which can increase mutation when diversity becomes too low and fixed which maintains a steady mutation rate. Lastly, there is an option to minimize inbreeding prior to crossover and mutation.

**Usage**

```
breed_next_gen(
  generation_matrix,
  new_parents,
  score_vec,
  number_of_parents,
  mutation = "fixed",
  minimize_inbreeding = FALSE,
  crossover = "uniform",
  mutation_rate = 0.01,
  ad_max_mutate = 0.1,
  ad_min_mutate = 0.01,
  ad_inflection = 0.3,
  ad_curve = 15,
  required_pop,
  number_of_crossovers = 1
)
```

**Arguments**

generation_matrix	matrix with ncol = gene_length and nrow = total number of creatures, consists only of 1s and 0s, no all-zero rows.
new_parents	a numeric vector with elements indexing the next generation of parents, length is total population x number_of_parents.
score_vec	a numeric vector with length equal to total population.
number_of_parents	is an integer defining the number of parents per offspring

mutation	a character either 'fixed' or 'adaptive' indicating the type of mutation
minimize_inbreeding	a logical indicating whether or not we minimize inbreeding.
crossover	a character that can be 'uniform', 'fitness', or 'k_point' indicating how to carry out crossover.
mutation_rate	a numeric between 0 and 1 indicating how often a creature is selected for mutation.
ad_max_mutate	max mutation rate for adaptive mutation, numeric between 0 and 1 and more than ad_min
ad_min_mutate	min mutation rate for adaptive mutation, numeric between 0 and 1 and less than ad_max
ad_inflection	percentage of diversity in population where adaptive mutation begins to increase rapidly
ad_curve	rate that influence how intensely adaptive mutation changes
required_pop	the number of offspring required
number_of_crossovers	number of k_point crossovers, needs to be less than gene_length

## Details

crossover Methods Uniform - each gene is randomly selected from 2 or more parents from a PMF proportional to the number of parents.

Fitness - each gene is randomly selected from 2 or more parents from a PMF proportional to the parent's fitness.

K-Point - parents genes are broken into k+1 segments, then the offspring inherits portions randomly from the parents. Takes the parameter number\_of\_crossovers which must be less than 1/2 gene\_length.

For all methods candidate offspring are accepted / rejected so that they don't have completely 0-vector genes.

mutation Fixed - Each offspring has a mutation\_rate chance of being selected for mutation. Once selected one gene is switched from one to zero or zero to one.

Adaptive - the overall population is measured for diversity. As diversity becomes lower, the mutation rate increases. Once selected for mutation a single gene is switched from one to zero or zero to one. The adaptive function is controlled by a simple logistic function with parameters ad\_min and ad\_max describing the minimum and maximum mutation rates. ad\_inflection controls where the logistics point pivots, and ad\_curve controls how rapidly the logistics curve increase.

For all mutation methods, candidate offspring are accepted / rejected so that they don't have completely 0-vector genes.

Minimize inbreeding. his option reduces (though does not remove) the chance of similar creatures creating offspring together. Each parent is assigned new partner(s) randomly from a PMF proportional to how different their genes are. Parents are drawn without replacement so that if they were selected to become parents, they will still remain parents.

## Value

returns matrix of 1s and 0s with no all-zero rows representing the genes of the next generation after crossover and mutation

**Examples**

```

generation_matrix <- matrix(rbinom(10*10,1,.5),nc=10)
new_parents <- sample(1:10,20,replace = TRUE)
mutation <- 'fixed'
crossover <- 'uniform'
number_of_parents <- 2
required_pop <- 10
score_vec <-abs(rnorm(10))

next_generation_matrix <- breed_next_gen(generation_matrix = generation_matrix,
new_parents = new_parents, mutation = mutation, crossover = crossover,
  number_of_parents = number_of_parents,required_pop = required_pop,
  score_vec = score_vec)

```

---

```
create_initial_generation
```

*Creates the Initial Gene Pool for Genetic Algorithm*

---

**Description**

This function creates the initial population to be used in the genetic algorithm. It checks to make sure there are now 0-vectors because 0-vectors are meaningless in the context of LM and will cause LM to fail. Function allows users to specify number of population gene length, probability of genes being represented and specify initial population.

**Usage**

```
create_initial_generation(pop, gene_length, prob = 0.5, user_genes = NULL)
```

**Arguments**

pop	an integer representing the total population maintained for each generation of the genetic algorithm
gene_length	an integer defining how many genes are encoded for each creature, needs to be the same length as the number of columns in the independent variable matrix
prob	a number 0-1 representing the chance that an individual has any given gene
user_genes	a matrix consisting of 1s and 0s without any rows with all zeros ncol equal to gene_length and nrow less than or equal to pop

**Value**

returns a matrix of 1s and 0s without any rows with all zeros representing the initial genes for the first generation of the genetic algorithm.

**Examples**

```

pop <- 500
gene_length <- 50
prob <- .25

generation_matrix <- create_initial_generation(pop = pop, gene_length = gene_length,prob = prob)

```

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generate_data	<i>Generates normal data with 50 Covariates.</i>
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### Description

This function creates a matrix that is 51 x 1000 where the first column is the response variables and the remain 50 are independent variables. The covariates are generated uniform(0,100) The parameter for each covariate is defined such that the first one is  $20 \times 0.9e1$  followed by  $20 \times 0.9e2$  with each subsequent parameter decaying until the last one is  $20 \times 0.9e50$ . This allows us to validate a genetic algorithm while generating a large dataset

### Usage

```
generate_data()
```

### Value

a 1000x51 matrix

### Examples

```
generate_data()
```

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score_fitness2	<i>Scores fitness for an entire generation of creatures</i>
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### Description

This takes a generation\_matrix representing all the genes of a single generation, the data, and user input describing the metric such as R2, AIC, BIC, and AICC and can even use a custom function defined by the user. The underlying fitness function for R2 is lm() and the underlying fitness function for AIC, BIC, and AICC is glm(). AIC, BIC, and AICC has the option to specify a specific family of functions however, the data needs to be defined across the support for the given family for instance exponential must be greater than 0.

### Usage

```
score_fitness2(
  gene,
  data,
  metric = "AIC",
  family = "gaussian",
  custom_function = NULL,
  fittest = "high"
)
```

**Arguments**

gene	matrix with all 0s and 1s with ncol = gene_length and nrow = pop
data	a matrix or dataframe with ncol = gene_length plus 1
metric	a character, a user specified statistic such as R2, AIC, BIC, or AICc
family	, model family corresponding to GLM. Defaults to 'gaussian'
custom_function	defaults to NULL, if defined takes a single row from a generation_matrix and returns a numeric value
fittest	whether a custom function has the highest value corresponding to the fittest or the lowest value

**Value**

returns a list with the first element being a vector of processed fitness scores to for continued use by the algorithm and element 2 being true (user specified) values user reference, for instance true AIC values

**Examples**

```
gene <- matrix(rbinom(2*10,1,.5),nc=10)
data <- matrix(rnorm(11*3),nc=11)
pop_required <- 10
metric <- 'AIC'

score_vec <- score_fitness2(data = data,gene = gene,metric = metric)
```

---

see_if_terminate	<i>Tests if early termination conditions are met.</i>
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**Description**

This function defines additional termination criteria which will run in addition to the max\_iteration. Default is null for all values. User can specify a percentage\_convergence such that when diversity falls below a specific threshold the program terminates. User can identify a estimate (from the standard summary() function that if the estimate reaches a specific threshold the program terminates or if the estimate pauses for a certain number of iterations terminates.

**Usage**

```
see_if_terminate(
  generation_matrix,
  summary_data_frame,
  estimator = NULL,
  pause_length = NULL,
  score_threshold = NULL,
  percent_converge = NULL,
  iteration,
  metric = "AIC",
  fittest = "high"
)
```

## Arguments

generation_matrix	generation matrix with all 0s and 1s with ncol = gene_length and nrow = pop
summary_data_frame	a matrix that captures the summary() data for each generation's scores
estimator	character string referencing the named entry from summary() for instance Min.
pause_length	a numeric indicating how many iterations without improvement in the estimator before you terminate
score_threshold	a numeric indicating a threshold to cutoff if the estimator reaches that value
percent_converge	percentage of diversity when algorithm terminates for instance .1 will terminate if there are only .90 of the population is represented by the same genes
iteration	is the current iteration the main algorithm is on
metric	is the user specified statistic such as R2, AIC, BIC, or AICc
fittest	whether a custom function has the highest value corresponding to the fittest or the lowest value

## Details

summary\_data\_frame - is imported from the main function and updated each iteration

estimator - can be nominated from the summary() function aka Min., 1st Qu., Median, Mean, 3rd Qu., or Max.

percent\_converge - terminates once diversity falls below a certain percentage. diversity is  $\text{sum}(\text{unique}(\text{genes}))/\text{total\_genes}$

## Value

TRUE if terminate conditions are met with a reason, FALSE otherwise

## Examples

```
generation_matrix <- matrix(rbinom(2*10,1,.5),ncol=10)
summary_data_frame <- data.frame(matrix(1:12,ncol=6))
names(summary_data_frame) <- c("Min.", "1st Qu.", "Median", "Mean", "3rd Qu.", "Max.")
estimator <- 'Mean'
score_threshold <- 2.4
iteration <- 2

confirm_terminate <- see_if_terminate(generation_matrix,
summary_data_frame, estimator = 'Mean',
score_threshold = score_threshold, iteration = iteration)
```



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`select`*Select - Runs a Genetic Algorithm*

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### Description

This function optimizes a linear regression using a genetic algorithm. User can enter a custom function or select a metric from (AIC, BIC, AICC, R2) to optimize features to include in the linear regression. This function has a broad range of genetic algorithm features including multiple parent selection methods, crossover options, mutation options and other features such as elitism, minimizing-inbreeding, using more than two parents and selecting from a range of early termination options. See below for details)

### Usage

```
select(  
  total_number_generations,  
  number_of_parents = 2,  
  pop,  
  gene_length,  
  response_vec,  
  independent_vars,  
  prob = 0.05,  
  user_genes = NULL,  
  metric = "AIC",  
  family = "gaussian",  
  method = "roulette",  
  susN = 1,  
  tourn_size = 2,  
  mutation = "fixed",  
  mutation_rate = 0.02,  
  minimize_inbreeding = FALSE,  
  crossover = "uniform",  
  number_of_crossovers = 1,  
  elitism = TRUE,  
  elite_prop = 0.05,  
  ad_max_mutate = 0.1,  
  ad_min_mutate = 0.01,  
  ad_inflection = 0.3,  
  ad_curve = 15,  
  custom_function = NULL,  
  estimator = NULL,  
  pause_length = NULL,  
  percent_converge = NULL,  
  score_threshold = NULL,  
  fittest = "high"  
)
```

### Arguments

`total_number_generations`  
an integer representing the maximum number of iterations

number_of_parents	an integer defining the number of parents per offspring
pop	an integer defining the number of creatures per a generation
gene_length	an integer representing the number of genes per a creature
response_vec	a numeric vector without infinite or NA values
independent_vars	a matrix or dataframe with ncol equal to number of genes and nrow with the same length as the response_vec
prob	a number 0-1 representing the chance that an individual has any given gene
user_genes	a matrix consisting of 1s and 0s without any rows with all zeros ncol equal to gene_length and nrow less than or equal to pop
metric	a character from the following 'R2', 'AIC', 'BIC', or 'AICc', the statistic LM or GLM is returning
family	the GLM family of distributions (must have the same support as the data for instance exponential cannot have negative numbers)
method	the method of choosing parents, 'roulette', 'rank', 'tournament', and 'sus'
susN	if sus is selected how many parents are chosen scholastically
tourn_size	if tournament is chosen how many candidates are in the tournament
mutation	a character either 'fixed' or 'adaptive' indicating the type of mutation
mutation_rate	a numeric between 0 and 1 indicating how often a creature is selected for mutation.
minimize_inbreeding	a logical indicating whether or not we minimize inbreeding.
crossover	a character that can be 'uniform', 'fitness', or 'k_point' indicating how to carry out crossover.
number_of_crossovers	number of k_point crossovers, needs to be less than gene_length
elitism	a logical representing whether elitism is requested
elite_prop	the proportion of each generation that is selected for elitism
ad_max_mutate	max mutation rate for adaptive mutation, numeric between 0 and 1 and more than ad_min
ad_min_mutate	min mutation rate for adaptive mutation, numeric between 0 and 1 and less than ad_max
ad_inflection	percentage of diversity in population where adaptive mutation begins to increase rapidly
ad_curve	rate that influence how intensely adaptive mutation changes
custom_function	user defined custom mast take vector representing a single creatures genes, data, and return a single numeric
estimator	character string from 'Min.', '1st Qu.', 'Median', 'Mean', '3rd Qu.', or 'Max.'. This term controls termination conditions for instance, terminating after the Mean AIC is above a certain threshold
pause_length	a numeric indicating how many iterations without improvement in the estimator before you terminate

percent_converge	percentage of diversity when algorithm terminates for instance .1 will terminate if there are only .90 of the population is represented by the same genes
score_threshold	a numeric indicating a threshold to cutoff if the estimator reaches that value
fittest	a character either 'high' or 'low' defining whether a custom functions

## Details

`user_genes` allows the user specific genes to the initial generation provided that the matrix consist only of 1s and 0s has no all-zero rows, `ncol = gene_length`, and has `nrow` less than or equal the total population `pop`

`custom_function` allows the user to specify a custom function instead of `lm()` or `glm()`. User-provided function must have its first two arguments be (1) `generation_matrix` and (2) `data`. Function needs to take a single row of a `generation_matrix` and return a single numeric without NAs or infinities.

Otherwise, user should specify a metric from R2, AIC, BIC, or AICC. The underlying fitness function for R2 is `lm()` and the underlying fitness function for AIC, BIC, and AICC is `glm()`. AIC, BIC, and AICC has the option to specify a specific family of functions however, the data needs to be defined across the support for the given family for instance exponential must be greater than 0.

Parents are selected via a number of methods: #'Roulette Method selects parents randomly with a probability proportional to their fitness

Rank Method selects parents randomly with a probability proportional to the rank of their fitness

Tournament uses `tourn_size` to randomly group that many creatures together. The most fit in that group becomes a parent.

Stochastic Universal Sampling works like roulette but also selects a number (`susN`) more candidates at a fixed width from the first draw to increase diversity

crossover Methods Uniform - each gene is randomly selected from 2 or more parents from a PMF proportional to the number of parents.

Fitness - each gene is randomly selected from 2 or more parents from a PMF proportional to the parent's fitness.

K-Point - parents genes are broken into  $k+1$  segments, then the offspring inherits portions randomly from the parents. Takes the parameter `number_of_crossovers` which must be less than  $1/2$  `gene_length`.

For all methods candidate offspring are accepted / rejected so that they don't have completely 0-vector genes.

mutation Fixed - Each offspring has a `mutation_rate` chance of being selected for mutation. Once selected one gene is switched from one to zero or zero to one.

Adaptive - the overall population is measured for diversity. As diversity becomes lower, the mutation rate increases. Once selected for mutation a single gene is switched from one to zero or zero to one. The adaptive function is controlled by a simple logistic function with parameters `ad_min` and `ad_max` describing the minimum and maximum mutation rates. `ad_inflection` controls where the logistics point pivots, and `ad_curve` controls how rapidly the logistics curve increase.

For all mutation methods, candidate offspring are accepted / rejected so that they don't have completely 0-vector genes.

Minimize inbreeding. his option reduces (though does not remove) the chance of similar creatures creating offspring together. Each parent is assigned new partner(s) randomly from a PMF proportional to how different their genes are. Parents are drawn without replacement so that if they were selected to become parents, they will still remain parents.

Elitism preserves the most-fit creatures from each generation. by selecting a number of most fit creatures equal to the ceiling(pop \* elite\_prop) and guarantees that they make it to the next generation. Additionally, this features makes a copy of each most-fit creature and conducts one gene mutation randomly on each creature. If the copy is more fit than the original, it is returned instead of the original so that the final returned matrix of elite creatures are at least as fit as the incoming elite creatures.

Early Termination Conditions: User can define early termination criteria to include a percentage\_convergence such that when diversity falls below a specific threshold the program terminates. User can identify a estimate (from the standard summary() function) that if the estimate reaches a specific threshold the program terminates or if the estimate pauses for a certain number of iterations terminates.

estimator - can be nominated from the summary() function aka Min., 1st Qu., Median, Mean, 3rd Qu., or Max. so for instance estimator=Max. metric = 'AIC' and score\_threshold = 500 would terminate when the Max. AIC falls below 500.

diversity is defined as sum(unique(genes))/total\_genes

## Value

returns a list consisting of [[1]] the fittest gene, [[2]] the fittest gene's score, [[3]] the most fit score by generation, [[4]] the summary data by generation and [[5]] the final generation's genes.

## Examples

```
pop <- 50
gene_length <- 10
response_vec <- rnorm(100)
independent_vars <- matrix(rnorm(100*10),ncol=10)
total_number_generations <- 15
select(pop = pop, gene_length = gene_length,
response_vec = response_vec, independent_vars = independent_vars,
total_number_generations = total_number_generations)

response_vec <- rnorm(100)
independent_vars <- matrix(rnorm(100*50),ncol=50)
pop <- 50
gene_length <- 50
elitism <- TRUE
elite_prop <- .05
mutation_rate <- .1
crossover <- 'k_point'
method <- "rank"
number_generations <- 50

select(pop = pop, gene_length = gene_length,
response_vec = response_vec, independent_vars = independent_vars,
total_number_generations = total_number_generations,
elitism = elitism, mutation_rate = mutation_rate, crossover = crossover,
method = method)
```

---

select_parent	<i>Selects parents for the next generation of creatures</i>
---------------	-------------------------------------------------------------

---

## Description

This function's purpose is to take a score vector and to return a vector of the next generation of parents. To do this it takes the number of parents required per an offspring, and the general population required. The resulting new\_parents vector will be of length pop\_required \* number\_of\_parents.

## Usage

```
select_parent(  
  score_vec,  
  number_of_parents,  
  method = "roulette",  
  susN = 1,  
  tourn_size = 4,  
  pop_required  
)
```

## Arguments

score_vec	a positive, numeric vector with length equal to the total population
number_of_parents	an integer indicating the number of parents per offspring
method	the method of choosing parents, 'roulette', 'rank', 'tournament', and 'sus'
susN	if sus is selected how many parents are chosen scholastically
tourn_size	if tournament is chosen how many candidates are in the tournament
pop_required	number of offspring needed at the start of the next generation

## Details

Roulette Method selects parents randomly with a probability proportional to their fitness

Rank Method selects parents randomly with a probability proportional to the rank of their fitness

Tournament uses tourn\_size to randomly group that many creatures together. The most fit in that group becomes a parent.

Stochastic Universal Sampling works like roulette but also selects a number (susN) more candidates at a fixed width from the first draw to increase diversity

## Value

a numeric vector indexing which parents are reproducing for the next generation

**Examples**

```
score_vec <- abs(rnorm(10))
number_of_parents <- 2
pop_required <- 10

new_parents <- select_parent(score_vec = score_vec,
  number_of_parents = number_of_parents, pop_required = pop_required)
```

---

test_user_function	<i>Tests User_Provided Custom Function</i>
--------------------	--------------------------------------------

---

**Description**

This function confirms that a user-provided function takes genes from a `generation_matrix` and a data matrix and returns a score for each gene. It also confirms there are not NAs or infinity values. This function does not confirm that the scores are in descending order aka higher fitness creatures receive a higher fitness scores. It also does not confirm that all possible scores are defined.

**Usage**

```
test_user_function(func, generation_matrix, data)
```

**Arguments**

<code>func</code>	user provided function (needs <code>generation_matrix</code> followed by <code>data</code> )
<code>generation_matrix</code>	generation matrix with all 0s and 1s with <code>ncol = gene_length</code> and <code>nrow = pop</code>
<code>data</code>	a matrix or dataframe with <code>ncol = gene_length plus 1</code>

**Details**

User-provided function must have its first two arguments be (1) `generation_matrix` and (2) `data`. Function needs to take a single row of a `generation_matrix` and return a single numeric without NAs or infinities.

**Value**

TRUE if it passes and an error message otherwise

**Examples**

```
generation_matrix <- matrix(rbinom(2*10,1,.5),ncol=10)
data <- matrix(rnorm(11*3),nc=11)
func <- function(generation_matrix,data) {sum(generation_matrix)}

test <- test_user_function(func,generation_matrix,data)
```